



# Introduction to AMS Behavioral Modeling in SOC

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## Outline

- ◆ AMS circuits in SOC
- ◆ Behavioral modeling for analog circuits
- ◆ Applications of analog models
  - Noise interactions in AMS systems
    - Supply noise aware behavioral modeling
    - SCORE macromodel
  - Yield Enhancement
    - Analysis of process variation effects
    - Process variation aware behavioral modeling

# AMS Blocks in SOC

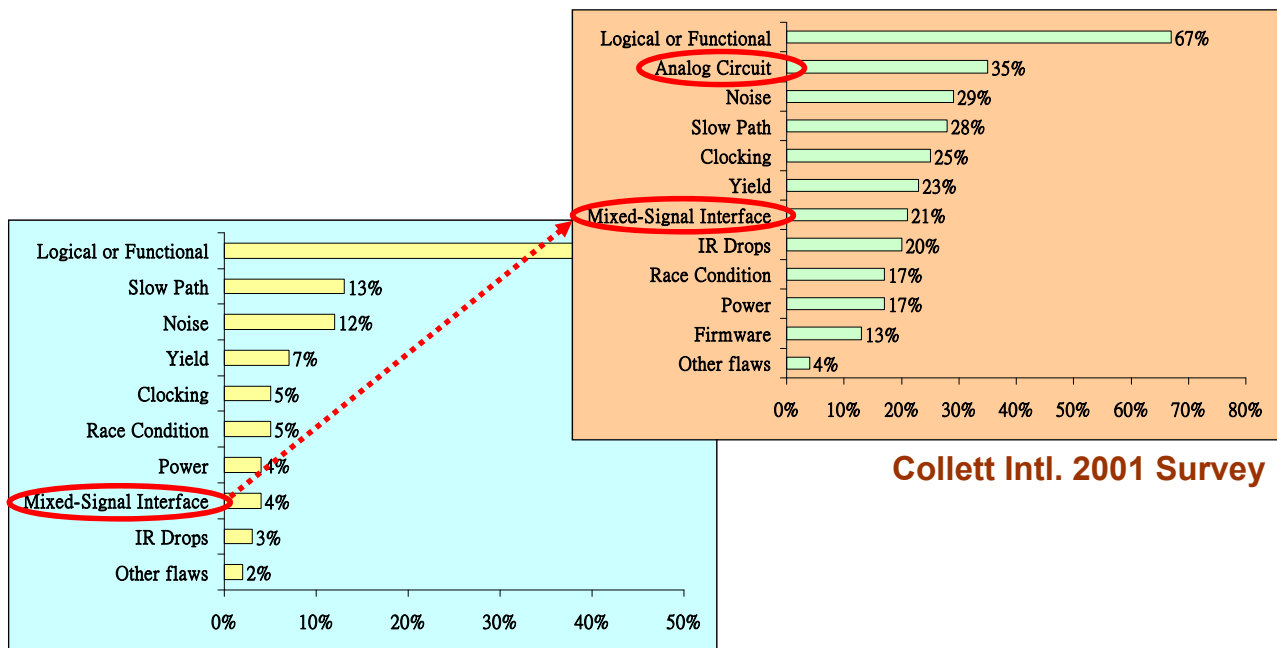
- ◆ Analog/Mixed-Signal (AMS) definitions
  - Analog: designs contain **continuous signal**  
(ex. continuous time filter, OP amp., mixer...)
  - Mixed-signal: designs contain **both** analog and digital signals (ex. A/D, D/A, PLL...)
    - Mainly focused on analog functionality
- ◆ SOC designs often include the analog interface to the outside world
- ◆ Synthesis still does not exist for AMS blocks
  - AMS languages only model the **behavior** of AMS blocks
  - Today, AMS VCs are in **hard (layout) form**



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## Major Respin Causes



Collett Intl. 2001 Survey

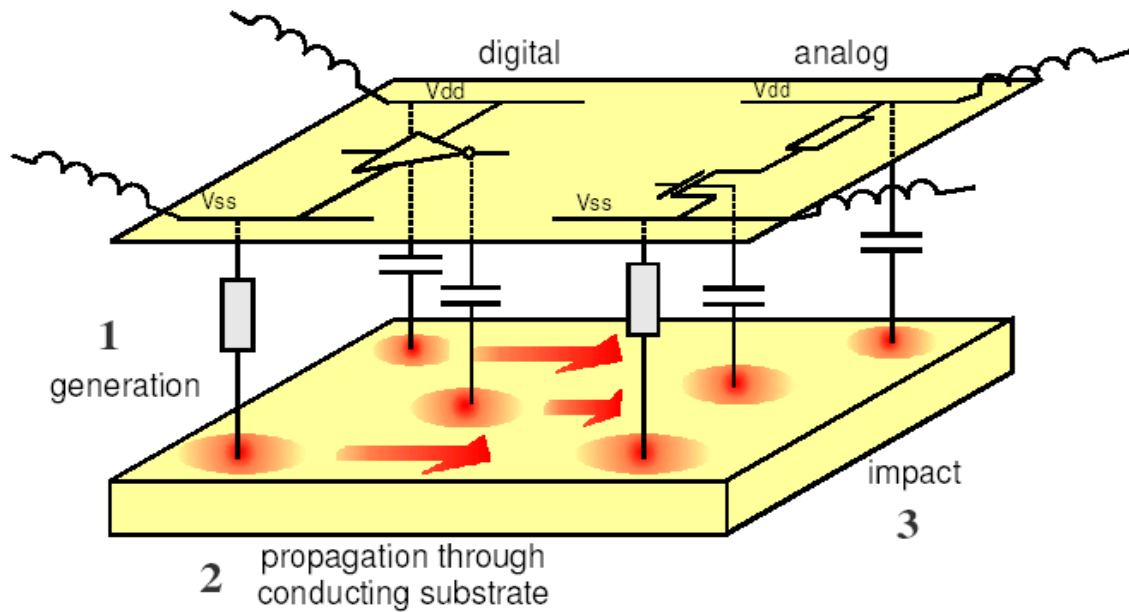
Collett Intl. 2000 Survey



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# Noise Coupling in AMS Designs



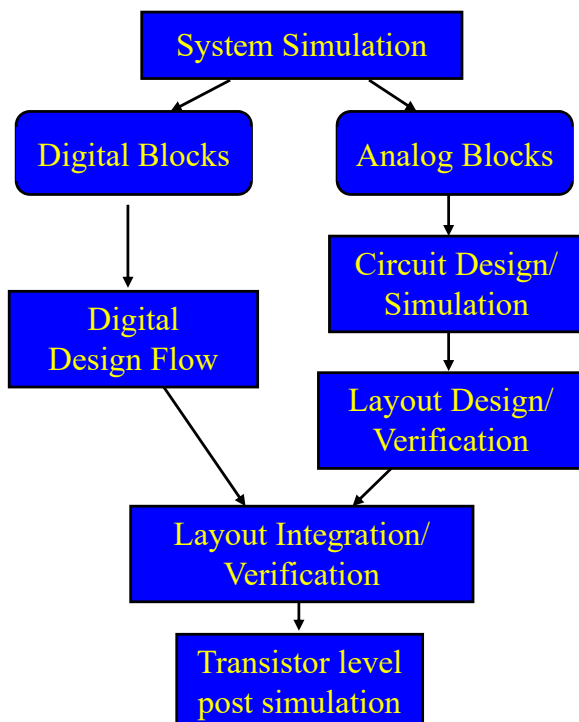
Source: Workshop on Substrate Noise-Coupling in Mixed-Signal ICs, Imec, Belgium, Sep. 2001



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## Conventional MS Design Approach



### ◆ Design/simulate digital and analog circuits separately

- May miss the interaction effects

### ◆ Can perform co-simulation at transistor level only

- High complexity
- Too slow

### ◆ Solutions

- Use a systematic, top-down design approach to capture design intent
- Develop some tools to rapidly target for different requirements



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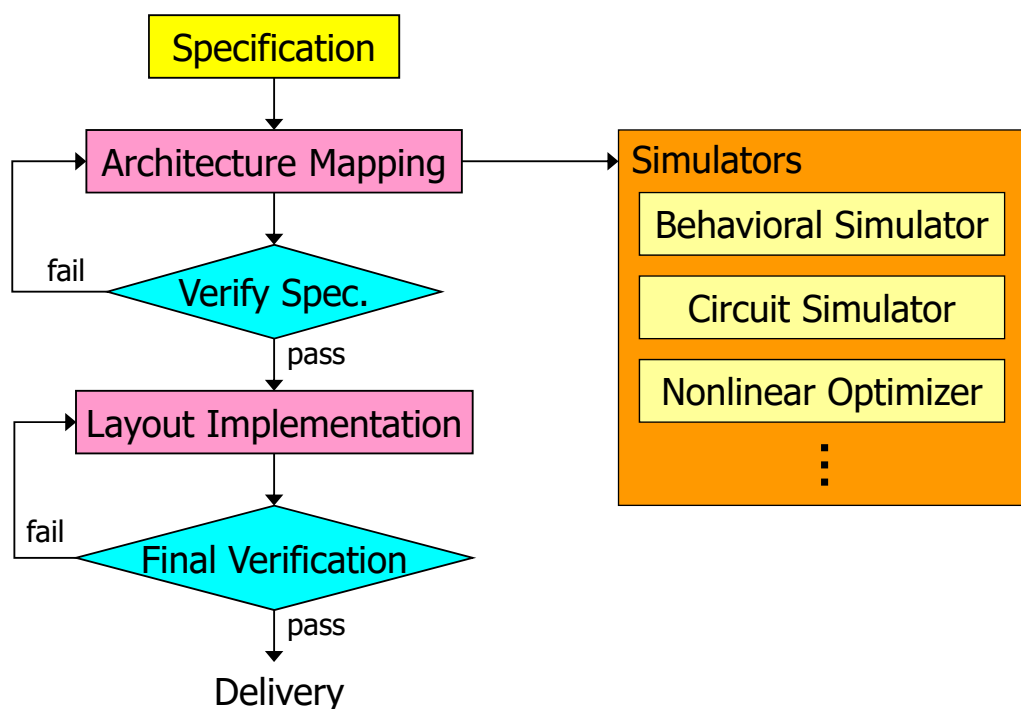
# Traditional Analog Simulation

- ◆ Analog designers have been using **SPICE** or SPICE-like tools for analog simulation over 30 years
  - Contain models of circuit elements (R, L, C, ...)
- ◆ Perform various analysis of circuits with high accuracy
  - DC, AC, transient, TF, ...
- ◆ Limited to small circuits due to long computation time
- ◆ Existing fast spice products are not still suitable for nanometer circuit analysis
  - Insufficient accuracy caused by simplified model
  - Latency assumption fails to address logically idle but electrically active nature of nanometer circuit behavior



## Top-Down AMS Design Flow

- ◆ Starting from **behavioral models** to check system behavior



# Adv. Of Top-Down Methodology

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- ◆ A widely accepted concept for digital designs
- ◆ Start design by using **behavioral modeling**
- ◆ Allow system simulation and architecture verification
- ◆ Allow design and verification of the circuit architecture before block design
- ◆ Allow mixed-level simulation with other digital circuits
- ◆ Allow changes with minimum impact to the design cycle



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# Analog Behavioral Modeling

- ◆ A mathematical model written in **Hardware Description Language (HDL)**
  - Verilog-AMS
  - VHDL-AMS
  - Matlab
  - C/C++
  - .....
- ◆ Emulate circuit block functionality by sensing and responding to circuit conditions
  - Simulate at **behavioral level**
- ◆ **Faster** simulation time
  - Allow **whole chip simulation**



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## An Example of Verilog-AMS Code

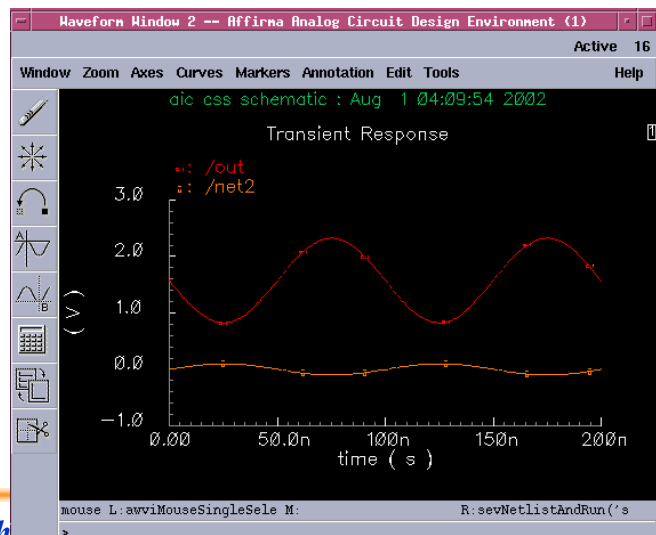
- ◆ **Keys to a good behavioral model**
  - Concise mathematical equations of the behavior
    - For faster simulation time
  - Appropriate value for each parameter
    - For accurate simulation results

```
// VerilogA for aic, cs, veriloga
#include "constants.h"
#include "discipline.h"

module cs(in, out);
input in;
output out;
electrical in, out;

parameter real gain=-7.5;
parameter real vdd=3.3;
parameter real id=0.23m;
parameter real rd=7.5e3;

analog begin
  V(out) <+ (gain * V(in))+vdd-(id*rd) ;
end
endmodule
```



