# Privacy

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## Challenges

- Al requires large datasets.
- Research and development of new AI technology need access to similarly large datasets.
- A lot of the data needed consists of sensitive or private information.
- The data needs to be protected before it can be used widely.
- Protection has a cost.

## Challenges

#### • Idea:

Access to a statistical database should not enable one to learn anything about an individual that could not be learned without access.

#### • Impossible:

Auxiliary information.

Ex: Suppose one's exact height were considered a sensitive piece of information.

Assume that the database yields the average heights of a certain group of people.

## Protecting the data – Differential privacy

- the risk to one's privacy should not substantially increase as a result of participating in a statistical database.
- A randomized function K gives  $\epsilon$ -differential privacy if for all data sets  $D_1$  and  $D_2$  differing on at most one element, and all  $S \subseteq \text{Range}(K)$

$$Pr[K(D_1) \in S] \le e^{\varepsilon}Pr[K(D_2) \in S]$$

## Protecting the data — Differential privacy

- Other variants of the definitions exists:
- A randomized function K gives  $(\varepsilon, \delta)$ -differential privacy if for all data sets  $D_1$  and  $D_2$  differing on at most one element, and all  $S \subseteq \text{Range}(K)$

$$Pr[K(D_1) \in S] \le e^{\varepsilon}Pr[K(D_2) \in S] + \delta.$$

• Preferably,  $\delta$ <1/ $\mid$  D<sub>1</sub>  $\mid$ 

C. Dwork, F. McSherry, K. Nissim, and A. Smith. "Calibrating noise to sensitivity in private data analysis". In TCC, pages 265–284. Springer, 2006.

## Protecting the data — Differential privacy

- Data utility will eventually be consumed:
- The Fundamental Law of Information Recovery states that overly accurate answers to too many questions will destroy privacy in a spectacular way.
- Differential privacy ensures that the same conclusions will be reached, independent of whether any individual opts into or opts out of the data set.

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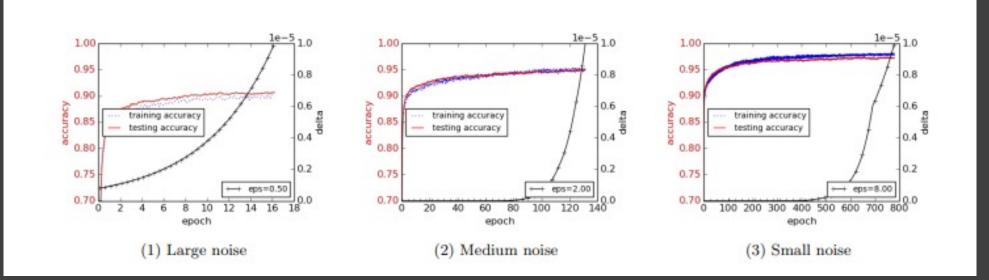
# SGD with Differential privacy

- Protect against modelinversion attacks.
- Assumes that the trained model is exposed.
- Compute SGD while clipping and adding noise to each step
- In this case, Gaussian noise is used
- Computing the cost:

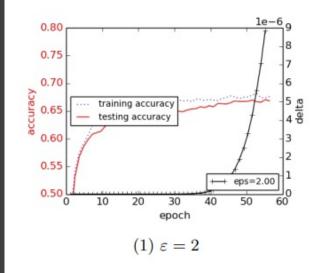
• 
$$\sigma = \frac{\sqrt{2log\frac{125}{\delta}}}{\varepsilon}$$

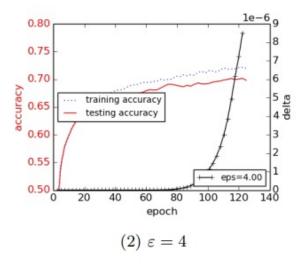
• is  $(O(q\epsilon\sqrt{T}), \delta)$ - differentially private

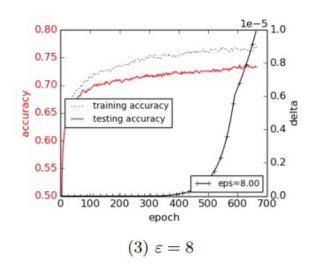
- Input:
  - Examples  $\{x_1, \ldots, x_N\}$ ,
  - loss function:  $L(\theta) = \frac{1}{N} \sum_{i} L(\theta, xi)$ .
- Parameters
  - learning rate η<sub>t</sub>,
  - noise scale σ,
  - group size L,
  - gradient norm bound C.
- Initialize  $\theta_0$  randomly
- for t ∈ [T] do
  - Take a random sample  $L_t$  with sampling probability L/N
  - For each  $i \in L_t$ , compute  $g_t(xi) \leftarrow \nabla \theta_t L(\theta_t, x_i)$
  - $g_t(x_i) \leftarrow g_t(x_i) / \max(1, \frac{||g_t(x_i)||_2}{C})$
  - $g_t \leftarrow \frac{1}{L} (\sum_i g_t(x_i) + N(0, \sigma^2 C^2 I))$
  - $\theta_{t+1} \leftarrow \theta_t \eta_t g_t$
- Output  $\theta_T$  and compute the overall privacy cost  $(\epsilon,\,\delta)$  using a privacy accounting method.



