



Longest Substring

No Capital Corp | Poly Team



The Problem

Return the **length** of the **longest**
substring **without repeating characters**
in *s*.



Some Javascript Recap

Creating Hashtable - $O(1)$

```
let hashtable = {};
```

```
let hashtable = new Object();
```



Some Javascript Recap

Inserting to Hashtable - $O(1)$

```
hashtable.key1 = "value";
```

```
hashtable["key2"] = "value";
```



Some Javascript Recap

Accessing Values in a Hashtable - $O(1)$

```
console.log(hashtable.key1);
```

```
console.log(hashtable["key2"]);
```



Some Javascript Recap

Deleting in Hashtable - $O(1)$

```
delete hashtable.key1;
```

```
delete hashtable["key2"];
```



Some Javascript Recap

Finding Max/Min - $O(1)$

```
let max_val = Math.max(2, 3);
```

```
let min_val = Math.min(2, 3);
```



Sliding Window

A sliding window looks like the following:

$$[i, j]$$



Sliding Window

To solve this problem, we use the following sliding window:

$$[i, j)$$



Example: Sliding Window

0	1	2	3	4
a	b	b	a	b

i \uparrow

j \uparrow

$[i, j) = ???$



Example: Sliding Window

0	1	2	3	4
a	b	b	a	b

i ↑

j ↑

$[i, j) = [0, 0)$



Example: Sliding Window

0	1	2	3	4
a	b	b	a	b

i ↑

j ↑

$[i, j) = [0, 0)$ # of elements = ???



Example: Sliding Window

	0	1	2	3	4
	a	b	b	a	b
i	↑				
j	↑				

$[i, j) = [0, 0)$ # of elements = 0



Example: Sliding Window

0	1	2	3	4
a	b	b	a	b

i ↑

j ↑

$[i, j) = [0, 0)$ $\text{set} = \{\}$



Example: Sliding Window

0	1	2	3	4
a	b	c	d	e

i

↑

j

↑

$[i, j) = ???$ $\text{set} = ???$



Example: Sliding Window

	0	1	2	3	4
	a	b	c	d	e
i		↑			
j					↑

$[i, j) = [1, 4)$ set = ???



Example: Sliding Window

	0	1	2	3	4
	a	b	c	d	e
i		↑			
j					↑

$[i, j) = [1, 4)$ $\text{set} = \{\mathbf{b}, \mathbf{c}, \mathbf{d}\}$



The Algorithm

- Maintain a set of characters in the current window



The Algorithm

- Maintain a set of characters in the current window
- Iterate if $j < s.length$ and $i < s.length$
- Check if $s[j]$ is in the set



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- If no, slide j further



The Algorithm

-
- Iterate if $j < s.length$ and $i < s.length$
- Check if $s[j]$ is in the set
- If no, slide j further
- If yes, slide i to the right



The Algorithm

-
- If yes, slide i to the right
- At some point, the set captures the required substring (why?)



Checking “abbab”

0	1	2	3	4
a	b	b	a	b

i ↑

L = 0

j ↑

$[i, j) = [0, 0)$ set = {}

Checking “abbab”

Does the set
contain a?

	0	1	2	3	4
	<u>a</u>	b	b	a	b
i	↑				
j	↑				

L = 0

$[i, j) = [0, 0)$ set = {}

Checking “abbab”

Does the set
contain a?

0	1	2	3	4
<u>a</u>	b	b	a	b

i ↑

L = 0

- No

j ↑

$[i, j) = [0, 0)$ set = {}

Checking “abbab”

Does the set
contain a?

0	1	2	3	4
<u>a</u>	b	b	a	b

i ↑

L = 0

- No
- Slide i

j ↑

$[i, j) = [0, 0)$ set = {}



Checking “abbab”

0	1	2	3	4
a	b	b	a	b

i \uparrow

$L = 1$

j \uparrow

$[i, j) = [0, 1)$ $\text{set} = \{a\}$



Checking “abbab”

Does the set
contain **b**?

	0	1	2	3	4
	a	<u>b</u>	b	a	b
i	↑				
j		↑			

$L = 1$

$[i, j) = [0, 1)$ set = {a}

Checking “abbab”

Does the set
contain **b**?

0	1	2	3	4
a	<u>b</u>	b	a	b

i ↑

L = 1

- No

j ↑

$[i, j) = [0, 1)$ set = {a}

Checking “abbab”

Does the set
contain **b**?