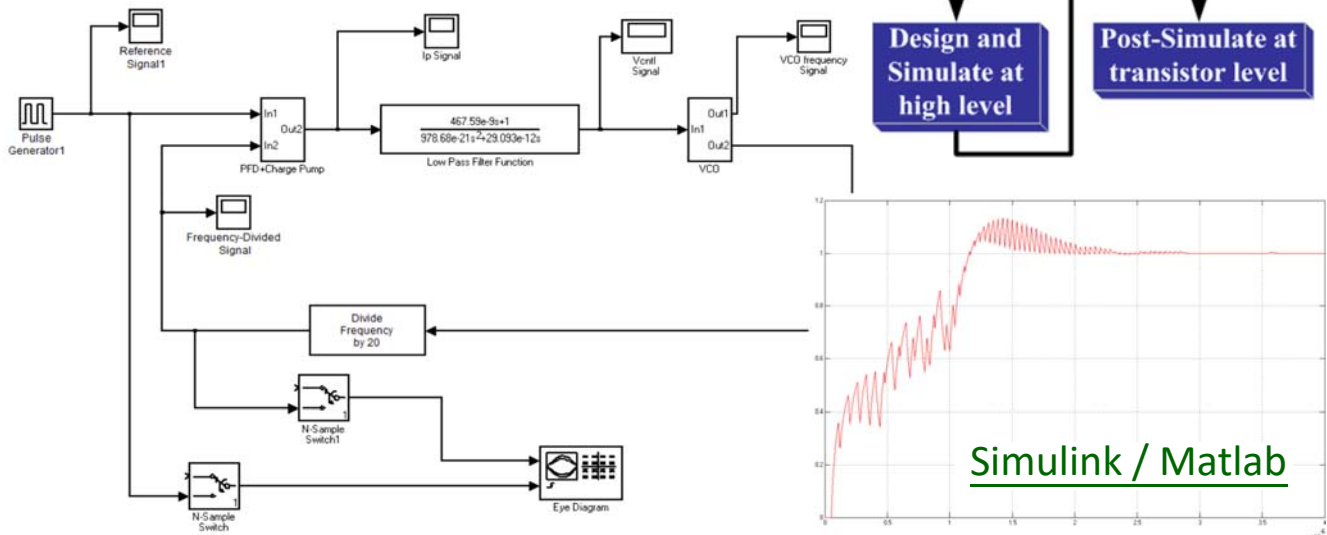
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# Top-down Modeling Approach

- ◆ **Top-down approach** can verify whole AMS system **roughly** before implemented
  - Suitable for **newly-created designs**

- ◆ **Issues:**

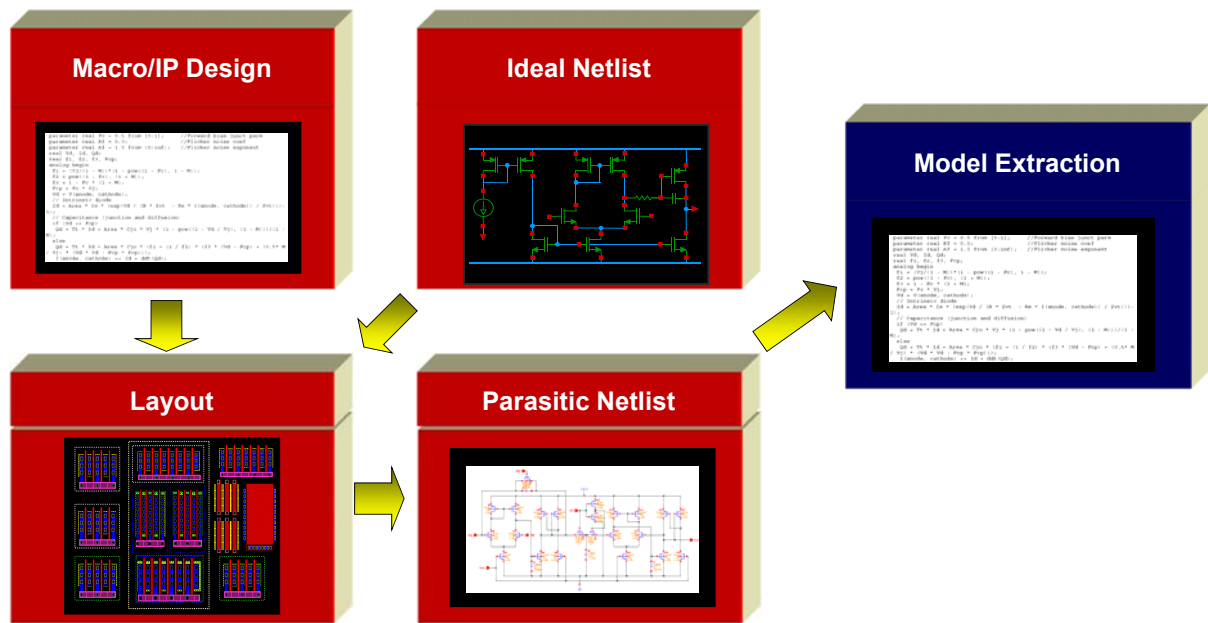
- **Lack of layout information** (loading, parasitic, ...)
- **Inaccurate on non-ideal circuit properties**



# Bottom-Up Modeling Approach

- ◆ While using **existing** blocks, bottom-up **behavior extraction** is required for system verification
  - An interesting research direction
- ◆ Bottom-up approach can be much accurate
  - **More accurate** (loading effects, parasitic effects, ... )
  - **Actual non-ideal circuit information**
  - **Signal interaction effects**
- ◆ Bottom-up approach can still effective when those design parameters are hard to obtain
  - Only have flattened transistor-level design
  - Suitable for IP-based designs (SOC designs)

# Bottom-Up Behavior Extraction



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# Accurate Behavior Extraction

- ◆ **Bottom-up extraction from simulation results**
  - More accurate
  - Still useful for flattened designs
- ◆ **Do not separate into sub-blocks**
  - Correctly deal with timing information, loading, parasitics and interactions
- ◆ **Do not measure from normal operations**
  - Develop a **special characterization mode**
  - Easily send special patterns to trigger the circuit
  - Long extracting time can be avoided



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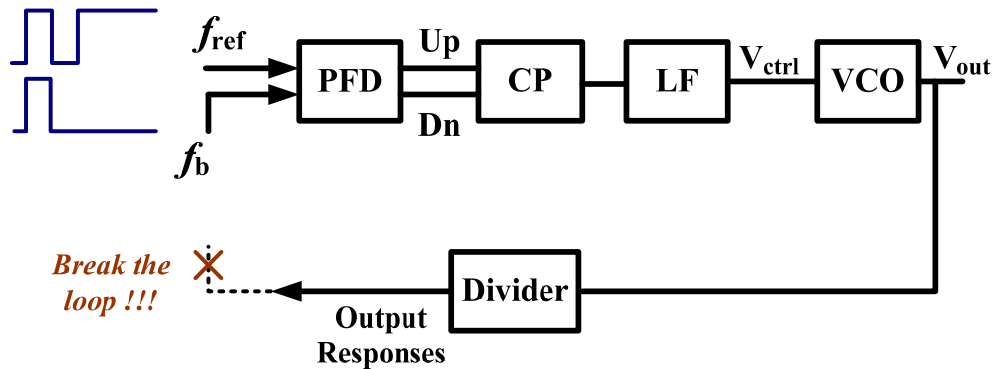
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# Characterization Mode

## ◆ Example: Charge Pump Phase-Locked Loop (CPPLL)

(Extraction patterns)



C.C. Kuo, Y.C. Wang, and C.N. Liu, "An Efficient Approach to Build Accurate PLL Behavioral Models of PLL Designs", *IEICE Trans. on Fundamentals (SCI)*, vol. E89-A, no. 2, pp. 391-398, Feb. 2006.

C.C. Kuo, Y.C. Wang, and C.N. Liu, "An Efficient Bottom-Up Extraction Approach to Build Accurate PLL Behavioral Models for SOC Designs", *ACM/IEEE GLSVLSI*, pp. 286-290, Apr. 2005.

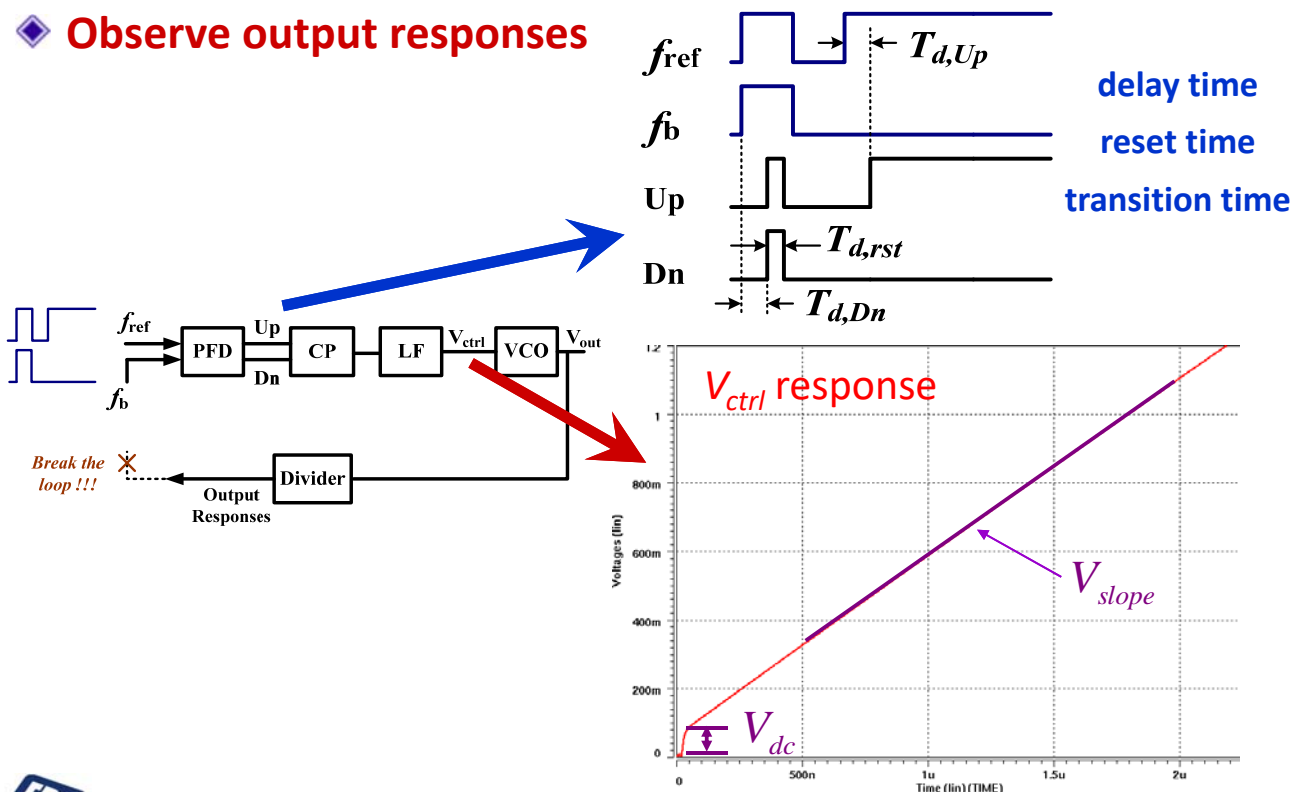


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## Extract Circuit Properties

### ◆ Observe output responses



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# Case Study

- ◆ Charge pump PLL
- ◆ Use Verilog-AMS language to describe PLL behaviors
- ◆ Simulation environment:
  - Analog Artist (Cadence)
  - Simulator: Spectre

	Specification
Process	TSMC 0.18um
Input freq.	25MHz
Output freq.	800MHz
$T_{\text{lock}}$	< 5us
pk-pk Jitter	< 20ps

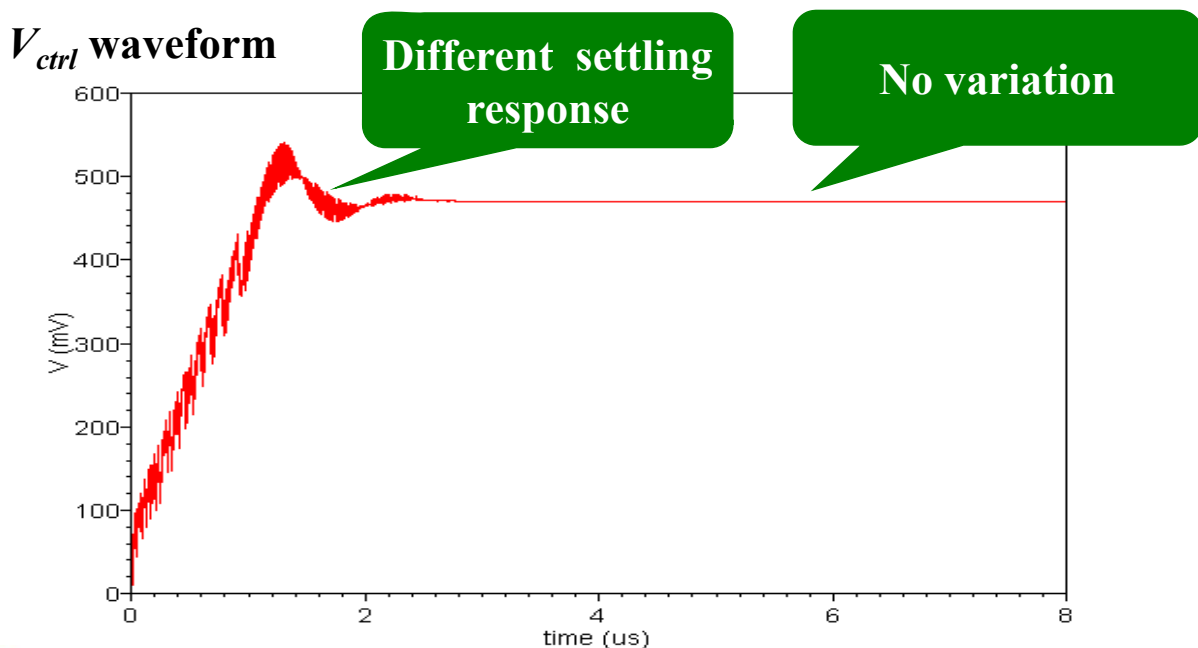


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## Ideal Behavioral Model

- ◆ Use the embedded behavioral blocks from Cadence's AHDL library

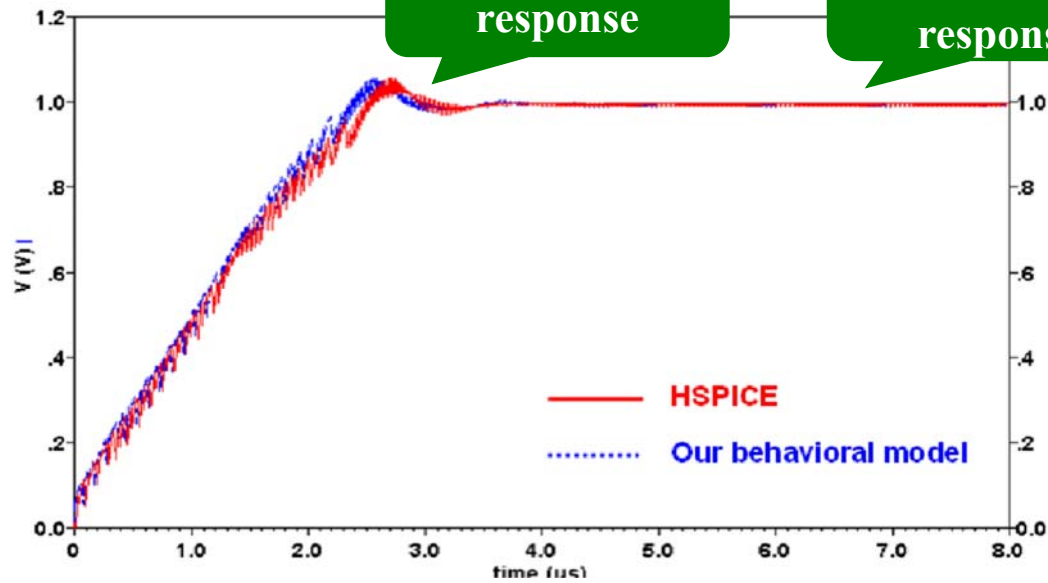


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# Extracted Behavioral Model

