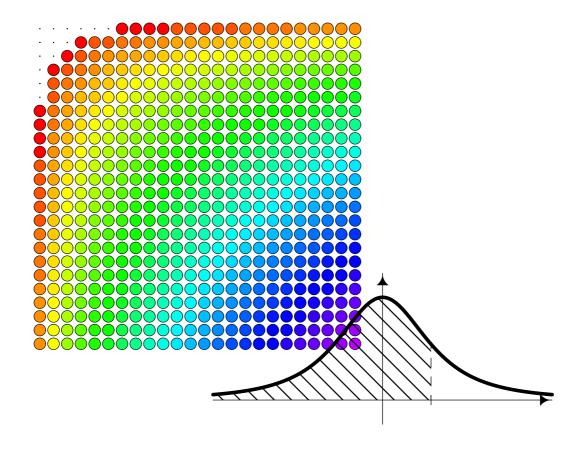
# **Statistical Tables**



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1. Binomial distribution 3

#### 1 Binomial distribution

#### Cumulative distribution function for $\theta \leq 0.09$

This section tabulates the cumulative distribution function (c.d.f.) of the binomial distribution, i.e. the distribution of the number of successes in n independent trials of an experiment which leads to a success with probability  $\theta$ . The c.d.f. is

$$F(x) = \mathbb{P}\{X \le x\} = \sum_{k=0}^{x} \mathbb{P}\{X = k\} = \sum_{k=0}^{x} \binom{n}{k} \theta^{k} (1 - \theta)^{n-k}.$$

The tables only cover  $\theta \leq \frac{1}{2}$ . For  $\theta > \frac{1}{2}$ , the rôles of successes and failures need to be reversed, i.e. if  $X \sim \mathrm{Bi}(n,\theta)$ , and  $Y \sim \mathrm{Bi}(n,1-\theta)$ , then  $\mathbb{P}\{X \leq x\} = 1 - \mathbb{P}\{Y \leq n-x-1\}$ .

							$\theta$					
n	$\boldsymbol{x}$	0.001	0.005	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
1	0	0.9990	0.9950	0.9900	0.9800	0.9700	0.9600	0.9500	0.9400	0.9300	0.9200	0.9100
	1	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
2	0	0.9980	0.9900	0.9801	0.9604	0.9409	0.9216	0.9025	0.8836	0.8649	0.8464	0.8281
_	1	1.0000	1.0000	0.9999	0.9996	0.9991	0.9984	0.9975	0.9964	0.9951	0.9936	0.9919
	2	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
3	0	0.9970	0.9851	0.9703	0.9412	0.9127	0.8847	0.8574	0.8306	0.8044	0.7787	0.7536
3	1	1.0000	0.9999	0.9997	0.9412	0.9127 $0.9974$	0.9953	0.9928	0.9896	0.9860	0.9818	0.7550 $0.9772$
	2	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9998	0.9997	0.9995	0.9993
	3	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
4	0	0.9960	0.9801	0.9606	0.9224	0.8853	0.8493	0.8145	0.7807	0.7481	0.7164	0.6857
	1	1.0000	0.9999	0.9994	0.9977	0.9948	0.9909	0.9860	0.9801	0.9733	0.9656	0.9570
	2	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9995	0.9992	0.9987	0.9981	0.9973
	3	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999
	4	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
5	0	0.9950	0.9752	0.9510	0.9039	0.8587	0.8154	0.7738	0.7339	0.6957	0.6591	0.6240
	1	1.0000	0.9998	0.9990	0.9962	0.9915	0.9852	0.9774	0.9681	0.9575	0.9456	0.9326
	2	1.0000	1.0000	1.0000	0.9999	0.9997	0.9994	0.9988	0.9980	0.9969	0.9955	0.9937
	3	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9998	0.9997
	4	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
6	0	0.9940	0.9704	0.9415	0.8858	0.8330	0.7828	0.7351	0.6899	0.6470	0.6064	0.5679
	1	1.0000	0.9996	0.9985	0.9943	0.9875	0.9784	0.9672	0.9541	0.9392	0.9227	0.9048
	2	1.0000	1.0000	1.0000	0.9998	0.9995	0.9988	0.9978	0.9962	0.9942	0.9915	0.9882
	3	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9997	0.9995	0.9992
	4	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
7	0	0.9930	0.9655	0.9321	0.8681	0.8080	0.7514	0.6983	0.6485	0.6017	0.5578	0.5168
	1	1.0000	0.9995	0.9980	0.9921	0.9829	0.9706	0.9556	0.9382	0.9187	0.8974	0.8745
	2	1.0000	1.0000	1.0000	0.9997	0.9991	0.9980	0.9962	0.9937	0.9903	0.9860	0.9807
	3	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9996	0.9993	0.9988	0.9982
	4	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999
	5	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
8	0	0.9920	0.9607	0.9227	0.8508	0.7837	0.7214	0.6634	0.6096	0.5596	0.5132	0.4703
	1	1.0000	0.9993	0.9973	0.9897	0.9777	0.9619	0.9428	0.9208	0.8965	0.8702	0.8423
	2	1.0000	1.0000	0.9999	0.9996	0.9987	0.9969	0.9942	0.9904	0.9853	0.9789	0.9711
	3	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9996	0.9993	0.9987	0.9978	0.9966
	4	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9997
	5	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
9	0	0.9910	0.9559	0.9135	0.8337	0.7602	0.6925	0.6302	0.5730	0.5204	0.4722	0.4279
	1	1.0000	0.9991	0.9966	0.9869	0.9718	0.9522	0.9288	0.9022	0.8729	0.8417	0.8088
	$\overline{2}$	1.0000	1.0000	0.9999	0.9994	0.9980	0.9955	0.9916	0.9862	0.9791	0.9702	0.9595
	3	1.0000	1.0000	1.0000	1.0000	0.9999	0.9997	0.9994	0.9987	0.9977	0.9963	0.9943
	4	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9997	0.9995
	5	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
10	0	0.9900	0.9511	0.9044	0.8171	0.7374	0.6648	0.5987	0.5386	0.4840	0.4344	0.3894
10	1	1.0000	0.9911 $0.9989$	0.9944 $0.9957$	0.9838	0.7574 $0.9655$	0.0048 $0.9418$	0.9937	0.8824	0.4840 $0.8483$	0.4344 $0.8121$	0.3694 $0.7746$
	1	1.0000	0.3303	0.5501	0.5050	0.3033	0.3410	0.9109	0.0024	0.0400	0.0121	0.1140

n	x	0.001	0.005	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
10	2	1.0000	1 0000	0.0000	0.0001	0.0079	0.0020	0.0005	0.0010	0.9717	0.0500	0.0460
10	2		1.0000 $1.0000$	0.9999	0.9991	0.9972 $0.9999$	0.9938 $0.9996$	0.9885 $0.9990$	0.9812		0.9599	0.9460
	$\frac{3}{4}$	1.0000 1.0000	1.0000	1.0000 1.0000	1.0000 1.0000	1.0000	1.0000	0.9990 $0.9999$	0.9980 $0.9998$	0.9964 $0.9997$	0.9942 $0.9994$	0.9912 $0.9990$
	5	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9990 $0.9999$
	6	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
11	0	0.9891	0.9464	0.8953	0.8007	0.7153	0.6382	0.5688	0.5063	0.4501	0.3996	0.3544
	1	0.9999	0.9987	0.9948	0.9805	0.9587	0.9308	0.8981	0.8618	0.8228	0.7819	0.7399
	2	1.0000	1.0000	0.9998	0.9988	0.9963	0.9917	0.9848	0.9752	0.9630	0.9481	0.9305
	3	1.0000	1.0000	1.0000	1.0000	0.9998	0.9993	0.9984	0.9970	0.9947	0.9915	0.9871
	4	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9997	0.9995	0.9990	0.9983
	5	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998
	6	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
12	0	0.9881	0.9416	0.8864	0.7847	0.6938	0.6127	0.5404	0.4759	0.4186	0.3677	0.3225
	1	0.9999	0.9984	0.9938	0.9769	0.9514	0.9191	0.8816	0.8405	0.7967	0.7513	0.7052
	2	1.0000	1.0000	0.9998	0.9985	0.9952	0.9893	0.9804	0.9684	0.9532	0.9348	0.9134
	3	1.0000	1.0000	1.0000	0.9999	0.9997	0.9990	0.9978	0.9957	0.9925	0.9880	0.9820
	4	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9996	0.9991	0.9984	0.9973
	5	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9997
	6	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
13	0	0.9871	0.9369	0.8775	0.7690	0.6730	0.5882	0.5133	0.4474	0.3893	0.3383	0.2935
	1	0.9999	0.9981	0.9928	0.9730	0.9436	0.9068	0.8646	0.8186	0.7702	0.7206	0.6707
	2	1.0000	1.0000	0.9997	0.9980	0.9938	0.9865	0.9755	0.9608	0.9422	0.9201	0.8946
	3	1.0000	1.0000	1.0000	0.9999	0.9995	0.9986	0.9969	0.9940	0.9897	0.9837	0.9758
	4	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9997	0.9993	0.9987	0.9976	0.9959
	5	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9997	0.9995
	6	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999
	7	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
14	0	0.9861	0.9322	0.8687	0.7536	0.6528	0.5647	0.4877	0.4205	0.3620	0.3112	0.2670
	1	0.9999	0.9978	0.9916	0.9690	0.9355	0.8941	0.8470	0.7963	0.7436	0.6900	0.6368
	2	1.0000	1.0000	0.9997	0.9975	0.9923	0.9833	0.9699	0.9522	0.9302	0.9042	0.8745
	3	1.0000	1.0000	1.0000	0.9999	0.9994	0.9981	0.9958	0.9920	0.9864	0.9786	0.9685
	4	1.0000	1.0000	1.0000	1.0000	1.0000	0.9998	0.9996	0.9990	0.9980	0.9965	0.9941
	5	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9996	0.9992
	6	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999
	7	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
15	0	0.9851	0.9276	0.8601	0.7386	0.6333	0.5421	0.4633	0.3953	0.3367	0.2863	0.2430
10	1	0.9999	0.9975	0.9904	0.9647	0.9270	0.8809	0.8290	0.7738	0.7168	0.6597	0.6035
	2	1.0000	0.9999	0.9996	0.9970	0.9906	0.9797	0.9638	0.9429	0.9171	0.8870	0.8531
	3	1.0000	1.0000	1.0000	0.9998	0.9992	0.9976	0.9945	0.9896	0.9825	0.9727	0.9601
	4	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9994	0.9986	0.9972	0.9950	0.9918
	5	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9997	0.9993	0.9987
	6	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998
	7	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
16	0	0.9841	0.9229	0.8515	0.7238	0.6143	0.5204	0.4401	0.3716	0.3131	0.2634	0.2211
10	1	0.9999	0.9229 $0.9971$	0.9891	0.1250	0.0143 $0.9182$	0.8673	0.4401	0.5710 $0.7511$	0.6902	0.2034 $0.6299$	0.2211 $0.5711$
	2	1.0000	0.9999	0.9995	0.9963	0.9887	0.9758	0.9571	0.9327	0.9031	0.8689	0.8306
	3	1.0000	1.0000	1.0000	0.9998	0.9989	0.9968	0.9930	0.9868	0.9779	0.9658	0.9504
	4	1.0000	1.0000	1.0000	1.0000	0.9999	0.9997	0.9991	0.9981	0.9962	0.9932	0.9889
	5	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9995	0.9990	0.9981
	6	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9997
	7	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
17	0	0.0021	0.0102	0.8490	0.7002	0.5050	0.4006	0.4101	0.2402	0.2012	0.9499	0.2012
17	0	0.9831 $0.9999$	0.9183 $0.9968$	0.8429 $0.9877$	0.7093 $0.9554$	0.5958 $0.9091$	0.4996 $0.8535$	0.4181 $0.7922$	0.3493 $0.7283$	0.2912 $0.6638$	0.2423 $0.6005$	0.2012 $0.5396$
	$\frac{1}{2}$	1.0000	0.9968 $0.9999$	0.9877	0.9554 $0.9956$	0.9091 $0.9866$	0.8535 $0.9714$	0.7922 $0.9497$	0.7283 $0.9218$	0.8882	0.8497	0.5396 $0.8073$
	3	1.0000	1.0000	1.0000	0.9950 $0.9997$	0.9860	0.9714 $0.9960$	0.9497 $0.9912$	0.9218 $0.9836$	0.882 $0.9727$	0.9581	0.8073 $0.9397$
	4	1.0000	1.0000	1.0000	1.0000	0.9980 $0.9999$	0.9996	0.9912 $0.9988$	0.9850 $0.9974$	0.9121	0.9911	0.9357 $0.9855$
	5	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9974 $0.9997$	0.9943	0.9911 $0.9985$	0.9973
	6	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9996
	7	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
18	0	0.9822	0.9137	0.8345	0.6951	0.5780	0.4796	0.3972	0.3283	0.2708	0.2229	0.1831

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n	x	0.001	0.005	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
18	1	0.9998	0.9964	0.9862	0.9505	0.8997	0.8393	0.7735	0.7055	0.6378	0.5719	0.5091
	2	1.0000	0.9999	0.9993	0.9948	0.9843	0.9667	0.9419	0.9102	0.8725	0.8298	0.7832
	3	1.0000	1.0000	1.0000	0.9996	0.9982	0.9950	0.9891	0.9799	0.9667	0.9494	0.9277
	4	1.0000	1.0000	1.0000	1.0000	0.9998	0.9994	0.9985	0.9966	0.9933	0.9884	0.9814
	5	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9995	0.9990	0.9979	0.9962
	6	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9997	0.9994
	7	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999
	8	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
19	0	0.9812	0.9092	0.8262	0.6812	0.5606	0.4604	0.3774	0.3086	0.2519	0.2051	0.1666
	1	0.9998	0.9960	0.9847	0.9454	0.8900	0.8249	0.7547	0.6829	0.6121	0.5440	0.4798
	2	1.0000	0.9999	0.9991	0.9939	0.9817	0.9616	0.9335	0.8979	0.8561	0.8092	0.7585
	3	1.0000	1.0000	1.0000	0.9995	0.9978	0.9939	0.9868	0.9757	0.9602	0.9398	0.9147
	4	1.0000	1.0000	1.0000	1.0000	0.9998	0.9993	0.9980	0.9956	0.9915	0.9853	0.9765
	5	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9994	0.9986	0.9971	0.9949
	6	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9996	0.9991
	7	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999
	8	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
20	0	0.9802	0.9046	0.8179	0.6676	0.5438	0.4420	0.3585	0.2901	0.2342	0.1887	0.1516
	1	0.9998	0.9955	0.9831	0.9401	0.8802	0.8103	0.7358	0.6605	0.5869	0.5169	0.4516
	2	1.0000	0.9999	0.9990	0.9929	0.9790	0.9561	0.9245	0.8850	0.8390	0.7879	0.7334
	3	1.0000	1.0000	1.0000	0.9994	0.9973	0.9926	0.9841	0.9710	0.9529	0.9294	0.9007
	4	1.0000	1.0000	1.0000	1.0000	0.9997	0.9990	0.9974	0.9944	0.9893	0.9817	0.9710
	5	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9997	0.9991	0.9981	0.9962	0.9932
	6	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9997	0.9994	0.9987
	7	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998
	8	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000

## Cumulative distribution function for $0.1 \leq \theta \leq 0.5$

							$\theta$					
n	x	0.1	0.125	0.15	0.2	0.25	0.3	0.3333	0.35	0.4	0.45	0.5
1	0	0.9000	0.8750	0.8500	0.8000	0.7500	0.7000	0.6667	0.6500	0.6000	0.5500	0.5000
	1	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
2	0	0.8100	0.7656	0.7225	0.6400	0.5625	0.4900	0.4444	0.4225	0.3600	0.3025	0.2500
	1	0.9900	0.9844	0.9775	0.9600	0.9375	0.9100	0.8889	0.8775	0.8400	0.7975	0.7500
	2	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
3	0	0.7290	0.6699	0.6141	0.5120	0.4219	0.3430	0.2963	0.2746	0.2160	0.1664	0.1250
	1	0.9720	0.9570	0.9392	0.8960	0.8438	0.7840	0.7407	0.7183	0.6480	0.5748	0.5000
	2	0.9990	0.9980	0.9966	0.9920	0.9844	0.9730	0.9630	0.9571	0.9360	0.9089	0.8750
	3	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
4	0	0.6561	0.5862	0.5220	0.4096	0.3164	0.2401	0.1975	0.1785	0.1296	0.0915	0.0625
	1	0.9477	0.9211	0.8905	0.8192	0.7383	0.6517	0.5926	0.5630	0.4752	0.3910	0.3125
	2	0.9963	0.9929	0.9880	0.9728	0.9492	0.9163	0.8889	0.8735	0.8208	0.7585	0.6875
	3	0.9999	0.9998	0.9995	0.9984	0.9961	0.9919	0.9877	0.9850	0.9744	0.9590	0.9375
	4	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
5	0	0.5905	0.5129	0.4437	0.3277	0.2373	0.1681	0.1317	0.1160	0.0778	0.0503	0.0312
	1	0.9185	0.8793	0.8352	0.7373	0.6328	0.5282	0.4609	0.4284	0.3370	0.2562	0.1875
	2	0.9914	0.9839	0.9734	0.9421	0.8965	0.8369	0.7901	0.7648	0.6826	0.5931	0.5000
	3	0.9995	0.9989	0.9978	0.9933	0.9844	0.9692	0.9547	0.9460	0.9130	0.8688	0.8125
	4	1.0000	1.0000	0.9999	0.9997	0.9990	0.9976	0.9959	0.9947	0.9898	0.9815	0.9688
	5	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
6	0	0.5314	0.4488	0.3771	0.2621	0.1780	0.1176	0.0878	0.0754	0.0467	0.0277	0.0156
	1	0.8857	0.8335	0.7765	0.6554	0.5339	0.4202	0.3512	0.3191	0.2333	0.1636	0.1094
	2	0.9842	0.9709	0.9527	0.9011	0.8306	0.7443	0.6804	0.6471	0.5443	0.4415	0.3437

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n	x	0.1	0.125	0.15	0.2	0.25	0.3	0.3333	0.35	0.4	0.45	0.5
<u>n</u>												
6	3	0.9987	0.9970	0.9941	0.9830	0.9624	0.9295	0.8999	0.8826	0.8208	0.7447	0.6562
	4	0.9999	0.9998	0.9996	0.9984	0.9954	0.9891	0.9822	0.9777	0.9590	0.9308	0.8906
	5 6	1.0000 $1.0000$	1.0000 $1.0000$	1.0000 $1.0000$	0.9999 $1.0000$	0.9998 $1.0000$	0.9993 $1.0000$	0.9986 $1.0000$	0.9982 $1.0000$	0.9959 $1.0000$	0.9917 $1.0000$	0.9844 $1.0000$
7	0	0.4783	0.3927	0.3206	0.2097	0.1335	0.0824	0.0585	0.0490	0.0280	0.0152	0.0078
	1	0.8503	0.7854	0.7166	0.5767	0.4449	0.3294	0.2634	0.2338	0.1586	0.1024	0.0625
	$\frac{2}{3}$	0.9743 $0.9973$	0.9537 $0.9938$	0.9262 $0.9879$	$0.8520 \\ 0.9667$	0.7564 $0.9294$	0.6471 $0.8740$	$0.5706 \\ 0.8267$	0.5323 $0.8002$	$0.4199 \\ 0.7102$	0.3164 $0.6083$	$0.2266 \\ 0.5000$
	3 4	0.9973 $0.9998$	0.9956 $0.9995$	0.9879	0.9953	0.9294 $0.9871$	0.8740 $0.9712$	0.8207 $0.9547$	0.8002 $0.9444$	0.7102 $0.9037$	0.8471	0.7734
	5	1.0000	1.0000	0.9999	0.9996	0.9987	0.9112 $0.9962$	0.9931	0.9444 $0.9910$	0.9812	0.9643	0.7734 $0.9375$
	6	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9995	0.9994	0.9984	0.9963	0.9922
	7	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
8	0	0.4305	0.3436	0.2725	0.1678	0.1001	0.0576	0.0390	0.0319	0.0168	0.0084	0.0039
0	1	0.4303	0.7363	0.2123 $0.6572$	0.5033	0.3671	0.0570 $0.2553$	0.0350 $0.1951$	0.0319 $0.1691$	0.0163 $0.1064$	0.0632	0.0059 $0.0352$
	2	0.9619	0.9327	0.8948	0.7969	0.6785	0.5518	0.4682	0.4278	0.3154	0.2201	0.1445
	3	0.9950	0.9888	0.9786	0.9437	0.8862	0.8059	0.7414	0.7064	0.5941	0.4770	0.3633
	4	0.9996	0.9988	0.9971	0.9896	0.9727	0.9420	0.9121	0.8939	0.8263	0.7396	0.6367
	5	1.0000	0.9999	0.9998	0.9988	0.9958	0.9887	0.9803	0.9747	0.9502	0.9115	0.8555
	6	1.0000	1.0000	1.0000	0.9999	0.9996	0.9987	0.9974	0.9964	0.9915	0.9819	0.9648
	7	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9998	0.9993	0.9983	0.9961
	8	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
9	0	0.3874	0.3007	0.2316	0.1342	0.0751	0.0404	0.0260	0.0207	0.0101	0.0046	0.0020
	1	0.7748	0.6872	0.5995	0.4362	0.3003	0.1960	0.1431	0.1211	0.0705	0.0385	0.0195
	2	0.9470	0.9081	0.8591	0.7382	0.6007	0.4628	0.3772	0.3373	0.2318	0.1495	0.0898
	3	0.9917	0.9817	0.9661	0.9144	0.8343	0.7297	0.6503	0.6089	0.4826	0.3614	0.2539
	4	0.9991	0.9975	0.9944	0.9804	0.9511	0.9012	0.8552	0.8283	0.7334	0.6214	0.5000
	5	0.9999	0.9998	0.9994	0.9969	0.9900	0.9747	0.9576	0.9464	0.9006	0.8342	0.7461
	6	1.0000	1.0000	1.0000	0.9997	0.9987	0.9957	0.9917	0.9888	0.9750	0.9502	0.9102
	7	1.0000	1.0000	1.0000	1.0000	0.9999	0.9996	0.9990	0.9986	0.9962	0.9909	0.9805
	8	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9997	0.9992	0.9980
	9	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
10	0	0.3487	0.2631	0.1969	0.1074	0.0563	0.0282	0.0173	0.0135	0.0060	0.0025	0.0010
	1	0.7361	0.6389	0.5443	0.3758	0.2440	0.1493	0.1040	0.0860	0.0464	0.0233	0.0107
	2	0.9298	0.8805	0.8202	0.6778	0.5256	0.3828	0.2991	0.2616	0.1673	0.0996	0.0547
	3	0.9872	0.9725	0.9500	0.8791	0.7759	0.6496	0.5593	0.5138 $0.7515$	0.3823	0.2660	0.1719
	$\frac{4}{5}$	0.9984 $0.9999$	0.9955 $0.9995$	0.9901 $0.9986$	0.9672 $0.9936$	0.9219 $0.9803$	0.8497 $0.9527$	0.7869 $0.9234$	0.7515 $0.9051$	0.6331 $0.8338$	0.5044 $0.7384$	$0.3770 \\ 0.6230$
	6	1.0000	1.0000	0.9999	0.9991	0.9965	0.9894	0.9254 $0.9803$	0.9031 $0.9740$	0.9452	0.7384	0.0230 $0.8281$
	7	1.0000	1.0000	1.0000	0.9999	0.9996	0.9984	0.9966	0.9952	0.9877	0.9726	0.9453
	8	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9996	0.9995	0.9983	0.9955	0.9893
	9	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9997	0.9990
	10	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
-11												
11	0	0.3138	0.2302	0.1673	0.0859	0.0422	0.0198	0.0116	0.0088	0.0036	0.0014	0.0005
	$\frac{1}{2}$	0.6974 $0.9104$	0.5919 $0.8503$	0.4922 $0.7788$	0.3221 $0.6174$	0.1971 $0.4552$	$0.1130 \\ 0.3127$	0.0751 $0.2341$	0.0606 $0.2001$	0.0302 $0.1189$	0.0139 $0.0652$	$0.0059 \\ 0.0327$
	3	0.9104 $0.9815$	0.9610	0.9306	0.8389	0.4332 $0.7133$	0.5127 $0.5696$	0.2341 $0.4726$	0.2001 $0.4256$	0.1169 $0.2963$	0.0052 $0.1911$	0.0327 $0.1133$
	4	0.9972	0.9927	0.9841	0.9496	0.8854	0.7897	0.7110	0.6683	0.5328	0.3971	0.2744
	5	0.9997	0.9990	0.9973	0.9883	0.9657	0.9218	0.8779	0.8513	0.7535	0.6331	0.5000
	6	1.0000	0.9999	0.9997	0.9980	0.9924	0.9784	0.9614	0.9499	0.9006	0.8262	0.7256
	7	1.0000	1.0000	1.0000	0.9998	0.9988	0.9957	0.9912	0.9878	0.9707	0.9390	0.8867
	8	1.0000	1.0000	1.0000	1.0000	0.9999	0.9994	0.9986	0.9980	0.9941	0.9852	0.9673
	9	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9993	0.9978	0.9941
	10	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9998	0.9995
	11	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
12	0	0.2824	0.2014	0.1422	0.0687	0.0317	0.0138	0.0077	0.0057	0.0022	0.0008	0.0002
14	1	0.2524 $0.6590$	0.2014 $0.5467$	0.1422 $0.4435$	0.0037 $0.2749$	0.0517 $0.1584$	0.0150 $0.0850$	0.0540	0.0037 $0.0424$	0.0022 $0.0196$	0.0083	0.0002 $0.0032$
	2	0.8891	0.8180	0.7358	0.5583	0.3907	0.2528	0.1811	0.1513	0.0834	0.0421	0.0193
	3	0.9744	0.9472	0.9078	0.7946	0.6488	0.4925	0.3931	0.3467	0.2253	0.1345	0.0730
	4	0.9957	0.9887	0.9761	0.9274	0.8424	0.7237	0.6315	0.5833	0.4382	0.3044	0.1938
	5	0.9995	0.9982	0.9954	0.9806	0.9456	0.8822	0.8223	0.7873	0.6652	0.5269	0.3872
	6	0.9999	0.9998	0.9993	0.9961	0.9857	0.9614	0.9336	0.9154	0.8418	0.7393	0.6128
												,

