

Table 6. Photon energies ( $E_p$ 's) in the hydrogen spectrum used to construct Table 7 and Fig. 12. Bolded  $E_p$ 's are in the range 617.3-2239.5  $\text{cm}^{-1}$ . These  $E_p$ 's are for the points plotted in Fig. 12.

| $n_i$ | $n_f=4$         | $[i]$ | $n_f=5$         | $[i]$ | $n_f=6$         | $[i]$                   | $n_f=7$       | $[i]$         | $n_f=8$       |              |
|-------|-----------------|-------|-----------------|-------|-----------------|-------------------------|---------------|---------------|---------------|--------------|
| 5     | (High $E_p$ 's) |       | x               |       | x               |                         | x             |               | x             |              |
| 6     | ↓               | [15]  | <b>1341.2</b>   |       | x               |                         | x             |               | x             |              |
| 7     |                 | [2]   | <b>2149.9</b>   |       | [18]            | <b>808.7</b>            | x             |               | x             |              |
| 8     |                 |       | (High $E_p$ 's) |       | [15]            | <b>1333.6</b>           | 524.9         |               | x             |              |
| 9     |                 |       | ↓               |       | [11]            | <b>1693.5</b>           | [17]          | <b>884.8</b>  | 359.9         |              |
| 10    |                 |       |                 |       | [4]             | <b>1950.9</b>           | [16]          | <b>1142.2</b> | [19]          | <b>617.3</b> |
| 11    |                 |       |                 |       | [2]             | <b>2141.3</b>           | [15]          | <b>1332.6</b> | [18]          | <b>807.7</b> |
| 12    |                 |       |                 |       | (High $E_p$ 's) |                         | [14]          | <b>1477.5</b> | E ring        | 952.6        |
| 13    |                 |       |                 |       | ↓               |                         | [13]          | <b>1590.2</b> | E ring        | 1065.3       |
| 14    |                 |       |                 |       |                 |                         | [12]          | <b>1679.6</b> | E ring        | 1154.8       |
| 15    |                 |       |                 |       |                 |                         | [9]           | <b>1751.8</b> | E ring        | 1226.9       |
| 16    |                 |       |                 |       |                 |                         | [8]           | <b>1810.9</b> | E ring        | 1286.0       |
| 17    |                 |       |                 |       |                 |                         | [7]           | <b>1859.8</b> | E ring        | 1334.9       |
| 18    |                 |       |                 |       |                 |                         | [6]           | <b>1900.8</b> | E ring        | 1375.9       |
| 19    |                 |       |                 |       |                 |                         | [5]           | <b>1935.6</b> | E ring        | 1410.7       |
| 20    |                 |       |                 |       |                 | A ring&[3] <sup>1</sup> | <b>1965.2</b> | E ring        | 1440.3        |              |
| 21    |                 |       |                 |       |                 | A ring                  | 1990.7        | E ring        | 1465.8        |              |
| 22    |                 |       |                 |       |                 | A ring                  | 2012.8        | E ring        | 1487.9        |              |
| 23    |                 |       |                 |       |                 | A ring                  | 2032.1        | E ring        | 1507.2        |              |
| 24    |                 |       |                 |       |                 | A ring                  | 2049.0        | E ring        | 1524.1        |              |
| 25    |                 |       |                 |       |                 | A ring                  | 2064.0        | E ring        | 1539.1        |              |
| ↓     |                 |       |                 |       |                 |                         | ↓             |               | ↓             |              |
| ∞     |                 |       |                 |       |                 | IE A[1]                 | <b>2239.5</b> | IE E[10]      | <b>1714.6</b> |              |

IE stands for Inner Edge.

A set of principal quantum numbers ( $n_f, n_i$ ) defines a transition in the hydrogen atom where  $n_i > n_f$ .

The column of integers on the far left contains values of  $n_i$ , the initial quantum number for the transition.

The row of integers along the top contains values of  $n_f$ , the final quantum number for a transition.

A photon energy  $E_p(n_f, n_i)$  in units of  $\text{cm}^{-1}$  is listed under each  $n_f$  and in a row where the initial quantum number is  $n_i$ .

Bolded  $E_p$ 's are assigned to individual satellites and ring inner edges in Saturn's satellite system.

Generally unbolded  $E_p$ 's contributed to the creation of the A ring and E ring. IE A is inner edge A ring.

The satellite index [ $i$ ] to the left of each bolded  $E_p$  is the index assigned to a satellite or ring edge in

Table 7. An [ $i$ ] value associates each  $E_p$  with a particular orbital radius of a satellite or ring

edge in Saturn's system. There are no unpaired  $E_p$ 's or orbital radii. Most importantly limits

$E_p(7, \infty)$  and  $E_p(8, \infty)$  are associated with the inner radii of the A and E rings respectively.

All unbolded close  $E_p$ 's contribute to either the A or E ring of Saturn.

<sup>1</sup>Daphnis ( $E_p(7, 20), [3]$ ) is in the Keeler Gap near the outer edge of the A ring. NASA(2021)

$E_p(7, 8)$  and  $E_p(8, 9)$  are out of the range of interest.

(High  $E_p$ 's) is indicated for many  $E_p$ 's because they are out of range of interest.

$E_p$ 's corresponding to  $n_f = 9$  or larger are not included. Apparently they did not create resonance.