

# Chapter 7

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## Chapter 7

### Section 7.1.1 martingale and deviance residuals

```
library(asauro)
library(survival)
#attach(pharmacoSmoking)
summary(pharmacoSmoking)
```

```
##      id          ttr          relapse          grp
## Min.   : 1.00   Min.   : 0.00   Min.   :0.000   combination:61
## 1st Qu.: 33.00   1st Qu.: 8.00   1st Qu.:0.000   patchOnly  :64
## Median : 67.00   Median : 49.00   Median :1.000
## Mean   : 66.15   Mean   : 77.44   Mean    :0.712
## 3rd Qu.: 99.00   3rd Qu.:182.00   3rd Qu.:1.000
## Max.   :130.00   Max.   :182.00   Max.    :1.000
##      age          gender          race          employment          yearsSmoking
## Min.   :22.00   Female:81   black   :38   ft      :72   Min.   : 9.00
## 1st Qu.:41.00   Male   :44   hispanic: 8   other:39   1st Qu.:22.00
## Median :49.00                                other   : 2   pt      :14   Median :30.00
## Mean   :48.84                                white   :77   Mean    :30.88
## 3rd Qu.:56.00                                Max.    :56.00
## levelSmoking ageGroup2 ageGroup4 priorAttempts longestNoSmoke
## heavy:89      21-49:66   21-34:16   Min.   : 0.00   Min.   : 0.0
## light:36      50+   :59   35-49:50   1st Qu.: 1.00   1st Qu.: 7.0
##                                50-64:48   Median : 2.00   Median : 90.0
##                                65+   :11   Mean    :12.68   Mean    :539.7
##                                3rd Qu.: 5.00   3rd Qu.:365.0
##                                Max.    :1000.00   Max.    :6205.0
```

```
priorAttemptsT <- pharmacoSmoking$priorAttempts
sum(priorAttemptsT > 20)
```

```
## [1] 4
priorAttemptsT[priorAttemptsT > 20] <- 20

result.0.coxph <- coxph(Surv(ttr, relapse) ~ 1, data=pharmacoSmoking)
rr.0 <- residuals(result.0.coxph, type="martingale")
sum(rr.0) #martingale residuals sum to zero!!

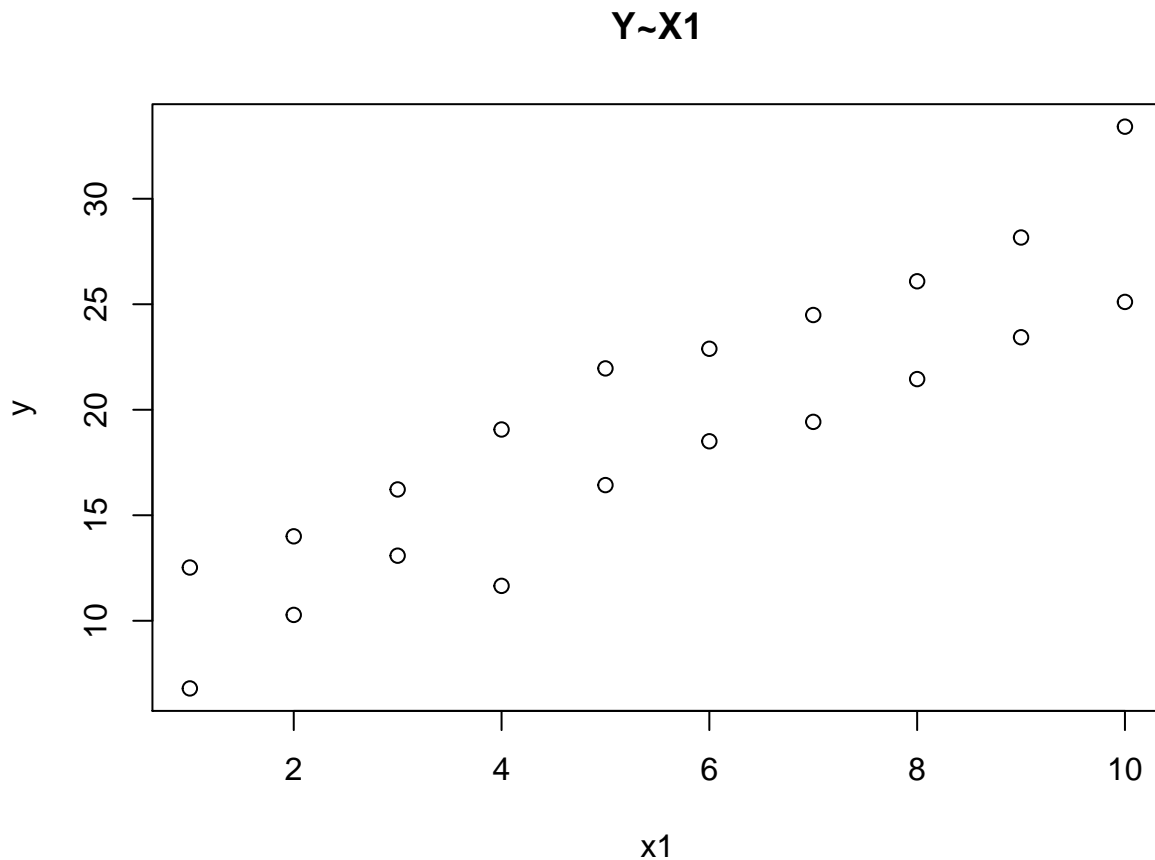
## [1] 4.884981e-15
summary(rr.0) #martingale residuals are less than 1

##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
## -1.2350 -1.2350  0.3029  0.0000  0.6949  0.9464
```

Motivation for the use of Martingale residuals to display covariate functional form

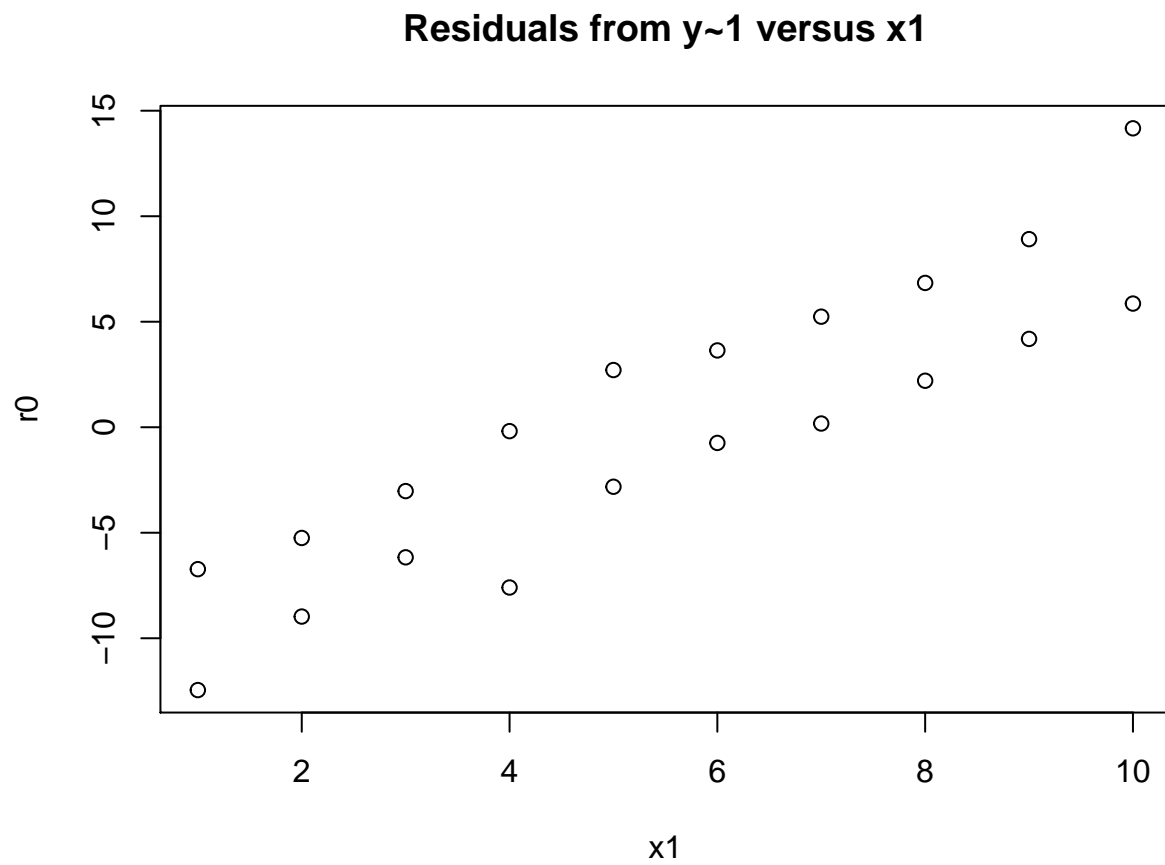
```
# simulate data for lm to see the idea
set.seed(1234)
x1 <- c(1:10, 1:10); x2 <- rep(c(1,2), each=10) #covariates
beta0 <- 1; beta1 <- 2; beta2 <- 5 #beta's
y <- rnorm(20, mean=beta0 + beta1*x1 + beta2*x2) #generate y's

plot(y~x1); title('Y~X1')
```



```
r0 <- resid(lm(y~1)) #residuals from model with no covariates
```

```
plot(r0~x1)
title('Residuals from y~1 versus x1')
```



```
plot(r0~x2)
title('Residuals from y~1 versus x2')
```