n	x	0.1	0.125	0.15	0.2	0.25	0.3	0.3333	0.35	0.4	0.45	0.5
12	7	1.0000	1.0000	0.9999	0.9994	0.9972	0.9905	0.9812	0.9745	0.9427	0.8883	0.8062
	8	1.0000	1.0000	1.0000	0.9999	0.9996	0.9983	0.9961	0.9944	0.9847	0.9644	0.9270
	9	1.0000	1.0000	1.0000	1.0000	1.0000	0.9998	0.9995	0.9992	0.9972	0.9921	0.9807
	10	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9997	0.9989	0.9968
	11	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998
	12	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
13	0	0.2542	0.1762	0.1209	0.0550	0.0238	0.0097	0.0051	0.0037	0.0013	0.0004	0.0001
	1	0.6213	0.5035	0.3983	0.2336	0.1267	0.0637	0.0385	0.0296	0.0126	0.0049	0.0017
	2	0.8661	0.7841	0.6920	0.5017	0.3326	0.2025	0.1387	0.1132	0.0579	0.0269	0.0112
	3	0.9658	0.9310	0.8820	0.7473	0.5843	0.4206	0.3224	0.2783	0.1686	0.0929	0.0461
	4	0.9935	0.9835	0.9658	0.9009	0.7940	0.6543	0.5520	0.5005	0.3530	0.2279	0.1334
	5	0.9991	0.9970	0.9925	0.9700	0.9198	0.8346	0.7587	0.7159	0.5744	0.4268	0.2905
	6	0.9999	0.9996	0.9987	0.9930	0.9757	0.9376	0.8965	0.8705	0.7712	0.6437	0.5000
	7	1.0000	1.0000	0.9998	0.9988	0.9944	0.9818	0.9653	0.9538	0.9023	0.8212	0.7095
	8	1.0000	1.0000	1.0000	0.9998	0.9990	0.9960	0.9912	0.9874	0.9679	0.9302	0.8666
	9	1.0000	1.0000	1.0000	1.0000	0.9999	0.9993	0.9984	0.9975	0.9922	0.9797	0.9539
	10	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9997	0.9987	0.9959	0.9888
	11	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9995	0.9983
	12	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999
	13	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
14	0	0.2288	0.1542	0.1028	0.0440	0.0178	0.0068	0.0034	0.0024	0.0008	0.0002	0.0001
14	1	0.5846	0.1642	0.3567	0.1979	0.1010	0.0475	0.0034 $0.0274$	0.0024 $0.0205$	0.0081	0.0029	0.0001
	2	0.8416	0.7490	0.6479	0.4481	0.2811	0.1608	0.0274 $0.1053$	0.0209	0.0398	0.0029 $0.0170$	0.0065
	3	0.9559	0.9127	0.8535	0.6982	0.5213	0.3552	0.2612	0.2205	0.1243	0.0632	0.0287
	4	0.9908	0.9770	0.9533	0.8702	0.5215 $0.7415$	0.5842	0.2012 $0.4755$	0.4227	0.1243 $0.2793$	0.0652 $0.1672$	0.0201
	5	0.9985	0.9953	0.9885	0.9561	0.8883	0.7805	0.6898	0.6405	0.4859	0.3373	0.2120
	6	0.9998	0.9993	0.9978	0.9884	0.9617	0.9067	0.8505	0.8164	0.6925	0.5461	0.3953
	7	1.0000	0.9999	0.9997	0.9976	0.9897	0.9685	0.9424	0.9247	0.8499	0.7414	0.6047
	8	1.0000	1.0000	1.0000	0.9996	0.9978	0.9917	0.9826	0.9757	0.9417	0.8811	0.7880
	9	1.0000	1.0000	1.0000	1.0000	0.9997	0.9983	0.9960	0.9940	0.9825	0.9574	0.9102
	10	1.0000	1.0000	1.0000	1.0000	1.0000	0.9998	0.9993	0.9989 $0.9999$	0.9961 $0.9994$	0.9886	0.9713
	11	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999			0.9978	0.9935
	12	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9997	0.9991
	$\frac{13}{14}$	1.0000 $1.0000$	1.0000 $1.0000$	1.0000 $1.0000$	1.0000	1.0000 $1.0000$	1.0000 $1.0000$	1.0000 $1.0000$	1.0000 $1.0000$	1.0000 $1.0000$	1.0000 $1.0000$	0.9999 $1.0000$
				1.0000	1.0000	1.0000		1.0000	1.0000	1.0000		1.0000
15	0	0.2059	0.1349	0.0874	0.0352	0.0134	0.0047	0.0023	0.0016	0.0005	0.0001	0.0000
	1	0.5490	0.4241	0.3186	0.1671	0.0802	0.0353	0.0194	0.0142	0.0052	0.0017	0.0005
	2	0.8159	0.7132	0.6042	0.3980	0.2361	0.1268	0.0794	0.0617	0.0271	0.0107	0.0037
	3	0.9444	0.8922	0.8227	0.6482	0.4613	0.2969	0.2092	0.1727	0.0905	0.0424	0.0176
	4	0.9873	0.9689	0.9383	0.8358	0.6865	0.5155	0.4041	0.3519	0.2173	0.1204	0.0592
	5	0.9978	0.9930	0.9832	0.9389	0.8516	0.7216	0.6184	0.5643	0.4032	0.2608	0.1509
	6	0.9997	0.9988	0.9964	0.9819	0.9434	0.8689	0.7970	0.7548	0.6098	0.4522	0.3036
	7	1.0000	0.9998	0.9994	0.9958	0.9827	0.9500	0.9118	0.8868	0.7869	0.6535	0.5000
	8	1.0000	1.0000	0.9999	0.9992	0.9958	0.9848	0.9692	0.9578	0.9050	0.8182	0.6964
	9	1.0000	1.0000	1.0000	0.9999	0.9992	0.9963	0.9915	0.9876	0.9662	0.9231	0.8491
	10	1.0000	1.0000	1.0000	1.0000	0.9999	0.9993	0.9982	0.9972	0.9907	0.9745	0.9408
	11	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9997	0.9995	0.9981	0.9937	0.9824
	12	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9997	0.9989	0.9963
	13	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9995
	14	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
16	0	0.1853	0.1181	0.0743	0.0281	0.0100	0.0033	0.0015	0.0010	0.0003	0.0001	0.0000
	1	0.5147	0.3879	0.2839	0.1407	0.0635	0.0261	0.0137	0.0098	0.0033	0.0010	0.0003
	2	0.7892	0.6771	0.5614	0.3518	0.1971	0.0994	0.0594	0.0451	0.0183	0.0066	0.0021
	3	0.9316	0.8698	0.7899	0.5981	0.4050	0.2459	0.1659	0.1339	0.0651	0.0281	0.0106
	4	0.9830	0.9593	0.9209	0.7982	0.6302	0.4499	0.3391	0.2892	0.1666	0.0853	0.0384
	5	0.9967	0.9900	0.9765	0.9183	0.8103	0.6598	0.5469	0.4900	0.3288	0.1976	0.1051
	6	0.9995	0.9981	0.9944	0.9733	0.9204	0.8247	0.7374	0.6881	0.5272	0.3660	0.2272
	7	0.9999	0.9997	0.9989	0.9930	0.9729	0.9256	0.8735	0.8406	0.7161	0.5629	0.4018
	8	1.0000	1.0000	0.9998	0.9985	0.9925	0.9743	0.9500	0.9329	0.8577	0.7441	0.5982
	9	1.0000	1.0000	1.0000	0.9998	0.9984	0.9929	0.9841	0.9771	0.9417	0.8759	0.7728

n	x	0.1	0.125	0.15	0.2	0.25	0.3	0.3333	0.35	0.4	0.45	0.5
16	10	1.0000	1.0000	1.0000	1.0000	0.9997	0.9984	0.9960	0.9938	0.9809	0.9514	0.8949
	11	1.0000	1.0000	1.0000	1.0000	1.0000	0.9997	0.9992	0.9987	0.9951	0.9851	0.9616
	12	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9991	0.9965	0.9894
	13	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9994	0.9979
	14	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9997
	15	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
17	0	0.1668	0.1033	0.0631	0.0225	0.0075	0.0023	0.0010	0.0007	0.0002	0.0000	0.0000
	1	0.4818	0.3542	0.2525	0.1182	0.0501	0.0193	0.0096	0.0067	0.0021	0.0006	0.0001
	2	0.7618	0.6409	0.5198	0.3096	0.1637	0.0774	0.0442	0.0327	0.0123	0.0041	0.0012
	3	0.9174	0.8457	0.7556	0.5489	0.3530	0.2019	0.1304	0.1028	0.0464	0.0184	0.0064
	4	0.9779	0.9482	0.9013	0.7582	0.5739	0.3887	0.2814	0.2348	0.1260	0.0596	0.0245
	5	0.9953	0.9862	0.9681	0.8943	0.7653	0.5968	0.4777	0.4197	0.2639	0.1471	0.0717
	6	0.9992	0.9971	0.9917	0.9623	0.8929	0.7752	0.6739	0.6188	0.4478	0.2902	0.1662
	7	0.9999	0.9995	0.9983	0.9891	0.9598	0.8954	0.8281	0.7872	0.6405	0.4743	0.3145
	8	1.0000	0.9999	0.9997	0.9974	0.9876	0.9597	0.9245	0.9006	0.8011	0.6626	0.5000
	9	1.0000	1.0000	1.0000	0.9995	0.9969	0.9873	0.9727	0.9617	0.9081	0.8166	0.6855
	10	1.0000	1.0000	1.0000	0.9999	0.9994	0.9968	0.9920	0.9880	0.9652	0.9174	0.8338
	11	1.0000	1.0000	1.0000	1.0000	0.9999	0.9993	0.9981	0.9970	0.9894	0.9699	0.9283
	12	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9997	0.9994	0.9975	0.9914	0.9755
	13	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9995	0.9981	0.9936
	14	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9997	0.9988
	15 16	1.0000 $1.0000$	1.0000 $1.0000$	1.0000 $1.0000$	1.0000 1.0000	1.0000 $1.0000$	1.0000 1.0000	1.0000 1.0000	1.0000 1.0000	1.0000 1.0000	1.0000 $1.0000$	0.9999 $1.0000$
18	0	0.1501	0.0904	0.0536	0.0180	0.0056	0.0016	0.0007	0.0004	0.0001	0.0000	0.0000
	1	0.4503	0.3228	0.2241	0.0991	0.0395	0.0142	0.0068	0.0046	0.0013	0.0003	0.0001
	2	0.7338	0.6051	0.4797	0.2713	0.1353	0.0600	0.0326	0.0236	0.0082	0.0025	0.0007
	3	0.9018	0.8201	0.7202	0.5010	0.3057	0.1646	0.1017	0.0783	0.0328	0.0120	0.0038
	$\frac{4}{5}$	0.9718 $0.9936$	0.9354 $0.9814$	0.8794 $0.9581$	0.7164 $0.8671$	0.5187 $0.7175$	0.3327 $0.5344$	0.2311 $0.4122$	0.1886 $0.3550$	0.0942 $0.2088$	0.0411 $0.1077$	0.0154 $0.0481$
	6	0.9988	0.9814 $0.9957$	0.9381 $0.9882$	0.8071 $0.9487$	0.7173 $0.8610$	0.5344 $0.7217$	0.4122 $0.6085$	0.5350 $0.5491$	0.2088 $0.3743$	0.1077 $0.2258$	0.0481 $0.1189$
	7	0.9998	0.9991	0.9973	0.9437	0.9431	0.7217	0.7767	0.7283	0.5634	0.2256 $0.3915$	0.1109 $0.2403$
	8	1.0000	0.9999	0.9995	0.9957	0.9807	0.9404	0.8924	0.8609	0.7368	0.5778	0.4073
	9	1.0000	1.0000	0.9999	0.9991	0.9946	0.9790	0.9567	0.9403	0.8653	0.7473	0.5927
	10	1.0000	1.0000	1.0000	0.9998	0.9988	0.9939	0.9856	0.9788	0.9424	0.8720	0.7597
	11	1.0000	1.0000	1.0000	1.0000	0.9998	0.9986	0.9961	0.9938	0.9797	0.9463	0.8811
	12	1.0000	1.0000	1.0000	1.0000	1.0000	0.9997	0.9991	0.9986	0.9942	0.9817	0.9519
	13	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9997	0.9987	0.9951	0.9846
	14	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9998	0.9990	0.9962
	15	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9993
	16	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999
	17	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
19	0	0.1351	0.0791	0.0456	0.0144	0.0042	0.0011	0.0005	0.0003	0.0001	0.0000	0.0000
	1	0.4203	0.2938	0.1985	0.0829	0.0310	0.0104	0.0047	0.0031	0.0008	0.0002	0.0000
	2	0.7054	0.5698	0.4413	0.2369	0.1113	0.0462	0.0240	0.0170	0.0055	0.0015	0.0004
	3	0.8850	0.7933	0.6841 $0.8556$	0.4551	0.2631 $0.4654$	0.1332	0.0787	0.0591	0.0230	0.0077	0.0022
	$\frac{4}{5}$	0.9648 $0.9914$	0.9209 $0.9757$	0.8550 $0.9463$	0.6733 $0.8369$	0.4654 $0.6678$	0.2822 $0.4739$	0.1879 $0.3519$	$0.1500 \\ 0.2968$	0.0696 $0.1629$	0.0280 $0.0777$	0.0096 $0.0318$
	6	0.9914 $0.9983$	0.9737 $0.9939$	0.9403 $0.9837$	0.8309 $0.9324$	0.8251	0.4759 $0.6655$	0.5319 $0.5431$	0.2908 $0.4812$	0.1029 $0.3081$	0.0777 $0.1727$	0.0318 $0.0835$
	7	0.9997	0.9988	0.9959	0.9767	0.9225	0.8180	0.7207	0.6656	0.4878	0.3169	0.1796
	8	1.0000	0.9998	0.9992	0.9933	0.9713	0.9161	0.8538	0.8145	0.6675	0.4940	0.3238
	9	1.0000	1.0000	0.9999	0.9984	0.9911	0.9674	0.9352	0.9125	0.8139	0.6710	0.5000
	10	1.0000	1.0000	1.0000	0.9997	0.9977	0.9895	0.9759	0.9653	0.9115	0.8159	0.6762
	11	1.0000	1.0000	1.0000	1.0000	0.9995	0.9972	0.9926	0.9886	0.9648	0.9129	0.8204
	12	1.0000	1.0000	1.0000	1.0000	0.9999	0.9994	0.9981	0.9969	0.9884	0.9658	0.9165
	13	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9996	0.9993	0.9969	0.9891	0.9682
	14	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9994	0.9972	0.9904
	15	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9995	0.9978
	16	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9996
	17	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000
20	0	0.1216	0.0692	0.0388	0.0115	0.0032	0.0008	0.0003	0.0002	0.0000	0.0000	0.0000
	1	0.3917	0.2669	0.1756	0.0692	0.0243	0.0076	0.0033	0.0021	0.0005	0.0001	0.0000
												,

n	x	0.1	0.125	0.15	0.2	0.25	0.3	0.3333	0.35	0.4	0.45	0.5
20	2	0.6769	0.5353	0.4049	0.2061	0.0913	0.0355	0.0176	0.0121	0.0036	0.0009	0.0002
	3	0.8670	0.7653	0.6477	0.4114	0.2252	0.1071	0.0604	0.0444	0.0160	0.0049	0.0013
	4	0.9568	0.9050	0.8298	0.6296	0.4148	0.2375	0.1515	0.1182	0.0510	0.0189	0.0059
	5	0.9887	0.9688	0.9327	0.8042	0.6172	0.4164	0.2972	0.2454	0.1256	0.0553	0.0207
	6	0.9976	0.9916	0.9781	0.9133	0.7858	0.6080	0.4793	0.4166	0.2500	0.1299	0.0577
	7	0.9996	0.9981	0.9941	0.9679	0.8982	0.7723	0.6615	0.6010	0.4159	0.2520	0.1316
	8	0.9999	0.9997	0.9987	0.9900	0.9591	0.8867	0.8095	0.7624	0.5956	0.4143	0.2517
	9	1.0000	0.9999	0.9998	0.9974	0.9861	0.9520	0.9081	0.8782	0.7553	0.5914	0.4119
	10	1.0000	1.0000	1.0000	0.9994	0.9961	0.9829	0.9624	0.9468	0.8725	0.7507	0.5881
	11	1.0000	1.0000	1.0000	0.9999	0.9991	0.9949	0.9870	0.9804	0.9435	0.8692	0.7483
	12	1.0000	1.0000	1.0000	1.0000	0.9998	0.9987	0.9963	0.9940	0.9790	0.9420	0.8684
	13	1.0000	1.0000	1.0000	1.0000	1.0000	0.9997	0.9991	0.9985	0.9935	0.9786	0.9423
	14	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9998	0.9997	0.9984	0.9936	0.9793
	15	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9997	0.9985	0.9941
	16	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9997	0.9987
	17	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9998
	18	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000

Cumulative distribution function 2. Poisson distribution

### 2 Poisson distribution

10

#### **Cumulative distribution function**

This section tabulates the cumulative distribution function (c.d.f.) of the Poisson distribution with expected value ("rate")  $\lambda$ , which is

$$F(x) = \mathbb{P}\{X \le x\} = \sum_{k=0}^{x} \mathbb{P}\{X = k\} = \sum_{k=0}^{x} \exp(-\lambda) \frac{\lambda^k}{k!}.$$

							$\lambda$						
x	0.02	0.04	0.06	0.08	0.1	0.15	0.2	0.25	0.3	0.35	0.4	0.45	0.5
0	0.9802	0.9608	0.9418	0.9231	0.9048	0.8607	0.8187	0.7788	0.7408	0.7047	0.6703	0.6376	0.6065
1	0.9998	0.9992	0.9983	0.9970	0.9953	0.9898	0.9825	0.9735	0.9631	0.9513	0.9384	0.9246	0.9098
$^{2}$	1.0000	1.0000	1.0000	0.9999	0.9998	0.9995	0.9989	0.9978	0.9964	0.9945	0.9921	0.9891	0.9856
3	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9997	0.9995	0.9992	0.9988	0.9982
4	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9998
5	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000

							$\lambda$						
x	0.55	0.6	0.65	0.7	0.75	0.8	0.85	0.9	0.95	1	1.1	1.2	1.3
0	0.5769	0.5488	0.5220	0.4966	0.4724	0.4493	0.4274	0.4066	0.3867	0.3679	0.3329	0.3012	0.2725
1	0.8943	0.8781	0.8614	0.8442	0.8266	0.8088	0.7907	0.7725	0.7541	0.7358	0.6990	0.6626	0.6268
2	0.9815	0.9769	0.9717	0.9659	0.9595	0.9526	0.9451	0.9371	0.9287	0.9197	0.9004	0.8795	0.8571
3	0.9975	0.9966	0.9956	0.9942	0.9927	0.9909	0.9889	0.9865	0.9839	0.9810	0.9743	0.9662	0.9569
4	0.9997	0.9996	0.9994	0.9992	0.9989	0.9986	0.9982	0.9977	0.9971	0.9963	0.9946	0.9923	0.9893
5	1.0000	1.0000	0.9999	0.9999	0.9999	0.9998	0.9997	0.9997	0.9995	0.9994	0.9990	0.9985	0.9978
6	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9999	0.9997	0.9996
7	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999
8	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000

							$\lambda$						
x	1.4	1.5	1.6	1.7	1.8	1.9	2	2.2	2.4	2.6	2.8	3	3.2
0	0.2466	0.2231	0.2019	0.1827	0.1653	0.1496	0.1353	0.1108	0.0907	0.0743	0.0608	0.0498	0.0408
1	0.5918	0.5578	0.5249	0.4932	0.4628	0.4337	0.4060	0.3546	0.3084	0.2674	0.2311	0.1991	0.1712
2	0.8335	0.8088	0.7834	0.7572	0.7306	0.7037	0.6767	0.6227	0.5697	0.5184	0.4695	0.4232	0.3799
3	0.9463	0.9344	0.9212	0.9068	0.8913	0.8747	0.8571	0.8194	0.7787	0.7360	0.6919	0.6472	0.6025
4	0.9857	0.9814	0.9763	0.9704	0.9636	0.9559	0.9473	0.9275	0.9041	0.8774	0.8477	0.8153	0.7806
5	0.9968	0.9955	0.9940	0.9920	0.9896	0.9868	0.9834	0.9751	0.9643	0.9510	0.9349	0.9161	0.8946
6	0.9994	0.9991	0.9987	0.9981	0.9974	0.9966	0.9955	0.9925	0.9884	0.9828	0.9756	0.9665	0.9554
7	0.9999	0.9998	0.9997	0.9996	0.9994	0.9992	0.9989	0.9980	0.9967	0.9947	0.9919	0.9881	0.9832
8	1.0000	1.0000	1.0000	0.9999	0.9999	0.9998	0.9998	0.9995	0.9991	0.9985	0.9976	0.9962	0.9943
9	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9996	0.9993	0.9989	0.9982
10	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9997	0.9995
11	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999
12	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000

							$\lambda$						
x	3.4	3.6	3.8	4	4.2	4.4	4.6	4.8	5	5.2	5.4	5.6	5.8
0	0.0334	0.0273	0.0224	0.0183	0.0150	0.0123	0.0101	0.0082	0.0067	0.0055	0.0045	0.0037	0.0030
1	0.1468	0.1257	0.1074	0.0916	0.0780	0.0663	0.0563	0.0477	0.0404	0.0342	0.0289	0.0244	0.0206
2	0.3397	0.3027	0.2689	0.2381	0.2102	0.1851	0.1626	0.1425	0.1247	0.1088	0.0948	0.0824	0.0715
3	0.5584	0.5152	0.4735	0.4335	0.3954	0.3594	0.3257	0.2942	0.2650	0.2381	0.2133	0.1906	0.1700
4	0.7442	0.7064	0.6678	0.6288	0.5898	0.5512	0.5132	0.4763	0.4405	0.4061	0.3733	0.3422	0.3127
5	0.8705	0.8441	0.8156	0.7851	0.7531	0.7199	0.6858	0.6510	0.6160	0.5809	0.5461	0.5119	0.4783
6	0.9421	0.9267	0.9091	0.8893	0.8675	0.8436	0.8180	0.7908	0.7622	0.7324	0.7017	0.6703	0.6384
7	0.9769	0.9692	0.9599	0.9489	0.9361	0.9214	0.9049	0.8867	0.8666	0.8449	0.8217	0.7970	0.7710

2. Poisson distribution Cumulative distribution function

x	3.4	3.6	3.8	4	4.2	4.4	4.6	4.8	5	5.2	5.4	5.6	5.8
8	0.9917	0.9883	0.9840	0.9786	0.9721	0.9642	0.9549	0.9442	0.9319	0.9181	0.9027	0.8857	0.8672
9	0.9973	0.9960	0.9942	0.9919	0.9889	0.9851	0.9805	0.9749	0.9682	0.9603	0.9512	0.9409	0.9292
10	0.9992	0.9987	0.9981	0.9972	0.9959	0.9943	0.9922	0.9896	0.9863	0.9823	0.9775	0.9718	0.9651
11	0.9998	0.9996	0.9994	0.9991	0.9986	0.9980	0.9971	0.9960	0.9945	0.9927	0.9904	0.9875	0.9841
12	0.9999	0.9999	0.9998	0.9997	0.9996	0.9993	0.9990	0.9986	0.9980	0.9972	0.9962	0.9949	0.9932
13	1.0000	1.0000	1.0000	0.9999	0.9999	0.9998	0.9997	0.9995	0.9993	0.9990	0.9986	0.9980	0.9973
14	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9999	0.9998	0.9997	0.9995	0.9993	0.9990
15	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9998	0.9998	0.9996
16	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9999
17	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000

							$\lambda$						
x	6	6.2	6.4	6.6	6.8	7	7.2	7.4	7.6	7.8	8	8.5	9
0	0.0025	0.0020	0.0017	0.0014	0.0011	0.0009	0.0007	0.0006	0.0005	0.0004	0.0003	0.0002	0.0001
1	0.0174	0.0146	0.0123	0.0103	0.0087	0.0073	0.0061	0.0051	0.0043	0.0036	0.0030	0.0019	0.0012
2	0.0620	0.0536	0.0463	0.0400	0.0344	0.0296	0.0255	0.0219	0.0188	0.0161	0.0138	0.0093	0.0062
3	0.1512	0.1342	0.1189	0.1052	0.0928	0.0818	0.0719	0.0632	0.0554	0.0485	0.0424	0.0301	0.0212
4	0.2851	0.2592	0.2351	0.2127	0.1920	0.1730	0.1555	0.1395	0.1249	0.1117	0.0996	0.0744	0.0550
5	0.4457	0.4141	0.3837	0.3547	0.3270	0.3007	0.2759	0.2526	0.2307	0.2103	0.1912	0.1496	0.1157
6	0.6063	0.5742	0.5423	0.5108	0.4799	0.4497	0.4204	0.3920	0.3646	0.3384	0.3134	0.2562	0.2068
7	0.7440	0.7160	0.6873	0.6581	0.6285	0.5987	0.5689	0.5393	0.5100	0.4812	0.4530	0.3856	0.3239
8	0.8472	0.8259	0.8033	0.7796	0.7548	0.7291	0.7027	0.6757	0.6482	0.6204	0.5925	0.5231	0.4557
9	0.9161	0.9016	0.8858	0.8686	0.8502	0.8305	0.8096	0.7877	0.7649	0.7411	0.7166	0.6530	0.5874
10	0.9574	0.9486	0.9386	0.9274	0.9151	0.9015	0.8867	0.8707	0.8535	0.8352	0.8159	0.7634	0.7060
11	0.9799	0.9750	0.9693	0.9627	0.9552	0.9467	0.9371	0.9265	0.9148	0.9020	0.8881	0.8487	0.8030
12	0.9912	0.9887	0.9857	0.9821	0.9779	0.9730	0.9673	0.9609	0.9536	0.9454	0.9362	0.9091	0.8758
13	0.9964	0.9952	0.9937	0.9920	0.9898	0.9872	0.9841	0.9805	0.9762	0.9714	0.9658	0.9486	0.9261
14	0.9986	0.9981	0.9974	0.9966	0.9956	0.9943	0.9927	0.9908	0.9886	0.9859	0.9827	0.9726	0.9585
15	0.9995	0.9993	0.9990	0.9986	0.9982	0.9976	0.9969	0.9959	0.9948	0.9934	0.9918	0.9862	0.9780
16	0.9998	0.9997	0.9996	0.9995	0.9993	0.9990	0.9987	0.9983	0.9978	0.9971	0.9963	0.9934	0.9889
17	0.9999	0.9999	0.9999	0.9998	0.9997	0.9996	0.9995	0.9993	0.9991	0.9988	0.9984	0.9970	0.9947
18	1.0000	1.0000	1.0000	0.9999	0.9999	0.9999	0.9998	0.9997	0.9996	0.9995	0.9993	0.9987	0.9976
19	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9999	0.9998	0.9997	0.9995	0.9989
20	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9998	0.9996
21	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998
22	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999
23	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000