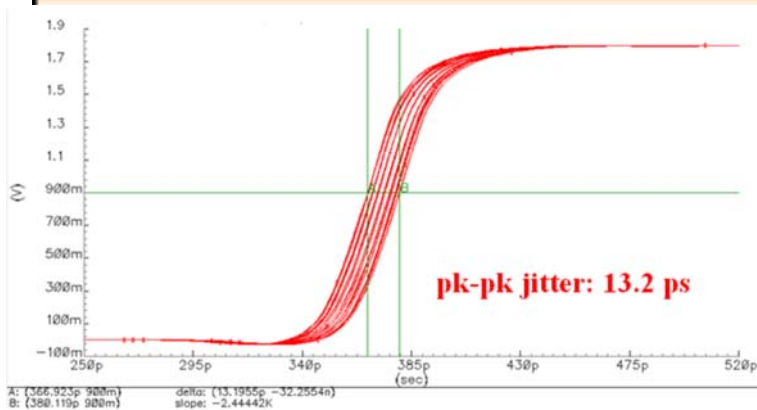
$V_{ctrl}$  waveform



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## Peak-to-peak Jitter

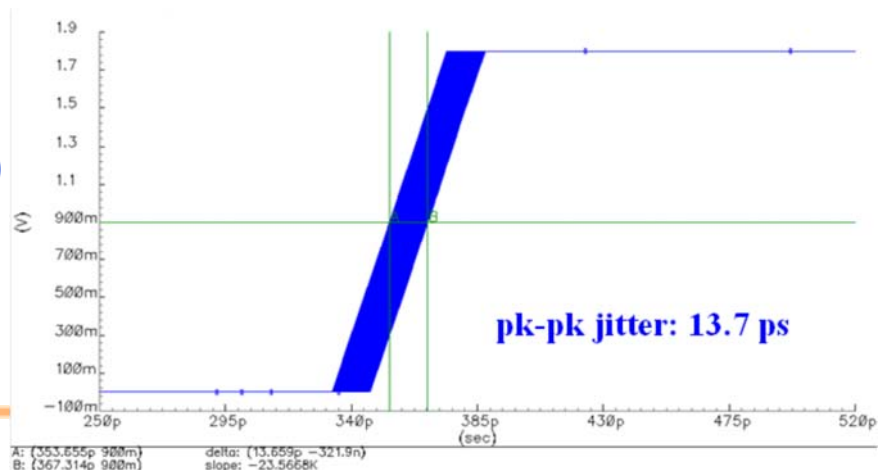


HSPICE : 13.2 ps

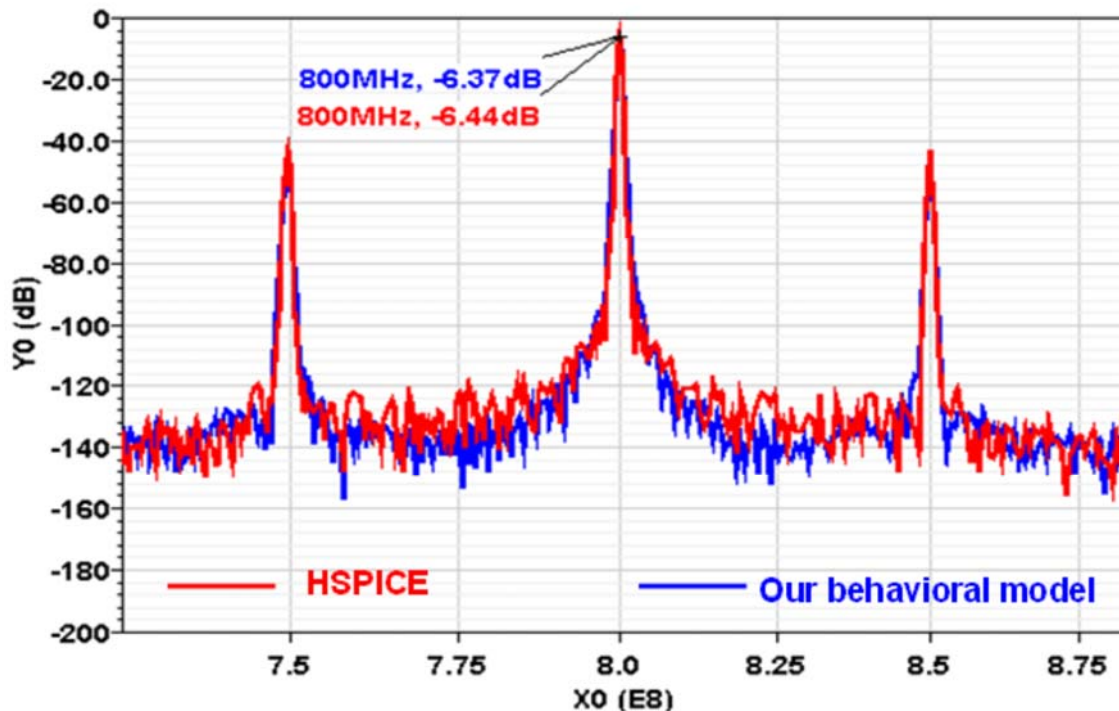
$T_{sim.}$  : 22074 sec

Beh model: 13.7ps

$T_{sim.}$  : 122 sec (180x)



# Similar Frequency Responses



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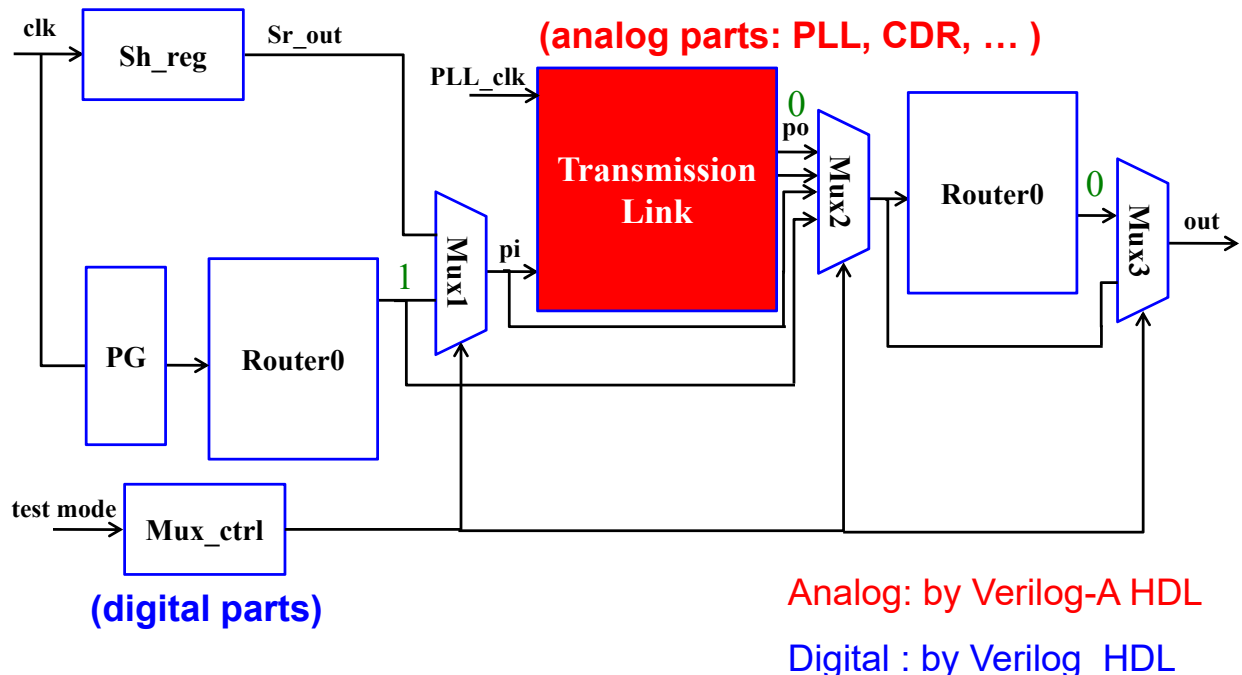
# Possible Applications

- ◆ Using analog behavioral models has fast simulation time
  - Can be used to replace the time-consuming simulation process in traditional design flow
  - Model accuracy is the key issue to be solved
- ◆ Used for system simulation with digital/analog circuits
  - Digital circuits are too large to be simulated by HSPICE
- ◆ Used for analyzing the noise effects in analog circuits
  - Noise-aware behavioral models can help to check noise issues
- ◆ Used for analyzing the design yield of analog circuits under process variation
  - Fast simulation time can speedup the Monte Carlo simulation
  - Enable designers to make improvement at behavioral level

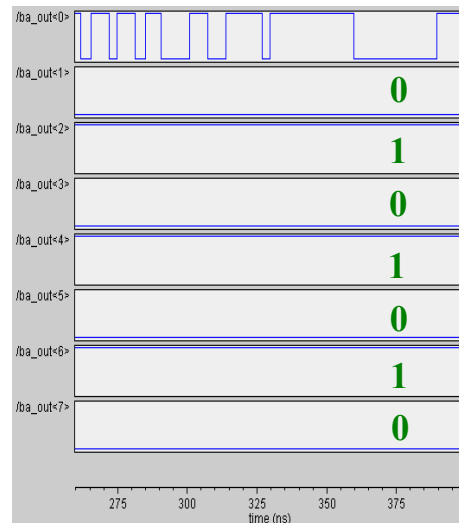
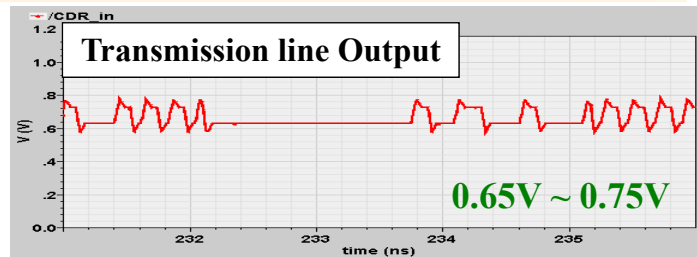
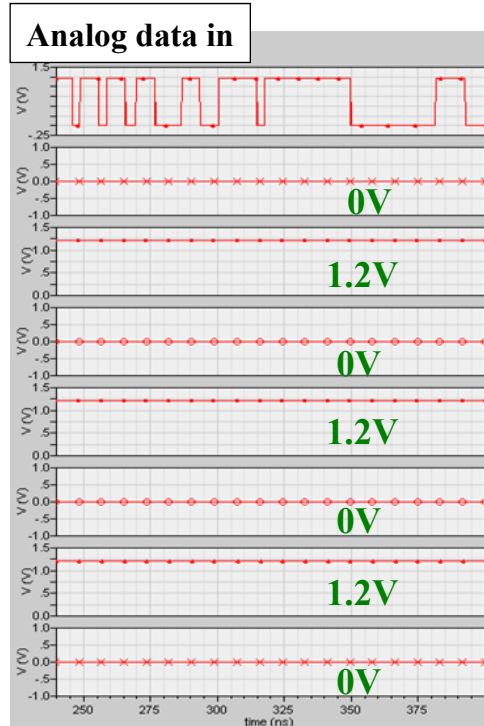


## Analog Models in System Design

### ◆ Transmission link system



# AMS System Simulation



Simulation Time : 2727 sec (5000 data)

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# Analog Performance Variations

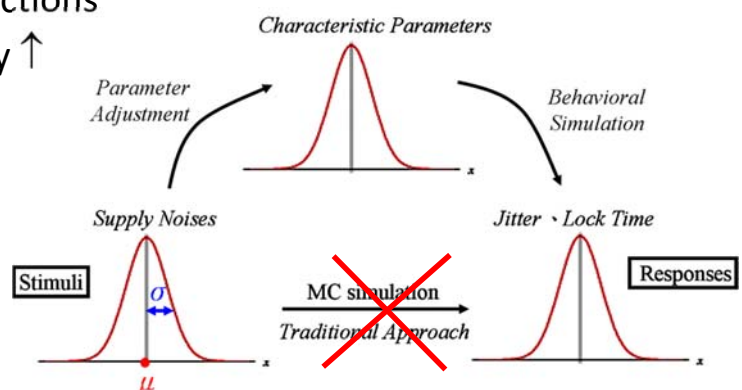
- ◆ **PVT** (**P**rocess, **V**oltage, and **T**emperature) variations have large performance impact
  - **Process variation**
  - **Supply noise**
  - Substrate noise
  - Temperature issue