## Residuals from y~1 versus x2

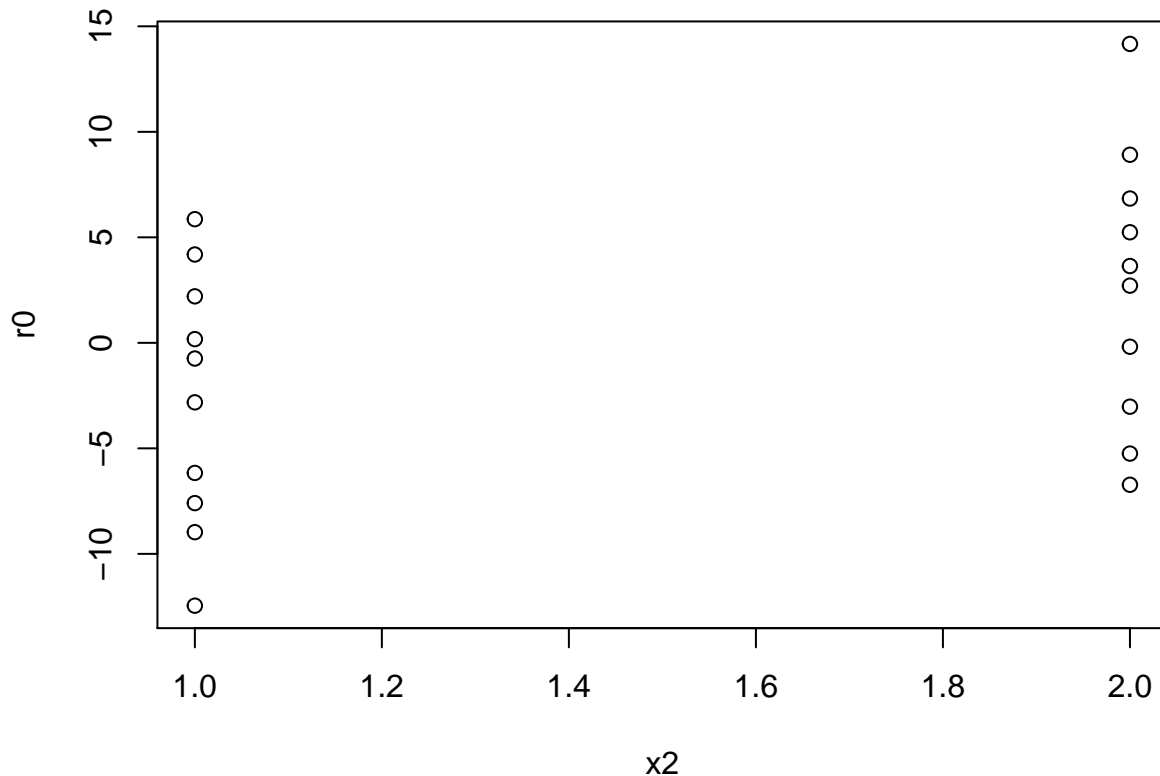


Figure 7.1

First, we need the “smoothSEcurve” function (also in the Appendix)

```
smoothSEcurve <- function(yy, xx) {
  # use after a call to "plot"
  # fit a lowess curve and 95% confidence interval curve
  xx.list <- min(xx) + ((0:100)/100)*(max(xx) - min(xx)) # make list of x values

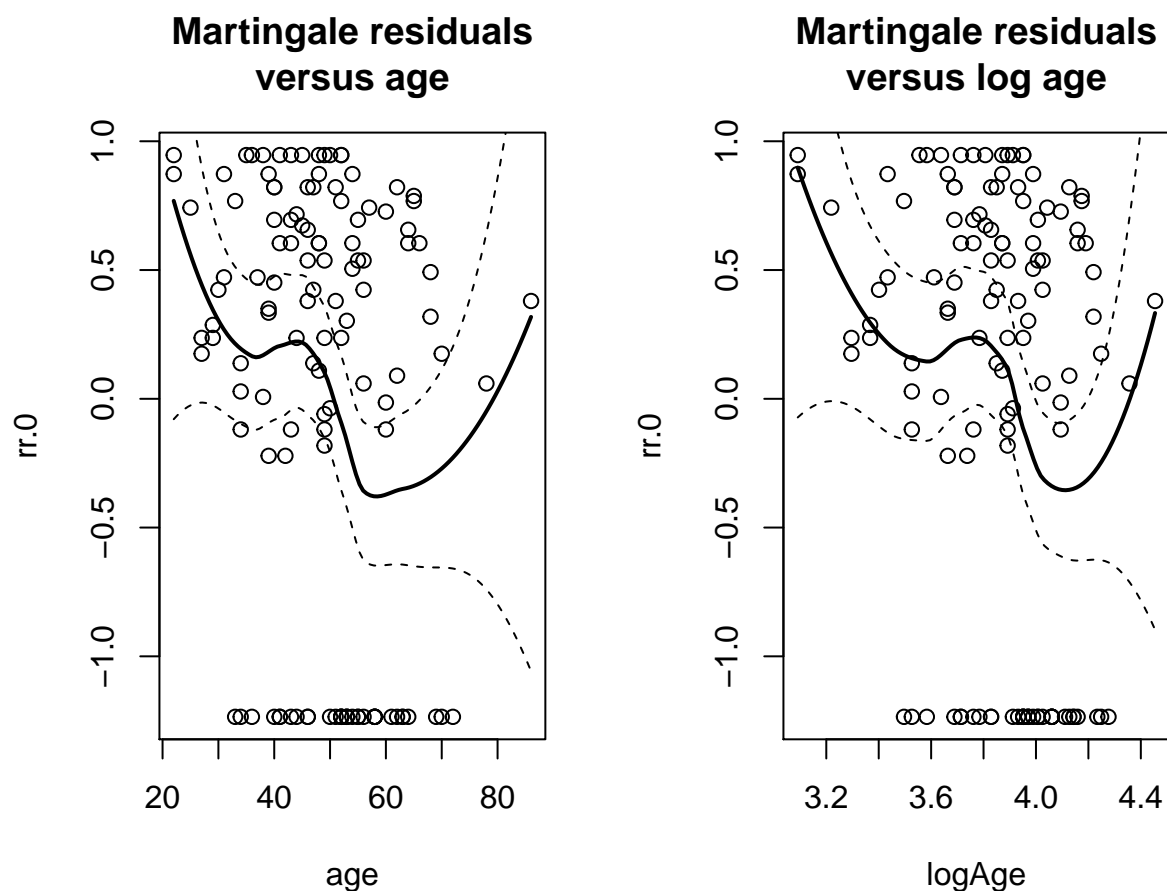
  # Then fit loess function through the points (xx, yy) at the listed values
  yy.xx <- predict(loess(yy ~ xx), se=T, newdata=data.frame(xx=xx.list))

  lines(yy.xx$fit ~ xx.list, lwd=2)
  lines(yy.xx$fit - qt(0.975, yy.xx$df)*yy.xx$se.fit ~ xx.list, lty=2)
  lines(yy.xx$fit + qt(0.975, yy.xx$df)*yy.xx$se.fit ~ xx.list, lty=2)
}

# Now the plot
oldpar=par(mfrow=c(1,2)) #save old graph params

plot(rr.0 ~ age, data=pharmacoSmoking)
smoothSEcurve(rr.0, pharmacoSmoking$age)
# Note that "\n" is a "newline" indicator
title("Martingale residuals\nversus age")
```