							$\lambda$						
x	9.5	10	10.5	11	11.5	12	12.5	13	13.5	14	14.5	15	15.5
0	0.0001	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
1	0.0008	0.0005	0.0003	0.0002	0.0001	0.0001	0.0001	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
2	0.0042	0.0028	0.0018	0.0012	0.0008	0.0005	0.0003	0.0002	0.0001	0.0001	0.0001	0.0000	0.0000
3	0.0149	0.0103	0.0071	0.0049	0.0034	0.0023	0.0016	0.0011	0.0007	0.0005	0.0003	0.0002	0.0001
4	0.0403	0.0293	0.0211	0.0151	0.0107	0.0076	0.0053	0.0037	0.0026	0.0018	0.0012	0.0009	0.0006
5	0.0885	0.0671	0.0504	0.0375	0.0277	0.0203	0.0148	0.0107	0.0077	0.0055	0.0039	0.0028	0.0020
6	0.1649	0.1301	0.1016	0.0786	0.0603	0.0458	0.0346	0.0259	0.0193	0.0142	0.0105	0.0076	0.0055
7	0.2687	0.2202	0.1785	0.1432	0.1137	0.0895	0.0698	0.0540	0.0415	0.0316	0.0239	0.0180	0.0135
8	0.3918	0.3328	0.2794	0.2320	0.1906	0.1550	0.1249	0.0998	0.0790	0.0621	0.0484	0.0374	0.0288
9	0.5218	0.4579	0.3971	0.3405	0.2888	0.2424	0.2014	0.1658	0.1353	0.1094	0.0878	0.0699	0.0552
10	0.6453	0.5830	0.5207	0.4599	0.4017	0.3472	0.2971	0.2517	0.2112	0.1757	0.1449	0.1185	0.0961
11	0.7520	0.6968	0.6387	0.5793	0.5198	0.4616	0.4058	0.3532	0.3045	0.2600	0.2201	0.1848	0.1538
12	0.8364	0.7916	0.7420	0.6887	0.6329	0.5760	0.5190	0.4631	0.4093	0.3585	0.3111	0.2676	0.2283
13	0.8981	0.8645	0.8253	0.7813	0.7330	0.6815	0.6278	0.5730	0.5182	0.4644	0.4125	0.3632	0.3171
14	0.9400	0.9165	0.8879	0.8540	0.8153	0.7720	0.7250	0.6751	0.6233	0.5704	0.5176	0.4657	0.4154
15	0.9665	0.9513	0.9317	0.9074	0.8783	0.8444	0.8060	0.7636	0.7178	0.6694	0.6192	0.5681	0.5170
16	0.9823	0.9730	0.9604	0.9441	0.9236	0.8987	0.8693	0.8355	0.7975	0.7559	0.7112	0.6641	0.6154
17	0.9911	0.9857	0.9781	0.9678	0.9542	0.9370	0.9158	0.8905	0.8609	0.8272	0.7897	0.7489	0.7052
18	0.9957	0.9928	0.9885	0.9823	0.9738	0.9626	0.9481	0.9302	0.9084	0.8826	0.8530	0.8195	0.7825
													$\rightarrow$

Cumulative distribution function 2. Poisson distribution

x	9.5	10	10.5	11	11.5	12	12.5	13	13.5	14	14.5	15	15.5
19	0.9980	0.9965	0.9942	0.9907	0.9857	0.9787	0.9694	0.9573	0.9421	0.9235	0.9012	0.8752	0.8455
20	0.9991	0.9984	0.9972	0.9953	0.9925	0.9884	0.9827	0.9750	0.9649	0.9521	0.9362	0.9170	0.8944
21	0.9996	0.9993	0.9987	0.9977	0.9962	0.9939	0.9906	0.9859	0.9796	0.9712	0.9604	0.9469	0.9304
22	0.9999	0.9997	0.9994	0.9990	0.9982	0.9970	0.9951	0.9924	0.9885	0.9833	0.9763	0.9673	0.9558
23	0.9999	0.9999	0.9998	0.9995	0.9992	0.9985	0.9975	0.9960	0.9938	0.9907	0.9863	0.9805	0.9730
24	1.0000	1.0000	0.9999	0.9998	0.9996	0.9993	0.9988	0.9980	0.9968	0.9950	0.9924	0.9888	0.9840
25	1.0000	1.0000	1.0000	0.9999	0.9998	0.9997	0.9994	0.9990	0.9984	0.9974	0.9959	0.9938	0.9909
26	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9997	0.9995	0.9992	0.9987	0.9979	0.9967	0.9950
27	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9998	0.9996	0.9994	0.9989	0.9983	0.9973
28	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9997	0.9995	0.9991	0.9986
29	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9998	0.9996	0.9993
30	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9998	0.9997
31	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998
32	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999
33	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000

							$\lambda$						
x	16	17	18	19	20	21	22	23	24	25	30	35	40
2	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
3	0.0001	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
4	0.0004	0.0002	0.0001	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
5	0.0014	0.0007	0.0003	0.0002	0.0001	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
6	0.0040	0.0021	0.0010	0.0005	0.0003	0.0001	0.0001	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
7	0.0100	0.0054	0.0029	0.0015	0.0008	0.0004	0.0002	0.0001	0.0000	0.0000	0.0000	0.0000	0.0000
8	0.0220	0.0126	0.0071	0.0039	0.0021	0.0011	0.0006	0.0003	0.0002	0.0001	0.0000	0.0000	0.0000
9	0.0433	0.0261	0.0154	0.0089	0.0050	0.0028	0.0015	0.0008	0.0004	0.0002	0.0000	0.0000	0.0000
10	0.0774	0.0491	0.0304	0.0183	0.0108	0.0063	0.0035	0.0020	0.0011	0.0006	0.0000	0.0000	0.0000
11	0.1270	0.0847	0.0549	0.0347	0.0214	0.0129	0.0076	0.0044	0.0025	0.0014	0.0001	0.0000	0.0000
12	0.1931	0.1350	0.0917	0.0606	0.0390	0.0245	0.0151	0.0091	0.0054	0.0031	0.0002	0.0000	0.0000
13	0.2745	0.2009	0.1426	0.0984	0.0661	0.0434	0.0278	0.0174	0.0107	0.0065	0.0004	0.0000	0.0000
14	0.3675	0.2808	0.2081	0.1497	0.1049	0.0716	0.0477	0.0311	0.0198	0.0124	0.0009	0.0000	0.0000
15	0.4667	0.3715	0.2867	0.2148	0.1565	0.1111	0.0769	0.0520	0.0344	0.0223	0.0019	0.0001	0.0000
16	0.5660	0.4677	0.3751	0.2920	0.2211	0.1629	0.1170	0.0821	0.0563	0.0377	0.0039	0.0003	0.0000
17	0.6593	0.5640	0.4686	0.3784	0.2970	0.2270	0.1690	0.1228	0.0871	0.0605	0.0073	0.0006	0.0000
18	0.7423	0.6550	0.5622	0.4695	0.3814	0.3017	0.2325	0.1748	0.1283	0.0920	0.0129	0.0012	0.0001
19	0.8122	0.7363	0.6509	0.5606	0.4703	0.3843	0.3060	0.2377	0.1803	0.1336	0.0219	0.0023	0.0002
20	0.8682	0.8055	0.7307	0.6472	0.5591	0.4710	0.3869	0.3101	0.2426	0.1855	0.0353	0.0043	0.0004
21	0.9108	0.8615	0.7991	0.7255	0.6437	0.5577	0.4716	0.3894	0.3139	0.2473	0.0544	0.0076	0.0007
22	0.9418	0.9047	0.8551	0.7931	0.7206	0.6405	0.5564	0.4723	0.3917	0.3175	0.0806	0.0128	0.0014
23	0.9633	0.9367	0.8989	0.8490	0.7875	0.7160	0.6374	0.5551	0.4728	0.3939	0.1146	0.0208	0.0026
24	0.9777	0.9594	0.9317	0.8933	0.8432	0.7822	0.7117	0.6346	0.5540	0.4734	0.1572	0.0324	0.0045
25	0.9869	0.9748	0.9554	0.9269	0.8878	0.8377	0.7771	0.7077	0.6319	0.5529	0.2084	0.0486	0.0076
26	0.9925	0.9848	0.9718	0.9514	0.9221	0.8826	0.8324	0.7723	0.7038	0.6294	0.2673	0.0705	0.0123
27	0.9959	0.9912	0.9827	0.9687	0.9475	0.9175	0.8775	0.8274	0.7677	0.7002	0.3329	0.0988	0.0193
28	0.9978	0.9950	0.9897	0.9805	0.9657	0.9436	0.9129	0.8726	0.8225	0.7634	0.4031	0.1343	0.0294
29	0.9989	0.9973	0.9941	0.9882	0.9782	0.9626	0.9398	0.9085	0.8679	0.8179	0.4757	0.1770	0.0432
30	0.9994	0.9986	0.9967	0.9930	0.9865	0.9758	0.9595	0.9360	0.9042	0.8633	0.5484	0.2269	0.0617
31	0.9997	0.9993	0.9982	0.9960	0.9919	0.9848	0.9735	0.9564	0.9322	0.8999	0.6186	0.2833	0.0855
32	0.9999	0.9996	0.9990	0.9978	0.9953	0.9907	0.9831	0.9711	0.9533	0.9285	0.6845	0.3449	0.1153
33	0.9999	0.9998	0.9995	0.9988	0.9973	0.9945	0.9895	0.9813	0.9686	0.9502	0.7444	0.4102	0.1514
34	1.0000	0.9999	0.9998	0.9994	0.9985	0.9968	0.9936	0.9882	0.9794	0.9662	0.7973	0.4775	0.1939
35	1.0000	1.0000	0.9999	0.9997	0.9992	0.9982	0.9962	0.9927	0.9868	0.9775	0.8426	0.5448	0.2424
36	1.0000	1.0000	0.9999	0.9998	0.9996	0.9990	0.9978	0.9956	0.9918	0.9854	0.8804	0.6102	0.2963
37	1.0000	1.0000	1.0000	0.9999	0.9998	0.9995	0.9988	0.9974	0.9950	0.9908	0.9110	0.6721	0.3547
38	1.0000	1.0000	1.0000	1.0000	0.9999	0.9997	0.9993	0.9985	0.9970	0.9943	0.9352	0.7291	0.4160
39	1.0000	1.0000	1.0000	1.0000	0.9999	0.9999	0.9996	0.9992	0.9983	0.9966	0.9537	0.7802	0.4790
40	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9996	0.9990	0.9980	0.9677	0.8249	0.5419
41	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9995	0.9988	0.9779	0.8631	0.6033
42	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9997	0.9993	0.9852	0.8950	0.6618
43	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9996	0.9903	0.9209	0.7162
													$\rightarrow$

2. Poisson distribution Cumulative distribution function

x	16	17	18	19	20	21	22	23	24	25	30	35	40
44	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9998	0.9937	0.9415	0.7657
45	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9960	0.9575	0.8097
46	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9975	0.9697	0.8479
47	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9985	0.9788	0.8804
48	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9991	0.9854	0.9075
49	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9995	0.9902	0.9297
50	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9997	0.9935	0.9474
51	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9998	0.9957	0.9613
52	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9973	0.9719
53	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9983	0.9800
54	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9989	0.9860
55	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9993	0.9903
56	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9996	0.9934
57	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9998	0.9956
58	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9971
59	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999	0.9981
60	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9988
61	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9992
62	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9995
63	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9997
64	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9998
65	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999
66	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	0.9999
67	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000

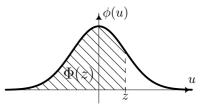
#### 3 Normal distribution

#### Cumulative distribution function $\Phi(z)$

The table below contains the probability

$$\Phi(z) = \mathbb{P}\{Z \le z\} = \int_{-\infty}^z \phi(u) \ du = \int_{-\infty}^z \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{u^2}{2}\right) \ du$$

for a normally distributed random variable Z with expected value 0 and variance 1. The table only contains the probabilities for  $z \geq 0$ . For z < 0, the probabilities can be obtained using the identity  $\Phi(z) = 1 - \Phi(-z)$ .

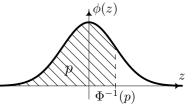


					,	z				
z	□.□0	□.□1	$\Box.\Box2$	□.□3	$\Box.\Box 4$	□.□5	□.□6	□.□7	□.□8	□.□9
$0.0\Box$	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
$0.1\Box$	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
$0.2\Box$	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
$0.3\Box$	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
$0.4\Box$	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
$0.5\Box$	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
$0.6\Box$	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
$0.7\Box$	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
$0.8\Box$	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
$1.0\Box$	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
$1.1\Box$	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
$1.2\Box$	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
$1.3\Box$	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
$1.4\Box$	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
$1.5\Box$	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
$1.6\Box$	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
$1.7\Box$	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8□	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
$1.9\Box$	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
$2.0\Box$	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
$2.1\Box$	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
$2.2\Box$	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
$2.3\Box$	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
$2.4\Box$	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
$2.5\Box$	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
$2.6\Box$	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
$2.7\Box$	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
$2.8\Box$	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981
$2.9\Box$	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
$3.0\Box$	0.9987	0.9987	0.9987	0.9988	0.9988	0.9989	0.9989	0.9989	0.9990	0.9990
$3.1\Box$	0.9990	0.9991	0.9991	0.9991	0.9992	0.9992	0.9992	0.9992	0.9993	0.9993
$3.2\Box$	0.9993	0.9993	0.9994	0.9994	0.9994	0.9994	0.9994	0.9995	0.9995	0.9995
$3.3\Box$	0.9995	0.9995	0.9995	0.9996	0.9996	0.9996	0.9996	0.9996	0.9996	0.9997
$3.4\square$	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9998
$3.5\square$	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998	0.9998
$3.6\square$	0.9998	0.9998	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999
$3.7\Box$	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999
$3.8\square$	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999	0.9999
$3.9\Box$	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000	1.0000

## Inverse $\Phi^{-1}(p)$ of the cumulative distribution function (quantiles)

The table below contains the quantiles of the standard normal distribution. For 0 the quantile is the value of <math>z for which  $\mathbb{P}\{Z \leq z\} = p$ , where  $Z \sim \mathsf{N}(0,1)$ . Thus  $z = \Phi^{-1}(p)$ .

The table only contains the quantiles for  $p \ge \frac{1}{2}$ . For  $p < \frac{1}{2}$  quantiles can be obtained by exploiting the symmetry of the normal distribution:  $\Phi^{-1}(p) = -\Phi^{-1}(1-p)$ .



					1	p				
p	00	$0.\Box\Box 1$	$0.\Box\Box2$	0.□□3	0.□□4	0.005	0.□□6	0.007	0.□□8	0.009
0.50□	0.0000	0.0025	0.0050	0.0075	0.0100	0.0125	0.0150	0.0175	0.0201	0.0226
0.51	0.0251	0.0276	0.0301	0.0326	0.0351	0.0376	0.0401	0.0426	0.0451	0.0476
$0.52\square$	0.0502	0.0527	0.0552	0.0577	0.0602	0.0627	0.0652	0.0677	0.0702	0.0728
$0.53\square$	0.0753	0.0778	0.0803	0.0828	0.0853	0.0878	0.0904	0.0929	0.0954	0.0979
$0.54 \square$	0.1004	0.1030	0.1055	0.1080	0.1105	0.1130	0.1156	0.1181	0.1206	0.1231
$0.55\square$	0.1257	0.1282	0.1307	0.1332	0.1358	0.1383	0.1408	0.1434	0.1459	0.1484
0.56□	0.1510	0.1535	0.1560	0.1586	0.1611	0.1637	0.1662	0.1687	0.1713	0.1738
$0.57\Box$	0.1764	0.1789	0.1815	0.1840	0.1866	0.1891	0.1917	0.1942	0.1968	0.1993
0.58□	0.2019	0.2045	0.2070	0.2096	0.2121	0.2147	0.2173	0.2198	0.2224	0.2250
0.59	0.2275	0.2301	0.2327	0.2353	0.2378	0.2404	0.2430	0.2456	0.2482	0.2508
$0.60\Box$	0.2533	0.2559	0.2585	0.2611	0.2637	0.2663	0.2689	0.2715	0.2741	0.2767
0.61	0.2793	0.2819	0.2845	0.2871	0.2898	0.2924	0.2950	0.2976	0.3002	0.3029
$0.62\Box$	0.3055	0.3081	0.3107	0.3134	0.3160	0.3186	0.3213	0.3239	0.3266	0.3292
0.63	0.3319	0.3345	0.3372	0.3398	0.3425	0.3451	0.3478	0.3505	0.3531	0.3558
$0.64 \square$	0.3585	0.3611	0.3638	0.3665	0.3692	0.3719	0.3745	0.3772	0.3799	0.3826
$0.65 \square$	0.3853	0.3880	0.3907	0.3934	0.3961	0.3989	0.4016	0.4043	0.4070	0.4097
$0.66 \square$	0.4125	0.4152	0.4179	0.4207	0.4234	0.4261	0.4289	0.4316	0.4344	0.4372
$0.67 \square$	0.4399	0.4427	0.4454	0.4482	0.4510	0.4538	0.4565	0.4593	0.4621	0.4649
$0.68 \square$	0.4677	0.4705	0.4733	0.4761	0.4789	0.4817	0.4845	0.4874	0.4902	0.4930
0.69	0.4959	0.4987	0.5015	0.5044	0.5072	0.5101	0.5129	0.5158	0.5187	0.5215
$0.70\Box$	0.5244	0.5273	0.5302	0.5330	0.5359	0.5388	0.5417	0.5446	0.5476	0.5505
0.71	0.5534	0.5563	0.5592	0.5622	0.5651	0.5681	0.5710	0.5740	0.5769	0.5799
$0.72\square$	0.5828	0.5858	0.5888	0.5918	0.5948	0.5978	0.6008	0.6038	0.6068	0.6098
0.73	0.6128	0.6158	0.6189	0.6219	0.6250	0.6280	0.6311	0.6341	0.6372	0.6403
$0.74\square$	0.6433	0.6464	0.6495	0.6526	0.6557	0.6588	0.6620	0.6651	0.6682	0.6713
$0.75\square$	0.6745	0.6776	0.6808	0.6840	0.6871	0.6903	0.6935	0.6967	0.6999	0.7031
$0.76 \square$	0.7063	0.7095	0.7128	0.7160	0.7192	0.7225	0.7257	0.7290	0.7323	0.7356
$0.77\Box$	0.7388	0.7421	0.7454	0.7488	0.7521	0.7554	0.7588	0.7621	0.7655	0.7688
$0.78\square$	0.7722	0.7756	0.7790	0.7824	0.7858	0.7892	0.7926	0.7961	0.7995	0.8030
0.79	0.8064	0.8099	0.8134	0.8169	0.8204	0.8239	0.8274	0.8310	0.8345	0.8381
$0.80\Box$	0.8416	0.8452	0.8488	0.8524	0.8560	0.8596	0.8633	0.8669	0.8705	0.8742
0.81	0.8779	0.8816	0.8853	0.8890	0.8927	0.8965	0.9002	0.9040	0.9078	0.9116
$0.82\square$	0.9154	0.9192	0.9230	0.9269	0.9307	0.9346	0.9385	0.9424	0.9463	0.9502
0.83	0.9542	0.9581	0.9621	0.9661	0.9701	0.9741	0.9782	0.9822	0.9863	0.9904
$0.84\square$	0.9945	0.9986	1.0027	1.0069	1.0110	1.0152	1.0194	1.0237	1.0279	1.0322
$0.85\square$	1.0364	1.0407	1.0450	1.0494	1.0537	1.0581	1.0625	1.0669	1.0714	1.0758
$0.86\square$	1.0803	1.0848	1.0893	1.0939	1.0985	1.1031	1.1077	1.1123	1.1170	1.1217
0.87	1.1264	1.1311	1.1359	1.1407	1.1455	1.1503	1.1552	1.1601	1.1650	1.1700
$0.88\square$	1.1750	1.1800	1.1850	1.1901	1.1952	1.2004	1.2055	1.2107	1.2160	1.2212
0.89□	1.2265	1.2319	1.2372	1.2426	1.2481	1.2536	1.2591	1.2646	1.2702	1.2759
$0.90\Box$	1.2816	1.2873	1.2930	1.2988	1.3047	1.3106	1.3165	1.3225	1.3285	1.3346
0.91	1.3408	1.3469	1.3532	1.3595	1.3658	1.3722	1.3787	1.3852	1.3917	1.3984
0.92	1.4051	1.4118	1.4187	1.4255	1.4325	1.4395	1.4466	1.4538	1.4611	1.4684
0.93□	1.4758	1.4833	1.4909	1.4985	1.5063	1.5141	1.5220	1.5301	1.5382	1.5464
$0.94 \Box$	1.5548	1.5632	1.5718	1.5805	1.5893	1.5982	1.6072	1.6164	1.6258	1.6352
0.95□	1.6449	1.6546	1.6646	1.6747	1.6849	1.6954	1.7060	1.7169	1.7279	1.7392
0.96□	1.7507	1.7624	1.7744	1.7866	1.7991	1.8119	1.8250	1.8384	1.8522	1.8663
0.97	1.8808	1.8957	1.9110	1.9268	1.9431	1.9600	1.9774	1.9954	2.0141	2.0335
0.98□	2.0537	2.0749	2.0969	2.1201	2.1444	2.1701	2.1973	2.2262	2.2571	2.2904
0.99□	2.3263	2.3656	2.4089	2.4573	2.5121	2.5758	2.6521	2.7478	2.8782	3.0902

## Selected quantiles $\Phi^{-1}(\boldsymbol{p})$ in high precision

p	$\Phi^{-1}(p)$	_	p	$\Phi^{-1}(p)$	_	p	$\Phi^{-1}(p)$
0.9	1.2815515655	_	0.999	3.0902323062		0.99999	4.2648907939
0.95	1.6448536270		0.9995	3.2905267315		0.999995	4.4171734135
0.975	1.9599639845		0.99975	3.4807564043		0.9999975	4.5647877303
0.99	2.3263478740		0.9999	3.7190164855		0.999999	4.7534243088
0.995	2.5758293035		0.99995	3.8905918864		0.9999995	4.8916384757
0.9975	2.8070337683	_	0.999975	4.0556269811	_	0.99999975	5.0263128360

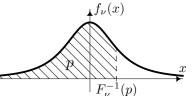
4. Student's t distribution 17

### 4 Student's t distribution

## Inverse ${\cal F}_{\nu}^{-1}(p)$ of the cumulative distribution function (quantiles)

The table below contains the quantiles of Student's t distribution with  $\nu$  degrees of freedom. For 0 the quantile is the value of <math>x for which  $\mathbb{P}\{X \leq x\} = p$ , where  $X \sim \mathsf{t}(\nu)$ . Thus  $x = F_{\nu}^{-1}(p)$ .

 $X \sim \mathsf{t}(\nu)$ . Thus  $x = F_{\nu}^{-1}(p)$ . The table only contains the quantiles for  $p \geq \frac{1}{2}$ . For  $p < \frac{1}{2}$  quantiles can be obtained by exploiting the symmetry of the t distribution:  $F_{\nu}^{-1}(p) = -F_{\nu}^{-1}(1-p)$ .