— especially from digital circuits
- ◆ Performance variation analysis of **analog circuits** often needs **expensive transistor-level simulation**
- ◆ **Efficient analyzer** is necessary for system design
  - **Variation-aware behavioral modeling approach**



## Noise-Aware Behavioral Models

- ◆ Process variation and outside noise have large impacts on analog circuits
  - Often appear as random variables
- ◆ Typical approach: model the performance (timing, jitter, ...) as a function of those random variables
  - Use curve fitting to obtain the parameters of those functions
  - # variables  $\uparrow$ , complexity  $\uparrow$
- ◆ Alternative approach:
  - Use behavioral models
  - Find suitable internal parameters instead of trying to fit the final performance directly



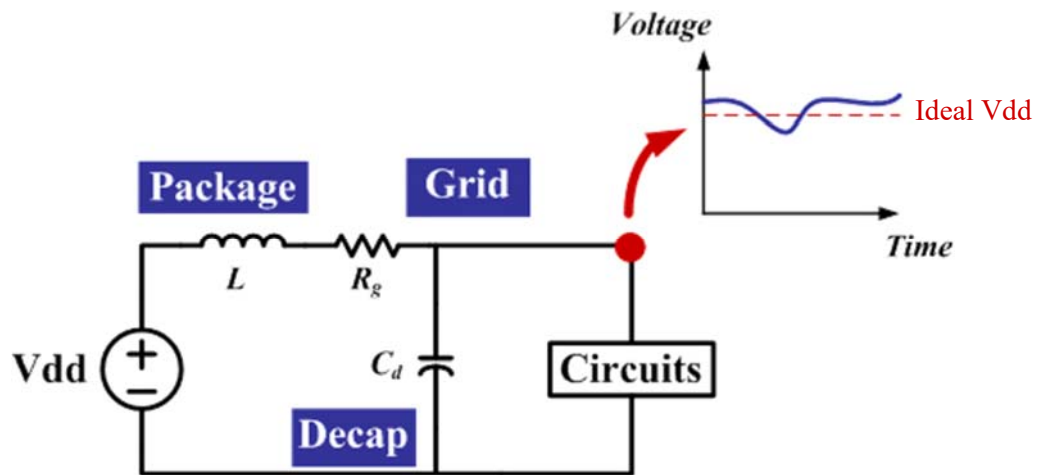
# Supply Noise

## Issues

- $L \frac{di}{dt}$
- IR drop

## Impacts

- Performance loss
- Yield loss



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# Stochastic Analysis Approaches

Random noise



(Gaussian)



(Uniform)

Supply noise



Random generator



Circuit performance

Issues:

- ➡ Rough prediction
- ➡ May be quite different in real cases



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# Regular Noise Analysis

Known waveform



Supply noise

Issues:

- ➡ Need complicated equations
- ➡ Not actual supply noise:
  - Unpredictable and Irregular

Regression  
or  
circuit analysis

Circuit performance

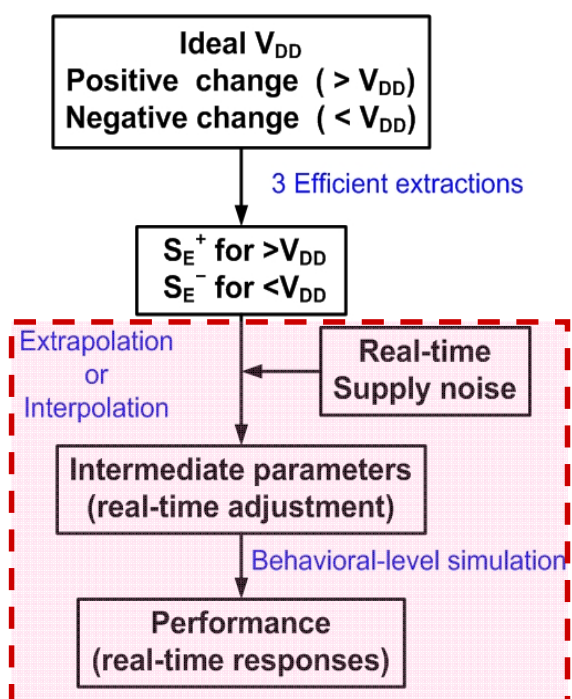


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## Handle Irregular Supply Noise

- ◆ Behavioral-level simulation
  - Save much simulation time
- ◆ Dynamic adjustment
  - Real-time calculation using current noise status
- ◆ Suitable for real systems
  - Handle unpredictable noise



C.C. Kuo and C.N. Liu, "Accurate Behavioral Modeling Approach for PLL Designs with Supply Noise Effects", IEEE BMAS, pp. 48-53, Sept. 2005.

C.C. Kuo and C.N. Liu, "On Efficient Behavioral Modeling to Accurately Predict Supply Noise Effects of PLL Designs in Real Systems", IFIP VLSISOC, pp. 116-121, Oct. 2006.



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# Linear Model for Intermediate Parameters

For example:

$$T_d + \Delta t = f(V_{DD} + \Delta v_{dd})$$



Sensitivity analysis under different  $V_{DD}$ :

$$S_E = \frac{\Delta \text{delay}}{\Delta V_{DD}} \text{ (constant)}$$

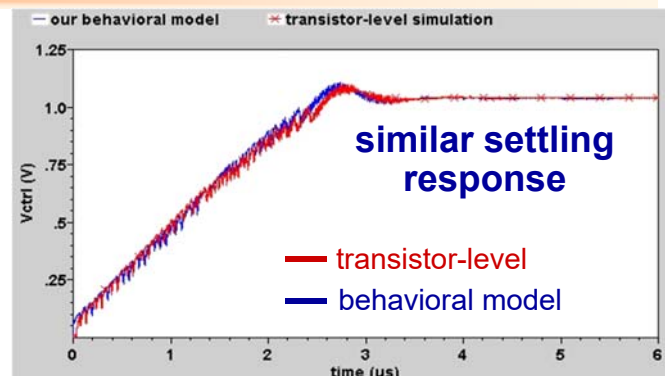
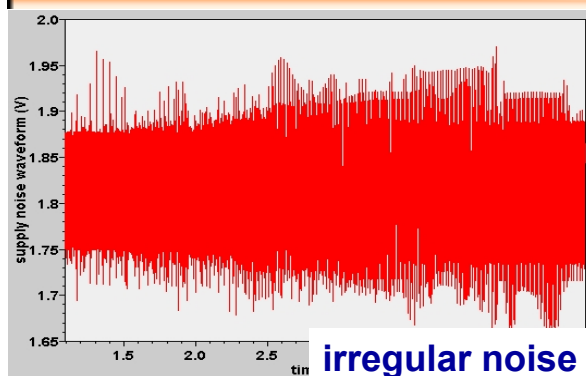
$$\longrightarrow S_E = \frac{(T_d + \Delta t) - T_d}{(V_{DD} + \Delta v_{dd}) - V_{DD}} \quad \begin{cases} S_E^+ & \text{for } \Delta v_{dd} > 0 \\ S_E^- & \text{for } \Delta v_{dd} < 0 \end{cases}$$



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## Simulation with Supply Noise



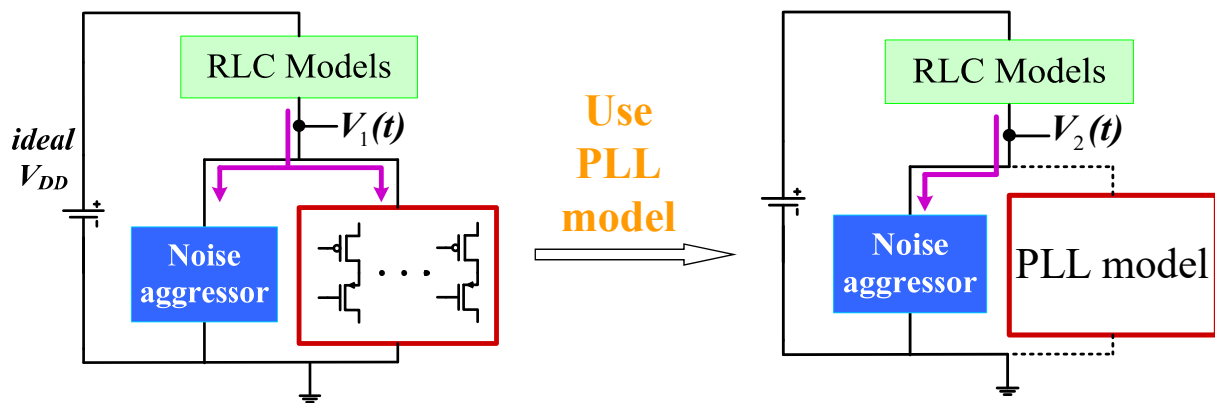
		Circuit-level	Ours	Noise free model
From $V_{ctrl}$ waveform	$V_{max}$ (V)	1.095	1.102	1.083
	$V_{lock}$ (V)	1.0352	1.0348	1.034
	$\Delta V_{ctrl}$ (mV)	6.6	6.8	6.1
	pk-pk PJ @ 800MHz (UI)	0.0176	0.016	0.0082
	$T_{simulation}$ (sec)	40413	1507	824



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# Noise Issues in AMS Integration



◆ **Using a noise-aware behavioral model** may not accurately analyze supply noise effects

- $V_{DD}$  waveform is independent on PLL behaviors
- Only consider the external supply noise
- When the noise affects PLL behaviors, the behavior changes also influence the noise waveform

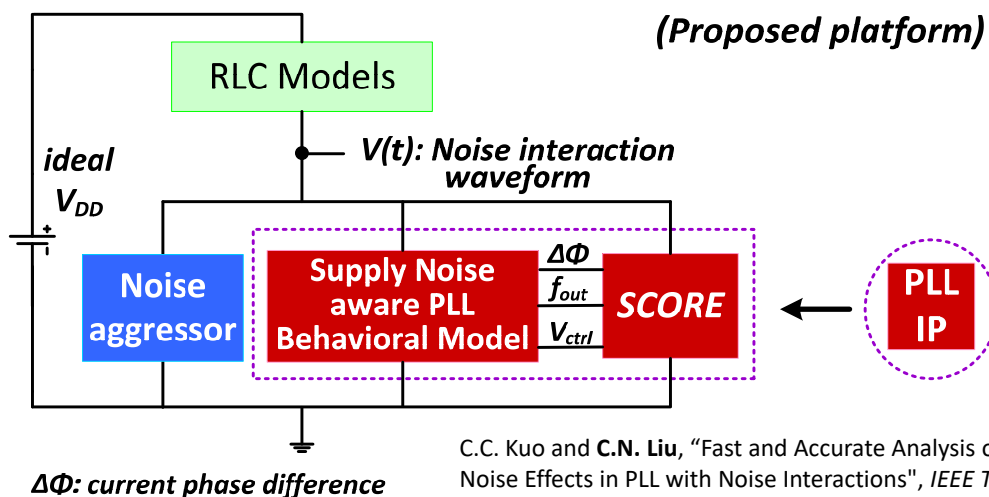


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## SCORE Macromodel for Noise Interaction

- ◆ **SCORE: State-controlled resistors**
- ◆ **Help PLL models handle supply noise interaction issues**
  - Provide accurate  $V_{DD}$  waveforms with PLL interactions
  - Can be combined with other noise-aware approaches



C.C. Kuo and C.N. Liu, "Fast and Accurate Analysis of Supply Noise Effects in PLL with Noise Interactions", *IEEE Trans. on Circuits and Systems I*, vol.57, no.1, pp.44-52, Jan. 2010.

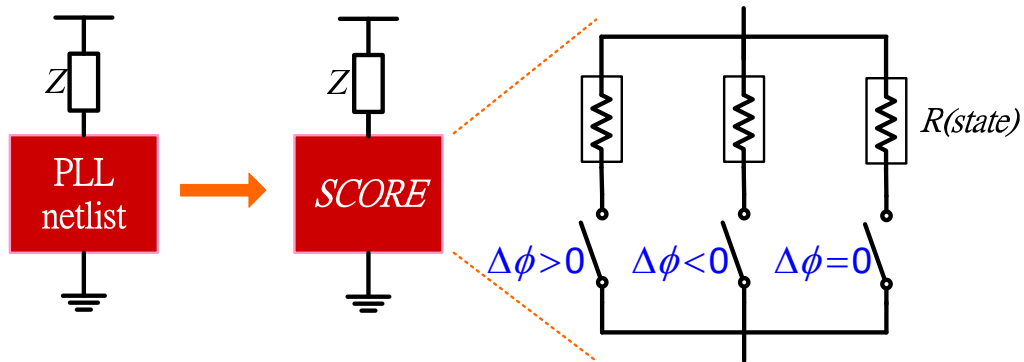


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# Ideas of SCORE Macromodel

- ◆ **Treat whole PLL design as a black-box**
- ◆ **Approximate the PLL behaviors** under a parasitic power line
- ◆ **Not record entire PLL  $I_{DD}$  waveform** to reduce cost
  - Extract the **peak voltages** induced by the PLL  $I_{DD,peak}$
- ◆ Model the PLL as **state-controlled switches** and **resistors**
  - PLL behaviors **in system view: 3-state machine**

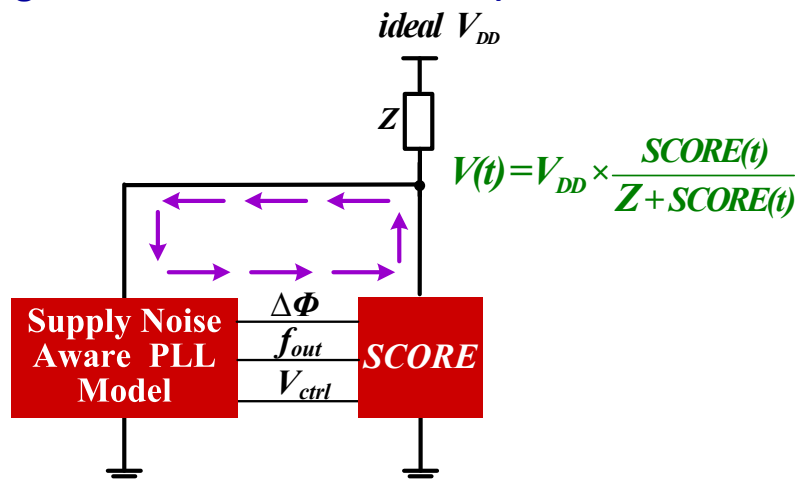


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# Recursive Simulation Platform for PLL