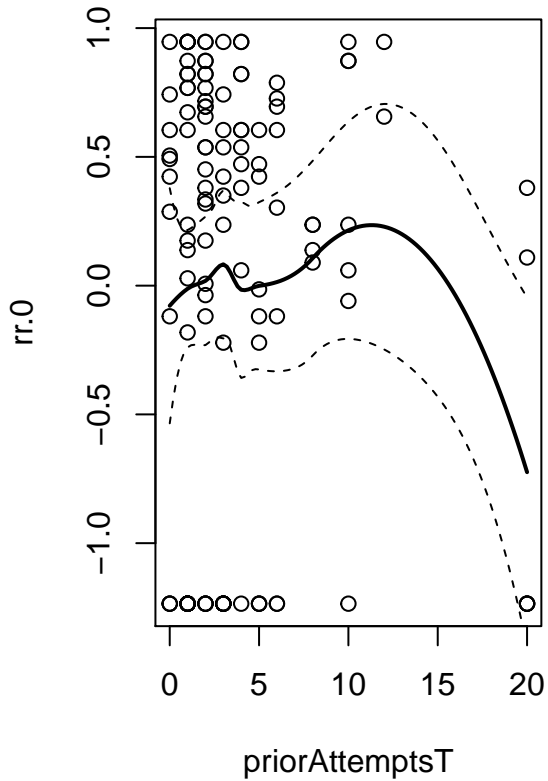
```
logAge <- log(pharmacoSmoking$age)
plot(rr.0 ~ logAge)
smoothSEcurve(rr.0, logAge)
title("Martingale residuals\nversus log age")
```



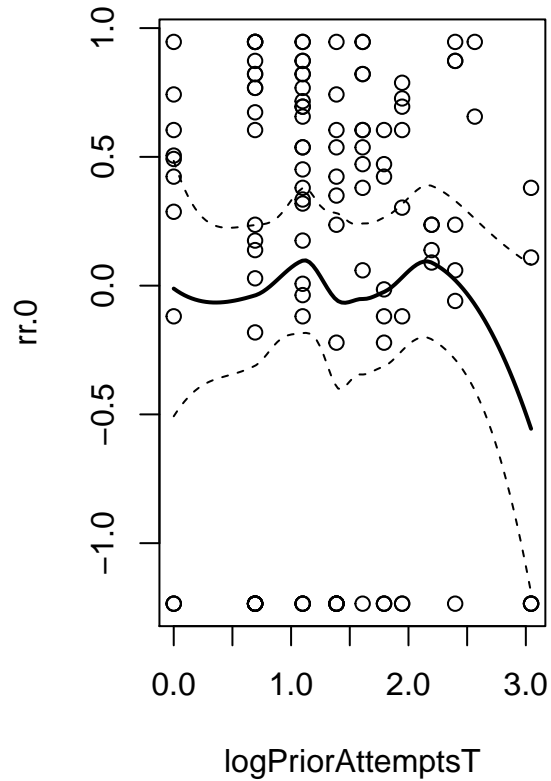
```
plot(rr.0 ~ priorAttemptsT)
smoothSEcurve(rr.0, priorAttemptsT)
title("Martingale residuals versus\nprior attempts")

logPriorAttemptsT <- log(priorAttemptsT + 1)
plot(rr.0 ~ logPriorAttemptsT)
smoothSEcurve(rr.0, logPriorAttemptsT)
title("Martingale residuals versus\nlog prior attempts")
```

**Martingale residuals versus  
prior attempts**



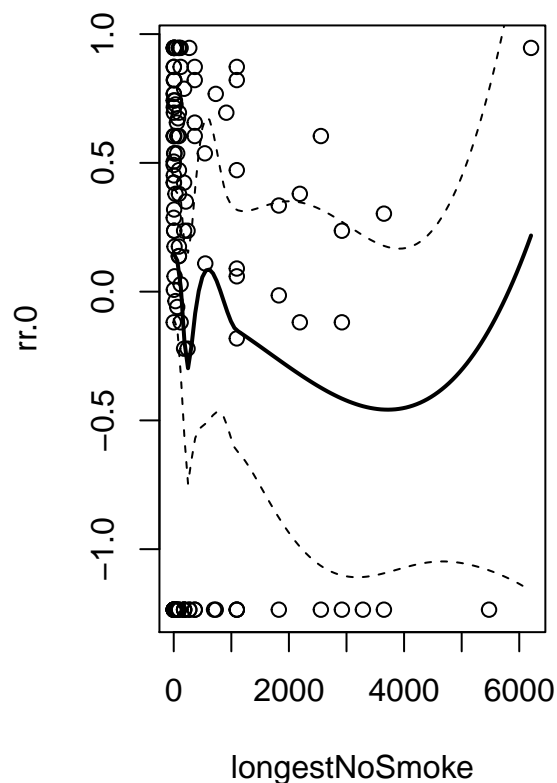
**Martingale residuals versus  
log prior attempts**



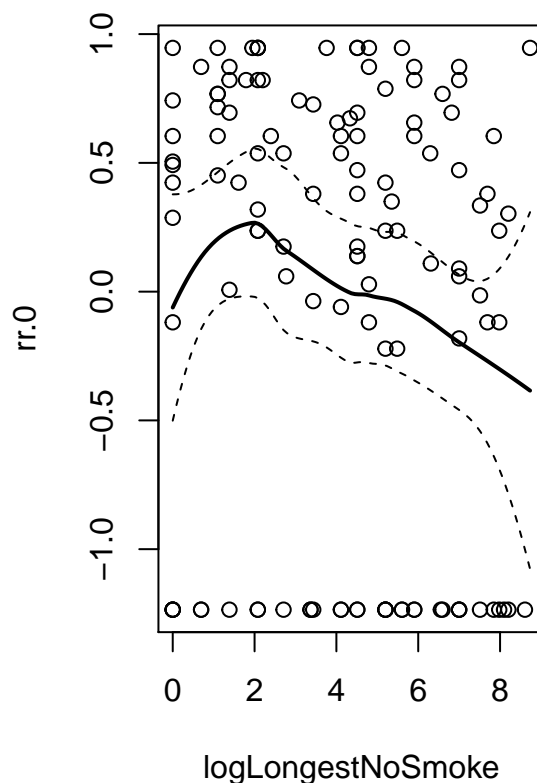
```
plot(rr.0 ~ longestNoSmoke, data=pharmacoSmoking)
smoothSEcurve(rr.0, pharmacoSmoking$longestNoSmoke)
title("Martingale residuals versus\nlongest period without smoking")

logLongestNoSmoke <- log(pharmacoSmoking$longestNoSmoke + 1)
plot(rr.0 ~ logLongestNoSmoke)
smoothSEcurve(rr.0, logLongestNoSmoke)
title("Martingale residuals versus\nlog of longest period without smoking")
```

