

1. *Problem 3.6* An information source produces binary triplets $\{000, 111, 010, 101, 001, 110, 100, 011\}$, corresponding probabilities $\{1/4, 1/4, 1/8, 1/8, 1/16, 1/16, 1/16, 1/16\}$. A binary code assigns a codeword of length $-\log_2 p_k$ to triplet k . Let X be the length of the string assigned to the output of the information source.
 - (a) Show the mapping from S to S_x , the range of X .
 - (b) Find the probabilities for the various values of X .
2. *Problem 3.13* Let X be a random variable with pmf $p_k = c/k^2$ for $k = 1, 2, \dots$.
 - (a) Estimate the value of c numerically. Note that the series converges.
 - (b) Find $P[X > 4]$.
 - (c) Find $P[6 \leq X \leq 8]$.
3. *Problem 3.49* Let X be binomial random variable that results from performance of n Bernoulli trials with probability of success p .
 - (a) Suppose that $X = 1$. Find the probability that the single event occurred in the k th Bernoulli trial.
 - (b) Suppose that $X = 2$. Find the probability that the two events occurred in the j th and k th Bernoulli trials where $j < k$.
 - (c) In light of your answers to part a and part b in what sense are the successes distributed “completely at random” over the n Bernoulli trials?
4. *Problem 3.52* A sequence of characters is transmitted over a channel that introduces errors with probability $p = 0.01$.
 - (a) What is the pmf of N , the number of error-free characters between erroneous characters?
 - (b) What is $E[N]$?
 - (c) Suppose we want to be 99% sure that at least 1000 characters are received correctly before a bad one occurs. What is the appropriate value of p ?
5. *Problem 3.59* The number of page requests that arrive at a Web server is a Poisson random variable with an average of 6000 requests per minute.
 - (a) Find the probability that there are no requests in a 100-ms period.
 - (b) Find the probability that there are between 5 and 10 requests in a 100-ms period.

6. *Problem 3.66* A data center has 10,000 disk drives. Suppose that a disk drive fails in a given day with probability 10^{-3} .
- (a) Find the probability that there are no failures in a given day.
 - (b) Find the probability that there are fewer than 10 failures in two days.
 - (c) Find the number of spare disk drives that should be available so that all failures in a day can be replaced with probability 99%.