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As of June 19, 2022

# Contents

file <- "210\_bayes\_summary.md"

PURPOSE: Summary of Bayes.

:::TODO::: - set matrix A equal to matrix B, in equation. - in math mode double / ends the line - in non-math mode use p a r - under Event Space add to 2nd line first flip is H - short text needs to be verbatim - powerset

% comment in .tex, but not comment to pandoc - WILL appear in .pdf

## Sample Space

All possible outcomes from 1 experiment.

Ex: toss 2 coins  $S = \{HH, HT, TH, TT\}$

## Event Space

This actually a bit more complicated:

$$E_1 = HE_2 = HH, HT \quad (1)$$

In general, E subset of powerset (S)

$$X \in \mathcal{P}(A)$$

|number of elements| =  $2^k$

## Bayes Rule:

A = Event B = Event

$$P(A | B) = \frac{P(B | A)P(A)}{P(B)}$$

Joint Probability:

$$P(A \cap B)$$

Conditional:

$$P(A | B)$$

Law of Total Probability:

$$P(A) = \sum_{i=1}^n P(A | B_i)P(B_i)$$

## Likelihood

Often probability of event B,  $P(B)$  is unknown, but we do have information about another event A and its affect on B.  $P(B|A = \text{known})$

We can try to learn something from  $P(B | A)$  by treating B as a variable and trying to construct a function to compare different values of A.  $f_A(B)$  In words, given event A what is likelihood of B

$$L(A|B = \text{unknown}) = P(B = \text{unknown}|A)$$

## Fake or Real News ?

Suppose we examine  $N = 150$  news articles and record the following information:

A = event article uses !

B = event article is fake

Join probability

$$P(A \cap B)$$

```
\begin{matrix}
44 & 88 \\
16 & 2
\end{matrix}
```

Or as a proportion of total:

```
\begin{matrix}
\frac{44}{150} & \frac{88}{150} \\
\frac{16}{150} & \frac{2}{150}
\end{matrix}
```