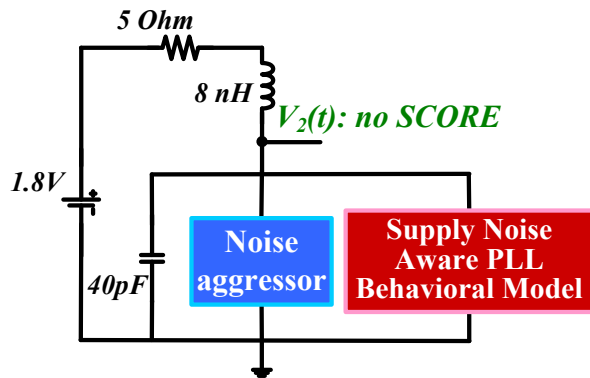
- ◆ The real-time supply noise  $V(t)$  affects the PLL behaviors
- ◆ The PLL behaviors also affect the supply noise  $V(t)$ 
  - **Supply noise is not only an independent input**
  - $V(t)$  also varies with real-time circuit behavior  
(just like using a transistor-level simulator)



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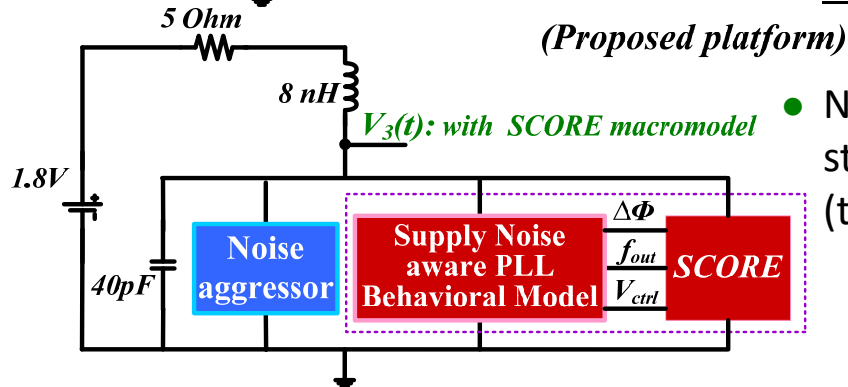
# Experiments



◆ **Golden reference:**  
HSPICE simulation

◆ **Comparison**

- Supply noise waveform
- PLL responses under such noise



- Noise aggressor: 3-stage buffer chain (transistor-level netlist)



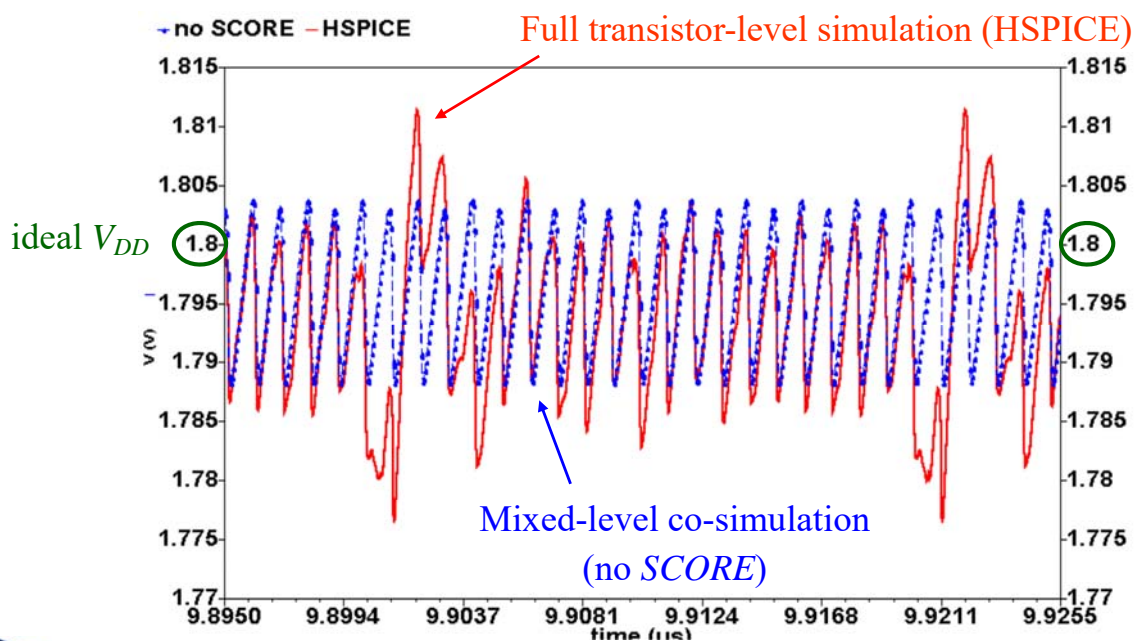
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## Without SCORE Macromodel

◆ Replace the PLL netlist by

- Only using a noise-aware PLL behavioral model



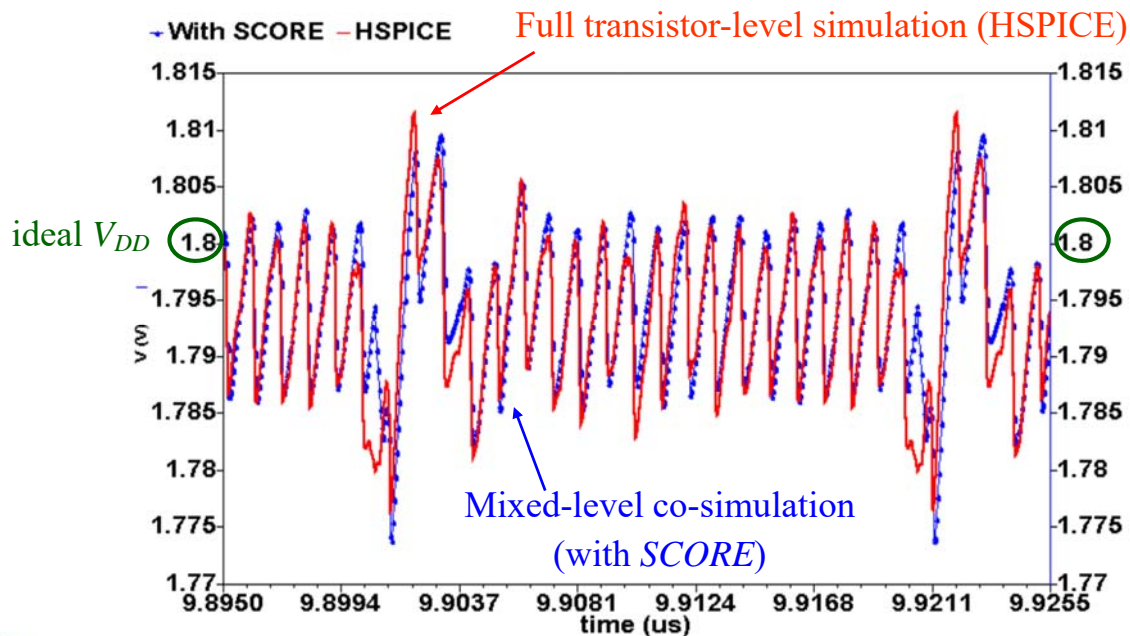
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# Recursive Approach

◆ Replace the PLL nelist by

- PLL behavioral model + SCORE macromodel



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## Comparison Results

Ideal $V_{DD} = 1.8V$		With supply noise interaction			No interaction	
		HSPICE	With SCORE	Error  (%)	No SCORE	Error  (%)
Supply noise waveform	PPV (V)	1.8113	1.8095	0.1	1.8035	0.4
	NPV (V)	1.7763	1.7737	0.2	1.7881	0.7
	RMS value (mV)	6.75	6.38	5.4	5.04	25.4
	Correlation coefficient	1	0.92	-	0.72	-
PLL responses	$V_{lock}$ (V)	0.9945	0.9943	0.02	0.9940	0.05
	$T_{lock}$ (us)	3.505	3.482	0.7	3.561	1.6
	pk-pk jitter (ps)	34.3	35.2	2.6	27.5	19.8
$T_{extract}$ for SCORE (sec)		-	247	-	-	-
$T_{sim}$ (sec)		37721	1218	-	1153	-

↑  
fast and accurate



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# Outline

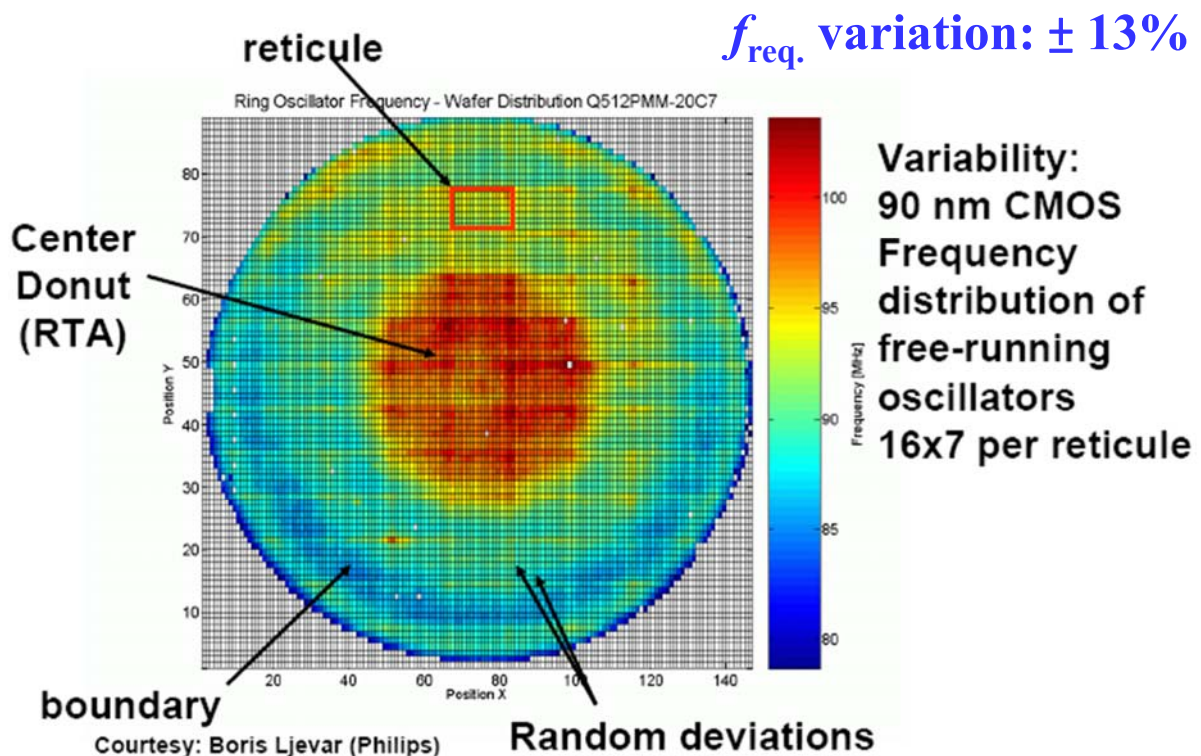
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## Process Variation

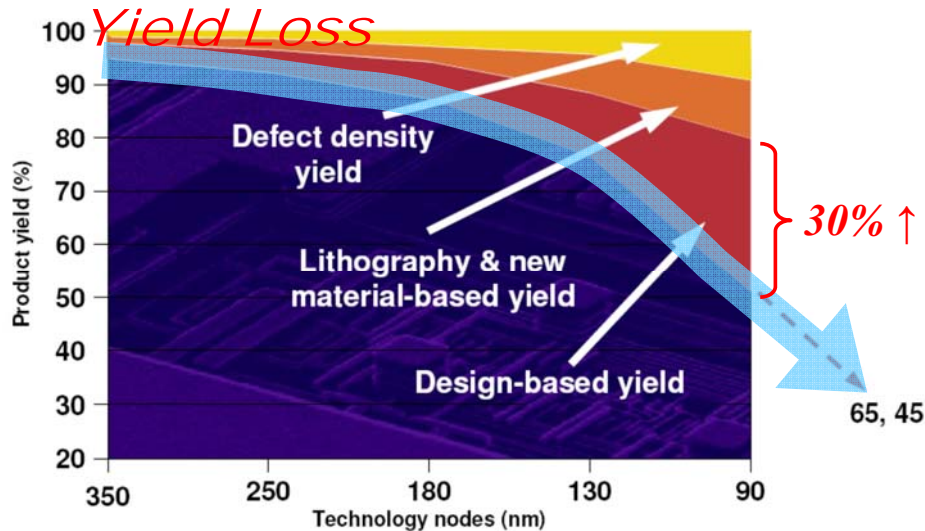


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# Yield Loss Issues

- ◆ In deep-submicron technology, **yield loss** issues are more and more serious
- ◆ Parametric variability will dominate yield loss



Ref: Michael Pronath, "Circuit Design for Yield with MunEDA WiCkEd", MunEDA Technical Forum 2008

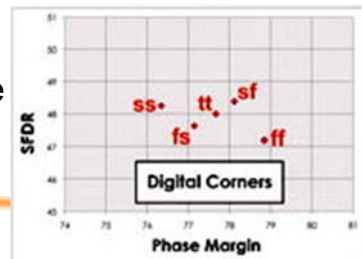
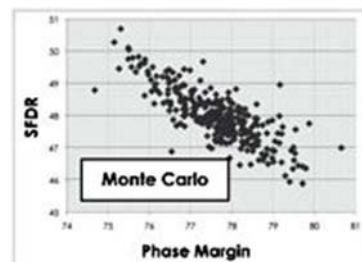
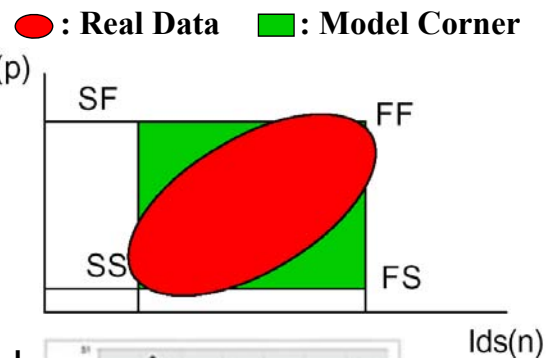


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# Corner Simulation

- ◆ Typical verification approach: simulating the **process corners**
  - Provided in technology file
  - Require only a few simulations
- ◆ Often results in over-design
  - Things may not go so worse
- ◆ The process corner may not be the real distribution corner
  - Wrong estimation
- ◆ There are more and more corners in advanced process
  - Combinations of every PVT corners (process, voltage, temperature) are huge
  - How to simulate hundreds of corners?