**Martingale residuals versus  
longest period without smoking**



**Martingale residuals versus  
log of longest period without smoking**



```
par(oldpar)
```

```
#Use step to identify a good AIC model
```

```
# initial model
```

```
result.grp.coxph <- coxph(Surv(ttr, relapse) ~ grp, data=pharmacoSmoking)
```

```
result.step <- step(result.grp.coxph, scope=list(upper=~ grp +  
  gender + race + employment + yearsSmoking +  
  levelSmoking + age + priorAttemptsT +  
  logLongestNoSmoke, lower=~grp) )
```

```
## Start: AIC=766.32
```

```
## Surv(ttr, relapse) ~ grp
```

```
##
```

```
##           Df    AIC
```

```
## + age      1 762.48
```

```
## + logLongestNoSmoke 1 765.19
```

```
## + yearsSmoking 1 765.76
```

```
## <none>      766.32
```

```
## + employment 2 767.24
```

```
## + gender     1 767.43
```

```
## + priorAttemptsT 1 767.63
```

```
## + levelSmoking 1 768.27
```

```
## + race       3 770.72
```

```
##
```

```
## Step: AIC=762.48
```

```
## Surv(ttr, relapse) ~ grp + age
```

```
##
```

```
##              Df      AIC
## + employment      2 758.28
## + logLongestNoSmoke 1 761.99
## <none>              762.48
## + yearsSmoking     1 764.12
## + gender           1 764.20
## + priorAttemptsT   1 764.28
## + levelSmoking     1 764.48
## - age              1 766.32
## + race             3 766.52
##
## Step:  AIC=758.28
## Surv(ttr, relapse) ~ grp + age + employment
##
##              Df      AIC
## <none>              758.28
## + logLongestNoSmoke 1 758.55
## + yearsSmoking     1 759.80
## + priorAttemptsT   1 759.87
## + gender           1 760.27
## + levelSmoking     1 760.28
## + race             3 761.10
## - employment      2 762.48
## - age             1 767.24

result.step

## Call:
## coxph(formula = Surv(ttr, relapse) ~ grp + age + employment,
##       data = pharmacoSmoking)
##
##              coef exp(coef) se(coef)      z      p
## grppatchOnly    0.6079     1.8365  0.2184  2.78 0.0054
## age            -0.0353     0.9653  0.0108 -3.28 0.0010
## employmentother 0.7035     2.0208  0.2693  2.61 0.0090
## employmentpt    0.6537     1.9226  0.3273  2.00 0.0458
##
## Likelihood ratio test=22  on 4 df, p=0.000198
## n= 125, number of events= 89
```

Figure 7.2

```
rr.final <- residuals(result.step, type="martingale")

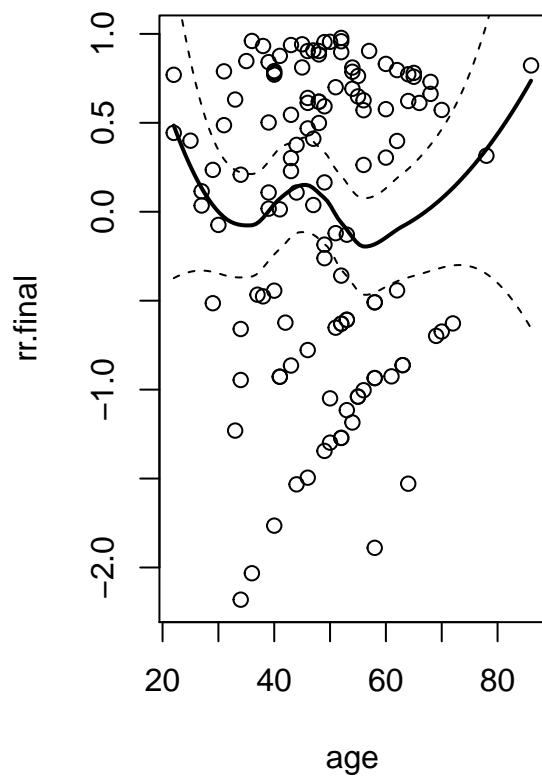
oldpar <- par(mfrow=c(1,2))

plot(rr.final ~ age, data=pharmacoSmoking)
smoothSEcurve(rr.final, pharmacoSmoking$age)
title("Martingale residuals\nversus age")

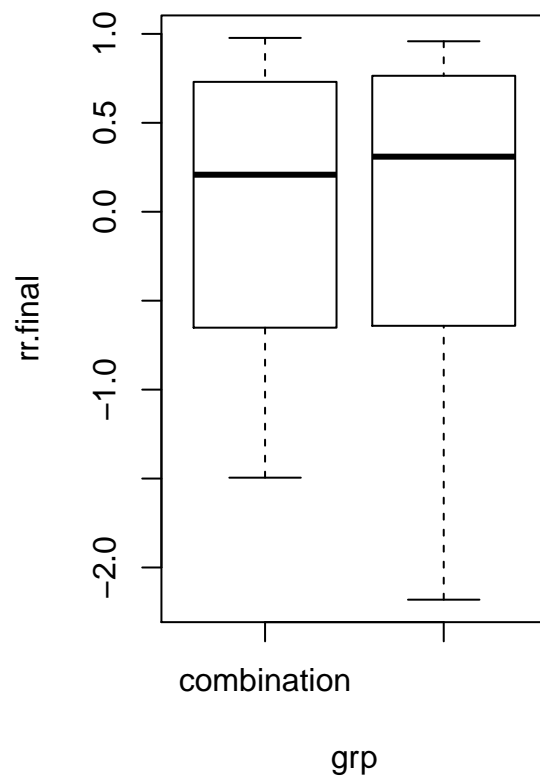
plot(rr.final ~ grp, data=pharmacoSmoking)
title("Martingale residuals\nversus treatment group")
```



**Martingale residuals  
versus age**

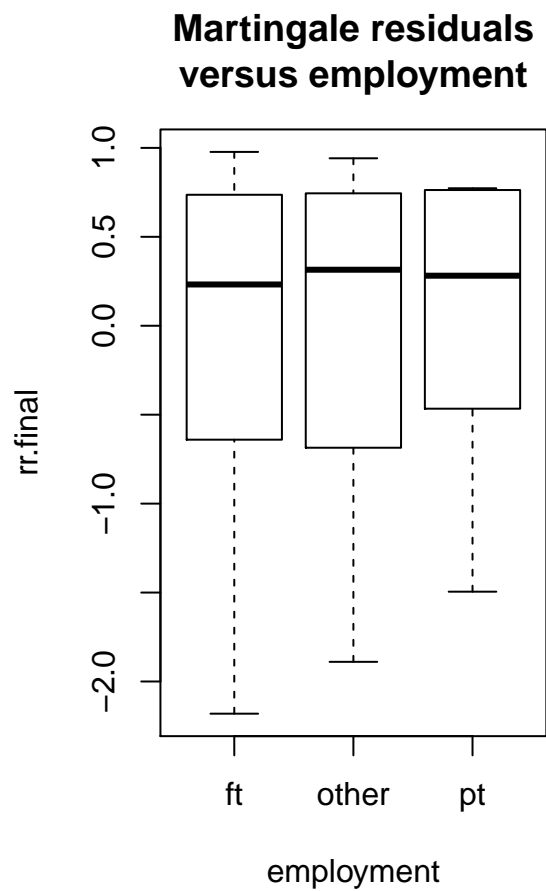


**Martingale residuals  
versus treatment group**



```
plot(rr.final ~ employment, data=pharmacoSmoking)
title("Martingale residuals\nversus employment")

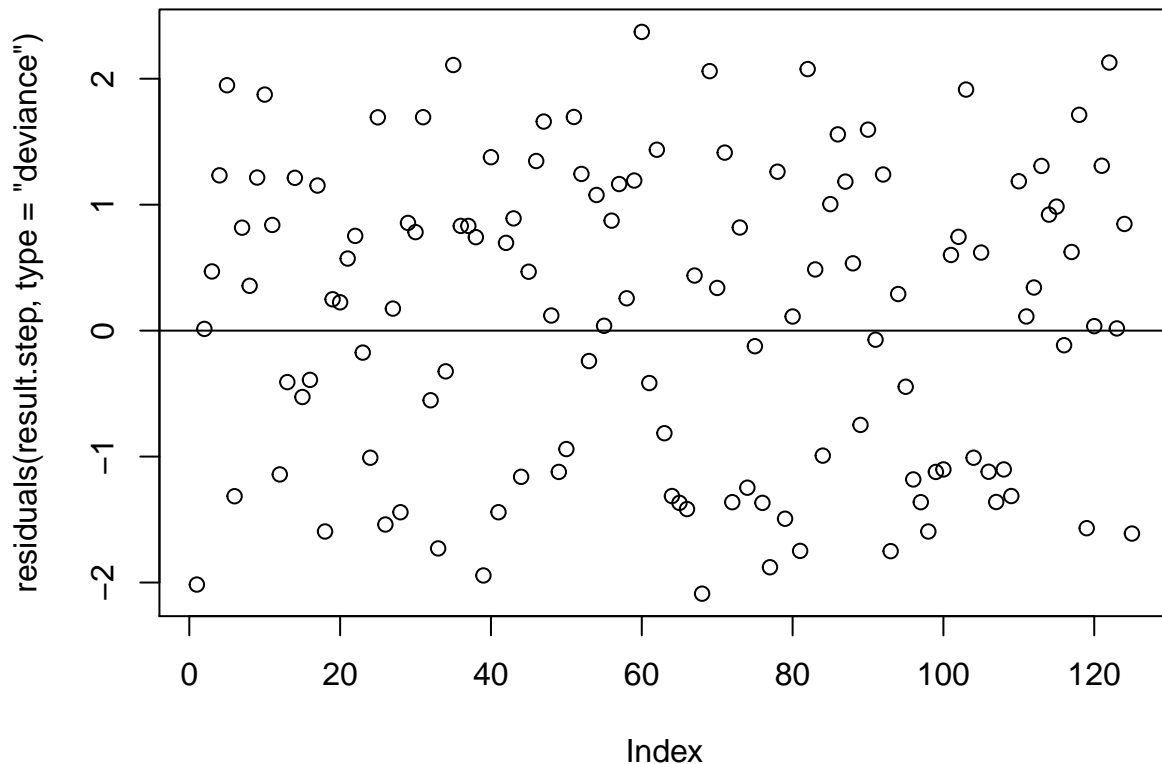
par(oldpar)
```