						1	9					
$\nu$	0.6	0.7	0.75	0.8	0.85	0.9	0.95	0.975	0.99	0.995	0.999	0.9995
1	0.3249	0.7265	1.0000	1.3764	1.9626	3.0777	6.3138	12.706	31.821	63.657	318.31	636.62
2	0.2887	0.6172	0.8165	1.0607	1.3862	1.8856	2.9200	4.3027	6.9646	9.9248	22.327	31.599
3	0.2767	0.5844	0.7649	0.9785	1.2498	1.6377	2.3534	3.1824	4.5407	5.8409	10.215	12.924
4	0.2707	0.5686	0.7407	0.9410	1.1896	1.5332	2.1318	2.7764	3.7469	4.6041	7.1732	8.6103
5	0.2672	0.5594	0.7267	0.9195	1.1558	1.4759	2.0150	2.5706	3.3649	4.0321	5.8934	6.8688
6	0.2648	0.5534	0.7176	0.9057	1.1342	1.4398	1.9432	2.4469	3.1427	3.7074	5.2076	5.9588
7	0.2632	0.5491	0.7111	0.8960	1.1192	1.4149	1.8946	2.3646	2.9980	3.4995	4.7853	5.4079
8	0.2619	0.5459	0.7064	0.8889	1.1081	1.3968	1.8595	2.3060	2.8965	3.3554	4.5008	5.0413
9	0.2610	0.5435	0.7027	0.8834	1.0997	1.3830	1.8331	2.2622	2.8214	3.2498	4.2968	4.7809
10	0.2602	0.5415	0.6998	0.8791	1.0931	1.3722	1.8125	2.2281	2.7638	3.1693	4.1437	4.5869
11	0.2596	0.5399	0.6974	0.8755	1.0877	1.3634	1.7959	2.2010	2.7181	3.1058	4.0247	4.4370
12	0.2590	0.5386	0.6955	0.8726	1.0832	1.3562	1.7823	2.1788	2.6810	3.0545	3.9296	4.3178
13	0.2586	0.5375	0.6938	0.8702	1.0795	1.3502	1.7709	2.1604	2.6503	3.0123	3.8520	4.2208
14	0.2582	0.5366	0.6924	0.8681	1.0763	1.3450	1.7613	2.1448	2.6245	2.9768	3.7874	4.1405
15	0.2579	0.5357	0.6912	0.8662	1.0735	1.3406	1.7531	2.1314	2.6025	2.9467	3.7328	4.0728
16	0.2576	0.5350	0.6901	0.8647	1.0711	1.3368	1.7459	2.1199	2.5835	2.9208	3.6862	4.0150
17	0.2573	0.5344	0.6892	0.8633	1.0690	1.3334	1.7396	2.1098	2.5669	2.8982	3.6458	3.9651
18	0.2571	0.5338	0.6884	0.8620	1.0672	1.3304	1.7341	2.1009	2.5524	2.8784	3.6105	3.9216
19	0.2569	0.5333	0.6876	0.8610	1.0655	1.3277	1.7291	2.0930	2.5395	2.8609	3.5794	3.8834
20	0.2567	0.5329	0.6870	0.8600	1.0640	1.3253	1.7247	2.0860	2.5280	2.8453	3.5518	3.8495
21	0.2566	0.5325	0.6864	0.8591	1.0627	1.3232	1.7207	2.0796	2.5176	2.8314	3.5272	3.8193
22	0.2564	0.5321	0.6858	0.8583	1.0614	1.3212	1.7171	2.0739	2.5083	2.8188	3.5050	3.7921
23	0.2563	0.5317	0.6853	0.8575	1.0603	1.3195	1.7139	2.0687	2.4999	2.8073	3.4850	3.7676
24	0.2562	0.5314	0.6848	0.8569	1.0593	1.3178	1.7109	2.0639	2.4922	2.7969	3.4668	3.7454
25	0.2561	0.5312	0.6844	0.8562	1.0584	1.3163	1.7081	2.0595	2.4851	2.7874	3.4502	3.7251
26	0.2560	0.5309	0.6840	0.8557	1.0575	1.3150	1.7056	2.0555	2.4786	2.7787	3.4350	3.7066
27	0.2559	0.5306	0.6837	0.8551	1.0567	1.3137	1.7033	2.0518	2.4727	2.7707	3.4210	3.6896
28	0.2558	0.5304	0.6834	0.8546	1.0560	1.3125	1.7011	2.0484	2.4671	2.7633	3.4082	3.6739
29	0.2557	0.5302	0.6830	0.8542	1.0553	1.3114	1.6991	2.0452	2.4620	2.7564	3.3962	3.6594
30	0.2556	0.5300	0.6828	0.8538	1.0547	1.3104	1.6973	2.0423	2.4573	2.7500	3.3852	3.6460
31	0.2555	0.5298	0.6825	0.8534	1.0541	1.3095	1.6955	2.0395	2.4528	2.7440	3.3749	3.6335
32	0.2555	0.5297	0.6822	0.8530	1.0535	1.3086	1.6939	2.0369	2.4487	2.7385	3.3653	3.6218
33	0.2554	0.5295	0.6820	0.8526	1.0530	1.3077	1.6924	2.0345	2.4448	2.7333	3.3563	3.6109
34	0.2553	0.5294	0.6818	0.8523	1.0525	1.3070	1.6909	2.0322	2.4411	2.7284	3.3479	3.6007
35	0.2553	0.5292	0.6816	0.8520	1.0520	1.3062	1.6896	2.0301	2.4377	2.7238	3.3400	3.5911
36	0.2552	0.5291	0.6814	0.8517	1.0516	1.3055	1.6883	2.0281	2.4345	2.7195	3.3326	3.5821
37	0.2552	0.5289	0.6812	0.8514	1.0512	1.3049	1.6871	2.0262	2.4314	2.7154	3.3256	3.5737
38	0.2551	0.5288	0.6810	0.8512	1.0508	1.3042	1.6860	2.0244	2.4286	2.7116	3.3190	3.5657
39	0.2551	0.5287	0.6808	0.8509	1.0504	1.3036	1.6849	2.0227	2.4258	2.7079	3.3128	3.5581
40	0.2550	0.5286	0.6807	0.8507	1.0500	1.3031	1.6839	2.0211	2.4233	2.7045	3.3069	3.5510
41	0.2550	0.5285	0.6805	0.8505	1.0497	1.3025	1.6829	2.0195	2.4208	2.7012	3.3013	3.5442
42	0.2550	0.5284	0.6804	0.8503	1.0494	1.3020	1.6820	2.0181	2.4185	2.6981	3.2960	3.5377
43	0.2549	0.5283	0.6802	0.8501	1.0491	1.3016	1.6811	2.0167	2.4163	2.6951	3.2909	3.5316
44	0.2549	0.5282	0.6801	0.8499	1.0488	1.3011	1.6802	2.0154	2.4141	2.6923	3.2861	3.5258
45	0.2549	0.5281	0.6800	0.8497	1.0485	1.3006	1.6794	2.0141	2.4121	2.6896	3.2815	3.5203
46	0.2548	0.5281	0.6799	0.8495	1.0483	1.3002	1.6787	2.0129	2.4102	2.6870	3.2771	3.5150
47	0.2548	0.5280	0.6797	0.8493	1.0480	1.2998	1.6779	2.0117	2.4083	2.6846	3.2729	3.5099
48	0.2548	0.5279	0.6796	0.8492	1.0478	1.2994	1.6772	2.0106	2.4066	2.6822	3.2689	3.5051
49	0.2547	0.5278	0.6795	0.8490	1.0475	1.2991	1.6766	2.0096	2.4049	2.6800	3.2651	3.5004

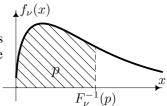
$\nu$	0.6	0.7	0.75	0.8	0.85	0.9	0.95	0.975	0.99	0.995	0.999	0.9995
50	0.2547	0.5278	0.6794	0.8489	1.0473	1.2987	1.6759	2.0086	2.4033	2.6778	3.2614	3.4960
51	0.2547	0.5277	0.6793	0.8487	1.0471	1.2984	1.6753	2.0076	2.4017	2.6757	3.2579	3.4918
52	0.2546	0.5276	0.6792	0.8486	1.0469	1.2980	1.6747	2.0066	2.4002	2.6737	3.2545	3.4877
53	0.2546	0.5276	0.6791	0.8485	1.0467	1.2977	1.6741	2.0057	2.3988	2.6718	3.2513	3.4838
54	0.2546	0.5275	0.6791	0.8483	1.0465	1.2974	1.6736	2.0049	2.3974	2.6700	3.2481	3.4800
55	0.2546	0.5275	0.6790	0.8482	1.0463	1.2971	1.6730	2.0040	2.3961	2.6682	3.2451	3.4764
56	0.2546	0.5274	0.6789	0.8481	1.0461	1.2969	1.6725	2.0032	2.3948	2.6665	3.2423	3.4729
57	0.2545	0.5273	0.6788	0.8480	1.0459	1.2966	1.6720	2.0025	2.3936	2.6649	3.2395	3.4696
58	0.2545	0.5273	0.6787	0.8479	1.0458	1.2963	1.6716	2.0017	2.3924	2.6633	3.2368	3.4663
59	0.2545	0.5272	0.6787	0.8478	1.0456	1.2961	1.6711	2.0010	2.3912	2.6618	3.2342	3.4632
60	0.2545	0.5272	0.6786	0.8477	1.0455	1.2958	1.6706	2.0003	2.3901	2.6603	3.2317	3.4602
61	0.2545	0.5272	0.6785	0.8476	1.0453	1.2956	1.6702	1.9996	2.3890	2.6589	3.2293	3.4573
62	0.2544	0.5271	0.6785	0.8475	1.0452	1.2954	1.6698	1.9990	2.3880	2.6575	3.2270	3.4545
63	0.2544	0.5271	0.6784	0.8474	1.0450	1.2951	1.6694	1.9983	2.3870	2.6561	3.2247	3.4518
64	0.2544	0.5270	0.6783	0.8473	1.0449	1.2949	1.6690	1.9977	2.3860	2.6549	3.2225	3.4491
65	0.2544	0.5270	0.6783	0.8472	1.0448	1.2947	1.6686	1.9971	2.3851	2.6536	3.2204	3.4466
66	0.2544	0.5269	0.6782	0.8471	1.0446	1.2945	1.6683	1.9966	2.3842	2.6524	3.2184	3.4441
67	0.2544	0.5269	0.6782	0.8470	1.0445	1.2943	1.6679	1.9960	2.3833	2.6512	3.2164	3.4417
68	0.2543	0.5269	0.6781	0.8469	1.0444	1.2941	1.6676	1.9955	2.3824	2.6501	3.2145	3.4394
69	0.2543	0.5268	0.6781	0.8469	1.0443	1.2939	1.6672	1.9949	2.3816	2.6490	3.2126	3.4372
70	0.2543	0.5268	0.6780	0.8468	1.0442	1.2938	1.6669	1.9944	2.3808	2.6479	3.2108	3.4350
71	0.2543	0.5268	0.6780	0.8467	1.0441	1.2936	1.6666	1.9939	2.3800	2.6469	3.2090	3.4329
72	0.2543	0.5267	0.6779	0.8466	1.0440	1.2934	1.6663	1.9935	2.3793	2.6459	3.2073	3.4308
73	0.2543	0.5267	0.6779	0.8466	1.0438	1.2933	1.6660	1.9930	2.3785	2.6449	3.2057	3.4289
74	0.2543	0.5267	0.6778	0.8465	1.0437	1.2931	1.6657	1.9925	2.3778	2.6439	3.2041	3.4269
75	0.2542	0.5266	0.6778	0.8464	1.0436	1.2929	1.6654	1.9921	2.3771	2.6430	3.2025	3.4250
76	0.2542	0.5266	0.6777	0.8464	1.0436	1.2928	1.6652	1.9917	2.3764	2.6421	3.2010	3.4232
77	0.2542	0.5266	0.6777	0.8463	1.0435	1.2926	1.6649	1.9913	2.3758	2.6412	3.1995	3.4214
78	0.2542	0.5266	0.6776	0.8463	1.0434	1.2925	1.6646	1.9908	2.3751	2.6403	3.1980	3.4197
79	0.2542	0.5265	0.6776	0.8462	1.0433	1.2924	1.6644	1.9905	2.3745	2.6395	3.1966	3.4180
80	0.2542	0.5265	0.6776	0.8461	1.0432	1.2922	1.6641	1.9901	2.3739	2.6387	3.1953	3.4163
81	0.2542	0.5265	0.6775	0.8461	1.0431	1.2921	1.6639	1.9897	2.3733	2.6379	3.1939	3.4147
82	0.2542	0.5264	0.6775	0.8460	1.0430	1.2920	1.6636	1.9893	2.3727	2.6371	3.1926	3.4132
83	0.2542	0.5264	0.6775	0.8460	1.0429	1.2918	1.6634	1.9890	2.3721	2.6364	3.1913	3.4116
84	0.2542	0.5264	0.6774	0.8459	1.0429	1.2917	1.6632	1.9886	2.3716	2.6356	3.1901	3.4102
85	0.2541	0.5264	0.6774	0.8459	1.0428	1.2916	1.6630	1.9883	2.3710	2.6349	3.1889	3.4087
86	0.2541	0.5263	0.6774	0.8458	1.0427	1.2915	1.6628	1.9879	2.3705	2.6342	3.1877	3.4073
87	0.2541	0.5263	0.6773	0.8458	1.0426	1.2914	1.6626	1.9876	2.3700	2.6335	3.1866	3.4059
88	0.2541	0.5263	0.6773	0.8457	1.0426	1.2912	1.6624	1.9873	2.3695	2.6329	3.1854	3.4045
89	0.2541	0.5263	0.6773	0.8457	1.0425	1.2911	1.6622	1.9870	2.3690	2.6322	3.1843	3.4032
90	0.2541	0.5263	0.6772	0.8456	1.0424	1.2910	1.6620	1.9867	2.3685	2.6316	3.1833	3.4019
91	0.2541	0.5262	0.6772	0.8456	1.0424	1.2909	1.6618	1.9864	2.3680	2.6309	3.1822	3.4007
92	0.2541	0.5262	0.6772	0.8455	1.0423	1.2908	1.6616	1.9861	2.3676	2.6303	3.1812	3.3994
93	0.2541	0.5262	0.6771	0.8455	1.0422	1.2907	1.6614	1.9858	2.3671	2.6297	3.1802	3.3982
94	0.2541	0.5262	0.6771	0.8455	1.0422	1.2906	1.6612	1.9855	2.3667	2.6291	3.1792	3.3971
95	0.2541	0.5262	0.6771	0.8454	1.0421	1.2905	1.6611	1.9853	2.3662	2.6286	3.1782	3.3959
96	0.2541	0.5261	0.6771	0.8454	1.0421	1.2904	1.6609	1.9850	2.3658	2.6280	3.1773	3.3948
97	0.2540	0.5261	0.6770	0.8453	1.0420	1.2903	1.6607	1.9847	2.3654	2.6275	3.1764	3.3937
98	0.2540	0.5261	0.6770	0.8453	1.0419	1.2902	1.6606	1.9845	2.3650	2.6269	3.1755	3.3926
99	0.2540	0.5261	0.6770	0.8453	1.0419	1.2902	1.6604	1.9842	2.3646	2.6264	3.1746	3.3915
100	0.2540	0.5261	0.6770	0.8452	1.0418	1.2901	1.6602	1.9840	2.3642	2.6259	3.1737	3.3905
110	0.2540	0.5259	0.6767	0.8449	1.0413	1.2893	1.6588	1.9818	2.3607	2.6213	3.1660	3.3812
120	0.2539	0.5258	0.6765	0.8446	1.0409	1.2886	1.6577	1.9799	2.3578	2.6174	3.1595	3.3735
150	0.2538	0.5255	0.6761	0.8440	1.0400	1.2872	1.6551	1.9759	2.3515	2.6090	3.1455	3.3566
200	0.2537	0.5252	0.6757	0.8434	1.0391	1.2858	1.6525	1.9719	2.3451	2.6006	3.1315	3.3398
500	0.2535	0.5247	0.6750	0.8423	1.0375	1.2832	1.6479	1.9647	2.3338	2.5857	3.1066	3.3101

5.  $\chi^2$  distribution

## 5 $\chi^2$ distribution

## Inverse $F_{\nu}^{-1}(p)$ of the cumulative distribution function (quantiles)

The table below contains the quantiles of the  $\chi^2$  (chi-squared) distribution with  $\nu$  degrees of freedom. For 0 the quantile is the value of <math>x for which  $\mathbb{P}\{X \leq x\} = p$ , where  $X \sim \chi^2(\nu)$ . Thus  $x = F_{\nu}^{-1}(p)$ .



						1	9					
$\nu$	0.005	0.01	0.025	0.05	0.1	0.5	0.9	0.95	0.975	0.99	0.995	0.999
1	0.0000	0.0002	0.0010	0.0039	0.0158	0.4549	2.7055	3.8415	5.0239	6.6349	7.8794	10.828
2	0.0100	0.0002	0.0506	0.0039 $0.1026$	0.0138 $0.2107$	1.3863	4.6052	5.9915	7.3778	9.2103	10.594	13.816
3	0.0100 $0.0717$	0.0201 $0.1148$	0.0300 $0.2158$	0.1020 $0.3518$	0.2107 $0.5844$	2.3660	6.2514	7.8147	9.3484	$\frac{9.2105}{11.345}$	10.397 $12.838$	16.266
4	0.2070	0.2971	0.4844	0.7107	1.0636	3.3567	7.7794	9.4877	11.143	13.277	14.860	18.467
5	0.4117	0.5543	0.8312	1.1455	1.6103	4.3515	9.2364	11.070	12.833	15.086	16.750	20.515
6	0.6757	0.8721	1.2373	1.6354	2.2041	5.3481	10.645	12.592	14.449	16.812	18.548	22.458
7	0.9893	1.2390	1.6899	2.1673	2.8331	6.3458	12.017	14.067	16.013	18.475	20.278	24.322
8	1.3444	1.6465	2.1797	2.7326	3.4895	7.3441	13.362	15.507	17.535	20.090	21.955	26.124
9	1.7349	2.0879	2.7004	3.3251	4.1682	8.3428	14.684	16.919	19.023	21.666	23.589	27.877
10	2.1559	2.5582	3.2470	3.9403	4.8652	9.3418	15.987	18.307	20.483	23.209	25.188	29.588
11	2.6032	3.0535	3.8157	4.5748	5.5778	10.341	17.275	19.675	21.920	24.725	26.757	31.264
12	3.0738	3.5706	4.4038	5.2260	6.3038	11.340	18.549	21.026	23.337	26.217	28.300	32.909
13	3.5650	4.1069	5.0088	5.8919	7.0415	12.340	19.812	22.362	24.736	27.688	29.819	34.528
14	4.0747	4.6604	5.6287	6.5706	7.7895	13.339	21.064	23.685	26.119	29.141	31.319	36.123
15	4.6009	5.2293	6.2621	7.2609	8.5468	14.339	22.307	24.996	27.488	30.578	32.801	37.697
16	5.1422	5.8122	6.9077	7.9616	9.3122	15.338	23.542	26.296	28.845	32.000	34.267	39.252
17	5.6972	6.4078	7.5642	8.6718	10.085	16.338	24.769	27.587	30.191	33.409	35.718	40.790
18	6.2648	7.0149	8.2307	9.3905	10.865	17.338	25.989	28.869	31.526	34.805	37.156	42.312
										36.191		43.820
19	6.8440	7.6327	8.9065	10.117	11.651	18.338	27.204	30.144	32.852		38.582	
20	7.4338	8.2604	9.5908	10.851	12.443	19.337	28.412	31.410	34.170	37.566	39.997	45.315
21	8.0337	8.8972	10.283	11.591	13.240	20.337	29.615	32.671	35.479	38.932	41.401	46.797
22	8.6427	9.5425	10.982	12.338	14.041	21.337	30.813	33.924	36.781	40.289	42.796	48.268
23	9.2604	10.196	11.689	13.091	14.848	22.337	32.007	35.172	38.076	41.638	44.181	49.728
24	9.8862	10.856	12.401	13.848	15.659	23.337	33.196	36.415	39.364	42.980	45.559	51.179
25	10.520	11.524	13.120	14.611	16.473	24.337	34.382	37.652	40.646	44.314	46.928	52.620
26	11.160	12.198	13.844	15.379	17.292	25.336	35.563	38.885	41.923	45.642	48.290	54.052
27	11.808	12.879	14.573	16.151	18.114	26.336	36.741	40.113	43.195	46.963	49.645	55.476
28	12.461	13.565	15.308	16.928	18.939	27.336	37.916	41.337	44.461	48.278	50.993	56.892
29	13.121	14.256	16.047	17.708	19.768	28.336	39.087	42.557	45.722	49.588	52.336	58.301
30	13.787	14.953	16.791	18.493	20.599	29.336	40.256	43.773	46.979	50.892	53.672	59.703
					20.399 $21.434$							
$\frac{31}{32}$	14.458	15.655	17.539	19.281		30.336	41.422	44.985	48.232	52.191	55.003	61.098
	15.134	16.362	18.291	20.072	22.271	31.336	42.585	46.194	49.480	53.486	56.328	62.487
33	15.815	17.074	19.047	20.867	23.110	32.336	43.745	47.400	50.725	54.776	57.648	63.870
34	16.501	17.789	19.806	21.664	23.952	33.336	44.903	48.602	51.966	56.061	58.964	65.247
35	17.192	18.509	20.569	22.465	24.797	34.336	46.059	49.802	53.203	57.342	60.275	66.619
36	17.887	19.233	21.336	23.269	25.643	35.336	47.212	50.998	54.437	58.619	61.581	67.985
37	18.586	19.960	22.106	24.075	26.492	36.336	48.363	52.192	55.668	59.893	62.883	69.346
38	19.289	20.691	22.878	24.884	27.343	37.335	49.513	53.384	56.896	61.162	64.181	70.703
39	19.996	21.426	23.654	25.695	28.196	38.335	50.660	54.572	58.120	62.428	65.476	72.055
40	20.707	22.164	24.433	26.509	29.051	39.335	51.805	55.758	59.342	63.691	66.766	73.402
41	21.421	22.906	25.215	27.326	29.907	40.335	52.949	56.942	60.561	64.950	68.053	74.745
42	22.138	23.650	25.999	28.144	30.765	41.335	54.090	58.124	61.777	66.206	69.336	76.084
43	22.859	24.398	26.785	28.965	31.625	42.335	55.230	59.304	62.990	67.459	70.616	77.419
44	23.584	25.148	27.575	29.787	32.487	43.335	56.369	60.481	64.201	68.710	71.893	78.750
45	24.311	25.901	28.366	30.612	33.350	44.335	57.505	61.656	65.410	69.957	73.166	80.077
46	25.041	26.657	29.160	31.439	34.215	45.335	58.641	62.830	66.617	71.201	74.437	81.400
47	25.775	27.416	29.956	32.268	35.081	46.335	59.774	64.001	67.821	72.443	75.704	82.720
48	26.511	28.177	30.755	33.098	35.949	47.335	60.907	65.171	69.023	73.683	76.969	84.037
10	20.011	20.111	55.155	55.050	55.510	11.000	00.001	00.111	00.020	10.000	10.000	→
												$\rightarrow$

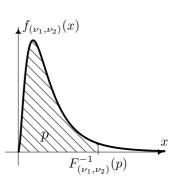
$\nu$	0.005	0.01	0.025	0.05	0.1	0.5	0.9	0.95	0.975	0.99	0.995	0.999
49	27.249	28.941	31.555	33.930	36.818	48.335	62.038	66.339	70.222	74.919	78.231	85.351
50	27.991	29.707	32.357	34.764	37.689	49.335	63.167	67.505	71.420	76.154	79.490	86.661
51	28.735	30.475	33.162	35.600	38.560	50.335	64.295	68.669	72.616	77.386	80.747	87.968
52	29.481	31.246	33.968	36.437	39.433	51.335	65.422	69.832	73.810	78.616	82.001	89.272
53	30.230	32.018	34.776	37.276	40.308	52.335	66.548	70.993	75.002	79.843	83.253	90.573
54	30.981	32.793	35.586	38.116	41.183	53.335	67.673	72.153	76.192	81.069	84.502	91.872
55	31.735	33.570	36.398	38.958	42.060	54.335	68.796	73.311	77.380	82.292	85.749	93.168
56	32.490	34.350	37.212	39.801	42.937	55.335	69.919	74.468	78.567	83.513	86.994	94.461
57	33.248	35.131	38.027	40.646	43.816	56.335	71.040	75.624	79.752	84.733	88.236	95.751
58 50	34.008	35.913	38.844	41.492	44.696	57.335	72.160	76.778	80.936	85.950 87.166	89.477 $90.715$	97.039
59	34.770	36.698	39.662	42.339	45.577	58.335	73.279	77.931	82.117	87.166		98.324
60	35.534	37.485	40.482	43.188	46.459	59.335	74.397	79.082	83.298	88.379	91.952	99.607
61	36.301	38.273	41.303	44.038	47.342	60.335	75.514	80.232	84.476	89.591	93.186	100.89
62	37.068	39.063	42.126	44.889	48.226	61.335	76.630	81.381	85.654	90.802	94.419	102.17
63	37.838	39.855	42.950	45.741	49.111	62.335	77.745	82.529	86.830	92.010	95.649	103.44 $104.72$
$64 \\ 65$	38.610 39.383	$40.649 \\ 41.444$	43.776 44.603	46.595 $47.450$	49.996 50.883	63.335 $64.335$	78.860 $79.973$	83.675 84.821	88.004 89.177	93.217 $94.422$	96.878 $98.105$	104.72 $105.99$
66	40.158	42.240	45.431	48.305	51.770	65.335	81.085	85.965	90.349	95.626	99.330	105.35 $107.26$
67	40.935	43.038	46.261	49.162	52.659	66.335	82.197	87.108	91.519	96.828	100.55	108.53
68	41.713	43.838	47.092	50.020	53.548	67.335	83.308	88.250	92.689	98.028	101.78	109.79
69	42.494	44.639	47.924	50.879	54.438	68.334	84.418	89.391	93.856	99.228	103.00	111.06
70	43.275	45.442	48.758	51.739	55.329	69.334	85.527	90.531	95.023	100.43	104.21	112.32
71	44.058	46.246	49.592	52.600	56.221	70.334	86.635	91.670	96.189	100.43 $101.62$	105.43	113.58
72	44.843	47.051	50.428	53.462	57.113	71.334	87.743	92.808	97.353	102.82	106.65	114.84
73	45.629	47.858	51.265	54.325	58.006	72.334	88.850	93.945	98.516	104.01	107.86	116.09
74	46.417	48.666	52.103	55.189	58.900	73.334	89.956	95.081	99.678	105.20	109.07	117.35
75	47.206	49.475	52.942	56.054	59.795	74.334	91.061	96.217	100.84	106.39	110.29	118.60
76	47.997	50.286	53.782	56.920	60.690	75.334	92.166	97.351	102.00	107.58	111.50	119.85
77	48.788	51.097	54.623	57.786	61.586	76.334	93.270	98.484	103.16	108.77	112.70	121.10
78	49.582	51.910	55.466	58.654	62.483	77.334	94.374	99.617	104.32	109.96	113.91	122.35
79	50.376	52.725	56.309	59.522	63.380	78.334	95.476	100.75	105.47	111.14	115.12	123.59
80	51.172	53.540	57.153	60.391	64.278	79.334	96.578	101.88	106.63	112.33	116.32	124.84
81	51.969	54.357	57.998	61.261	65.176	80.334	97.680	103.01	107.78	113.51	117.52	126.08
82	52.767	55.174	58.845	62.132	66.076	81.334	98.780	104.14	108.94	114.69	118.73	127.32
83	53.567	55.993	59.692	63.004	66.976	82.334	99.880	105.27	110.09	115.88	119.93	128.56
84	54.368	56.813	60.540	63.876	67.876	83.334 84.334	100.98	106.39 $107.52$	111.24 $112.39$	117.06	121.13	129.80
85 86	55.170 55.973	57.634 58.456	61.389 $62.239$	64.749 $65.623$	68.777 $69.679$	84.334 85.334	$102.08 \\ 103.18$	107.52 $108.65$	112.39 $113.54$	$118.24 \\ 119.41$	$122.32 \\ 123.52$	131.04 $132.28$
87	56.777	59.279	63.089	66.498	70.581	86.334	103.18	109.77	114.69	120.59	123.52 $124.72$	132.26 $133.51$
88	57.582	60.103	63.941	67.373	71.484	87.334	104.20 $105.37$	110.90	115.84	120.55 $121.77$	125.91	134.75
89	58.389	60.928	64.793	68.249	72.387	88.334	106.47	112.02	116.99	122.94	127.11	135.98
90	59.196	61.754	65.647	69.126	73.291	89.334	107.57	113.15	118.14	124.12	128.30	137.21
91	60.005	62.581	66.501	70.003	73.291 $74.196$	90.334	107.57	113.13 $114.27$	119.14	124.12 $125.29$	128.30 $129.49$	137.21 $138.44$
92	60.815	63.409	67.356	70.882	75.100	91.334	109.76	115.39	120.43	126.29 $126.46$	130.68	139.67
93	61.625	64.238	68.211	71.760	76.006	92.334	110.85	116.51	120.13 $121.57$	127.63	131.87	140.89
94	62.437	65.068	69.068	72.640	76.912	93.334	111.94	117.63	122.72	128.80	133.06	142.12
95	63.250	65.898	69.925	73.520	77.818	94.334	113.04	118.75	123.86	129.97	134.25	143.34
96	64.063	66.730	70.783	74.401	78.725	95.334	114.13	119.87	125.00	131.14	135.43	144.57
97	64.878	67.562	71.642	75.282	79.633	96.334	115.22	120.99	126.14	132.31	136.62	145.79
98	65.694	68.396	72.501	76.164	80.541	97.334	116.32	122.11	127.28	133.48	137.80	147.01
99	66.510	69.230	73.361	77.046	81.449	98.334	117.41	123.23	128.42	134.64	138.99	148.23
100	67.328	70.065	74.222	77.929	82.358	99.334	118.50	124.34	129.56	135.81	140.17	149.45
110	75.550	78.458	82.867	86.792	91.471	109.33	129.39	135.48	140.92	147.41	151.95	161.58
120	83.852	86.923	91.573	95.705	100.62	119.33	140.23	146.57	152.21	158.95	163.65	173.62
150	109.14	112.67	117.98	122.69	128.28	149.33	172.58	179.58	185.80	193.21	198.36	209.26
200	152.24	156.43	162.73	168.28	174.84	199.33	226.02	233.99	241.06	249.45	255.26	267.54
500	422.30	429.39	439.94	449.15	459.93	499.33	540.93	553.13	563.85	576.49	585.21	603.45

#### 6 F distribution

## Inverse $F^{-1}_{(\nu_1,\nu_2)}(p)$ of the cumulative distribution function (quantiles)

The table below contains the quantiles of the F distribution with  $\nu_1$  and  $\nu_2$  degrees of freedom. For 0 the quantile is the value of <math>x for which  $\mathbb{P}\{X \leq x\} = p$ , where  $X \sim \mathsf{F}(\nu_1, \nu_2)$ . Thus  $x = F_{(\nu_1, \nu_2)}^{-1}(p)$ .