Courtesy: Solido Design Automation



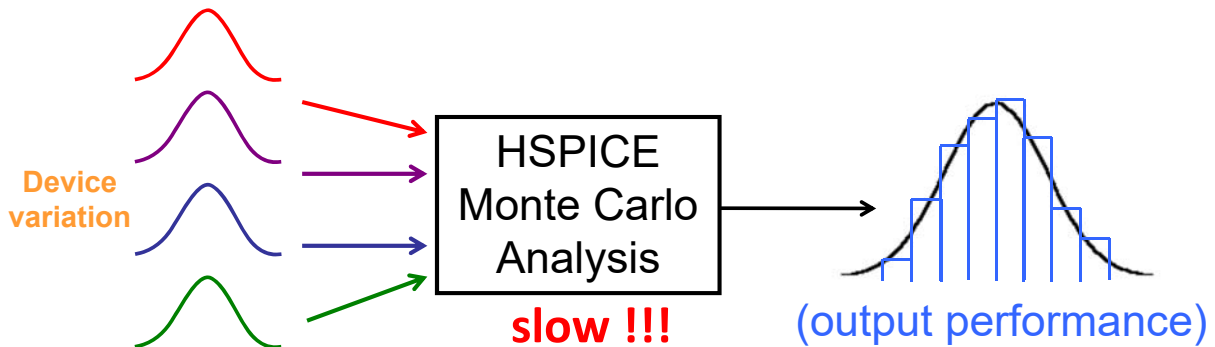
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# Monte Carlo (MC) Analysis

- ◆ MC analysis is a comprehensive method to check the process variation effects
  - Corner simulations often result in over design
- ◆ Simulate a circuit with **random samples of devices variations** (ex:  $W$ ,  $L$ ,  $V_{th}$ , and  $T_{ox}$  variations)
  - **Huge amount of simulations**
- ◆ **Transistor-level simulation** is often required for analog circuits
  - **Extremely time-consuming**

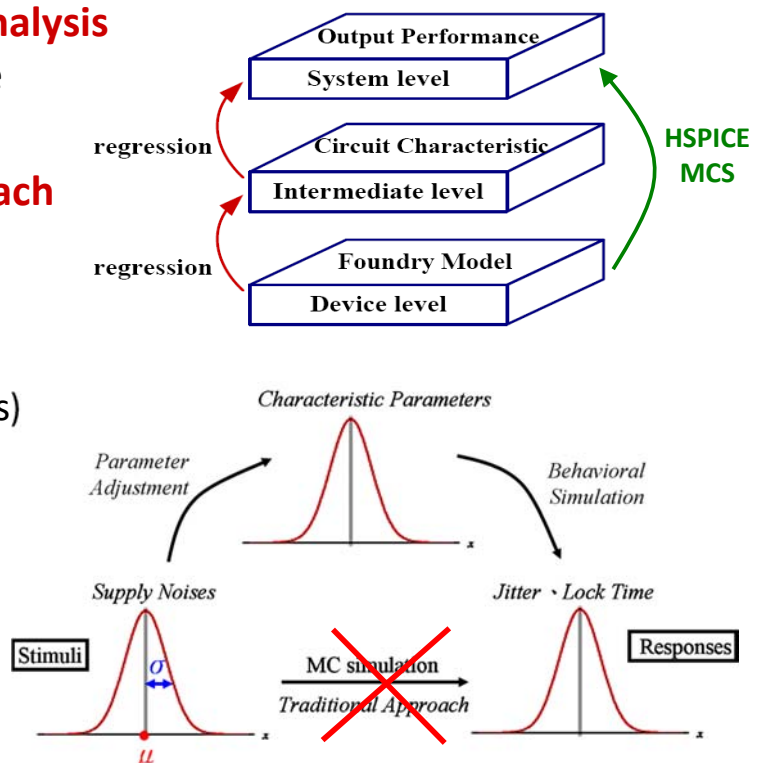


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## Hierarchical Statistical Analysis

- ◆ **Hierarchical statistical analysis** is popular to improve the analysis speed
- ◆ **Regression-based approach**
  - **Regression cost** is often expensive
  - **Poor observability** (only statistical numbers)
- ◆ Our approach: use **behavioral models**
  - Avoid fitting the final performance directly



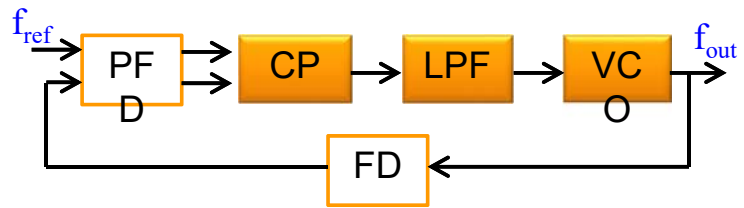
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# Behavioral Monte Carlo Analysis

## Behavioral Monte Carlo Simulation (BMCS)

- Take a CPPLL design as the first study case to analyze its process variation effects



## The behavioral model accuracy is the most critical issue

- Ideal top-down model is not accurate enough
- Use bottom-up method to extract actual circuit properties to improve the accuracy

## Sensitivity analysis (SA) and quasi-SA models are adopted instead of RSM

- Timing: traditional SA (linear)
- Analog: quasi-SA (non-linear)

C.C. Kuo, M.J. Lee, C.N. Liu, and C.J. Huang, "Fast Statistical Analysis of Process Variation Effects Using Accurate PLL Behavioral Models", *IEEE Trans. on Circuits and Systems I*, pp.1160-1172, Jun. 2009.



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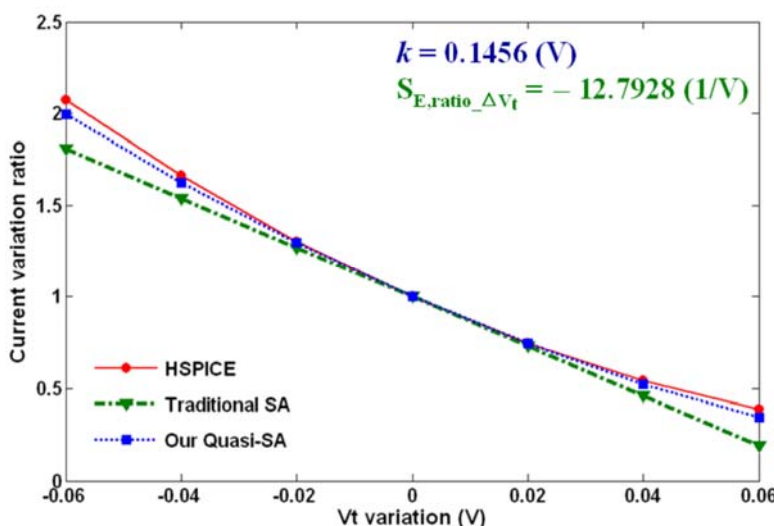
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## Quasi-SA for CP

### Estimate the current variation ratio under $V_t$ variation:

$$\begin{aligned} \text{ratio}(\Delta V_t) &= \frac{I_{CP}(\Delta V_t)}{I_{CP,0}} \cong \frac{[V_{GS} - (V_{t0} + \Delta V_t)]^2}{(V_{GS} - V_{t0})^2} = \left( \frac{(V_{GS} - V_{t0}) - \Delta V_t}{V_{GS} - V_{t0}} \right)^2 \\ &= \left( 1 - \frac{\Delta V_t}{V_{GS} - V_{t0}} \right)^2 = \left( 1 - \frac{\Delta V_t}{k} \right)^2 \end{aligned}$$

Extract the  $k$  value



Same extraction time as in traditional SA

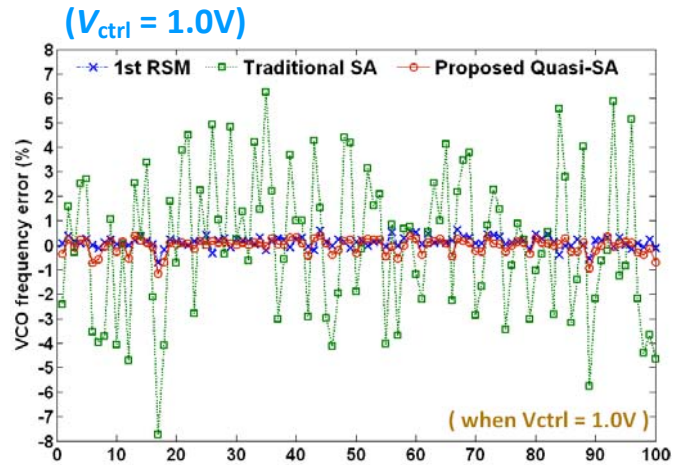
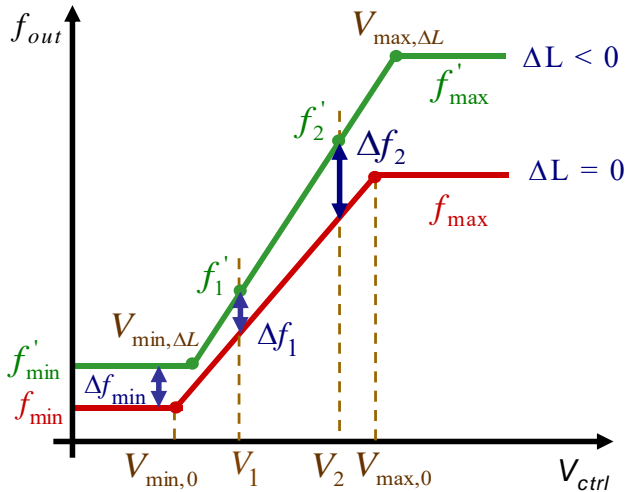
More accurate: similar to HSPICE results

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# Quasi-SA for VCO

- ◆ Traditional sensitivity analysis is not accurate in VCO
  - Different  $V_{ctrl}$  has different sensitivity
- ◆ Consider  $V_{ctrl}$  effects in the proposed model

**Quasi-SA model:**  
 $f_{VCO}$  error  $< \pm 1\%$



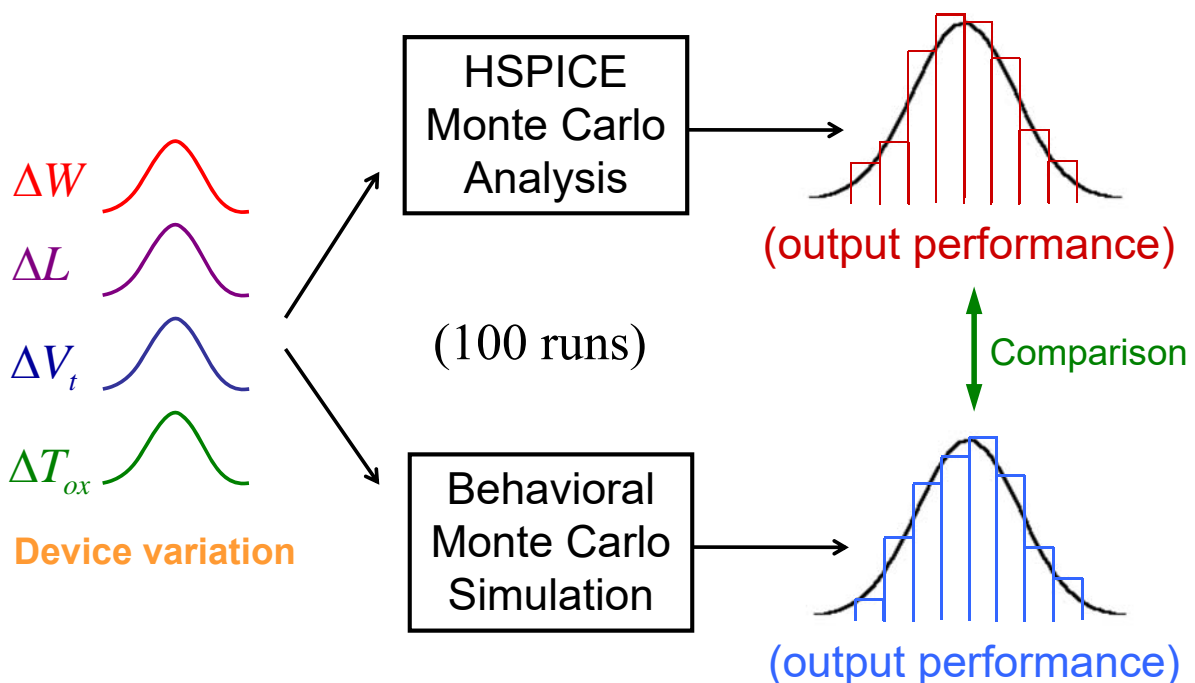
\*RSM: Response Surface Methodology



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## Comparison of Different MC Approaches