- Tested on the MNIST dataset
- Baseline model:
  - a 60-dimensional PCA projection layer and a single hidden layer with 1,000 hidden units.
  - Using the lot size of 600, we can reach accuracy of 98.30% in about 100 epochs
- Differential privacy: same architecture with three levels of noise





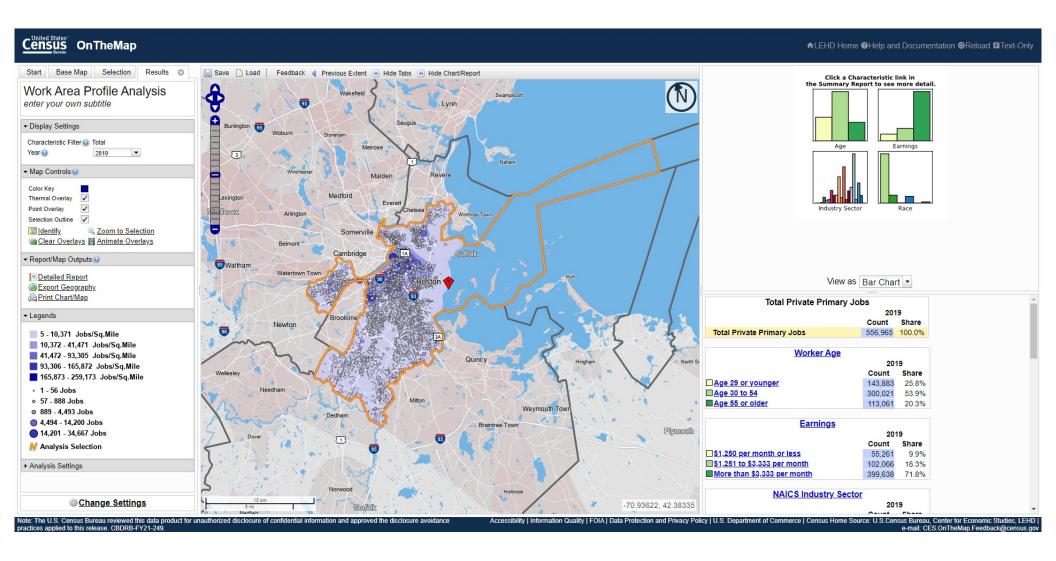


- Tested on the CIFAR-10 dataset
- Baseline model:
  - Network architecture from the TensorFlow convolutional neural networks tutorial.
  - Two convolutional layers followed by two fully connected layers.
  - Reaches about 86% accuracy in 500 epochs.
- Differential privacy: same architecture with three levels of noise

## In practice: OnTheMap

- Mapping program to show the commuting patterns of the USA population.
- Shows where American workers are employed and where they live.
- Data from the US census bureau.
- The data can't be used directly because of privacy concerns.

https://onthemap.ces.census.gov/



## In practice: OnTheMap

- Data points contain id, origin block, destination block.
- Destination block are public data.
- Origin block is treated as the sensitive attribute.
- Looked at different criterias for privacy.
- Used original Differential privacy criteria.
- Uses synthethic data generation to anonymize the data.
- Privacy comes from the bias from the model and noise from random sampling.

Machanavajjhala, Ashwin, Daniel Kifer, John Abowd, Johannes Gehrke, and Lars Vilhuber, "Privacy: Theory Meets Practice On the Map," International Conference on Data Engineering (ICDE) 2008, pp. 277-286.

## **Problems**

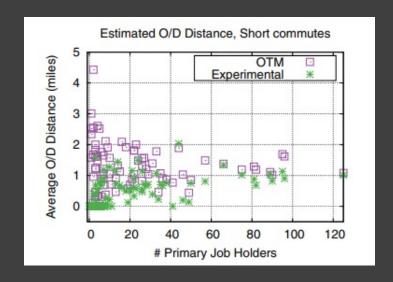
- Differential Privacy requires consider adversaries who know all but one data point.
- Needs more than 913 people in each block to satisfy the criteria.
- Cause: worst case scenario.
- Generates completely unrepresentative synthetic data.
- Extremely unlikely
- Variation to relax Differential Privacy: Probabilistic Differential Privacy.

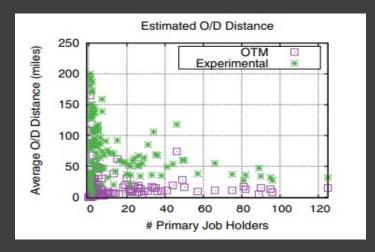
## **Problems**

- Unrepresentative data can be generated.
  - the accept/reject method, is to choose a "representativeness" metric and rerun the algorithm until we get an output which is representative of the input
  - Needs an acceptance metric that is compatible with Probabilistic Differential Privacy.
- Needs noise in each block to satisfy Probabilistic Differential Privacy, but the data is sparse.
  - Clustering.
  - Needs a clustering algorithm that is compatible with Probabilistic Differential Privacy.

• Compared the average commute distance for each destination block and compared it to the ground truth from the data.

• Long commutes are overestimated.

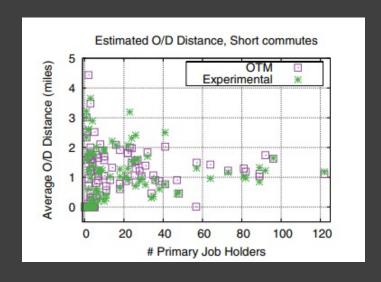


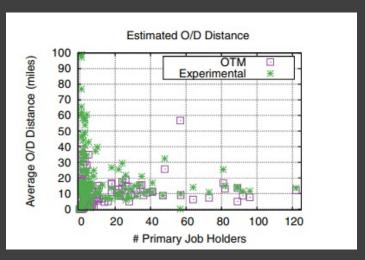


• Compared the average commute distance for each destination block and compared it to the ground truth from the data.

• Long commutes are overestimated.

• Added more restrictions to prevent Outliers.





## Improvements

- Preventing drops in accuracy when integrating Differential privacy to a model.
- Dealing with scarcity of data to prevent outliers.

## Questions?