The table only contains the quantiles for  $p \geq \frac{1}{2}$ . For  $p < \frac{1}{2}$  quantiles can be obtained by exploiting the symmetry of the F distribution:  $F_{(\nu_1,\nu_2)}^{-1}(p) = \frac{1}{F_{(\nu_2,\nu_1)}^{-1}(1-p)}$ .



$ u_1$	$\nu_2$	0.9	0.95	$\frac{p}{0.975}$	0.99	0.995	$\nu_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995
1		39.863	161.45	647.79	4052.2	16211	2	8	3.1131	4.4590	6.0595	8.6491	11.042
1	$\frac{1}{2}$	8.5263	18.513	38.506	98.503	198.50		9	3.0065	4.2565	5.7147	8.0215	10.107
	3	5.5383	10.128	17.443	34.116	55.552		10	2.9245	4.1028	5.4564	7.5594	9.4270
	4	4.5448	7.7086	12.218	21.198	31.333		11	2.8595	3.9823	5.2559	7.2057	8.9122
	5	4.0604	6.6079	10.007	16.258	22.785		12	2.8068	3.8853	5.0959	6.9266	8.5096
	6	3.7759	5.9874	8.8131	13.745	18.635		13	2.7632	3.8056	4.9653	6.7010	8.1865
	7	3.5894	5.5914	8.0727	12.246	16.236		14	2.7265	3.7389	4.8567	6.5149	7.9216
	8	3.4579	5.3177	7.5709	11.259	14.688		15	2.6952	3.6823	4.7650	6.3589	7.7008
	9	3.3603	5.1174	7.2093	10.561	13.614		16	2.6682	3.6337	4.6867	6.2262	7.5138
	10	3.2850	4.9646	6.9367	10.044	12.826		17	2.6446	3.5915	4.6189	6.1121	7.3536
	11	3.2252	4.8443	6.7241	9.6460	12.226		18	2.6239	3.5546	4.5597	6.0129	7.2148
	12	3.1765	4.7472	6.5538	9.3302	11.754		19	2.6056	3.5219	4.5075	5.9259	7.0935
	13	3.1362	4.6672	6.4143	9.0738	11.374		20	2.5893	3.4928	4.4613	5.8489	6.9865
	14	3.1022	4.6001	6.2979	8.8616	11.060		21	2.5746	3.4668	4.4199	5.7804	6.8914
	15	3.0732	4.5431	6.1995	8.6831	10.798		22	2.5613	3.4434	4.3828	5.7190	6.8064
	16	3.0481	4.4940	6.1151	8.5310	10.575		23	2.5493	3.4221	4.3492	5.6637	6.7300
	17	3.0262	4.4513	6.0420	8.3997	10.384		24	2.5383	3.4028	4.3187	5.6136	6.6609
	18	3.0070	4.4139	5.9781	8.2854	10.218		25	2.5283	3.3852	4.2909	5.5680	6.5982
	19	2.9899	4.3807	5.9216	8.1849	10.073		30	2.4887	3.3158	4.1821	5.3903	6.3547
	20	2.9747	4.3512	5.8715	8.0960	9.9439		35	2.4609	3.2674	4.1065	5.2679	6.1878
	21	2.9610	4.3248	5.8266	8.0166	9.8295		40	2.4404	3.2317	4.0510	5.1785	6.0664
	22	2.9486	4.3009	5.7863	7.9454	9.7271		45	2.4245	3.2043	4.0085	5.1103	5.9741
	23	2.9374	4.2793	5.7498	7.8811	9.6348		50	2.4120	3.1826	3.9749	5.0566	5.9016
	24	2.9271	4.2597	5.7166	7.8229	9.5513		60	2.3933	3.1504	3.9253	4.9774	5.7950
	25	2.9177	4.2417	5.6864	7.7698	9.4753		70	2.3800	3.1277	3.8903	4.9219	5.7204
	30	2.8807	4.1709	5.5675	7.5625	9.1797		80	2.3701	3.1108	3.8643	4.8807	5.6652
	35	2.8547	4.1213	5.4848	7.4191	8.9763		100	2.3564	3.0873	3.8284	4.8239	5.5892
	40	2.8354	4.0847	5.4239	7.3141	8.8279		120	2.3473	3.0718	3.8046	4.7865	5.5393
	45	2.8205	4.0566	5.3773	7.2339	8.7148		150	2.3383	3.0564	3.7811	4.7495	5.4900
	50	2.8087	4.0343	5.3403	7.1706	8.6258		200	2.3293	3.0411	3.7578	4.7129	5.4412
	60	2.7911	4.0012	5.2856	7.0771	8.4946		500	2.3132	3.0138	3.7162	4.6478	5.3549
	70	2.7786	3.9778	5.2470	7.0114	8.4027		$+\infty$	2.3026	2.9957	3.6889	4.6052	5.2983
	80	2.7693	3.9604	5.2184	6.9627	8.3346	3	1	53.593	215.71	864.16	5403.4	21615
	100	2.7564	3.9361	5.1786	6.8953	8.2406		2	9.1618	19.164	39.165	99.166	199.17
	120	2.7478	3.9201	5.1523	6.8509	8.1788		3	5.3908	9.2766	15.439	29.457	47.467
	150	2.7393	3.9042	5.1263	6.8069	8.1177		4	4.1909	6.5914	9.9792	16.694	24.259
	200	2.7308	3.8884	5.1004	6.7633	8.0572		5	3.6195	5.4095	7.7636	12.060	16.530
	500	2.7156	3.8601	5.0543	6.6858	7.9498		6	3.2888	4.7571	6.5988	9.7795	12.917
	$+\infty$	2.7055	3.8415	5.0239	6.6349	7.8794		7	3.0741	4.3468	5.8898	8.4513	10.882
2	1	49.500	199.50	799.50	4999.5	19999		8	2.9238	4.0662	5.4160	7.5910	9.5965
	2	9.0000	19.000	39.000	99.000	199.00		9	2.8129	3.8625	5.0781	6.9919	8.7171
	3	5.4624	9.5521	16.044	30.817	49.799		10	2.7277	3.7083	4.8256	6.5523	8.0807
	4	4.3246	6.9443	10.649	18.000	26.284		11	2.6602	3.5874	4.6300	6.2167	7.6004
	5	3.7797	5.7861	8.4336	13.274	18.314		12	2.6055	3.4903	4.4742	5.9525	7.2258
	6	3.4633	5.1433	7.2599	10.925	14.544		13	2.5603	3.4105	4.3472	5.7394	6.9258
	7	3.2574	4.7374	6.5415	9.5466	12.404		14	2.5222	3.3439	4.2417	5.5639	6.6804
						$\rightarrow$							$\rightarrow$

$\nu_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995	$ u_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995
3	15	2.4898	3.2874	4.1528	5.4170	6.4760	4	500	1.9561	2.3898	2.8114	3.3569	3.7632
	16	2.4618	3.2389	4.0768	5.2922	6.3034		$+\infty$	1.9449	2.3719	2.7858	3.3192	3.7151
	17	2.4374	3.1968	4.0112	5.1850	6.1556	5	1	57.240	230.16	921.85	5763.6	23056
	18	2.4160	3.1599	3.9539	5.0919	6.0278	9	2	9.2926	19.296	39.298	99.299	199.30
	19	2.3970	3.1274	3.9034	5.0103	5.9161		3	5.3092	9.0135	14.885	28.237	45.392
	20	2.3801	3.0984	3.8587	4.9382	5.8177		4	4.0506	6.2561	9.3645	15.522	22.456
	21	2.3649	3.0725	3.8188	4.8740	5.7304		5	3.4530	5.0503	7.1464	10.967	14.940
	22	2.3512	3.0491	3.7829	4.8166	5.6524		6	3.1075	4.3874	5.9876	8.7459	11.464
	23	2.3387	3.0280	3.7505	4.7649	5.5823		7	2.8833	3.9715	5.2852	7.4604	9.5221
	24	2.3274	3.0088	3.7211	4.7181	5.5190		8	2.7264	3.6875	4.8173	6.6318	8.3018
	25	2.3170	2.9912	3.6943	4.6755	5.4615		9	2.6106	3.4817	4.4844	6.0569	7.4712
	30	2.2761	2.9223	3.5894	4.5097	5.2388		10	2.5216	3.3258	4.2361	5.6363	6.8724
	35	2.2474	2.8742	3.5166	4.3957	5.0865		11	2.4512	3.2039	4.0440	5.3160	6.4217
	40	2.2261	2.8387	3.4633	4.3126	4.9758		12	2.3940	3.1059	3.8911	5.0643	6.0711
	45	2.2097	2.8115	3.4224	4.2492	4.8918		13	2.3467	3.0254	3.7667	4.8616	5.7910
	50	2.1967	2.7900	3.3902	4.1993	4.8259		14	2.3069	2.9582	3.6634	4.6950	5.5623
	60	2.1774	2.7581	3.3425	4.1259	4.7290		15	2.2730	2.9013	3.5764	4.5556	5.3721
	70	2.1637	2.7355	3.3090	4.0744	4.6613		16	2.2438	2.8524	3.5021	4.4374	5.2117
	80	2.1535	2.7188	3.2841	4.0363	4.6113		17	2.2183	2.8100	3.4379	4.3359	5.0746
	100	2.1394	2.6955	3.2496	3.9837	4.5424		18	2.1958	2.7729	3.3820	4.2479	4.9560
	120	2.1300	2.6802	3.2269	3.9491	4.4972		19	2.1760	2.7401	3.3327	4.1708	4.8526
	150	2.1207	2.6649	3.2044	3.9149	4.4525		20	2.1582	2.7109	3.2891	4.1027	4.7616
	200 500	2.1114 2.0948	2.6498 $2.6227$	3.1820	3.8810 $3.8210$	4.4084		21	2.1423	2.6848	3.2501	4.0421	4.6809
	$+\infty$	2.0948 $2.0838$	2.6049	3.1423 $3.1161$	3.7816	4.3304 $4.2794$		22	2.1279	2.6613	3.2151	3.9880	4.6088
								23	2.1149	2.6400	3.1835	3.9392	4.5441
4	1	55.833	224.58	899.58	5624.6	22500		24	2.1030	2.6207	3.1548	3.8951	4.4857
	2	9.2434	19.247	39.248	99.249	199.25		25	2.0922	2.6030	3.1287	3.8550	4.4327
	3	5.3426	9.1172	15.101	28.710	46.195		30	2.0492	2.5336	3.0265	3.6990	4.2276
	4	4.1072	6.3882	9.6045	15.977	23.155		35	2.0191	2.4851	2.9557	3.5919	4.0876
	$\frac{5}{6}$	3.5202 $3.1808$	5.1922 $4.5337$	7.3879 $6.2272$	11.392 $9.1483$	$15.556 \\ 12.028$		$\frac{40}{45}$	1.9968	$2.4495 \\ 2.4221$	2.9037 $2.8640$	3.5138 $3.4544$	3.9860 $3.9090$
	7	2.9605	4.3337 $4.1203$	5.5226	7.8466	12.028 $10.050$			1.9796				
	8	2.8064	3.8379	5.0526	7.0460	8.8051		50	1.9660	2.4004	2.8327	3.4077	3.8486
	9	2.6927	3.6331	4.7181	6.4221	7.9559		60	1.9457	2.3683	2.7863	3.3389	3.7599
								70	1.9313	2.3456	2.7537	3.2907	3.6980
	10	2.6053	$3.4780 \\ 3.3567$	4.4683	5.9943	7.3428		80	1.9206	2.3287 $2.3053$	2.7295	3.2550 $3.2059$	3.6524
	$\begin{array}{c} 11 \\ 12 \end{array}$	2.5362 $2.4801$	3.2592	$4.2751 \\ 4.1212$	5.6683 $5.4120$	6.8809 $6.5211$		$100 \\ 120$	$1.9057 \\ 1.8959$	2.3033 $2.2899$	2.6961 $2.6740$	3.2039 $3.1735$	3.5895 $3.5482$
	13	2.4337	3.2592 $3.1791$	3.9959	5.2053	6.2335		150	1.8861	2.2745	2.6521	3.1416	3.5075
	14	2.3947	3.1122	3.8919	5.0354	5.9984		200	1.8763	2.2592	2.6304	3.1100	3.4674
	15	2.3614	3.0556	3.8043	4.8932	5.8029		500	1.8588	2.2320	2.5919	3.0540	3.3963
	16	2.3327	3.0069	3.7294	4.7726	5.6378		$+\infty$	1.8473	2.2141	2.5665	3.0173	3.3499
	17	2.3077	2.9647	3.6648	4.6690	5.4967			F0 204				
	18	2.2858	2.9277	3.6083	4.5790	5.3746	6	$\frac{1}{2}$	58.204 $9.3255$	233.99 19.330	937.11 39.331	5859.0 $99.333$	23437 $199.33$
	19	2.2663	2.8951	3.5587	4.5003	5.2681		3	5.2847	8.9406	14.735	27.911	44.838
	20	2.2489	2.8661	3.5147	4.4307	5.1743		$\frac{3}{4}$	4.0097	6.1631	9.1973	15.207	21.975
	21	2.2333	2.8401	3.4754	4.3688	5.0911		5	3.4045	4.9503	6.9777	10.672	14.513
	22	2.2193	2.8167	3.4401	4.3134	5.0168		6	3.0546	4.2839	5.8198	8.4661	11.073
	23	2.2065	2.7955	3.4083	4.2636	4.9500		7	2.8274	3.8660	5.1186	7.1914	9.1553
	24	2.1949	2.7763	3.3794	4.2184	4.8898		8	2.6683	3.5806	4.6517	6.3707	7.9520
	25	2.1842	2.7587	3.3530	4.1774	4.8351		9	2.5509	3.3738	4.3197	5.8018	7.1339
	30	2.1422	2.6896	3.2499	4.0179	4.6234		10	2.4606	3.2172	4.0721	5.3858	6.5446
	35	2.1128	2.6415	3.1785	3.9082	4.4788		11	2.3891	3.0946	3.8807	5.0692	6.1016
	40	2.0909	2.6060	3.1261	3.8283	4.3738		12	2.3310	2.9961	3.7283	4.8206	5.7570
	45	2.0742	2.5787	3.0860	3.7674	4.2941		13	2.2830	2.9153	3.6043	4.6204	5.4819
	50	2.0608	2.5572	3.0544	3.7195	4.2316		14	2.2426	2.8477	3.5014	4.4558	5.2574
	60	2.0410	2.5252	3.0077	3.6490	4.1399		15	2.2081	2.7905	3.4147	4.3183	5.0708
	70	2.0269	2.5027	2.9748	3.5996	4.0758		16	2.1783	2.7413	3.3406	4.2016	4.9134
	80	2.0165	2.4859	2.9504	3.5631	4.0285		17	2.1524	2.6987	3.2767	4.1015	4.7789
	100	2.0019	2.4626	2.9166	3.5127	3.9634		18	2.1296	2.6613	3.2209	4.0146	4.6627
	120	1.9923	2.4472	2.8943	3.4795	3.9207		19	2.1094	2.6283	3.1718	3.9386	4.5614
	150	1.9827	2.4320	2.8722	3.4467	$\frac{3.8785}{3.8368}$		20	2.0913	2.5990	3.1283	3.8714	4.4721
	200	1.9732	2.4168	2.8503	3.4143	$\begin{array}{c} 3.8368 \\ \rightarrow \end{array}$		21	2.0751	2.5727	3.0895	3.8117	4.3931
						$\rightarrow$							$\rightarrow$

$\nu_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995	_	$ u_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995
6	22	2.0605	2.5491	3.0546	3.7583	4.3225		8	6	2.9830	4.1468	5.5996	8.1017	10.566
	23	2.0472	2.5277	3.0232	3.7102	4.2591			7	2.7516	3.7257	4.8993	6.8400	8.6781
	24	2.0351	2.5082	2.9946	3.6667	4.2019			8	2.5893	3.4381	4.4333	6.0289	7.4959
	25	2.0241	2.4904	2.9685	3.6272	4.1500			9	2.4694	3.2296	4.1020	5.4671	6.6933
	30	1.9803	2.4205	2.8667	3.4735	3.9492			10	2.3772	3.0717	3.8549	5.0567	6.1159
	35	1.9496	2.3718	2.7961	3.3679	3.8123			11	2.3040	2.9480	3.6638	4.7445	5.6821
	40	1.9269	2.3359	2.7444	3.2910	3.7129			12	2.2446	2.8486	3.5118	4.4994	5.3451
	45	1.9094	2.3083	2.7048	3.2325	3.6376			13	2.1953	2.7669	3.3880	4.3021	5.0761
	50	1.8954	2.2864	2.6736	3.1864	3.5785			14	2.1539	2.6987	3.2853	4.1399	4.8566
	60	1.8747	2.2541	2.6274	3.1187	3.4918			15	2.1185	2.6408	3.1987	4.0045	4.6744
	70	1.8600	2.2312	2.5949	3.0712	3.4313			16	2.0880	2.5911	3.1248	3.8896	4.5207
	80	1.8491	2.2142	2.5708	3.0361	3.3867			17	2.0613	2.5480	3.0610	3.7910	4.3894
	100	1.8339	2.1906	2.5374	2.9877	3.3252			18	2.0379	2.5102	3.0053	3.7054	4.2759
	120	1.8238	2.1750	2.5154	2.9559	3.2849			19	2.0171	2.4768	2.9563	3.6305	4.1770
	150	1.8138	2.1595	2.4936	2.9244	3.2452			20	1.9985	2.4471	2.9128	3.5644	4.0900
	200	1.8038	2.1441	2.4720	2.8933	3.2059			21	1.9819	2.4205	2.8740	3.5056	4.0300
	500	1.7859	2.1167	2.4335	2.8381	3.1366			22	1.9668	2.3965	2.8392	3.4530	3.9440
	$+\infty$	1.7741	2.0986	2.4082	2.8020	3.0913			23	1.9531	2.3748	2.8077	3.4057	3.8822
7	1	58.906	236.77	948.22	5928.4	23715			$\frac{20}{24}$	1.9407	2.3551	2.7791	3.3629	3.8264
'	2	9.3491	19.353	39.355	99.356	199.36			25	1.9292	2.3371	2.7531	3.3239	3.7758
	3	5.2662	8.8867	14.624	27.672	44.434			30	1.8841	2.2662	2.6513	3.1726	3.5801
	4	3.9790	6.0942	9.0741	14.976	21.622			35	1.8524	2.2167	2.5807	3.0687	3.4466
	5	3.3679	4.8759	6.8531	10.456	14.200			40	1.8289	2.1802	2.5289	2.9930	3.3498
	6	3.0145	4.2067	5.6955	8.2600	10.786			45	1.8107	2.1521	2.4892	2.9353	3.2764
	7	2.7849	3.7870	4.9949	6.9928	8.8854			50	1.7963	2.1299	2.4579	2.8900	3.2189
	8	2.6241	3.5005	4.5286	6.1776	7.6941			60	1.7748	2.1299 $2.0970$	2.4379 $2.4117$	2.8900 $2.8233$	3.1344
	9	2.5053	3.2927	4.1970	5.6129	6.8849			70	1.7748	2.0970 $2.0737$	2.4117 $2.3791$	2.7765	3.0755
									80	1.7390 $1.7483$	2.0737 $2.0564$	2.3791 $2.3549$	2.7420	3.0320
	10 11	2.4140 $2.3416$	3.1355 $3.0123$	3.9498 $3.7586$	5.2001 $4.8861$	6.3025 $5.8648$			100	1.7403 $1.7324$	2.0304 $2.0323$	2.3349 $2.3215$	2.6943	2.9722
	$\frac{11}{12}$	2.3410 $2.2828$	$\frac{3.0123}{2.9134}$	3.6065	4.6395	5.5245			120	1.7324 $1.7220$	2.0323 $2.0164$	2.3213 $2.2994$	2.6629	2.9330
	13	2.2323	2.8321	3.4827	4.0393 $4.4410$	5.2529			150	1.7115	2.0006	2.2775	2.6319	2.8942
	14	2.2341 $2.1931$	2.7642	3.4627 $3.3799$	4.2779	5.2329			200	1.7011	1.9849	2.2558	2.6013	2.8560
	15	2.1581 $2.1582$	2.7042	3.2934	4.2779 $4.1415$	4.8473			500	1.6825	1.9569	2.2172	2.5469	2.7885
	16	2.1382 $2.1280$	2.6572	3.2194	4.0259	4.6920			$+\infty$	1.6702	1.9384	2.1918	2.5113	2.7444
	17	2.1200 $2.1017$	2.6143	3.1556	3.9267	4.5594								
	18	2.0785	2.5767	3.0999	3.8406	4.4448		9	1	59.858	240.54	963.28	6022.5	24091
	19	2.0580	2.5435	3.0509	3.7653	4.3448			2	9.3805	19.385	39.387	99.388	199.39
	20	2.0397	2.5140	3.0074	3.6987	4.2569			3	5.2400 $3.9357$	8.8123 5.9988	$14.473 \\ 8.9047$	27.345 $14.659$	43.882
		2.0397 $2.0233$	2.3140 $2.4876$	2.9686	3.6396	4.2509 $4.1789$			$\frac{4}{5}$	3.3163	4.7725	6.6811	14.059 $10.158$	21.139 $13.772$
	$\frac{21}{22}$	2.0233 $2.0084$	2.4638	2.9338	3.5867	4.1769			6	2.9577	4.7723	5.5234	7.9761	10.391
	23	1.9949	2.4422	2.9023	3.5390	4.0469			7	2.7247	3.6767	4.8232	6.7188	8.5138
	24	1.9826	2.4226	2.8738	3.4959	3.9905			8	2.5612	3.3881	4.3572	5.9106	7.3386
	25	1.9714	2.4047	2.8478	3.4568	3.9394			9	2.4403	3.1789	4.0260	5.3511	6.5411
	30	1.9269	2.3343	2.7460	3.3045	3.7416								
	35	1.8957	2.2852	2.6755	3.2000	3.6066			10	2.3473	3.0204	3.7790	4.9424	5.9676
	40	1.8725	2.2490	2.6238	3.1238	3.5088			11 12	2.2735	2.8962 $2.7964$	3.5879	4.6315	5.5368
	45	1.8547	2.2212	2.5842	3.0658	3.4346			12 13	2.2135 $2.1638$	2.7964 $2.7144$	3.4358	4.3875 $4.1911$	5.2021 $4.9351$
	50	1.8405	2.1992	2.5530	3.0202	3.3765			13 14	2.1038 $2.1220$	2.7144 $2.6458$	3.3120 $3.2093$	4.1911 $4.0297$	4.9331 $4.7173$
	60	1.8405 $1.8194$	2.1992 $2.1665$	2.5068	$\frac{3.0202}{2.9530}$	3.2911			14 15	2.1220 $2.0862$	2.5876	3.2093 $3.1227$	3.8948	4.7173
	70	1.8044	2.1435	2.4743	2.9060	3.2315			16	2.0552 $2.0553$	2.5377	3.0488	3.7804	4.3838
	80	1.7933	2.1463	2.4502	2.8713	3.1876			17	2.0284	2.4943	2.9849	3.6822	4.2535
	100	1.7778	2.1205 $2.1025$	2.4362 $2.4168$	2.8233	3.1271			18	2.0264 $2.0047$	2.4543 $2.4563$	2.9291	3.5971	4.1410
	120	1.7675	2.0868	2.3948	2.7918	3.0874			19	1.9836	2.4227	2.8801	3.5225	4.0428
	150	1.7572	2.0711	2.3730	2.7606	3.0483								
	200	1.7470	2.0556	2.3513	2.7298	3.0097			20	1.9649	2.3928	2.8365	3.4567	3.9564
	500	1.7288	2.0279	2.3129	2.6751	2.9414			21	1.9480	2.3660	2.7977	3.3981	3.8799
	$+\infty$	1.7167	2.0096	2.2875	2.6393	2.8968			22	1.9327	2.3419	2.7628	3.3458	3.8116
									$\frac{23}{24}$	1.9189 $1.9063$	2.3201 $2.3002$	$2.7313 \\ 2.7027$	3.2986 $3.2560$	3.7502 $3.6949$
8	1	59.439	238.88	956.66	5981.1	23925			$\frac{24}{25}$	1.8947	2.3002 $2.2821$	2.7027 $2.6766$	3.2300 $3.2172$	3.6949 $3.6447$
	$\frac{2}{3}$	9.3668 $5.2517$	19.371 $8.8452$	39.373 $14.540$	99.374 $27.489$	$199.37 \\ 44.126$			30	1.8490	2.2821 $2.2107$	2.5746	3.2172 $3.0665$	3.4505
	3 4	3.9549	6.8452 $6.0410$	8.9796	27.489 14.799	$\frac{44.126}{21.352}$			35	1.8168	2.1608	2.5740 $2.5039$	2.9630	3.3180
	5	3.3393	4.8183	6.7572	14.799	13.961			40	1.7929	2.1240	2.4519	2.8876	3.2220
	9	0.0000	4.0100	0.1014	10.209	10.501			10	1.1020	1_10			→