	0	1	2	3	4
	a	<u>b</u>	b	a	b

i ↑

L = 1

- No
- Slide j

j ↑

$[i, j) = [0, 1)$ set = {a}



Checking “abbab”

0	1	2	3	4
a	b	b	a	b

i ↑

L = 2

j ↑

$[i, j) = [0, 2)$ set = {a, b}



Checking “abbab”

Does the set
contain **b**?

	0	1	2	3	4
	a	b	<u>b</u>	a	b
i	↑				
j			↑		

$L = 2$

$[i, j) = [0, 2)$ $\text{set} = \{\mathbf{a}, \mathbf{b}\}$

Checking “abbab”

Does the set
contain **b**?

0	1	2	3	4
a	b	<u>b</u>	a	b

i ↑

L = 2

- Yes

j ↑

$[i, j) = [0, 2)$ set = {a, b}

Checking “abbab”

Does the set
contain **b**?

0	1	2	3	4
a	b	<u>b</u>	a	b

i

↑

L = 2

- Yes

- Slide i

j

↑

$[i, j) = [1, 2)$ set = {a, b}

Checking “abbab”

Does the set
contain **b**?

0	1	2	3	4
a	b	<u>b</u>	a	b

i

↑

L = 1

- Yes

- Slide i

j

↑

$[i, j) = [1, 2)$ set = {~~a~~, b}

Checking “abbab”

Does the set
contain **b**?

0	1	2	3	4
a	b	<u>b</u>	a	b

i

↑

L = 1

- Yes
- Slide i

j

↑

$[i, j) = [1, 2)$ set = {**b**}

Checking “abbab”

Does the set
contain **b**?

0	1	2	3	4
a	b	<u>b</u>	a	b

i

↑

L = 1

- Yes

- Slide i

j

↑

$[i, j) = [1, 2)$ set = {**b**}



Checking “abbab”

0	1	2	3	4
a	b	b	a	b

i

↑

L = 1

j

↑

$[i, j) = [1, 2)$ set = {b}



Checking “abbab”

0	1	2	3	4
a	b	<u>b</u>	a	b

i

↑

L = 1

j

↑

$[i, j) = [1, 2)$ set = {b}



Checking “abbab”

0	1	2	3	4
a	b	<u>b</u>	a	b

i

↑

L = 0

j

↑

$[i, j) = [2, 2)$ $\text{set} = \{\}$



Checking “abbab”

0	1	2	3	4
a	b	b	a	b

i



L = 0

j



$[i, j) = [2, 2)$ $\text{set} = \{\}$



Checking “abbab”

0	1	2	3	4
a	b	<u>b</u>	a	b

i

↑

L = 0

j

↑

$[i, j) = [2, 2)$ $\text{set} = \{\}$



Checking “abbab”

0	1	2	3	4
a	b	b	a	b

i

↑

L = 1

j

↑

$[i, j) = [2, 3)$ set = {b}



Checking “abbab”

0	1	2	3	4
a	b	b	<u>a</u>	b

i

↑

L = 1

j

↑

$[i, j) = [2, 3)$ set = {b}



Checking “abbab”

0	1	2	3	4
a	b	b	a	<u>b</u>

i

↑

L = 2

j

↑

$[i, j) = [2, 4)$ $\text{set} = \{\mathbf{b}, \mathbf{a}\}$



Checking “abbab”

0	1	2	3	4
a	b	b	a	<u>b</u>

i

↑

L = 1

j

↑

$[i, j) = [3, 4)$ set = {a}



Checking “abbab”

0	1	2	3	4	5
a	b	b	a	b	

i

↑

L = 2

j

↑

$[i, j) = [3, 5)$ $\text{set} = \{a, b\}$

Checking “abbab”

0 1 2 3 4 5

a b b a b

Did you see

that \mathcal{L}

captures the

required

length at

some point?

i

↑

$L = 2$

j

↑

$[i, j) = [3, 5)$ $\text{set} = \{a, b\}$



Checking “pwkeww”

	0	1	2	3	4	5
	p	w	k	e	w	w

i ↑

L = 0

j ↑

Max = 0

$[i, j) = [0, 0)$ set = {}



Checking “pwkeww”

	0	1	2	3	4	5
	<u>p</u>	w	k	e	w	w

i ↑

L = 0

j ↑

Max = 0

$[i, j) = [0, 0)$ set = {}



Checking “pwkeww”