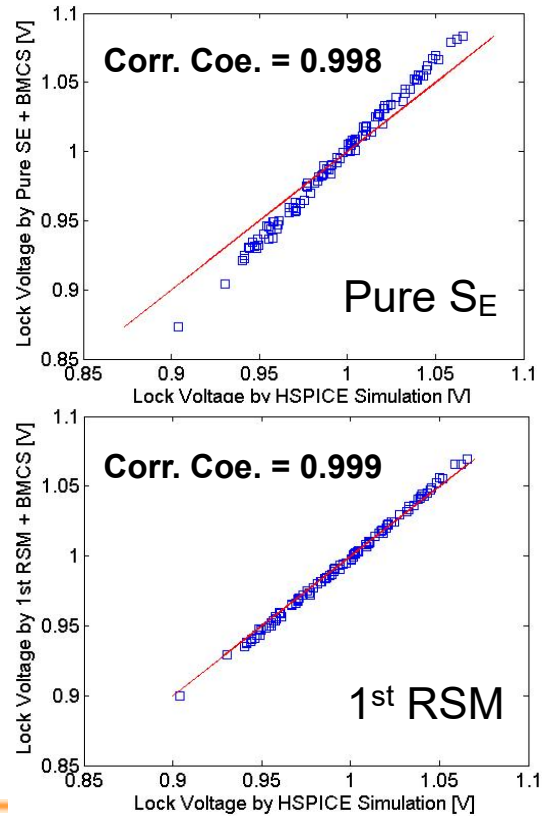
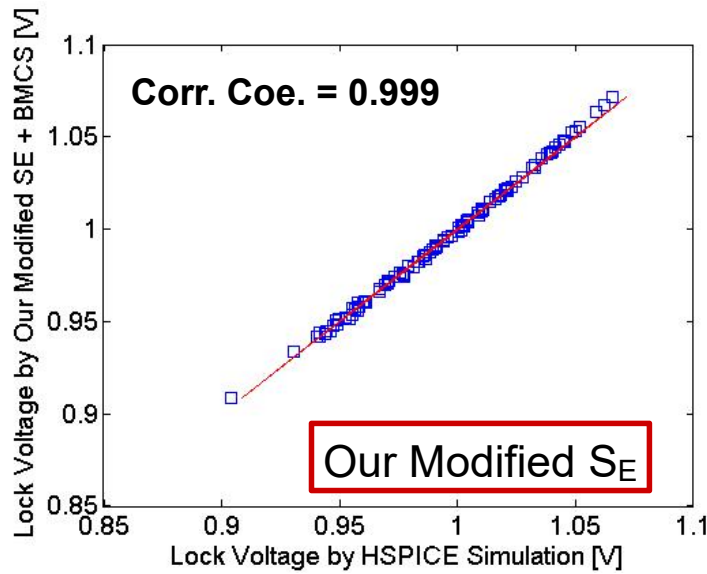


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# Scatter Plots – $V_{lock}$ (100 runs)

◆ **Corr. Coe. : correlation coefficient**



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## Comparison Results: 100-run MCS

$f_{out}$ : 800MHz		1 <sup>st</sup> RSM + BMCS	SA + BMCS	<b>Quasi-SA + BMCS</b>	HSPICE
$V_{lock}$ (V)	Mean	0.993 (-0.1%)	0.993 (-0.1 %)	<b>0.995 (0.1 %)</b>	<b>0.994</b>
	St. Dev.	0.036 (6.4%)	0.045 (32.1 %)	<b>0.035 (1.7 %)</b>	<b>0.034</b>
$T_{lock}$ (us)	Mean	3.449 (2.2%)	3.441 (2.0 %)	<b>3.438 (1.9 %)</b>	<b>3.374</b>
	St. Dev.	0.573 (-0.6%)	0.541 (-6.2 %)	<b>0.572 (-0.8 %)</b>	<b>0.576</b>
pk-pk Jitter (ps)	Mean	12.2 (-7.6%)	12.4 (-6.1 %)	<b>12.4 (-6.1 %)</b>	<b>13.2</b>
	St. Dev.	1.36 (-2.9%)	2.29 (63.6 %)	<b>1.41 (0.7 %)</b>	<b>1.40</b>
	Worst	16.6 (-2.4 %)	16.4 (-3.5 %)	<b>16.7 (-1.8 %)</b>	<b>17.0</b>
$T_{extract}$ (hr)		34.2	8.55	<b>8.55</b>	<b>N/A</b>
$T_{sim.}$ (hr)		2.95	2.93	<b>3.50</b>	<b>598.54</b>

St. Dev. : Standard Deviation

↑  
**Low regression cost & accurate**

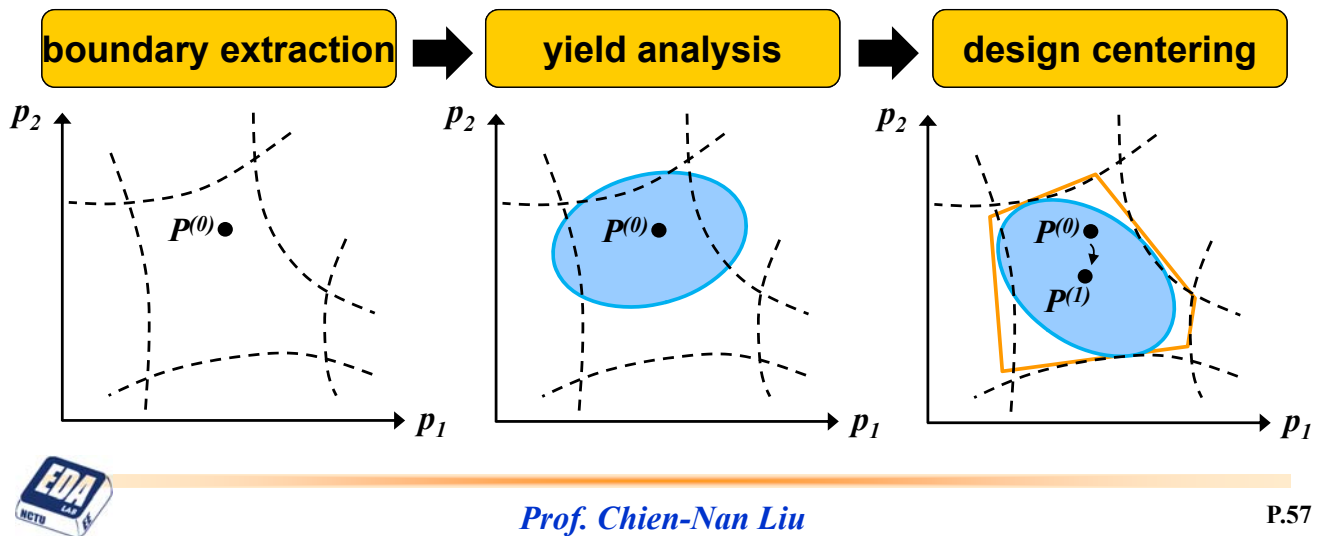


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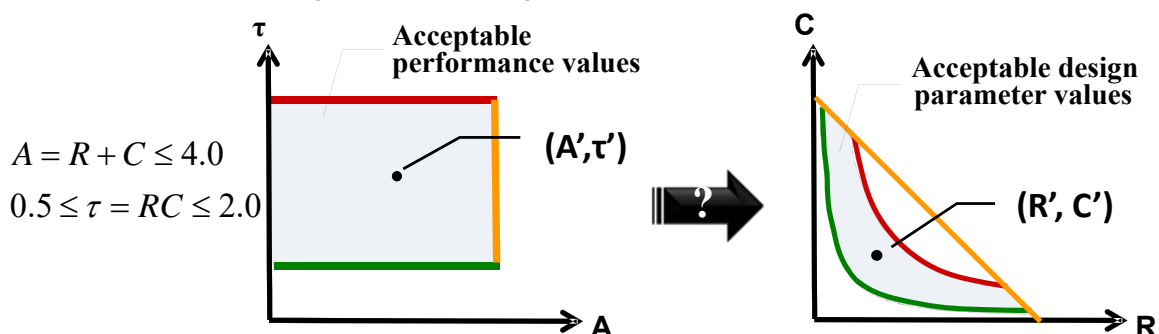
# Design Centering

- ◆ In early design stages, process variation impacts must be considered to reduce the yield loss
- ◆ **Design centering** approach is often used to improve the design-based yield
- ◆ Need to extract the boundary of the feasible design region before computing the “center” → **a heavy**



## Acceptable Design Region

- ◆ For analog circuits, it is not easy to figure out the acceptable design region at device level
  - Ex: a simple RC low-pass filter

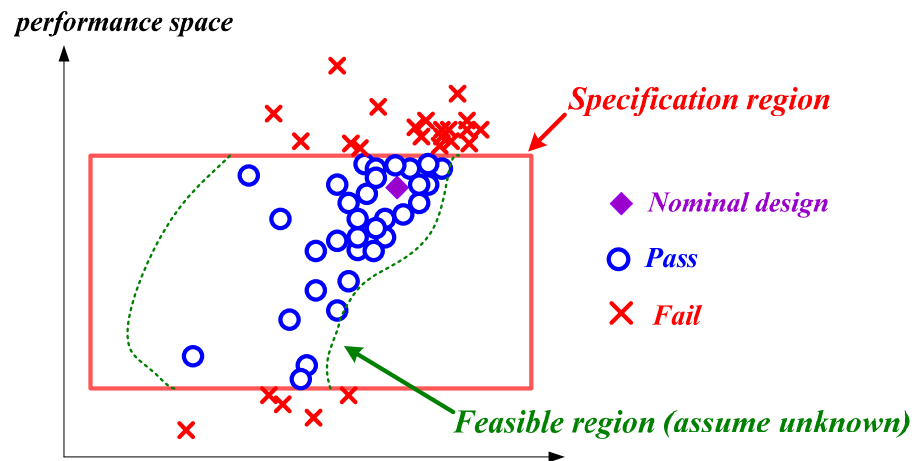


- ◆ Numerous design constraints are also big troubles
  - Ex: optimize a PLL using geometric programming approach
  - **40,000** optimization variables
  - **150,000** design constraints

Ref: Helmut E. Graeb, “Analog design centering and sizing”, Springer, 2007.  
 D. Colleran et al. “Optimization of Phase-Locked Loop Circuits via Geometric Programming,” CICC, 2003.

# Why not Forgetting the Boundary ?

- ◆ Performance distribution in the yield analysis has partial information of the feasible region
- ◆ **Reusing yield analysis results** has no extra simulation cost
  - Yield analysis is essential in the design flow
  - The heavy overhead for boundary extraction can be avoided

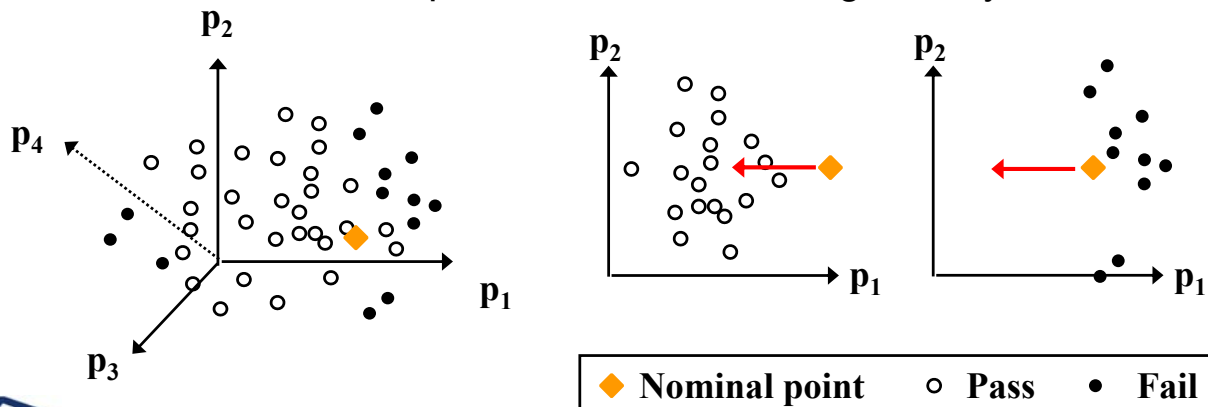


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# Force-Directed Nominal Point Moving

- ◆ Force-directed **nominal point moving (NPM)** algorithm
  - Close to the Pass group (attraction)
  - Far from the Fail group (repulsion)
  - The force equilibrium point is the new nominal point
- ◆ Iteratively calculate the forces until the nominal point is stable
  - May not find the best location in one calculation
  - Push the nominal point to better location gradually

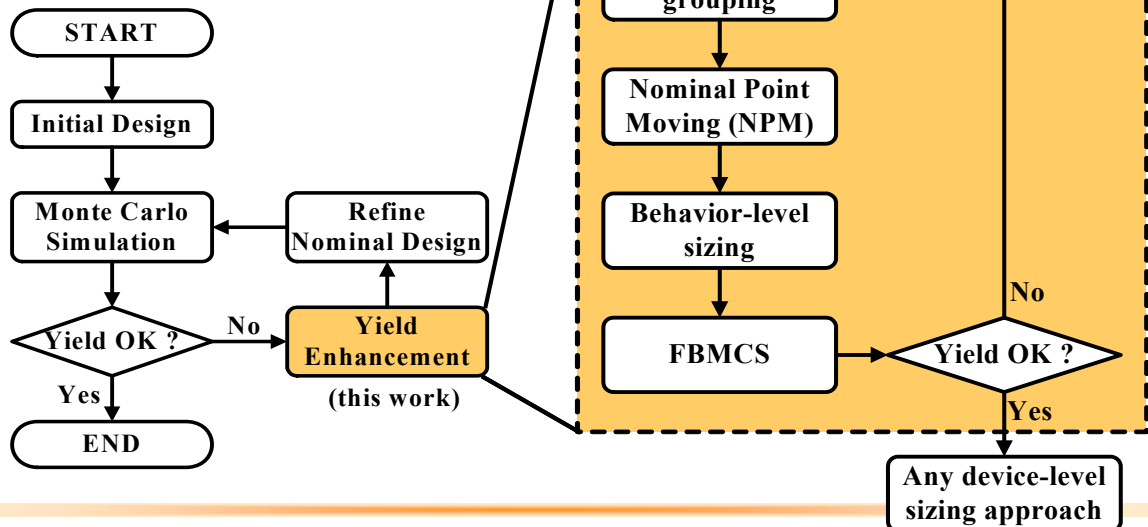


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# Proposed Yield Enhancement Flow