$ u_1$	$ u_2$	0.9	0.95	0.975	0.99	0.995		$ u_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995
9	45	1.7745	2.0958	2.4122	2.8301	3.1492	•	11	13	2.1155	2.6347	3.1975	4.0245	4.7240
9								11	14	2.1133 $2.0729$	2.5655	3.1975 $3.0946$	$\frac{4.0245}{3.8640}$	4.7240 $4.5085$
	50	1.7598	2.0734	2.3808	2.7850	3.0920			15	2.0366	2.5068	3.0078	3.7299	4.3295
	60	1.7380	2.0401	2.3344	2.7185	3.0083			16	2.0051	2.4564	2.9337	3.6162	4.1785
	70	1.7225	2.0166	2.3017	2.6719	2.9498			17	1.9777	2.4126	2.8696	3.5185	4.0496
	80	1.7110	1.9991	2.2775	2.6374	2.9066			18	1.9535	2.3742	2.8137	3.4338	3.9382
	$\frac{100}{120}$	1.6949 $1.6842$	$1.9748 \\ 1.9588$	$2.2439 \\ 2.2217$	2.5898 $2.5586$	2.8472 $2.8083$			19	1.9321	2.3402	2.7645	3.3596	3.8410
	150	1.6736	1.9428	2.2217 $2.1998$	2.5277	2.7698			20	1.9129	2.3100	2.7209	3.2941	3.7555
	200	1.6630	1.9426 $1.9269$	2.1780	2.4971	2.7319			21	1.8956	2.3100 $2.2829$	2.6819	3.2341 $3.2359$	3.6798
	500	1.6441	1.8986	2.1392	2.4429	2.6649			22	1.8801	2.2585	2.6469	3.1837	3.6122
	$+\infty$	1.6315	1.8799	2.1136	2.4073	2.6210			23	1.8659	2.2364	2.6152	3.1368	3.5515
-10									24	1.8530	2.2163	2.5865	3.0944	3.4967
10	1	60.195	241.88	968.63	6055.8	24224			25	1.8412	2.1979	2.5603	3.0558	3.4470
	2	9.3916	19.396	39.398	99.399	199.40			30	1.7944	2.1256	2.4577	2.9057	3.2547
	3	5.2304	8.7855 $5.9644$	14.419	27.229	43.686			35	1.7614	2.0750	2.3866	2.8026	3.1236
	$\frac{4}{5}$	3.9199 $3.2974$	$\frac{5.9644}{4.7351}$	8.8439 $6.6192$	$14.546 \\ 10.051$	$20.967 \\ 13.618$			40	1.7369	2.0376	2.3343	2.7274	3.0284
	6	$\frac{3.2974}{2.9369}$	4.7331 $4.0600$	5.4613	7.8741	10.250			45	1.7180	2.0088	2.2943	2.6701	2.9563
	7	2.7025	3.6365	4.7611	6.6201	8.3803			50	1.7029	1.9861	2.2627	2.6250	2.8997
	8	2.7025 $2.5380$	3.3472	4.7011 $4.2951$	5.8143	7.2106			60	1.6805	1.9522	2.2159	2.5587	2.8166
	9	2.4163	3.1373	3.9639	5.2565	6.4172			70	1.6645	1.9283	2.1829	2.5122	2.7587
									80	1.6526	1.9105	2.1584	2.4777	2.7159
	10	2.3226	2.9782	3.7168	4.8491	5.8467			100	1.6360	1.8857	2.1245	2.4302	2.6570
	$\begin{array}{c} 11 \\ 12 \end{array}$	2.2482 $2.1878$	2.8536 $2.7534$	3.5257 $3.3736$	$4.5393 \\ 4.2961$	5.4183			120	1.6250	1.8693	2.1021	2.3990	2.6183
	13	2.1376	2.7534 $2.6710$	3.2497	4.2901 $4.1003$	5.0855 $4.8199$			150	1.6140	1.8530	2.0799	2.3681	2.5802
	14	2.1370 $2.0954$	2.6022	3.2497 $3.1469$	3.9394	4.6199 $4.6034$			200	1.6031	1.8368	2.0578	2.3375	2.5425
	15	2.0594 $2.0593$	2.5437	3.0602	3.8049	4.4235			500	1.5835	1.8078	2.0186	2.2833	2.4760
	16	2.0281	2.4935	2.9862	3.6909	4.2719			$+\infty$	1.5705	1.7886	1.9927	2.2477	2.4324
	17	2.0009	2.4499	2.9222	3.5931	4.1424	•	12	1	60.705	243.91	976.71	6106.3	24426
	18	1.9770	2.4117	2.8664	3.5082	4.0305			2	9.4081	19.413	39.415	99.416	199.42
	19	1.9557	2.3779	2.8172	3.4338	3.9329			3	5.2156	8.7446	14.337	27.052	43.387
	20	1.9367	2.3479	2.7737	3.3682	3.8470			4	3.8955	5.9117	8.7512	14.374	20.705
	21	1.9197	2.3210	2.7348	3.3098	3.7709			5	3.2682	4.6777	6.5245	9.8883	13.384
	22	1.9043	2.2967	2.6998	3.2576	3.7030			6	2.9047	3.9999	5.3662	7.7183	10.034
	23	1.8903	2.2747	2.6682	3.2106	3.6420			7	2.6681	3.5747	4.6658	6.4691	8.1764
	24	1.8775	2.2547	2.6396	3.1681	3.5870			8	2.5020	3.2839	4.1997	5.6667	7.0149
	25	1.8658	2.2365	2.6135	3.1294	3.5370			9	2.3789	3.0729	3.8682	5.1114	6.2274
	30	1.8195	2.1646	2.5112	2.9791	3.3440			10	2.2841	2.9130	3.6209	4.7059	5.6613
	35	1.7869	2.1143	2.4403	2.8758	3.2123			11	2.2087	2.7876	3.4296	4.3974	5.2363
	40	1.7627	2.0772	2.3882	2.8005	3.1167			12	2.1474	2.6866	3.2773	4.1553	4.9062
	45	1.7440	2.0487	2.3483	2.7432	3.0443			13	2.0966	2.6037	3.1532	3.9603	4.6429
	50	1.7291	2.0261	2.3168	2.6981	2.9875			14	2.0537	2.5342	3.0502	3.8001	4.4281
	60	1.7070	1.9926	2.2702	2.6318	2.9042			15	2.0171	2.4753	2.9633	3.6662	4.2497
	70	1.6913	1.9689	2.2374	2.5852	2.8460			16	1.9854	2.4247	2.8890	3.5527	4.0994
	80	1.6796	1.9512	2.2130	2.5508	2.8031			17	1.9577	2.3807	2.8249	3.4552	3.9709
	100	1.6632	1.9267	2.1793	2.5033	2.7440			18	1.9333	2.3421	2.7689	3.3706	3.8599
	120	1.6524	1.9105	2.1570	2.4721	2.7052			19	1.9117	2.3080	2.7196	3.2965	3.7631
	150	1.6416	1.8943	2.1349	2.4412	2.6669			20	1.8924	2.2776	2.6758	3.2311	3.6779
	200	1.6308	1.8783	2.1130	2.4106	2.6292			21	1.8750	2.2504	2.6368	3.1730	3.6024
	500	1.6115	1.8496	2.0740	2.3565	2.5625			22	1.8593	2.2258	2.6017	3.1209	3.5350
	$+\infty$	1.5987	1.8307	2.0483	2.3209	2.5188			23	1.8450	2.2036	2.5699	3.0740	3.4745
11	1	60.473	242.98	973.03	6083.3	24334			24	1.8319	2.1834	2.5411	3.0316	3.4199
	2	9.4006	19.405	39.407	99.408	199.41			25	1.8200	2.1649	2.5149	2.9931	3.3704
	3	5.2224	8.7633	14.374	27.133	43.524			$\frac{30}{35}$	$1.7727 \\ 1.7394$	2.0921 $2.0411$	2.4120 $2.3406$	2.8431 $2.7400$	3.1787 $3.0480$
	4	3.9067	5.9358	8.7935	14.452	20.824			33 40	1.7394 $1.7146$	2.0411 $2.0035$	2.3400 $2.2882$	2.7400 $2.6648$	2.9531
	5	3.2816	4.7040	6.5678	9.9626	13.491			45	1.7140 $1.6954$	1.9745	2.2480	2.6046	2.8811
	6	2.9195	4.0274	5.4098	7.7896	10.133								
	7	2.6839	3.6030	4.7095	6.5382	8.2697			50 60	1.6802	1.9515	2.2162	2.5625	2.8247
	8	2.5186	3.3130	4.2434	5.7343	7.1045			60 70	1.6574	1.9174	2.1692	2.4961	2.7419
	9	2.3961	3.1025	3.9121	5.1779	6.3142			70 80	1.6413	1.8932	2.1361	2.4496	2.6840
	10	2.3018	2.9430	3.6649	4.7715	5.7462			80 100	$1.6292 \\ 1.6124$	1.8753 $1.8503$	2.1115 $2.0773$	2.4151 $2.3676$	2.6413 $2.5825$
	11	2.2269	2.8179	3.4737	4.4624	5.3197			120	1.60124 $1.6012$	1.8337	2.0773 $2.0548$	2.3363	2.5625 $2.5439$
	12	2.1660	2.7173	3.3215	4.2198	4.9884			120	1.0012	1.0001	2.0040	2.0000	2.040∂

$ u_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995	$ u_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995
12	150	1.5901	1.8172	2.0325	2.3053	2.5059	14	20	1.8588	2.2250	2.6030	3.1296	3.5530
	200	1.5789	1.8008	2.0103	2.2747	2.4683		21	1.8412	2.1975	2.5638	3.0715	3.4779
	500	1.5590	1.7715	1.9708	2.2204	2.4018		22	1.8252	2.1727	2.5285	3.0195	3.4108
	$+\infty$	1.5458	1.7522	1.9447	2.1847	2.3583		23	1.8107	2.1502	2.4966	2.9727	3.3506
19								24	1.7974	2.1298	2.4677	2.9303	3.2962
13	1	60.903	244.69	979.84	6125.9	24505		25	1.7853	2.1111	2.4413	2.8917	3.2469
	2	9.4145	19.419	39.421	99.422	199.42		30	1.7371	2.0374	2.3378	2.7418	3.0560
	3	5.2098	8.7287	14.304	26.983	43.271		35	1.7031	1.9858	2.2659	2.6387	2.9258
	4	3.8859	5.8911	8.7150	14.307	20.603		40	1.6778	1.9476	2.2130	2.5634	2.8312
	5	3.2567	4.6552	6.4876	9.8248	13.293		45	1.6582	1.9182	2.1725	2.5060	2.7595
	6	2.8920	3.9764	5.3290	7.6575	9.9501		50	1.6426	1.8949	2.1404	2.4609	2.7032
	7	2.6545	3.5503	4.6285	6.4100	8.0967		60	1.6420 $1.6193$	1.8602	2.1404 $2.0929$	2.4009 $2.3943$	2.7032 $2.6205$
	8	2.4876	3.2590	4.1622	5.6089	6.9384		70	1.6028	1.8357	2.0929 $2.0595$	2.3945 $2.3477$	2.5205 $2.5627$
	9	2.3640	3.0475	3.8306	5.0545	6.1530		80	1.5904	1.8174	2.0395 $2.0346$	2.3477	2.5027 $2.5201$
	10	2.2687	2.8872	3.5832	4.6496	5.5887		100	1.5731	1.7919	2.0340 $2.0001$	2.3151 $2.2654$	2.4614
	11	2.1930	2.7614	3.3917	4.3416	5.1649		120	1.5617	1.7919 $1.7750$	1.9773	2.2034 $2.2339$	2.4014 $2.4228$
	12	2.1313	2.6602	3.2393	4.0999	4.8358		150	1.55017 $1.5502$	1.7750 $1.7582$	1.9546	2.2339 $2.2028$	2.4226 $2.3847$
	13	2.0802	2.5769	3.1150	3.9052	4.5733		200	1.5388	1.7362 $1.7415$	1.9340 $1.9322$	2.2028 $2.1721$	2.3647 $2.3472$
	14	2.0370	2.5073	3.0119	3.7452	4.3591		500	1.5388 $1.5182$	1.7415 $1.7116$	1.8921	2.1171 $2.1174$	2.2806
	15	2.0001	2.4481	2.9249	3.6115	4.1813		$+\infty$	1.5046	1.6918	1.8656	2.1174 $2.0815$	2.2371
	16	1.9682	2.3973	2.8506	3.4981	4.0314		$+\infty$	1.5040		1.0000	2.0010	2.2371
	17	1.9404	2.3531	2.7863	3.4007	3.9033	15	1	61.220	245.95	984.87	6157.3	24630
	18	1.9158	2.3143	2.7302	3.3162	3.7926		2	9.4247	19.429	39.431	99.433	199.43
	19	1.8940	2.2800	2.6808	3.2422	3.6961		3	5.2003	8.7029	14.253	26.872	43.085
	20	1.8745	2.2495	2.6369	3.1769	3.6111		4	3.8704	5.8578	8.6565	14.198	20.438
	21	1.8570	2.2222	2.5978	3.1187	3.5358		5	3.2380	4.6188	6.4277	9.7222	13.146
	22	1.8411	2.1975	2.5626	3.0667	3.4686		6	2.8712	3.9381	5.2687	7.5590	9.8140
	23	1.8267	2.1752	2.5308	3.0199	3.4083		7	2.6322	3.5107	4.5678	6.3143	7.9678
	24	1.8136	2.1548	2.5019	2.9775	3.3538		8	2.4642	3.2184	4.1012	5.5151	6.8143
	25	1.8015	2.1362	2.4756	2.9389	3.3044		9	2.3396	3.0061	3.7694	4.9621	6.0325
	30	1.7538	2.0630	2.3724	2.7890	3.1132		10	2.2435	2.8450	3.5217	4.5581	5.4707
	35	1.7201	2.0117	2.3008	2.6859	2.9827		11	2.1671	2.7186	3.3299	4.2509	5.0489
	40	1.6950	1.9738	2.2481	2.6107	2.8880		12	2.1049	2.6169	3.1772	4.0096	4.7213
	45	1.6757	1.9446	2.2078	2.5534	2.8162		13	2.0532	2.5331	3.0527	3.8154	4.4600
								14	2.0095	2.4630	2.9493	3.6557	4.2468
	50 60	1.6602	$1.9214 \\ 1.8870$	2.1758	2.5083	2.7599		15	1.9722	2.4034	2.8621	3.5222	4.0698
	60 70	1.6372 $1.6209$	1.8627	2.1286 $2.0953$	2.4419 $2.3953$	2.6771 $2.6193$		16	1.9399	2.3522	2.7875	3.4089	3.9205
	80	1.6086	1.8445	2.0955 $2.0706$	2.3608	2.5767		17	1.9117	2.3077	2.7230	3.3117	3.7929
	100	1.5916	1.8443	2.0766	2.3008 $2.3132$	2.5180		18	1.8868	2.2686	2.6667	3.2273	3.6827
	120	1.5910 $1.5803$	1.8026	2.0303 $2.0136$	2.3132 $2.2818$	2.4794		19	1.8647	2.2341	2.6171	3.1533	3.5866
	150	1.5690	1.7859	1.9911	2.2518 $2.2508$	2.4413		20	1.8449	2.2033	2.5731	3.0880	3.5020
	200	1.5577	1.7694	1.9688	2.2303 $2.2201$	2.4413 $2.4038$		21	1.8449 $1.8271$	2.2053 $2.1757$	2.5731 $2.5338$	3.0300	3.4270
	500	1.5374	1.7398	1.9000 $1.9290$	2.2201 $2.1656$	2.4038 $2.3373$		$\frac{21}{22}$	1.8111	2.1757	2.3338 $2.4984$	2.9779	3.3600
	$+\infty$	1.5240	1.7333	1.9230 $1.9027$	2.1030 $2.1299$	2.2938		23	1.7964	2.1303 $2.1282$	2.4665	2.9311	3.2999
	$+\infty$							$\frac{23}{24}$	1.7831	2.1262 $2.1077$	2.4374	2.8887	3.2456
14	1	61.073	245.36	982.53	6142.7	24572		$\frac{24}{25}$	1.7708	2.0889	2.4110	2.8502	3.1963
	2	9.4200	19.424	39.427	99.428	199.43		30	1.7223	2.0148	2.3072	2.7002	3.0057
	3	5.2047	8.7149	14.277	26.924	43.172		35	1.6880	1.9629	2.2350	2.5970	2.8756
	4	3.8776	5.8733	8.6838	14.249	20.515		40	1.6624	1.9245	2.1819	2.5216	2.7811
	5	3.2468	4.6358	6.4556	9.7700	13.215		45	1.6426	1.8949	2.1412	2.4642	2.7094
	6	2.8809	3.9559	5.2968	7.6049	9.8774							
	7	2.6426	3.5292	4.5961	6.3590	8.0279		50	1.6269	1.8714	2.1090	2.4190	2.6531
	8	2.4752	3.2374	4.1297	5.5589	6.8721		60	1.6034	1.8364	2.0613	2.3523	2.5705
	9	2.3510	3.0255	3.7980	5.0052	6.0887		70	1.5866	1.8117	2.0277	2.3055	2.5127
	10	2.2553	2.8647	3.5504	4.6008	5.5257		80	1.5741	1.7932	2.0026	2.2709	2.4700
	11	2.1792	2.7386	3.3588	4.2932	5.1031		100	1.5566	1.7675	1.9679	2.2230	2.4113
	12	2.1173	2.6371	3.2062	4.0518	4.7748		120	1.5450	1.7505	1.9450	2.1915	2.3727
	13	2.0658	2.5536	3.0819	3.8573	4.5129		150	1.5334	1.7335	1.9222	2.1603	2.3346
	14	2.0224	2.4837	2.9786	3.6975	4.2993		200	1.5218	1.7166	1.8996	2.1294	2.2970
	15	1.9853	2.4244	2.8915	3.5639	4.1219		500	1.5010	1.6864	1.8592	2.0746	2.2304
	16	1.9532	2.3733	2.8170	3.4506	3.9723		$+\infty$	1.4871	1.6664	1.8326	2.0385	2.1868
	17	1.9252	2.3290	2.7526	3.3533	3.8445	16	1	61.350	246.46	986.92	6170.1	24681
	18	1.9004	2.2900	2.6964	3.2689	3.7341		2	9.4289	19.433	39.435	99.437	199.44
	19	1.8785	2.2556	2.6469	3.1949	3.6378		3	5.1964	8.6923	14.232	26.827	43.008
													_

$ u_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995		$ u_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995
16	4	3.8639	5.8441	8.6326	14.154	20.371	-	17	35	1.6622	1.9240	2.1828	2.5266	2.7911
	5	3.2303	4.6038	6.4032	9.6802	13.086			40	1.6362	1.8851	2.1293	2.4511	2.6966
	6	2.8626	3.9223	5.2439	7.5186	9.7582			45	1.6161	1.8551	2.0883	2.3935	2.6249
	7	2.6230	3.4944	4.5428	6.2750	7.9148			50	1.6000	1.8313	2.0558	2.3481	2.5686
	8	2.4545	3.2016	4.0761	5.4766	6.7633			60	1.5760	1.7959	2.0076	2.3481 $2.2811$	2.4859
	9	2.3295	2.9890	3.7441	4.9240	5.9829			70	1.5589	1.7708	1.9736	2.2341	2.4281
	10	2.2330	2.8276	3.4963	4.5204	5.4221			80	1.5461	1.7520	1.9483	2.1993	2.3854
	11	2.1563	2.7009	3.3044	4.2134	5.0011			100	1.5283	1.7920 $1.7259$	1.9132	2.1533 $2.1511$	2.3265
	12	2.0938	2.5989	3.1515	3.9724	4.6741			120	1.5164	1.7085	1.8900	2.1194	2.2878
	13	2.0419	2.5149	3.0269	3.7783	4.4132			150	1.5045	1.6913	1.8669	2.0880	2.2496
	14	1.9981	2.4446	2.9234	3.6187	4.2005			200	1.4926	1.6741	1.8440	2.0569	2.2118
	15	1.9605	2.3849	2.8360	3.4852	4.2003 $4.0237$			500	1.4320 $1.4712$	1.6432	1.8030	2.0003 $2.0016$	2.2116 $2.1449$
	16	1.9281	2.3335	2.7614	3.3720	3.8747			$+\infty$	1.4712 $1.4570$	1.6228	1.7759	1.9652	2.1011
	17	1.8997	2.2888	2.6968	3.2748	3.7473								
	18	1.8747	2.2496	2.6404	3.1904	3.6373		18	1	61.566	247.32	990.35	6191.5	24767
	19	1.8524	2.2149	2.5907	3.1165	3.5412			2	9.4358	19.440	39.442	99.444	199.44
									3	5.1898	8.6745	14.196	26.751	42.880
	20	1.8325	2.1840	2.5465	3.0512	3.4568			4	3.8531	5.8211	8.5924	14.080	20.258
	21	1.8146	2.1563	2.5071	2.9931	3.3818			5	3.2172	4.5785	6.3619	9.6096	12.985
	22	1.7984	2.1313	2.4717	2.9411	3.3150			6	2.8481	3.8957	5.2021	7.4507	9.6644
	23	1.7837	2.1086	2.4396	2.8943	3.2549			7	2.6074	3.4669	4.5008	6.2089	7.8258
	24	1.7703	2.0880	2.4105	2.8519	3.2007			8	2.4380	3.1733	4.0338	5.4116	6.6775
	25	1.7579	2.0691	2.3840	2.8133	3.1515			9	2.3123	2.9600	3.7015	4.8599	5.8994
	30	1.7090	1.9946	2.2799	2.6632	2.9611			10	2.2153	2.7980	3.4534	4.4569	5.3403
	35	1.6744	1.9424	2.2075	2.5599	2.8310			11	2.1380	2.6709	3.2612	4.1503	4.9205
	40	1.6486	1.9037	2.1542	2.4844	2.7365			12	2.0750	2.5684	3.1081	3.9095	4.5945
	45	1.6287	1.8740	2.1133	2.4269	2.6648			13	2.0227	2.4841	2.9832	3.7156	4.3344
	50	1.6128	1.8503	2.0810	2.3816	2.6086			14	1.9785	2.4134	2.8795	3.5561	4.1221
	60	1.5890	1.8151	2.0330	2.3148	2.5259			15	1.9407	2.3533	2.7919	3.4228	3.9459
	70	1.5721	1.7902	1.9992	2.2679	2.4681			16	1.9079	2.3016	2.7170	3.3096	3.7972
	80	1.5594	1.7716	1.9741	2.2332	2.4254			17	1.8792	2.2567	2.6522	3.2124	3.6701
	100	1.5418	1.7456	1.9391	2.1852	2.3666			18	1.8539	2.2172	2.5956	3.1280	3.5603
	120	1.5300	1.7285	1.9161	2.1536	2.3280			19	1.8314	2.1823	2.5457	3.0541	3.4645
	150	1.5182	1.7113	1.8931	2.1223	2.2898								
	200	1.5065	1.6943	1.8704	2.0913	2.2521			20	1.8113	2.1511	2.5014	2.9887	3.3802
	500	1.4854	1.6638	1.8297	2.0362	2.1854			21	1.7932	2.1232	2.4618	2.9306	3.3054
	$+\infty$	1.4714	1.6435	1.8028	2.0000	2.1417			22	1.7768	2.0980	2.4262	2.8786	3.2387
1.7	1			000 72	C101 4	0.4707	-		23	1.7619	2.0751	2.3940	2.8317	3.1787
17	1	61.464	246.92	988.73	6181.4	24727			24	1.7483	2.0543	2.3648	2.7892	3.1246
	2	9.4325	19.437	39.439	99.440	199.44			25	1.7358	2.0353	2.3381	2.7506	3.0754
	3	5.1929	8.6829	14.213	26.787	42.941			30	1.6862	1.9601	2.2334	2.6003	2.8852
	4	3.8582	5.8320	8.6113	14.115	20.311			35	1.6511	1.9073	2.1605	2.4967	2.7551
	5	3.2234	4.5904	6.3814	9.6429	13.033			40	1.6249	1.8682	2.1068	2.4210	2.6607
	6	2.8550	3.9083	5.2218	7.4827	9.7086			45	1.6046	1.8381	2.0656	2.3633	2.5889
	7	2.6148	3.4799	4.5206	6.2401	7.8678			50	1.5884	1.8141	2.0330	2.3178	2.5326
	8	2.4458	3.1867	4.0538	5.4423	6.7180			60	1.5642	1.7784	1.9846	2.2507	2.4498
	9	2.3205	2.9737	3.7216	4.8902	5.9388			70	1.5470	1.7531	1.9504	2.2036	2.3919
	10	2.2237	2.8120	3.4737	4.4869	5.3789			80	1.5340	1.7342	1.9250	2.1686	2.3492
	11	2.1467	2.6851	3.2816	4.1801	4.9586			100	1.5160	1.7079	1.8897	2.1203	2.2902
	12	2.0839	2.5828	3.1286	3.9392	4.6321			120	1.5039	1.6904	1.8663	2.0885	2.2514
	13	2.0318	2.4987	3.0039	3.7452	4.3716			150	1.4919	1.6730	1.8431	2.0570	2.2131
	14	1.9878	2.4282	2.9003	3.5857	4.1592			200	1.4799	1.6556	1.8200	2.0257	2.1753
	15	1.9501	2.3683	2.8128	3.4523	3.9827			500	1.4583	1.6245	1.7787	1.9702	2.1082
	16	1.9175	2.3167	2.7380	3.3391	3.8338			$+\infty$	1.4439	1.6038	1.7515	1.9336	2.0642
	17	1.8889	2.2719	2.6733	3.2419	3.7066	•	10		61 650				
	18	1.8638	2.2325	2.6168	3.1575	3.5967		19	1	61.658	247.69	991.80	6200.6	24803
	19	1.8414	2.1977	2.5670	3.0836	3.5008			2	9.4387	19.443	39.445	99.447	199.45
	20	1.8214	2.1667	2.5228	3.0183	3.4164			3	5.1870	8.6670	14.181	26.719	42.826
	$\frac{20}{21}$	1.8214 $1.8034$	2.1389	2.5228 $2.4833$	$\frac{3.0183}{2.9602}$	3.3416			4	3.8485	5.8114	8.5753	14.048	20.210
	$\frac{21}{22}$	1.8034 $1.7871$		2.4833 $2.4478$		3.3416 $3.2748$			5	3.2117	4.5678	6.3444	9.5797	12.942
			2.1138		2.9082				6	2.8419	3.8844	5.1844	7.4219	9.6247
	23	1.7723	2.0910	2.4157	2.8613	3.2148			7	2.6008	3.4551	4.4829	6.1808	7.7881
	24	1.7587	2.0703	2.3865	2.8189	3.1606			8	2.4310	3.1613	4.0158	5.3840	6.6411
	25	1.7463	2.0513	2.3599	2.7803	3.1114			9	2.3050	2.9477	3.6833	4.8327	5.8639
	30	1.6970	1.9765	2.2554	2.6301	2.9211			10	2.2077	2.7854	3.4351	4.4299	5.3055
						$\rightarrow$								$\rightarrow$