	0	1	2	3	4	5
	p	<u>w</u>	k	e	w	w

i ↑

L = 1

j ↑

Max = 1

$[i, j) = [0, 1)$ set = {p}



Checking “pwkeww”

	0	1	2	3	4	5
	p	w	<u>k</u>	e	w	w

i ↑

L = 2

j ↑

Max = 2

$[i, j) = [0, 2)$ set = {p, w}



Checking “pwkeww”

0	1	2	3	4	5
p	w	k	<u>e</u>	w	w

i

↑

L = 3

j

↑

Max = 3

$[i, j) = [0, 3)$ set = {p, w, k}



Checking “pwkeww”

	0	1	2	3	4	5
	p	w	k	e	<u>w</u>	w

i

↑

L = 4

j

↑

Max = 4

$[i, j) = [0, 4)$ set = {p, w, k, e}



Checking “pwkeww”

0	1	2	3	4	5
p	w	k	e	<u>w</u>	w

i

↑

L = 3

j

↑

Max = 4

$[i, j) = [1, 4)$ set = {~~p~~, w, k, e}



Checking “pwkeww”

0	1	2	3	4	5
p	w	k	e	<u>w</u>	w

i

↑

L = 3

j

↑

Max = 4

$[i, j) = [1, 4)$ set = {w, k, e}



Checking “pwkeww”

0	1	2	3	4	5
p	w	k	e	<u>w</u>	w

i

↑

L = 2

j

↑

Max = 4

$[i, j) = [2, 4)$ set = {~~w~~, k, e}



Checking “pwkeww”

0	1	2	3	4	5
p	w	k	e	<u>w</u>	w

i

↑

L = 2

j

↑

Max = 4

$[i, j) = [2, 4)$ set = {k, e}



Checking “pwkeww”

0	1	2	3	4	5
p	w	k	e	w	<u>w</u>

i

↑

L = 3

j

↑

Max = 4

$[i, j) = [2, 5)$ set = {k, e, w}



Checking “pwkeww”

0	1	2	3	4	5
p	w	k	e	w	<u>w</u>

i

↑

L = 2

j

↑

Max = 4

$[i, j) = [3, 5)$ $\text{set} = \{\text{k}, \text{e}, \text{w}\}$



Checking “pwkeww”

0	1	2	3	4	5
p	w	k	e	w	<u>w</u>

i

↑

L = 2

j

↑

Max = 4

$[i, j) = [3, 5)$ $\text{set} = \{e, w\}$



Checking “pwkeww”

0	1	2	3	4	5
p	w	k	e	w	<u>w</u>

i

↑

L = 1

j

↑

Max = 4

$[i, j) = [4, 5)$ set = {~~e~~, w}



Checking “pwkeww”

0	1	2	3	4	5
p	w	k	e	w	<u>w</u>

i

↑

L = 1

j

↑

Max = 4

$[i, j) = [4, 5)$ set = {w}



Checking “pwkeww”

0	1	2	3	4	5
p	w	k	e	w	<u>w</u>

i

↑

L = 0

j

↑

Max = 4

$[i, j) = [5, 5)$ set = {~~w~~}



Checking “pwkeww”

0	1	2	3	4	5
p	w	k	e	w	<u>w</u>

i

↑

L = 0

j

↑

Max = 4

$[i, j) = [5, 5)$ set = {}



Checking “pwkeww”

0	1	2	3	4	5
p	w	k	e	w	<u>w</u>

i

↑

L = 1

j

↑

Max = 4

$[i, j) = [5, 6)$ set = {w}



Checking “pwkeww”

0	1	2	3	4	5
p	w	k	e	w	w

i

↑

L = 1

j

↑

Max = 4

$[i, j) = [5, 6)$ set = {w}



Checking “pwkeww”

0	1	2	3	4	5
p	w	k	e	w	w

i

↑

L = 1

j

↑

Max = 4

$[i, j) = [5, 6)$ set = {w}



Checking “pwkeww”

0	1	2	3	4	5
p	w	k	e	w	w

i

↑

L = 1

j

↑

Max = 4

$[i, j) = [5, 6)$ set = {w}



Runtime?

$O(n)$



Runtime?

$O(n)$

Why?



Runtime?

$O(n)$

Why?

Hint: how many times did we access each element?



Runtime?

$O(n)$

Why?

Hint: how many times did we access each element? 2



Runtime?

$O(n)$