- ◆ Three major steps in the iterative yield enhancement flow
  - Use **force-directed model** to avoid boundary extraction cost
- ◆ Behavior-level yield enhancement approach is much faster
  - **A fast approximation !!**
  - Allow more iterations to approach the best solution

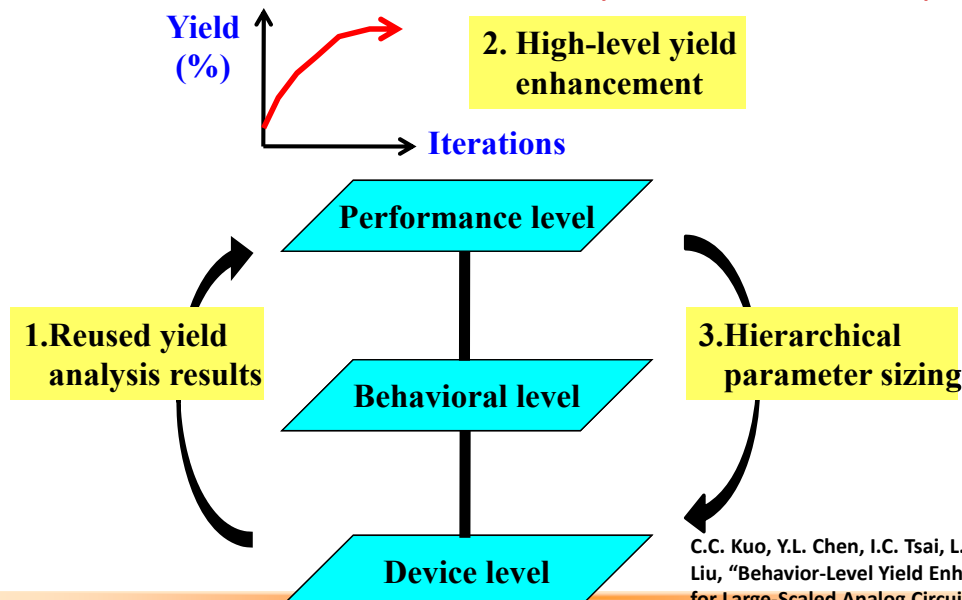


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# Behavior-Level Yield Enhancement

- ◆ Perform all steps at performance level and behavior level
  - **Reduce the iteration time** of the sizing-evaluation loop
- ◆ Perform device-level sizing/evaluation after yield enhancement
  - Become a one-time cost → **shorten yield enhancement process**



C.C. Kuo, Y.L. Chen, I.C. Tsai, L.Y. Chan, and C.N. Liu, "Behavior-Level Yield Enhancement Approach for Large-Scaled Analog Circuits", DAC 2010.

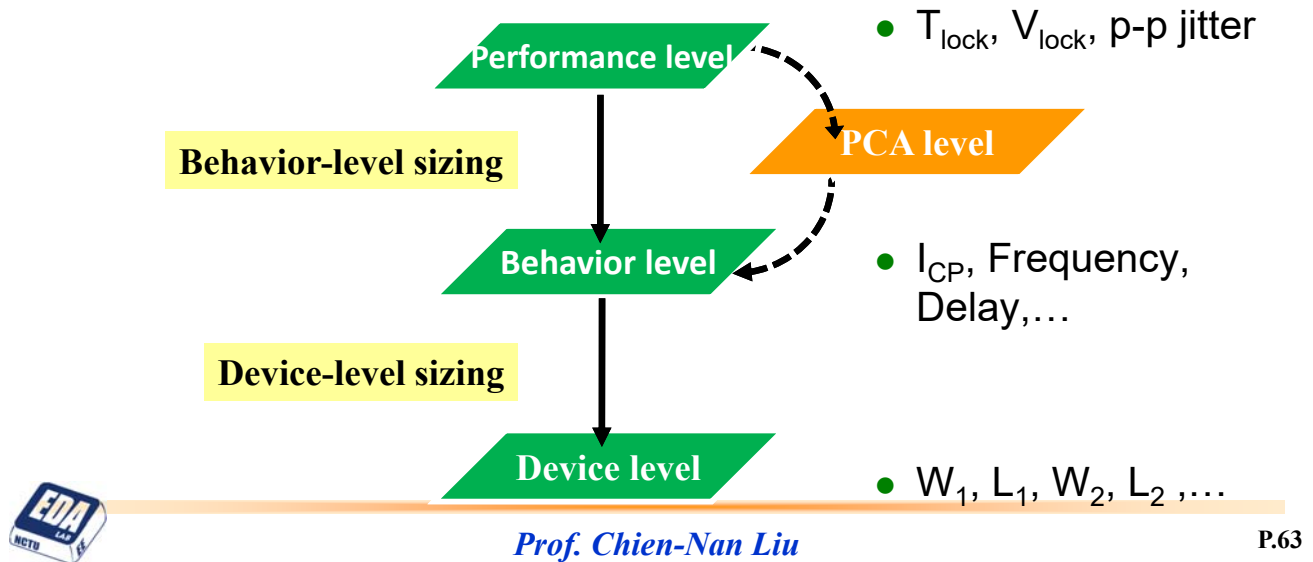
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# Behavior-Level Sizing

- ◆ Map the NPM results into behavioral parameters
- ◆ Hierarchical approach is often used for complicated analog circuits, such as PLLs
- ◆ Add an extra PCA level to reduce the regression efforts
  - PCA = Principal Component Analysis



## Principal Component Analysis

- ◆ Find a few linear combinations of behavioral parameters ( $B_j$ ) to represent the numerous samples

$$PC_i = \sum_{j=1}^n p_{ij} B_j$$

- PCs are orthogonal to each other
- ◆ Dimension reduction
  - Often results in fewer variables
- ◆ Include the correlation between parameters
  - Avoid infeasible solutions

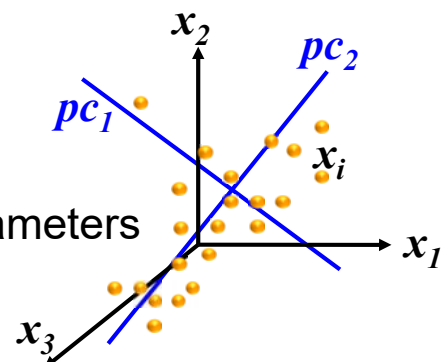
- ◆ Example:

- Variables:  $x_1, x_2, x_3$
- Principal component:  $pc_1(x_1, x_2, x_3), pc_2(x_1, x_2, x_3)$

$$pc_1 = a_{11}x_1 + a_{12}x_2 + a_{13}x_3 + \dots$$

$$pc_2 = a_{21}x_1 + a_{22}x_2 + a_{23}x_3 + \dots$$

⋮

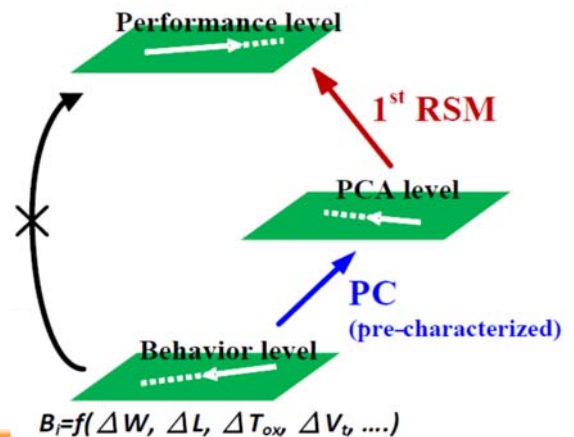




# FBMCS

- ◆ Is the yield of the new nominal design satisfied?
- ◆ How to perform next NPM without new distribution?
- ➡ **Fast Behavioral-level Monte Carlo Simulation (FBMCS)**
- ◆ It's an equation-based MC simulation
  - Generate random samples at behavior level
  - Translate to performance distribution through RSM equations
- ◆ Provide rough yield analysis to **guide next NPM**
  - Shorten the iteration time
  - Accurate analysis can be done after the iterations

PCs to performance:  $S_i = e_{io} + \sum_{j=0}^{m-1} d_{ij} PC_j$



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## Case Study: CPPLL

- ◆ This Charge-Pump PLL is consisted of 5 blocks
  - Phase-frequency detector (PFD), voltage-controlled oscillator (VCO), charge-pump (CP), low-pass filter (LPF), and frequency divider (FD)
  - Contain 163 transistors
- ◆ TSMC RF 0.18μm process
  - Process variation : ΔW, ΔL, ΔVt, ΔTox
- ◆ Simulation environment MC simulation:
  - 1000-run Behavioral MC simulation [17]
  - Analog Artist (Cadence) + Spectre
- ◆ Yield enhancement calculation :
  - Stop iterations when the yield value is stable within 1%
- ◆ Device sizing:
  - WiCkeD (MunEDA)

Performance	Specification
Lock voltage	1 V ± 0.2V
Lock time	< 5us
P-P jitter	< 34ps
Power	< 0.9mW

[17] C.C. Kuo, M.J. Lee, C.N. Liu, and C.J. Huang, "Fast Statistical Analysis of Process Variation Effects Using Accurate PLL Behavioral Models", *IEEE Trans. on Circuits and Systems I*, Jun. 2009.



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# Nominal Point Moving Results

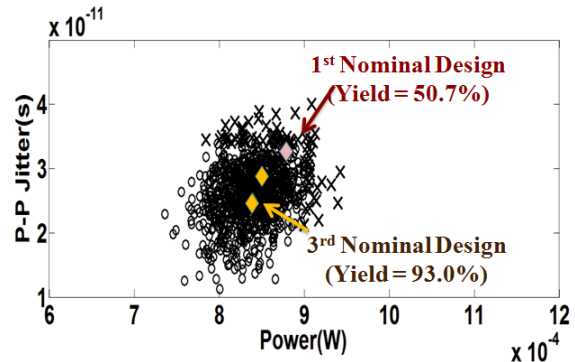
## Start from an existing design

- Nominal point meets all spec.
- Initial yield is only 50.7%

## Yield: 50.7% → 93.0%

- Only need 3 iterations

## Total run time: 4.43 seconds



Blocks	Parameters	Spec.	Initial Design	After Enhance
CPPLL (nominal)	V <sub>lock</sub> (V)	1 ± 0.2	0.99	1.08
	T <sub>lock</sub> (μs)	< 5	1.17	1.50
	pk-pk jitter (ps)	< 34	32.72	28.77
	power (mW)	<0.9	0.88	0.85
CP	Current ratio I <sub>ratio</sub>	—	1.00	1.00
	Switch time T <sub>sw</sub> (ns)		4.64	5.01
VCO	K <sub>VCO</sub> (GHz/V)		1.14	1.00
	f <sub>min</sub> (MHz)		317.3	275.5
	f <sub>max</sub> (MHz)		1036.1	904.1
Yield (%)			50.7	93.0

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# Device-Level Sizing Results

## Use commercial sizing tool to obtain the corresponding device sizes of the final nominal point

## Block-level sizing improves the sizing speed

- Use the obtained behavioral parameters as the sizing target of each sub-block
- Device sizing is performed block-by-block → **faster**
- Use the spec. directly for sizing the whole circuit is too slow

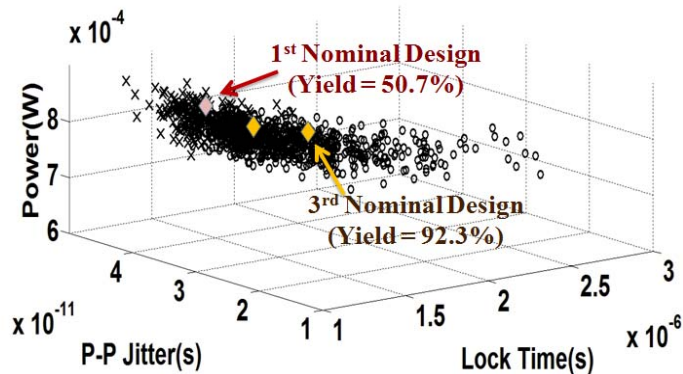
## A new circuit with the expected yield is really **achievable** !!

Blocks	Parameters	Spec.	Behavioral results	Whole PLL sizing	Block-level sizing
CPPLL (nominal)	V <sub>lock</sub> (V)	1 ± 0.2	1.08	1.11	1.09
	T <sub>lock</sub> (μs)	< 5	1.50	1.39	1.33
	jitter (ps)	< 34	28.77	25.59	26.9
	power (mW)	<0.9	0.85	0.86	0.86
Yield (%)			93.0	91.5	92.3
Area (μm <sup>2</sup> )			--	416.45	417.30
Optimization Time (min.)			0.07	300	6

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# Run Time Comparison

- ◆ Previous work about CPPLL circuits [3]
  - Use performance space exploration (PSE) method to extract the part of acceptable design region → **4-5 hours**
  - Behavior-level sizing → **1-2 hours**
- ◆ Only need **4.43 seconds** by using the proposed approach
  - Including NPM, behavior-level sizing, and FBMCS
- ◆ The final result has been confirmed with device-level sizing and evaluation



[3] J. Zou, D. Mueller, H. Graeb, and U. Schlichtmann, "A CPPLL Hierarchical Optimization Methodology Considering Jitter, Power and Locking Time", DAC'06



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## Conclusions

- ◆ Analog behavioral modeling is indeed useful for AMS system verification
  - Top-down behavioral modeling is for new designs
  - Bottom-up behavioral modeling is suitable for IP-based SOC designs
- ◆ Accurate behavioral models also have many useful applications
  - Analyze supply noise effects
  - Analyze design yield and make improvement
- ◆ CAD could also be useful to analog designers
  - Waiting for more investment !!!



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