$\nu_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995		$ u_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995
19	11	2.1302	2.6581	3.2428	4.1234	4.8863	•	20	100	1.4943	1.6764	1.8486	2.0666	2.2270
	12	2.0670	2.5554	3.0896	3.8827	4.5606			120	1.4821	1.6587	1.8249	2.0346	2.1881
	13	2.0145	2.4709	2.9646	3.6888	4.3008			150	1.4698	1.6410	1.8014	2.0028	2.1496
	14	1.9701	2.4000	2.8607	3.5294	4.0888			200	1.4575	1.6233	1.7780	1.9713	2.1116
	15	1.9321	2.3398	2.7730	3.3961	3.9127			500	1.4354	1.5916	1.7362	1.9152	2.0441
	16	1.8992	2.2880	2.6980	3.2829	3.7641			$+\infty$	1.4206	1.5705	1.7085	1.8783	1.9998
	17	1.8704	2.2429	2.6331	3.1857	3.6372	į	0.1		C1 01F				
	18	1.8450	2.2033	2.5764	3.1013	3.5275		21	1	61.815	248.31	994.29	6216.1	24866
	19	1.8224	2.1683	2.5265	3.0274	3.4318			2	9.4437	19.448	39.450	99.452	199.45
	20	1.8022			2.9620				3	5.1822	8.6540	14.155	26.664	42.733
	20		2.1370	2.4821 $2.4424$		3.3475			4	3.8405	5.7945	8.5460	13.994	20.128
	$\frac{21}{22}$	1.7840	2.1090		2.9039	3.2728			5	3.2021	4.5493	6.3142	9.5281	12.868
	23	$1.7675 \\ 1.7525$	2.0837 $2.0608$	$2.4067 \\ 2.3745$	2.8518 $2.8049$	3.2060 $3.1461$			6	2.8312	3.8649	5.1538	7.3722	9.5562
	$\frac{23}{24}$	1.7323	2.0008 $2.0399$	2.3452	2.7624	3.1401 $3.0920$			7	2.5892	3.4349	4.4520	6.1324	7.7230
	$\frac{24}{25}$	1.7263	2.0399 $2.0207$	2.3452 $2.3184$	2.7024 $2.7238$	3.0920 $3.0429$			8	2.4188	3.1404	3.9846	5.3364	6.5783
	30	1.6763	1.9452	2.3184 $2.2134$	2.7236 $2.5732$	$\frac{3.0429}{2.8526}$			9	2.2922	2.9263	3.6520	4.7856	5.8027
	35	1.6410	1.9452 $1.8922$	2.2134 $2.1403$	2.3732 $2.4695$	2.7226			10	2.1944	2.7636	3.4035	4.3831	5.2454
	40	1.6410 $1.6146$	1.8522	2.1403 $2.0864$	2.4095 $2.3937$	2.6281			11	2.1165	2.6358	3.2109	4.0769	4.8270
									12	2.0530	2.5328	3.0575	3.8363	4.5020
	45	1.5941	1.8226	2.0450	2.3359	2.5563			13	2.0001	2.4479	2.9322	3.6425	4.2426
	50	1.5778	1.7985	2.0122	2.2903	2.4999			14	1.9555	2.3768	2.8282	3.4832	4.0310
	60	1.5534	1.7625	1.9636	2.2230	2.4171			15	1.9172	2.3163	2.7403	3.3498	3.8552
	70	1.5360	1.7371	1.9293	2.1758	2.3591			16	1.8840	2.2642	2.6651	3.2367	3.7069
	80	1.5230	1.7180	1.9037	2.1408	2.3163			17	1.8550	2.2189	2.6000	3.1394	3.5801
	100	1.5047	1.6915	1.8682	2.0923	2.2572			18	1.8294	2.1791	2.5431	3.0550	3.4705
	120	1.4926	1.6739	1.8447	2.0604	2.2183			19	1.8066	2.1438	2.4930	2.9810	3.3749
	150	1.4804	1.6563	1.8213	2.0287	2.1800			20	1.7862	2.1124	2.4484	2.9156	3.2907
	200	1.4683	1.6388	1.7981	1.9973	2.1420			21	1.7678	2.0842	2.4484 $2.4086$	2.8574	3.2367 $3.2160$
	500	1.4464	1.6074	1.7566	1.9415	2.0748			22	1.7512	2.0542 $2.0587$	2.3728	2.8052	3.1494
	$+\infty$	1.4318	1.5865	1.7291	1.9048	2.0306			23	1.7312 $1.7360$	2.0356	2.3404	2.7583	3.0895
20	1	61.740	248.01	993.10	6208.7	24836			$\frac{23}{24}$	1.7222	2.0336 $2.0146$	2.3109	2.7157	3.0354
20	2	9.4413	19.446	39.448	99.449	199.45			$\frac{24}{25}$	1.7095	1.9953	2.2840	2.6770	2.9862
	3	5.1845	8.6602	14.167	26.690	42.778			30	1.6590	1.9192	2.1785	2.5262	2.7960
	4	3.8443	5.8025	8.5599	14.020	20.167			35	1.6232	1.8657	2.1769 $2.1049$	2.4222	2.6659
	5	3.2067	4.5581	6.3286	9.5526	12.903			40	1.5965	1.8260	2.0506	2.3461	2.5713
	6	2.8363	3.8742	5.1684	7.3958	9.5888			45	1.5757	1.7953	2.0089	2.2880	2.4994
	7	2.5947	3.4445	4.4667	6.1554	7.7540								
	8	2.4246	3.1503	3.9995	5.3591	6.6082			50	1.5592	1.7709	1.9759	2.2423	2.4429
	9	2.2983	2.9365	3.6669	4.8080	5.8318			60	1.5343	1.7346	1.9269	2.1747	2.3598
									70	1.5166	1.7088	1.8922	2.1271	2.3017
	10	2.2007	2.7740	3.4185	4.4054	5.2740			80	1.5034	1.6895	1.8664	2.0919	2.2587
	11	2.1230	2.6464	3.2261	4.0990	4.8552			100	1.4848	1.6626	1.8305	2.0431	2.1993
	12	2.0597	2.5436	3.0728	3.8584	4.5299			120	1.4724	1.6447	1.8067	2.0109	2.1603
	13	2.0070	2.4589	2.9477	3.6646	4.2703			150	1.4600	1.6268	1.7830	1.9790	2.1218
	14	1.9625	2.3879	2.8437	3.5052	4.0585			200	1.4476	1.6090	1.7595	1.9474	2.0836
	15	1.9243	2.3275	2.7559	3.3719	3.8826			500	1.4252	1.5770	1.7174	1.8910	2.0159
	16	1.8913	2.2756	2.6808	3.2587	3.7342			$+\infty$	1.4102	1.5557	1.6895	1.8539	1.9715
	17	1.8624	2.2304	2.6158	3.1615	3.6073		22	1	61.883	248.58	995.36	6222.8	24892
	18	1.8368	2.1906	2.5590	3.0771	3.4977			2	9.4458	19.450	39.452	99.454	199.45
	19	1.8142	2.1555	2.5089	3.0031	3.4020			3	5.1801	8.6484	14.144	26.640	42.693
	20	1.7938	2.1242	2.4645	2.9377	3.3178			4	3.8371	5.7872	8.5332	13.970	20.093
	21	1.7756	2.0960	2.4247	2.8796	3.2431			5	3.1979	4.5413	6.3011	9.5058	12.836
	22	1.7590	2.0707	2.3890	2.8274	3.1764			6	2.8266	3.8564	5.1406	7.3506	9.5264
	23	1.7439	2.0476	2.3567	2.7805	3.1165			7	2.5842	3.4260	4.4386	6.1113	7.6947
	24	1.7302	2.0267	2.3273	2.7380	3.0624			8	2.4135	3.1313	3.9711	5.3157	6.5510
	25	1.7175	2.0075	2.3005	2.6993	3.0133			9	2.2867	2.9169	3.6383	4.7651	5.7760
	30	1.6673	1.9317	2.1952	2.5487	2.8230			10	2.1887	2.7541	3.3897	4.3628	5.2192
	35	1.6317	1.8784	2.1218	2.4448	2.6930			11	2.1106	2.7341 $2.6261$	3.1970	4.0566	4.8012
	40	1.6052	1.8389	2.0677	2.3689	2.5984			11	2.1106 $2.0469$	2.5201 $2.5229$	3.1970 $3.0434$	3.8161	
	45	1.5846	1.8084	2.0262	2.3109	2.5266			13	1.9939		$\frac{3.0434}{2.9181}$	3.6224	4.4765 $4.2173$
	50	1.5681	1.7841	1.9933	2.2652	2.4702					2.4379			
	60	1.5435	1.7480	1.9955 $1.9445$	2.2052 $2.1978$	2.4702 $2.3872$			$\begin{array}{c} 14 \\ 15 \end{array}$	1.9490 $1.9106$	2.3667 $2.3060$	2.8139 $2.7260$	3.4630 $3.3297$	4.0058
	70	1.5455 $1.5259$	1.7480 $1.7223$	1.9100	2.1578 $2.1504$	2.3291			16	1.9106 $1.8774$	2.3060 $2.2538$	2.7260 $2.6507$	3.3297 3.2165	3.8301 $3.6819$
	80	1.5128	1.7223 $1.7032$	1.8843	2.1364 $2.1153$	2.3291 $2.2862$			17	1.8482	2.2338 $2.2084$	2.5855	3.2103 $3.1192$	3.5552
		1.0120	1.1002	1.0010	00				Τ1	1.0404	4.4004	2.0000	0.1194	5.000 <u>4</u>

$\nu_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995	$\nu_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995
22	18	1.8225	2.1685	2.5285	3.0348	3.4456	24	2	9.4496	19.454	39.456	99.458	199.46
	19	1.7997	2.1331	2.4783	2.9607	3.3500		3	5.1764	8.6385	14.124	26.598	42.622
	20	1.7792	2.1016	2.4337	2.8953	3.2659		4	3.8310	5.7744	8.5109	13.929	20.030
	21	1.7607	2.0733	2.4937 $2.3938$	2.8370	3.1912		5	3.1905	4.5272	6.2780	9.4665	12.780
	$\frac{21}{22}$	1.7440	2.0478	2.3579	2.7849	3.1912 $3.1246$		6	2.8183	3.8415	5.1172	7.3127	9.4742
	23	1.7288	2.0246	2.3254	2.7378	3.1240 $3.0647$		7	2.5753	3.4105	4.4150	6.0743	7.6450
	$\frac{23}{24}$	1.7249	2.0240 $2.0035$	2.3254 $2.2959$	2.6953	3.0106		8	2.4041	3.1152	3.9472	5.2793	6.5029
	$\frac{24}{25}$	1.7149 $1.7021$	1.9842	2.2690	2.6565	2.9615		9	2.2768	2.9005	3.6142	4.7290	5.7292
	30	1.7021 $1.6514$	1.9042 $1.9077$	2.2690 $2.1631$	2.5055	2.9013 $2.7712$		10	2.1784	2.7372	3.3654	4.3269	5.1732
	35	1.6154	1.8540	2.1031 $2.0893$	2.4014	2.7712 $2.6410$		11	2.1704	2.6090	3.1725	4.0209	4.7557
								12					
	$\frac{40}{45}$	1.5884 $1.5676$	1.8141 $1.7833$	2.0349 $1.9930$	2.3252 $2.2670$	$2.5463 \\ 2.4744$		13	2.0360 $1.9827$	2.5055 $2.4202$	3.0187 $2.8932$	3.7805 $3.5868$	$4.4314 \\ 4.1726$
								13 14	1.9377	2.4202 $2.3487$	2.7888	3.4274	3.9614
	50	1.5509	1.7588	1.9599	2.2211	2.4178		15	1.8990	2.2878	2.7006	3.4274 $3.2940$	3.7859
	60	1.5259	1.7222	1.9106	2.1533	2.3346		16	1.8656	2.2354	2.7000 $2.6252$	3.1808	3.6378
	70	1.5080	1.6962	1.8758	2.1057	2.2764							
	80	1.4947	1.6768	1.8499	2.0703	2.2333		17	1.8362	2.1898	2.5598	3.0835	3.5112
	100	1.4759	1.6497	1.8138	2.0214	2.1738		18	1.8103	2.1497	2.5027	2.9990	3.4017
	120	1.4634	1.6317	1.7899	1.9891	2.1347		19	1.7873	2.1141	2.4523	2.9249	3.3062
	150	1.4509	1.6137	1.7661	1.9570	2.0961		20	1.7667	2.0825	2.4076	2.8594	3.2220
	200	1.4383	1.5958	1.7424	1.9252	2.0578		21	1.7481	2.0540	2.3675	2.8010	3.1474
	500	1.4157	1.5635	1.7000	1.8686	1.9899		22	1.7312	2.0283	2.3315	2.7488	3.0807
	$+\infty$	1.4006	1.5420	1.6719	1.8313	1.9453		23	1.7159	2.0050	2.2989	2.7017	3.0208
23	1	61.945	248.83	996.35	6229.0	24917		24	1.7019	1.9838	2.2693	2.6591	2.9667
20	2	9.4478	19.452	39.454	99.456	199.46		25	1.6890	1.9643	2.2422	2.6203	2.9176
	3	5.1781	8.6432	14.134	26.618	42.656		30	1.6377	1.8874	2.1359	2.4689	2.7272
	4	3.8339	5.7805	8.5216	13.949	20.060		35	1.6013	1.8332	2.0617	2.3645	2.5969
	5	3.1941	4.5339	6.2891	9.4853	12.807		40	1.5741	1.7929	2.0069	2.2880	2.5020
	6	2.8223	3.8486	5.1284	7.3309	9.4992		45	1.5530	1.7618	1.9647	2.2296	2.4299
	7	2.5796	3.4179	4.4263	6.0921	7.6688		50	1.5361	1.7371	1.9313	2.1835	2.3732
	8	2.4086	3.4179 $3.1229$	3.9587	5.2967	6.5260		60	1.5107	1.7001	1.8817	2.1154	2.2898
	9	2.4000 $2.2816$	2.9084	3.6257	4.7463	5.7516		70	1.4926	1.6738	1.8466	2.0674	2.2313
								80	1.4790	1.6542	1.8204	2.0318	2.1881
	10	2.1833	2.7453	3.3770	4.3441	5.1953		100	1.4600	1.6267	1.7839	1.9826	2.1283
	11	2.1051	2.6172	3.1843	4.0380	4.7775		120	1.4472	1.6084	1.7597	1.9500	2.0890
	12	2.0412	2.5139	3.0306	3.7976	4.4530		150	1.4345	1.5902	1.7356	1.9177	2.0501
	13	1.9881	2.4287	2.9052	3.6038	4.1940		200	1.4217	1.5720	1.7117	1.8857	2.0116
	14	1.9431	2.3573	2.8009	3.4445	3.9827		500	1.3986	1.5392	1.6687	1.8285	1.9432
	15	1.9046	2.2966	2.7128	3.3111	3.8071		$+\infty$	1.3832	1.5173	1.6402	1.7908	1.8983
	16	1.8712	2.2443	2.6374	3.1979	3.6589		1 \infty	1.0002	1.0110	1.0402	1.1300	1.0000
	17	1.8420	2.1987	2.5721	3.1006	3.5323	25	1	62.055	249.26	998.08	6239.8	24960
	18	1.8162	2.1587	2.5151	3.0161	3.4228		2	9.4513	19.456	39.458	99.459	199.46
	19	1.7932	2.1233	2.4648	2.9421	3.3272		3	5.1747	8.6341	14.115	26.579	42.591
	20	1.7727	2.0917	2.4201	2.8766	3.2431		4	3.8283	5.7687	8.5010	13.911	20.002
	21	1.7541	2.0633	2.3801	2.8183	3.1684		5	3.1873	4.5209	6.2679	9.4491	12.755
	22	1.7374	2.0377	2.3442	2.7661	3.1018		6	2.8147	3.8348	5.1069	7.2960	9.4511
	23	1.7221	2.0144	2.3116	2.7191	3.0419		7	2.5714	3.4036	4.4045	6.0580	7.6230
	24	1.7081	1.9932	2.2821	2.6765	2.9878		8	2.3999	3.1081	3.9367	5.2631	6.4817
	$\frac{24}{25}$	1.6953	1.9738	2.2521 $2.2551$	2.6377	2.9387		9	2.2725	2.8932	3.6035	4.7130	5.7084
	30	1.6443	1.8972	2.1490	2.4865	2.7483		10	2.1739	2.7298	3.3546	4.3111	5.1528
	35	1.6081	1.8432	2.0750	2.3822	2.6181		11	2.0953	2.6014	3.1616	4.0051	4.7356
	40	1.5810	1.8031	2.0203	2.3052	2.5233		12	2.0333 $2.0312$	2.4977	3.0077	3.7647	4.4115
	45	1.5600	1.7722	1.9784	2.3033 $2.2476$	2.4513		13	1.9778	2.4123	2.8821	3.5710	4.1528
								14	1.9326	2.4123 $2.3407$	2.7777	3.4116	3.9417
	50	1.5432	1.7475	1.9451	2.2016	2.3947		15	1.9320 $1.8939$	2.3407 $2.2797$	2.6894	3.4110 $3.2782$	3.7662
	60	1.5180	1.7108	1.8956	2.1336	2.3114		16	1.8603	2.2797 $2.2272$	2.6694 $2.6138$	3.2782 $3.1650$	3.6182
	70	1.5000	1.6846	1.8606	2.0858	2.2530		17	1.8309	2.2272 $2.1815$	2.5484	3.1650 $3.0676$	3.4916
	80	1.4866	1.6651	1.8346	2.0504	2.2098		18	1.8049	2.1813 $2.1413$	2.3484 $2.4912$	2.9831	3.4910 $3.3822$
	100	1.4677	1.6378	1.7983	2.0012	2.1502		19	1.7818	2.1415 $2.1057$	2.4912 $2.4408$	2.9831 $2.9089$	3.3822 $3.2867$
	120	1.4550	1.6197	1.7743	1.9688	2.1110							
	150	1.4424	1.6015	1.7503	1.9367	2.0723		20	1.7611	2.0739	2.3959	2.8434	3.2025
	200	1.4297	1.5834	1.7265	1.9047	2.0339		21	1.7424	2.0454	2.3558	2.7850	3.1279
	500	1.4069	1.5509	1.6838	1.8479	1.9657		22	1.7255	2.0196	2.3198	2.7328	3.0613
	$+\infty$	1.3916	1.5292	1.6555	1.8104	1.9209		23	1.7101	1.9963	2.2871	2.6856	3.0014
24	1	62.002	249.05	997.25	6234.6	24940		24	1.6960	1.9750	2.2574	2.6430	2.9472
41	1	02.002	210.00	551.40	0204.0	~ <del>~</del> ~~~							$\rightarrow$

$ u_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995	$ u_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995
25	25	1.6831	1.9554	2.2303	2.6041	2.8981	35	9	2.2418	2.8422	3.5292	4.6020	5.5643
	30	1.6316	1.8782	2.1237	2.4526	2.7076		10	2.1420	2.6776	3.2794	4.2005	5.0110
	35	1.5950	1.8239	2.0493	2.3480	2.5772		11	2.0623	2.5480	3.0856	3.8948	4.5955
	40	1.5677	1.7835	1.9943	2.2714	2.4823		12	1.9971	2.4433	2.9309	3.6544	4.2725
	45	1.5464	1.7522	1.9521	2.2129	2.4101		13	1.9428	2.3570	2.8046	3.4606	4.0146
	50	1.5294	1.7273	1.9186	2.1667	2.3533		14	1.8968	2.2845	2.6994	3.3010	3.8040
	60	1.5039	1.6902	1.8687	2.0984	2.2697		15	1.8573	2.2227	2.6104	3.1674	3.6289
	70	1.4857	1.6638	1.8334	2.0503	2.2112		16	1.8230	2.1694	2.5342	3.0539	3.4811
	80	1.4720	1.6440	1.8071	2.0146	2.1678		17	1.7929	2.1229	2.4681	2.9563	3.3547
	100	1.4528	1.6163	1.7705	1.9652	2.1080		18	1.7663	2.0821	2.4103	2.8714	3.2453
	120	1.4399	1.5980	1.7462	1.9325	2.0686		19	1.7426	2.0458	2.3593	2.7969	3.1498
	150	1.4271	1.5796	1.7220	1.9001	2.0295		20	1.7213	2.0135	2.3139	2.7310	3.0656
	$\frac{200}{500}$	1.4142 $1.3909$	$1.5612 \\ 1.5282$	1.6978 $1.6546$	1.8679 $1.8105$	1.9909		21	1.7021	1.9844	2.2733	2.6723	2.9909
	$+\infty$	1.3753	1.5262 $1.5061$	1.6259	1.7726	$1.9223 \\ 1.8771$		22	1.6847	1.9581	2.2366	2.6197	2.9241
								23	1.6689	1.9342	2.2035	2.5722	2.8641
30	1	62.265	250.10	1001.4	6260.6	25044		24	1.6544	1.9124	2.1733	2.5292	2.8098
	2	9.4579	19.462	39.465	99.466	199.47		25	1.6410	1.8924	2.1458	2.4900	2.7605
	3	5.1681	8.6166	14.081	26.505	42.466		30	1.5877	1.8132	2.0372	2.3369	2.5691
	4	3.8174	5.7459	8.4613	13.838	19.892		$\frac{35}{40}$	$1.5497 \\ 1.5211$	$1.7571 \\ 1.7154$	$1.9611 \\ 1.9047$	2.2309 $2.1531$	2.4377 $2.3418$
	5 6	3.1741 $2.8000$	4.4957 $3.8082$	6.2269 $5.0652$	9.3793 $7.2285$	$12.656 \\ 9.3582$		45	1.4989	1.6830	1.8613	2.1931 $2.0934$	2.2687
	7	2.5555	3.3758	4.3624	5.9920	9.5562 7.5345							
	8	2.3830	3.0794	3.8940	5.1981	6.3961		50	1.4810	1.6571	1.8267	2.0463	2.2112
	9	2.2547	2.8637	3.5604	4.6486	5.6248		60 70	1.4541	1.6183	1.7752	1.9764	2.1263
								80	1.4348 $1.4203$	1.5906 $1.5699$	$1.7386 \\ 1.7112$	$1.9271 \\ 1.8904$	2.0666 $2.0223$
	10 11	2.1554 $2.0762$	2.6996 $2.5705$	3.3110 $3.1176$	4.2469 $3.9411$	5.0706 $4.6543$		100	1.3998	1.5407	1.7112 $1.6729$	1.8393	1.9610
	12	2.0702 $2.0115$	2.4663	2.9633	3.7008	4.0343 $4.3309$		120	1.3861	1.5213	1.6475	1.8055	1.9205
	13	1.9576	2.3803	2.9053 $2.8372$	3.5070	4.0727		150	1.3723	1.5018	1.6220	1.7719	1.8803
	14	1.9119	2.3082	2.7324	3.3476	3.8619		200	1.3583	1.4822	1.5966	1.7383	1.8404
	15	1.8728	2.2468	2.6437	3.2141	3.6867		500	1.3331	1.4467	1.5508	1.6783	1.7692
	16	1.8388	2.1938	2.5678	3.1007	3.5389		$+\infty$	1.3160	1.4229	1.5201	1.6383	1.7221
	17	1.8090	2.1477	2.5020	3.0032	3.4124	40	1	62.529	251.14	1005.6	6286.8	25148
	18	1.7827	2.1071	2.4445	2.9185	3.3030	40	2	9.4662	19.471	39.473	99.474	199.47
	19	1.7592	2.0712	2.3937	2.8442	3.2075		3	5.1597	8.5944	14.037	26.411	42.308
	20	1.7382	2.0391	2.3486	2.7785	3.1234		4	3.8036	5.7170	8.4111	13.745	19.752
	21	1.7193	2.0102	2.3082	2.7200	3.0488		5	3.1573	4.4638	6.1750	9.2912	12.530
	22	1.7021	1.9842	2.2718	2.6675	2.9821		6	2.7812	3.7743	5.0125	7.1432	9.2408
	23	1.6864	1.9605	2.2389	2.6202	2.9221		7	2.5351	3.3404	4.3089	5.9084	7.4224
	24	1.6721	1.9390	2.2090	2.5773	2.8679		8	2.3614	3.0428	3.8398	5.1156	6.2875
	25	1.6589	1.9192	2.1816	2.5383	2.8187		9	2.2320	2.8259	3.5055	4.5666	5.5186
	30	1.6065	1.8409	2.0739	2.3860	2.6278		10	2.1317	2.6609	3.2554	4.1653	4.9659
	35	1.5691	1.7856	1.9986	2.2806	2.4969		11	2.0516	2.5309	3.0613	3.8596	4.5508
	40	1.5411	1.7444	1.9429	2.2034	2.4015		12	1.9861	2.4259	2.9063	3.6192	4.2282
	45	1.5193	1.7126	1.9000	2.1443	2.3288		13	1.9315	2.3392	2.7797	3.4253	3.9704
	50	1.5018	1.6872	1.8659	2.0976	2.2717		14	1.8852	2.2664	2.6742	3.2656	3.7600
	60	1.4755	1.6491	1.8152	2.0285	2.1874		15	1.8454	2.2043	2.5850	3.1319	3.5850
	70	1.4567	1.6220	1.7792	1.9797	2.1283		16	1.8108	2.1507	2.5085	3.0182	3.4372
	80	1.4426	1.6017	1.7523	1.9435	2.0845		17	1.7805	2.1040	2.4422	2.9205	3.3108
	$\frac{100}{120}$	1.4227 $1.4094$	$1.5733 \\ 1.5543$	$1.7148 \\ 1.6899$	1.8933 $1.8600$	2.0239 1.9840		18 19	$1.7537 \\ 1.7298$	2.0629	2.3842 $2.3329$	2.8354 $2.7608$	3.2014
	150	1.4094 $1.3960$	1.5343 $1.5354$	1.6651	1.8270	1.9640 $1.9444$				2.0264			3.1058
	200	1.3826	1.5164	1.6403	1.7941	1.9051		20	1.7083	1.9938	2.2873	2.6947	3.0215
	500	1.3582	1.4821	1.5957	1.7353	1.8352		21	1.6890	1.9645	2.2465	2.6359	2.9467
	$+\infty$	1.3419	1.4591	1.5660	1.6964	1.7891		22	1.6714	1.9380	2.2097	2.5831	2.8799
- or								$\frac{23}{24}$	1.6554 $1.6407$	1.9139 $1.8920$	2.1763 $2.1460$	2.5355 $2.4923$	2.8197 $2.7654$
35	1	62.416	250.69	1003.8	6275.6	25103		$\frac{24}{25}$	1.6407 $1.6272$	1.8920 $1.8718$	2.1460 $2.1183$	2.4923 $2.4530$	2.7654 $2.7160$
	$\frac{2}{3}$	9.4627 $5.1633$	$19.467 \\ 8.6039$	39.469 $14.055$	99.471 $26.451$	$199.47 \\ 42.376$		30	1.5732	1.7918	2.1163 $2.0089$	2.4930 $2.2992$	2.7100 $2.5241$
	$\frac{3}{4}$	3.8096	5.7294	8.4327	13.785	$\frac{42.370}{19.812}$		35	1.5346	1.7310 $1.7351$	1.9321	2.1926	2.3922
	5	3.1645	4.4775	6.4927 $6.1973$	9.3291	12.584		40	1.5056	1.6928	1.8752	2.1142	2.2958
	6	2.7893	3.7889	5.0352	7.1799	9.2913		45	1.4830	1.6599	1.8313	2.0542	2.2224
	7	2.5439	3.3557	4.3319	5.9444	7.4707		50	1.4648	1.6337	1.7963	2.0066	2.1644
	8	2.3707	3.0586	3.8632	5.1512	6.3343		50	1.4040	1.0001	T.1300	2.0000	$2.1044$ $\rightarrow$
						,							•