Deviance residuals are used for outlier detection. Plots of these should look like a random normal sample when there is light to moderate censoring.

```
plot(residuals(result.step, type="deviance") )  
abline(h=0)  
title('Deviance residuals for final model')
```

## Deviance residuals for final model



### Section 7.1.2 case deletion residuals

```
result.coxph <- coxph(Surv(ttr, relapse) ~ grp + employment + age, data=pharmacoSmoking)
coef.all <- result.coxph$coef[4] #extract coef for age
coef.all
```

```
##          age
## -0.03528934
```

```
n.obs <- nrow(pharmacoSmoking)
```

```
# this is the way the book computes the jackknife resids
```

```
jkbeta.vec <- rep(NA, n.obs)
```

```
attach(pharmacoSmoking) #this can lead to errors if you have variables with the same
# names in your workspace!!!
```

```
for (i in 1:n.obs) {
  tt.i <- ttr[-i]
  delta.i <- relapse[-i]
  grp.i <- grp[-i]
  employment.i <- employment[-i]
  age.i <- age[-i]
  result.coxph.i <- coxph(Surv(tt.i, delta.i) ~ grp.i +
    employment.i + age.i)
  coef.i <- result.coxph.i$coef[4]
  jkbeta.vec[i] <- (coef.all - coef.i)
```

```

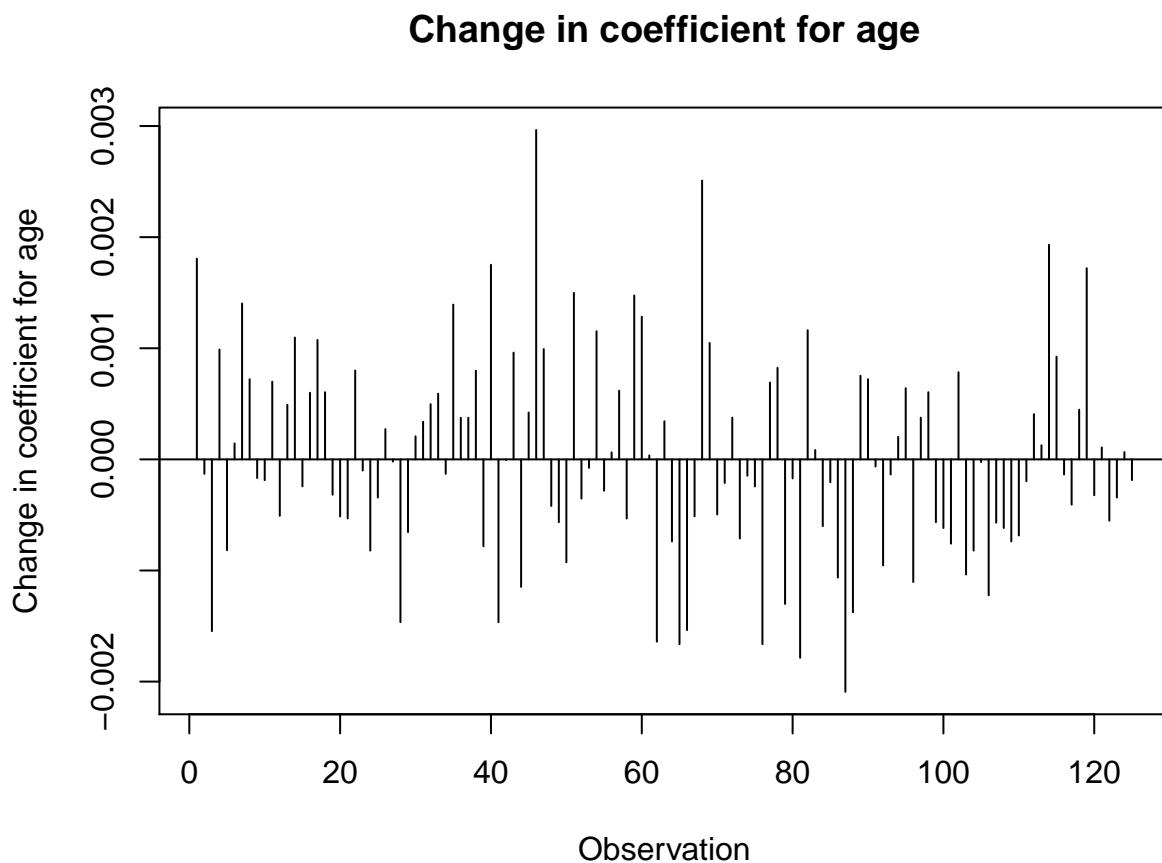
}
detach(pharmacoSmoking)

# this is a more efficient way to compute the jackknife resids
jackbeta.vec <- rep(NA, n.obs)
for (i in 1:n.obs){
  result.coxph.i <- coxph(Surv(ttr, relapse) ~ grp + employment + age,
                          data=pharmacoSmoking, subset=(i != (1:n.obs)))
  jackbeta.vec[i] <- result.coxph.i$coef[4]
}
jackbeta.vec <- coef.all - jackbeta.vec

sum(jackbeta.vec!=jkbeta.vec) # the two methods are equivalent

## [1] 0
index.obs <- 1:n.obs
plot(jkbeta.vec ~ index.obs, type="h",
     xlab="Observation", ylab="Change in coefficient for age")
abline(h=0)
title('Change in coefficient for age')

```



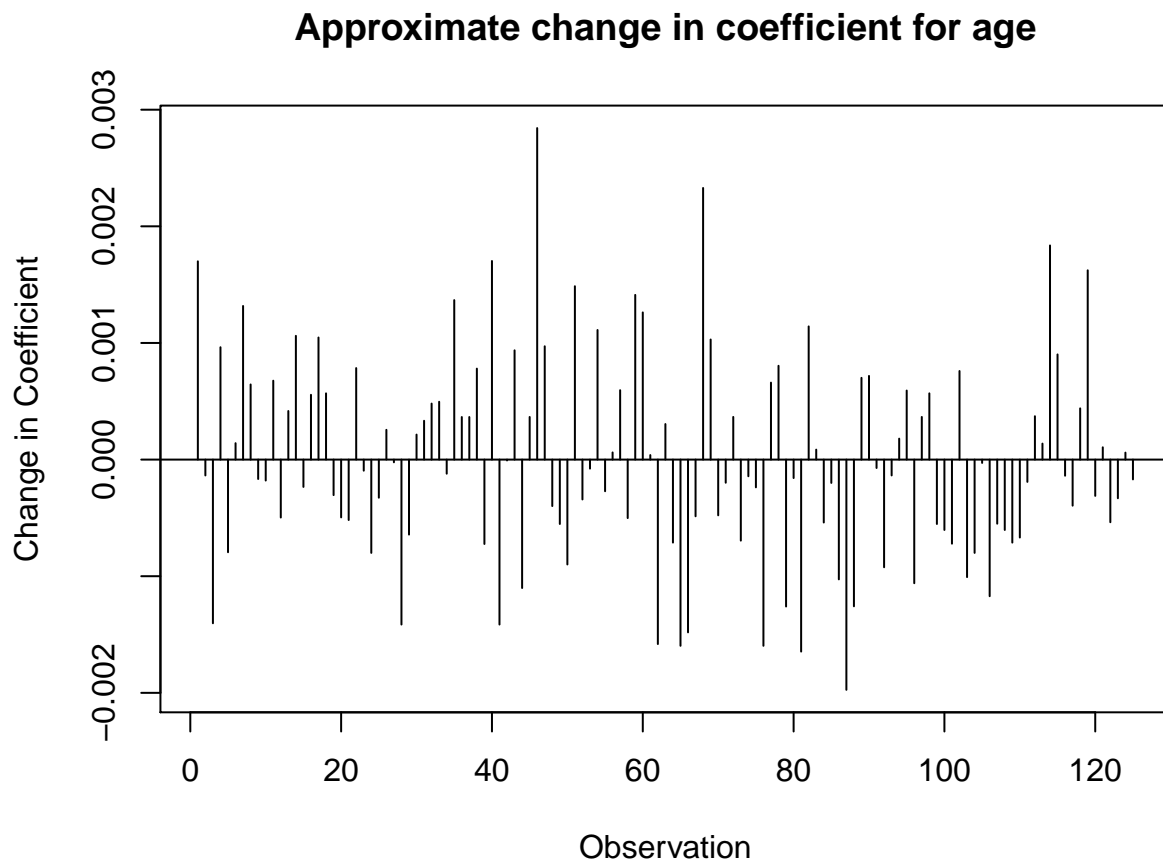
```

#identify(jkbeta.vec ~ index.obs) # click on points to get their identifying label.
# Press the "Esc" button to quit the "identify" mode.

```

dfbeta residuals (dfbetas are scaled by standard error of coefficients)

```
resid.dfbeta <- residuals(result.coxph,type='dfbeta')
plot(resid.dfbeta[,4]~index.obs, type='h', xlab='Observation', ylab='Change in Coefficient')
abline(h=0)
title('Approximate change in coefficient for age')
```



## Checking the proportional hazards assumption

Section 7.2.1; log cumulative hazard plots

```
#attach(pancreatic2)
summary(pancreatic2)
```

```
##      pfs          os      status  stage
##  Min.   : 36.0    Min.   : 36.0    Min.   :1   LA: 8
##  1st Qu.: 57.0    1st Qu.:109.0    1st Qu.:1   M :33
##  Median :119.0    Median :192.0    Median :1
##  Mean   :178.6    Mean   :255.4    Mean   :1
##  3rd Qu.:185.0    3rd Qu.:361.0    3rd Qu.:1
##  Max.   :975.0    Max.   :975.0    Max.   :1
```

```
#pfs.month <- pancreatic2$pfs/30.25  #this creates a global variable in the workspace
#locally advanced
```

```
result.surv.LA <- survfit(Surv(pfs/30.25, status) ~ stage, subset={stage == "LA"}, data=pancreatic2)
time.LA <- result.surv.LA$time
```

```

surv.LA <- result.surv.LA$surv
surv.LA  #last value is zero!

## [1] 0.875 0.750 0.625 0.500 0.375 0.250 0.125 0.000

cloglog.LA <- log(-log(surv.LA))[-length(surv.LA)]
logtime.LA <- log(time.LA)[-length(surv.LA)]

#metastatic
result.surv.M <- survfit(Surv(pfs/30.25, status) ~ stage, subset={stage == "M"}, data=pancreatic2)
time.M <- result.surv.M$time
surv.M <- result.surv.M$surv
surv.M  #last value is zero!

## [1] 0.96969697 0.93939394 0.90909091 0.87878788 0.81818182 0.78787879
## [7] 0.75757576 0.72727273 0.69696970 0.63636364 0.60606061 0.54545455
## [13] 0.51515152 0.48484848 0.45454545 0.42424242 0.39393939 0.36363636
## [19] 0.33333333 0.30303030 0.27272727 0.24242424 0.21212121 0.18181818
## [25] 0.15151515 0.12121212 0.09090909 0.06060606 0.03030303 0.00000000

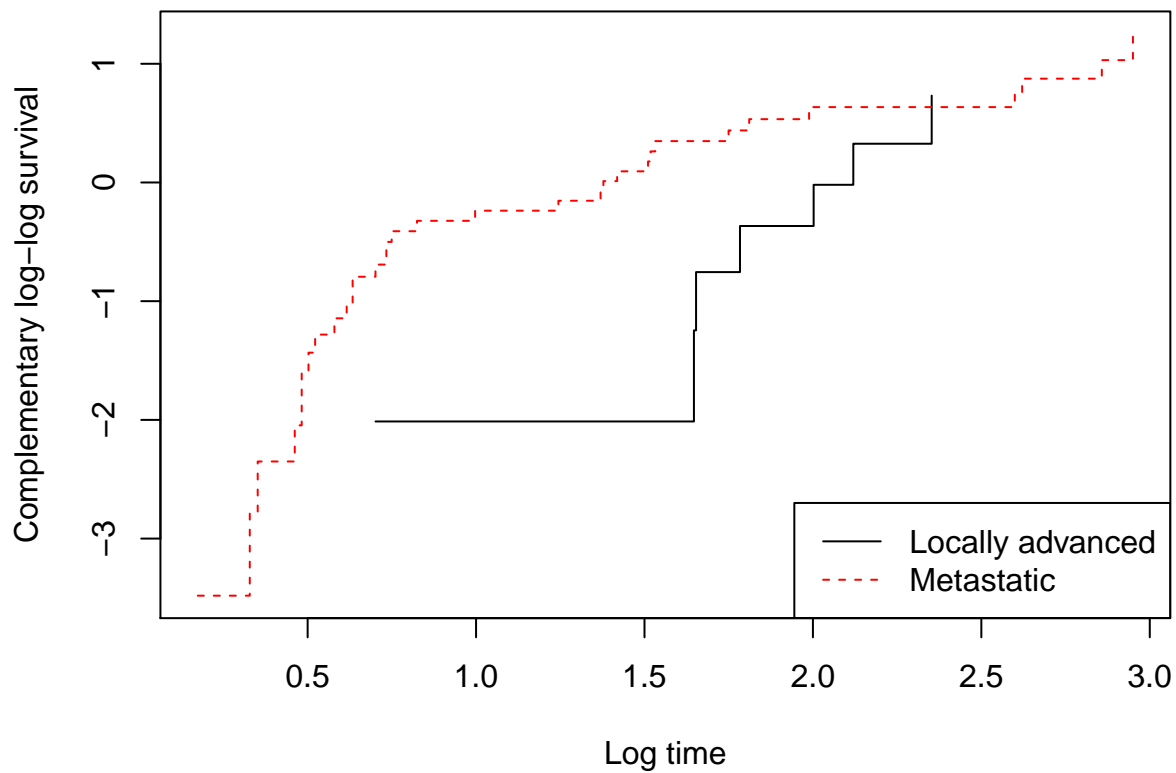
cloglog.M <- log(-log(surv.M))[-length(surv.M)]
logtime.M <- log(time.M)[-length(surv.M)]

# Fig 7.4 - ### the book's plot does not cover the entire graph!!

plot(cloglog.LA ~ logtime.LA, type="s", col=1,lty=1, xlim=c(min(logtime.LA,logtime.M),
  max(logtime.LA,logtime.M)), ylim=c(min(cloglog.LA,cloglog.M),max(cloglog.LA,cloglog.M)),
  xlab="Log time", ylab="Complementary log-log survival")
lines(cloglog.M ~ logtime.M, col=2,lty=2, type="s")
legend("bottomright", legend=c("Locally advanced", "Metastatic"),
  col=1:2, lty=1:2)
title('Cloglog of Survival curves for Locally advanced, Metastatic patients')

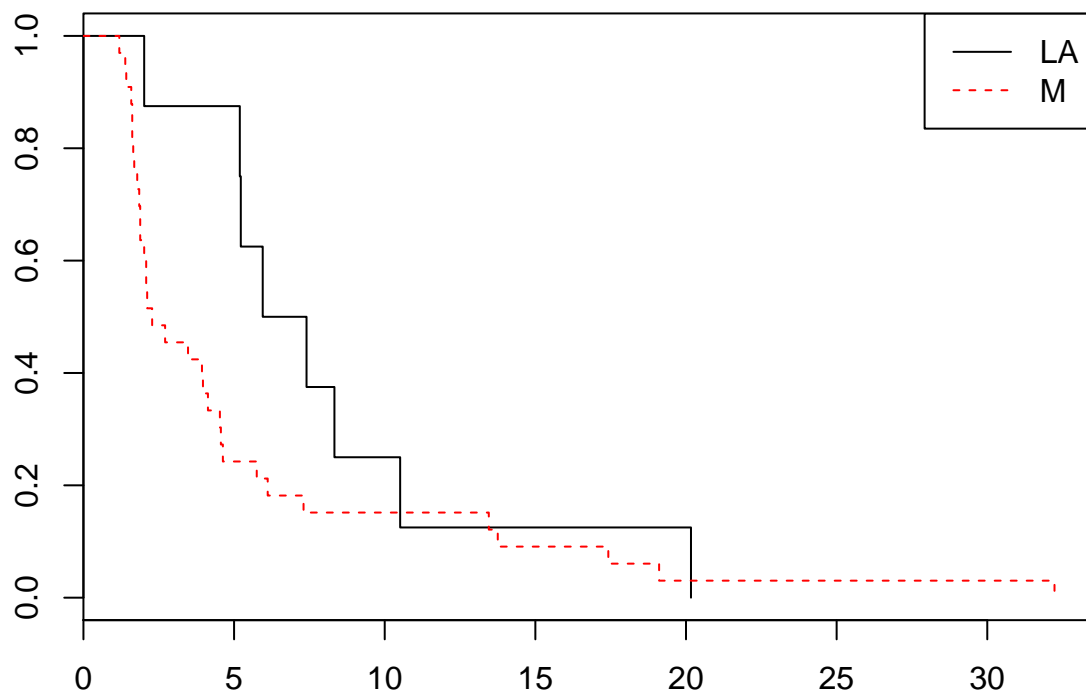
```

## Cloglog of Survival curves for Locally advanced, Metastatic patient:



```
# plot survival curves using survfit
plot(survfit(Surv(pfs/30.25, status) ~ stage, data=pancreatic2),lty=1:2, col=1:2)
legend('topright',levels(pancreatic2$stage),lty=1:2, col=1:2)
title('Progression-free survival versus stage')
```

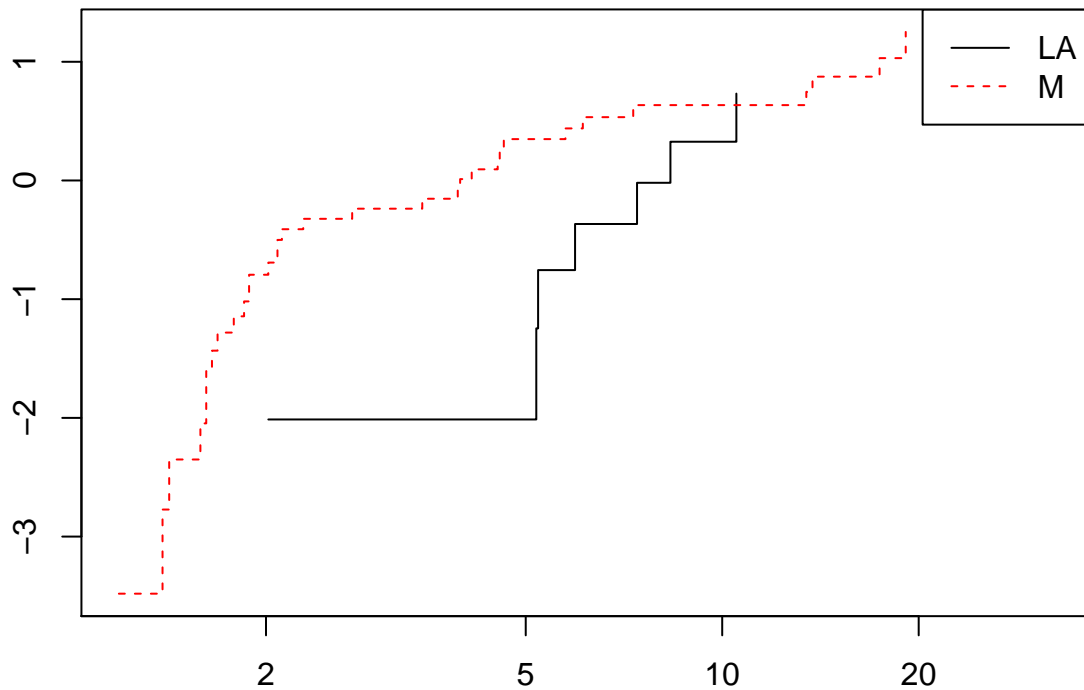
## Progression-free survival versus stage



```
# This is a better way to get cloglog of survivor curves
plot(survfit(Surv(pfs/30.25, status) ~ stage, data=pancreatic2),fun='cloglog',
     lty=1:2, col=1:2)
legend('topright',levels(pancreatic2$stage),lty=1:2, col=1:2)
title('Cloglog of Progression-free survival versus stage')
```



## Cloglog of Progression-free survival versus stage



```
#detach(pancreatic2)
```

### Section 7.2.2 Schoenfeld residuals - Test proportional hazards assumption

```
tt <- c(6, 7, 10, 15, 19, 25)
delta <- c(1, 0, 1, 1, 0, 1)
trt <- c(0, 0, 1, 0, 1, 1)
result.coxph <- coxph(Surv(tt, delta) ~ trt)
result.coxph$coef
```

```
##      trt
## -1.326129
```

```
residuals(result.coxph, type="schoenfeld")
```

```
##          6          10          15          25
## -0.2098004  0.5566351 -0.3468347  0.0000000
```

```
resid.unscaled <- residuals(result.coxph, type="schoenfeld")
resid.scaled <- resid.unscaled * as.vector(result.coxph$var) * sum(delta)
```

```
resid.unscaled
```

```
##          6          10          15          25
## -0.2098004  0.5566351 -0.3468347  0.0000000
```

```

resid.scaled

##           6           10           15           25
## -1.313064  3.483776 -2.170712  0.000000

resid.scaled + result.coxph$coef

##           6           10           15           25
## -2.639193  2.157647 -3.496841 -1.326129

#obtain scaled Schoenfeld resids using cox.zph
resid.sch <- cox.zph(result.coxph)
resid.sch$y

##           trt
## 6  -2.639193
## 10  2.157647
## 15 -3.496841
## 25 -1.326129

resid.sch$x #transformed time by 1-KM

## [1] 0.0000000 0.1666667 0.3750000 0.5833333

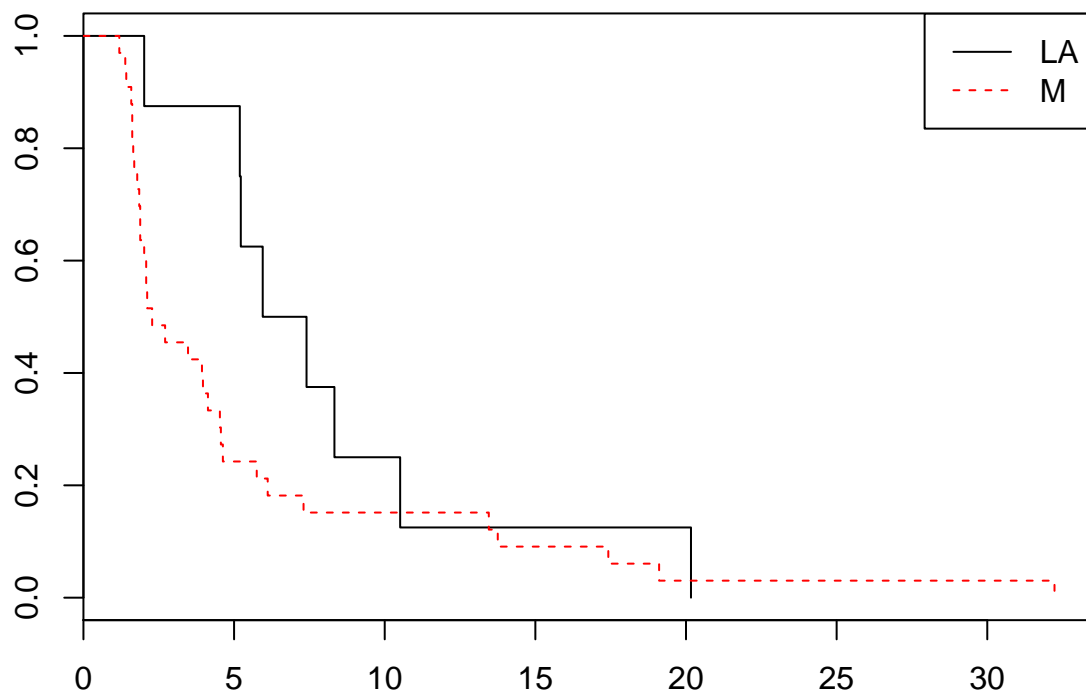
#attach(pancreatic2)
#pfs.month <- pfs/30.25
result.coxph <- coxph(Surv(pfs/30.25, status) ~ stage, data=pancreatic2)
summary(result.coxph)

## Call:
## coxph(formula = Surv(pfs/30.25, status) ~ stage, data = pancreatic2)
##
##      n= 41, number of events= 41
##
##              coef exp(coef) se(coef)      z Pr(>|z|)
## stageM 0.5931      1.8095   0.4007 1.48    0.139
##
##              exp(coef) exp(-coef) lower .95 upper .95
## stageM      1.81      0.5526   0.8251   3.969
##
## Concordance= 0.589 (se = 0.041 )
## Rsquare= 0.058 (max possible= 0.996 )
## Likelihood ratio test= 2.43 on 1 df,  p=0.1188
## Wald test = 2.19 on 1 df,  p=0.1389
## Score (logrank) test = 2.25 on 1 df,  p=0.1335

#Do the KM curves cross?
plot(survfit(Surv(pfs/30.25, status) ~ stage, data=pancreatic2),
     mark.time=TRUE, lty=1:2, col=1:2)
legend('topright', levels(pancreatic2$stage), lty=1:2, col=1:2)
title('Progression-free survival versus stage')

```

## Progression-free survival versus stage



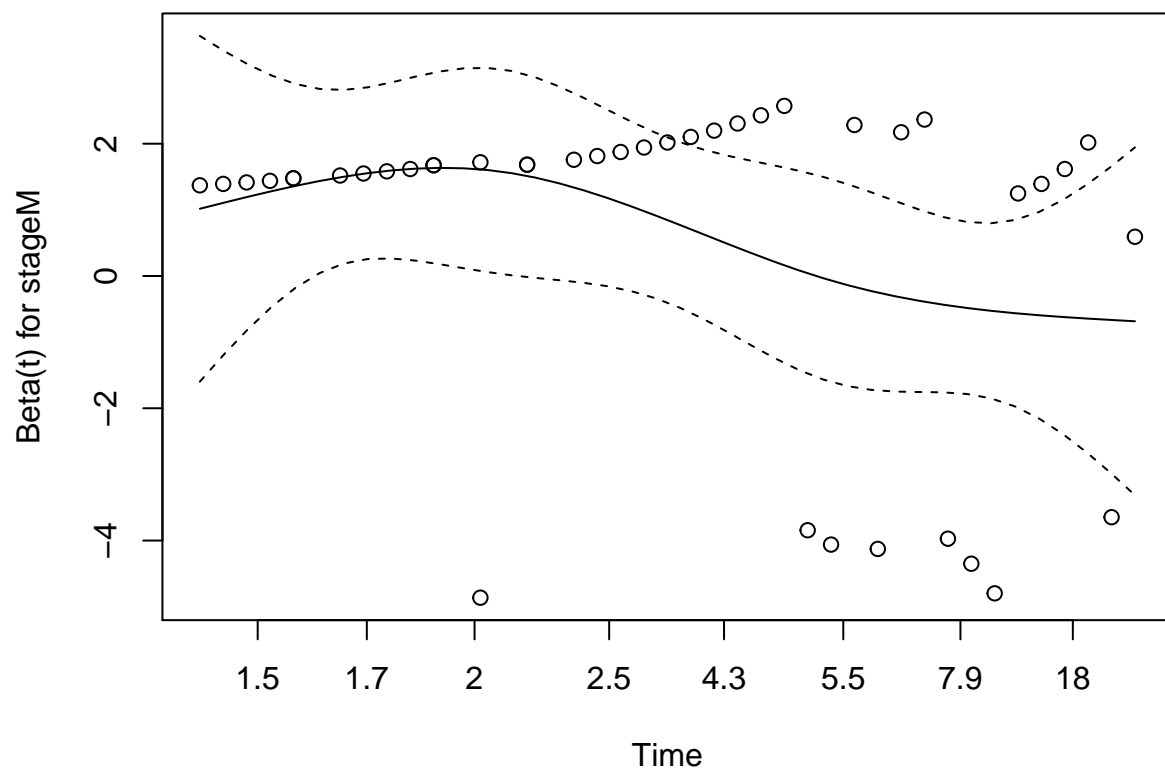
```
result.sch.resid <- cox.zph(result.coxph, transform="km")
result.sch.resid
```

```
##           rho chisq      p
## stageM -0.328  3.86 0.0496
```

```
# Fig 7.5
```

```
plot(result.sch.resid)
title('Schoenfeld residuals for pancreatic stage vs km time')
```

## Schoenfeld residuals for pancreatic stage vs km time

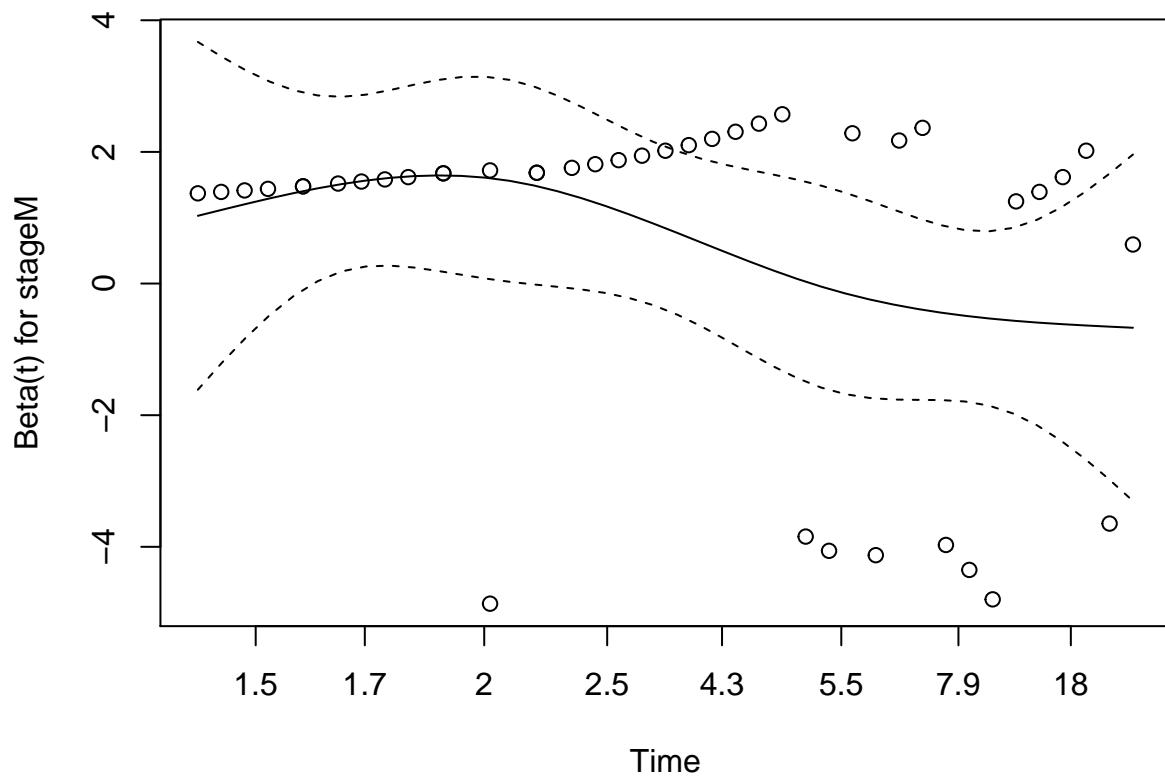


```
result.sch.rank <- cox.zph(result.coxph, transform="rank")
result.sch.rank
```

```
##          rho chisq      p
## stageM -0.33  3.89 0.0486
```

```
plot(result.sch.rank)
title('Schoenfeld residuals for pancreatic stage vs rank time')
```

### Schoenfeld residuals for pancreatic stage vs rank time



```
#detach(pancreatic2)
```