$ u_1$	$ u_2$	0.9	0.95	0.975	0.99	0.995		$ u_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995
								50		1.8284		2.5488		
40	60 70	1.4373 $1.4176$	$1.5943 \\ 1.5661$	$1.7440 \\ 1.7069$	1.9360 $1.8861$	2.0789 $2.0186$		90	15 16	1.6264 $1.7934$	2.1780 $2.1240$	2.3488 $2.4719$	3.0814 $2.9675$	3.5225 $3.3747$
	80	1.4027	1.5449	1.6790	1.8489	1.9739			17	1.7628	2.0769	2.4053	2.8694	3.2482
	100	1.3817	1.5151	1.6401	1.7972	1.9119			18	1.7356	2.0354	2.3468	2.7841	3.1387
	120	1.3676	1.4952	1.6141	1.7628	1.8709			19	1.7114	1.9986	2.2952	2.7093	3.0430
	150	1.3534	1.4752	1.5882	1.7286	1.8302			20	1.6896	1.9656	2.2493	2.6430	2.9586
	200	1.3390	1.4551	1.5621	1.6945	1.7897			21	1.6700	1.9360 $1.9360$	2.2493 $2.2081$	2.5838	2.9380 $2.8837$
	500	1.3129	1.4186	1.5151	1.6332	1.7172			22	1.6521	1.9092	2.2001 $2.1710$	2.5308	2.8167
	$+\infty$	1.2951	1.3940	1.4835	1.5923	1.6691			23	1.6358	1.8848	2.1374	2.4829	2.7564
45	1	62.617	251.49	1007.0	6295.5	25183	•		24	1.6209	1.8625	2.1067	2.4395	2.7018
10	2	9.4690	19.474	39.476	99.477	199.48			25	1.6072	1.8421	2.0787	2.3999	2.6522
	3	5.1569	8.5870	14.022	26.379	42.255			30	1.5522	1.7609	1.9681	2.2450	2.4594
	4	3.7990	5.7073	8.3943	13.714	19.705			35	1.5127	1.7032	1.8902	2.1374	2.3266
	5	3.1517	4.4530	6.1576	9.2616	12.487			40	1.4830	1.6600	1.8324	2.0581	2.2295
	6	2.7748	3.7629	4.9947	7.1145	9.2014			45	1.4597	1.6264	1.7876	1.9972	2.1553
	7	2.5282	3.3285	4.2908	5.8803	7.3847			50	1.4409	1.5995	1.7520	1.9490	2.0967
	8	2.3540	3.0304	3.8215	5.0878	6.2510			60	1.4126	1.5590	1.6985	1.8772	2.0100
	9	2.2242	2.8131	3.4869	4.5390	5.4827			70	1.3922	1.5300	1.6604	1.8263	1.9488
	10	2.1236	2.6477	3.2366	4.1377	4.9306			80	1.3767	1.5081	1.6318	1.7883	1.9033
	11	2.0432	2.5174	3.0422	3.8320	4.5158			100	1.3548	1.4772	1.5917	1.7353	1.8400
	12	1.9774	2.4121	2.8870	3.5915	4.1934			120	1.3400	1.4565	1.5649	1.7000	1.7981
	13	1.9225	2.3252	2.7601	3.3976	3.9358			150	1.3251	1.4357	1.5379	1.6648	1.7563
	14	1.8760	2.2521	2.6544	3.2378	3.7254			200	1.3100	1.4146	1.5108	1.6295	1.7147
	15	1.8360	2.1897	2.5650	3.1039	3.5504			500	1.2823	1.3762	1.4616	1.5658	1.6398
	16	1.8012	2.1360	2.4883	2.9902	3.4026			$+\infty$	1.2633	1.3501	1.4284	1.5231	1.5898
	17 18	$1.7707 \\ 1.7437$	2.0890 $2.0477$	2.4218 $2.3635$	2.8922 $2.8071$	3.2762 $3.1667$		60	1	62.794	252.20	1009.8	6313.0	25253
	19	1.7437	2.0477 $2.0110$	2.3035 $2.3121$	2.7323	3.1007 $3.0711$			2	9.4746	19.479	39.481	99.482	199.48
									3	5.1512	8.5720	13.992	26.316	42.149
	20	1.6980	1.9783	2.2663	2.6661	2.9868			4	3.7896	5.6877	8.3604	13.652	19.611
	$\frac{21}{22}$	1.6785	1.9488	2.2253	2.6071	2.9119			5	3.1402	4.4314	6.1225	9.2020	12.402
	23	1.6608 $1.6446$	$1.9221 \\ 1.8979$	2.1883 $2.1548$	$2.5542 \\ 2.5065$	2.8449 $2.7847$			6 7	$2.7620 \\ 2.5142$	3.7398 $3.3043$	$4.9589 \\ 4.2544$	7.0567 $5.8236$	9.1219 $7.3088$
	$\frac{23}{24}$	1.6298	1.8757	2.1348 $2.1243$	2.4632	2.7303			8	2.3142 $2.3391$	3.0043	3.7844	5.0316	6.1772
	25	1.6161	1.8554	2.0964	2.4237	2.6808			9	2.2085	2.7872	3.4493	4.4831	5.4104
	30	1.5616	1.7748	1.9864	2.2693	2.4884								
	35	1.5226	1.7175	1.9090	2.1622	2.3560			10 11	2.1072 $2.0261$	2.6211 $2.4901$	3.1984 $3.0035$	4.0819 $3.7761$	$4.8592 \\ 4.4450$
	40	1.4932	1.6748	1.8516	2.0833	2.2593			12	1.9597	2.3842	2.8478	3.5355	4.1229
	45	1.4702	1.6415	1.8073	2.0228	2.1854			13	1.9043	2.2966	2.7204	3.3413	3.8655
	50	1.4517	1.6149	1.7719	1.9749	2.1272			14	1.8572	2.2229	2.6142	3.1813	3.6552
	60	1.4238	1.5749	1.7191	1.9037	2.0410			15	1.8168	2.1601	2.5242	3.0471	3.4803
	70	1.4037	1.5463	1.6814	1.8533	1.9803			16	1.7816	2.1058	2.4471	2.9330	3.3324
	80	1.3885	1.5247	1.6532	1.8157	1.9352			17	1.7506	2.0584	2.3801	2.8348	3.2058
	100	1.3670	1.4944	1.6136	1.7633	1.8725			18	1.7232	2.0166	2.3214	2.7493	3.0962
	120	1.3526	1.4741	1.5872	1.7284	1.8310			19	1.6988	1.9795	2.2696	2.6742	3.0004
	150	1.3380	1.4536	1.5607	1.6937	1.7898			20	1.6768	1.9464	2.2234	2.6077	2.9159
	200	1.3232	1.4330	1.5341	1.6590	1.7487			21	1.6569	1.9165	2.1819	2.5484	2.8408
	500	1.2963	1.3955	1.4860	1.5964	1.6750			22	1.6389	1.8894	2.1446	2.4951	2.7736
	$+\infty$	1.2779	1.3701	1.4536	1.5546	1.6259			23	1.6224	1.8648	2.1107	2.4471	2.7132
50	1	62.688	251.77	1008.1	6302.5	25211			24	1.6073	1.8424	2.0799	2.4035	2.6585
	2	9.4712	19.476	39.478	99.479	199.48			25	1.5934	1.8217	2.0516	2.3637	2.6088
	3	5.1546	8.5810	14.010	26.354	42.213			30	1.5376	1.7396	1.9400	2.2079	2.4151
	4	3.7952	5.6995	8.3808	13.690	19.667			35	1.4975	1.6811	1.8613	2.0994	2.2816
	5	3.1471	4.4444	6.1436	9.2378	12.454			$\frac{40}{45}$	1.4672	1.6373	1.8028	2.0194 $1.9579$	2.1838
	6	2.7697	3.7537	4.9804	7.0915	9.1697				1.4434	1.6031	1.7574		2.1090
	7 8	2.5226 $2.3481$	3.3189 $3.0204$	4.2763 $3.8067$	5.8577 $5.0654$	7.3544 $6.2215$			50	1.4242	1.5757	1.7211	1.9090	2.0499
	9	2.3481 $2.2180$	$\frac{3.0204}{2.8028}$	3.8067 $3.4719$	$\frac{5.0654}{4.5167}$	5.4539			60	1.3952	1.5343	1.6668	1.8363	1.9622
									70	1.3742	1.5046	1.6279	1.7846	1.9002
	10	2.1171	2.6371	3.2214	4.1155	4.9022			80	1.3583	1.4821	1.5987	1.7459	1.8540
	11	2.0364	2.5066	3.0268	3.8097	4.4876			100	1.3356	1.4504	1.5575	1.6918	1.7896
	12	1.9704	2.4010	2.8714	3.5692	4.1653			$\frac{120}{150}$	1.3203 $1.3048$	1.4290 $1.4074$	$1.5299 \\ 1.5022$	1.6557 $1.6195$	$1.7469 \\ 1.7041$
	$\frac{13}{14}$	1.9153 $1.8686$	2.3138	2.7443 $2.6384$	3.3752 $3.2153$	3.9078 $3.6975$			$\frac{150}{200}$	1.3048 $1.2891$	1.4074 $1.3856$	1.3022 $1.4742$	1.5195 $1.5833$	1.7041 $1.6614$
	14	1.0000	2.2405	2.0384	5.2155	ə. <del>09</del> 7ə			200	1.4091	1.0000	1.7174	1.0000	1.0014

$\nu_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995		$\nu_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995
60	500	1.2600	1.3455	1.4231	1.5174	1.5843		80	22	1.6218	1.8641	2.1108	2.4496	2.7187
	$+\infty$	1.2400	1.3180	1.3883	1.4730	1.5325			23	1.6051	1.8392	2.0766	2.4013	2.6581
70	1	62.870	252.50	1011.0	6320.6	25283			24	1.5897	1.8164	2.0454	2.3573	2.6031
10	2	9.4769	19.481	39.484	99.485	199.49			25	1.5755	1.7955	2.0169	2.3173	2.5532
	3	5.1487	8.5656	13.979	26.289	42.104			30	1.5187	1.7121	1.9039	2.1601	2.3584
	4	3.7855	5.6793	8.3458	13.625	19.570			35	1.4776	1.6525	1.8240	2.0505	2.2237
	5	3.1353	4.4220	6.1074	9.1763	12.366			40	1.4465	1.6077	1.7644	1.9694	2.1249
	6	2.7564	3.7298	4.9434	7.0318	9.0877			45	1.4221	1.5726	1.7181	1.9069	2.0491
	7	2.5082	3.2939	4.2386	5.7991	7.2760			50	1.4023	1.5445	1.6810	1.8571	1.9891
	8	2.3326	2.9944	3.7684	5.0073	6.1453			60	1.3722	1.5019	1.6252	1.7828	1.8998
	9	2.2017	2.7760	3.4330	4.4589	5.3791			70	1.3503	1.4711	1.5851	1.7298	1.8365
									80	1.3337	1.4477	1.5549	1.6901	1.7892
	10	2.1000	2.6095	3.1818	4.0577	4.8283			100	1.3100	1.4146	1.5122	1.6342	1.7231
	11	2.0187	2.4782	2.9867	3.7518	4.4143			120	1.2938	1.3922	1.4834	1.5968	1.6789
	12	1.9520	2.3720	2.8307	3.5111	4.0924			150	1.2774	1.3694	1.4543	1.5592	1.6347
	13	1.8963	2.2841	2.7030	3.3168	3.8350			200	1.2605	1.3463	1.4248	1.5212	1.5902
	14	1.8490	2.2102	2.5966	3.1567	3.6248			500	1.2292	1.3033	1.3704	1.4517	1.5091
	15	1.8083	2.1472	2.5064	3.0224	3.4498			$+\infty$	1.2072	1.2735	1.3329	1.4041	1.4540
	16	1.7729	2.0926	2.4291	2.9082	3.3018	-	100	1					05227
	17	$1.7418 \\ 1.7142$	2.0450 $2.0030$	2.3619 $2.3030$	2.8097	3.1752 $3.0655$		100	$\frac{1}{2}$	63.007	253.04	1013.2	6334.1	25337 $199.49$
	18 19	1.7142	1.9657	2.3030 $2.2509$	$2.7241 \\ 2.6488$	2.9695			3	9.4812 $5.1443$	19.486 $8.5539$	39.488 $13.956$	99.489 $26.240$	42.022
									3 4	3.7782	5.6641	8.3195	13.577	
	20	1.6674	1.9323	2.2045	2.5822	2.8849			5	3.1263	4.4051	6.0800	9.1299	19.497 $12.300$
	21	1.6474	1.9023	2.1629	2.5227	2.8097			6	$\frac{3.1203}{2.7463}$	$\frac{4.4051}{3.7117}$	4.9154	6.9867	9.0257
	22	1.6292	1.8751	2.1254	2.4693	2.7424			7	2.7403 $2.4971$	3.7117 $3.2749$	4.9154 $4.2101$	5.7547	7.2165
	23	1.6125	1.8503	2.0913	2.4210	2.6818			8	2.4971 $2.3208$	$\frac{3.2749}{2.9747}$	3.7393	4.9633	6.0875
	24	1.5973	1.8276	2.0603	2.3773	2.6270			9	2.3208 $2.1892$	2.7556	3.4034	4.9055 $4.4150$	5.3223
	25	1.5833	1.8069	2.0319	2.3373	2.5772								
	30	1.5269	1.7240	1.9195	2.1808	2.3829			10	2.0869	2.5884	3.1517	4.0137	4.7721
	35	1.4862	1.6649	1.8402	2.0716	2.2488			11	2.0050	2.4566	2.9561	3.7077	4.3585
	40	1.4555	1.6205	1.7810	1.9911	2.1504			12	1.9379	2.3498	2.7996	3.4668	4.0368
	45	1.4313	1.5859	1.7351	1.9290	2.0751			13	1.8817	2.2614	2.6715	3.2723	3.7795
	50	1.4119	1.5580	1.6984	1.8797	2.0155			14	1.8340	2.1870	2.5646	3.1118	3.5692
	60	1.3822	1.5160	1.6433	1.8061	1.9269			15	1.7929	2.1234	2.4739	2.9772	3.3941
	70	1.3608	1.4857	1.6038	1.7537	1.8642			16	1.7570	2.0685	2.3961	2.8627	3.2460
	80	1.3444	1.4628	1.5740	1.7144	1.8174			17	1.7255	2.0204	2.3285	2.7639	3.1192
	100	1.3212	1.4303	1.5320	1.6594	1.7521			18	1.6976	1.9780	2.2692	2.6779	3.0093
	120	1.3055	1.4083	1.5038	1.6226	1.7086			19	1.6726	1.9403	2.2167	2.6023	2.9131
	150	1.2895	1.3861	1.4753	1.5856	1.6651			20	1.6501	1.9066	2.1699	2.5353	2.8282
	200	1.2731	1.3636	1.4465	1.5485	1.6215			21	1.6298	1.8761	2.1280	2.4755	2.7527
	500	1.2428	1.3220	1.3937	1.4807	1.5423			22	1.6113	1.8486	2.0901	2.4217	2.6852
	$+\infty$	1.2218	1.2933	1.3575	1.4346	1.4888			23	1.5944	1.8234	2.0557	2.3732	2.6243
80	1	62.927	252.72	1011.9	6326.2	25306			24	1.5788	1.8005	2.0243	2.3291	2.5692
	$\overline{2}$	9.4787	19.483	39.485	99.487	199.49			25	1.5645	1.7794	1.9955	2.2888	2.5191
	3	5.1469	8.5607	13.970	26.269	42.070			30	1.5069	1.6950	1.8816	2.1307	2.3234
	4	3.7825	5.6730	8.3349	13.605	19.540			35	1.4653	1.6347	1.8009	2.0202	2.1880
	5	3.1316	4.4150	6.0960	9.1570	12.338			40	1.4336	1.5892	1.7405	1.9383	2.0884
	6	2.7522	3.7223	4.9318	7.0130	9.0619			45	1.4087	1.5536	1.6935	1.8751	2.0119
	7	2.5036	3.2860	4.2268	5.7806	7.2513			50	1.3885	1.5249	1.6558	1.8248	1.9512
	8	2.3277	2.9862	3.7563	4.9890	6.1213			60	1.3576	1.4814	1.5990	1.7493	1.8609
	9	2.1965	2.7675	3.4207	4.4407	5.3555			70	1.3352	1.4498	1.5581	1.6954	1.7966
	10	2.0946	2.6008	3.1694	4.0394	4.8050			80	1.3180	1.4259	1.5271	1.6548	1.7484
	11	2.0940 $2.0130$	2.4692	2.9740	3.7335	4.3912			100	1.2934	1.3917	1.4833	1.5977	1.6809
	12	1.9461	2.4692 $2.3628$	2.8178	3.4928	4.0693			120	1.2767	1.3685	1.4536	1.5592	1.6357
	13	1.8903	2.3028 $2.2747$	2.6900	3.4926 $3.2984$	3.8120			150	1.2595	1.3448	1.4234	1.5204	1.5901
	14	1.8428	2.2006	2.5833	3.1381	3.6017			200	1.2418	1.3206	1.3927	1.4811	1.5442
	15	1.8019	2.1373	2.4930	3.0037	3.4267			500	1.2086	1.2753	1.3356	1.4084	1.4598
	16	1.7664	2.0826	2.4154	2.8893	3.2787			$+\infty$	1.1850	1.2434	1.2956	1.3581	1.4017
	17	1.7351	2.0348	2.3481	2.7908	3.1520	•	120	1	63.061	253.25	1014.0	6339.4	25359
	18	1.7073	1.9927	2.2890	2.7050	3.0422			2	9.4829	19.487	39.490	99.491	199.49
	19	1.6826	1.9552	2.2368	2.6296	2.9462			3	5.1425	8.5494	13.947	26.221	41.989
									4	3.7753	5.6581	8.3092	13.558	19.468
	20	1.6603	1.9217	2.1902	2.5628	2.8614			5	3.1228	4.3985	6.0693	9.1118	12.274
	21	1.6401	1.8915	2.1485	2.5032	2.7861								$\rightarrow$

$ u_1$	$ u_2$	0.9	0.95	0.975	0.99	0.995	$ u_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995
120	6	2.7423	3.7047	4.9044	6.9690	9.0015	150	45	1.3900	1.5272	1.6596	1.8313	1.9607
120	7	2.4928	3.2674	4.1989	5.7373	7.1933	100						
	8	2.3162	2.9669	3.7279	4.9461	6.0649		50	1.3691	1.4977	1.6210	1.7799	1.8989
	9	2.1843	2.7475	3.3918	4.3978	5.3001		60 70	1.3372 $1.3137$	$1.4527 \\ 1.4200$	$1.5625 \\ 1.5202$	$1.7027 \\ 1.6472$	$1.8067 \\ 1.7408$
	10	2.0818	2.5801	3.1399	3.9965	4.7501		80	1.3137 $1.2957$	1.4200 $1.3949$	1.3202 $1.4880$	1.6053	1.6912
	11	1.9997	2.4480	2.9441	3.6904	4.7361 $4.3367$		100	1.2698	1.3549 $1.3591$	1.4422	1.5459	1.6213
	12	1.9323	2.3410	2.7874	3.4494	4.0149		120	1.2519	1.3345	1.4109	1.5057	1.5741
	13	1.8759	2.2524	2.6590	3.2548	3.7577		150	1.2335	1.3093	1.3789	1.4647	1.5264
	14	1.8280	2.1778	2.5519	3.0942	3.5473		200	1.2143	1.2832	1.3460	1.4229	1.4777
	15	1.7867	2.1141	2.4611	2.9595	3.3722		500	1.1775	1.2334	1.2836	1.3442	1.3868
	16	1.7507	2.0589	2.3831	2.8447	3.2240		$+\infty$	1.1505	1.1972	1.2387	1.2881	1.3224
	17	1.7191	2.0107	2.3153	2.7459	3.0971	200	1	63.167	253.68	1015.7	6350.0	25401
	18	1.6910	1.9681	2.2558	2.6597	2.9871	_00	2	9.4862	19.491	39.493	99.494	199.49
	19	1.6659	1.9302	2.2032	2.5839	2.8908		3	5.1390	8.5402	13.929	26.183	41.925
	20	1.6433	1.8963	2.1562	2.5168	2.8058		4	3.7695	5.6461	8.2885	13.520	19.411
	21	1.6228	1.8657	2.1141	2.4568	2.7302		5	3.1157	4.3851	6.0478	9.0754	12.222
	22	1.6041	1.8380	2.0760	2.4029	2.6625		6	2.7343	3.6904	4.8824	6.9336	8.9528
	23	1.5871	1.8128	2.0415	2.3542	2.6015		7	2.4841	3.2525	4.1764	5.7024	7.1466
	24	1.5715	1.7896	2.0099	2.3100	2.5463		8	2.3068	2.9513	3.7050	4.9114	6.0194
	25	1.5570	1.7684	1.9811	2.2696	2.4961		9	2.1744	2.7313	3.3684	4.3631	5.2554
	30	1.4989	1.6835	1.8664	2.1108	2.2998 $2.1637$		10	2.0713	2.5634	3.1161	3.9617	4.7058
	$\frac{35}{40}$	1.4568 $1.4248$	$1.6226 \\ 1.5766$	$1.7851 \\ 1.7242$	$1.9996 \\ 1.9172$	2.1637 $2.0636$		11	1.9888	2.4308	2.9198	3.6555	4.2926
	45	1.4246 $1.3995$	1.5406	1.7242 $1.6767$	1.8535	1.9865		12	1.9210	2.3233	2.7626	3.4143	3.9709
								13	1.8642	2.2343	2.6339	3.2194	3.7136
	50	1.3789	1.5115	1.6386	1.8026	1.9254		14	1.8159	2.1592	2.5264	3.0585	3.5032
	60 70	1.3476	1.4673	1.5810	1.7263	1.8341		15	1.7743	2.0950	2.4352	2.9235	3.3279
	70 80	1.3246 $1.3071$	$1.4351 \\ 1.4107$	1.5394 $1.5079$	1.6717 $1.6305$	$1.7691 \\ 1.7203$		16	1.7379	2.0395	2.3567	2.8084	3.1796
	100	1.2819	1.4107 $1.3757$	1.4631	1.5723	1.6516		17 18	1.7060 $1.6775$	1.9909 $1.9479$	2.2886 $2.2287$	$2.7092 \\ 2.6227$	3.0524 $2.9421$
	120	1.2646	1.3519	1.4327	1.5330	1.6055		19	1.6521	1.9479	2.2267 $2.1757$	2.5467	2.8456
	150	1.2468	1.3275	1.4017	1.4932	1.5590							
	200	1.2285	1.3024	1.3700	1.4527	1.5118		20 21	1.6292	1.8755	2.1284	2.4792	2.7603
	500	1.1936	1.2551	1.3105	1.3774	1.4245		22	1.6085 $1.5896$	1.8446 1.8165	2.0859 $2.0475$	2.4189 $2.3646$	2.6845 $2.6165$
	$+\infty$	1.1686	1.2214	1.2684	1.3246	1.3637		23	1.5723	1.7909	2.0126	2.3040 $2.3156$	2.5552
150	1	63.114	253.46	1014.9	6344.7	25380	•	$\frac{25}{24}$	1.5563	1.7675	1.9807	2.2710	2.4997
100	2	9.4846	19.489	39.491	99.492	199.49		25	1.5417	1.7460	1.9515	2.2303	2.4492
	3	5.1408	8.5448	13.938	26.202	41.957		30	1.4824	1.6597	1.8354	2.0700	2.2514
	4	3.7724	5.6521	8.2988	13.539	19.440		35	1.4393	1.5976	1.7527	1.9574	2.1140
	5	3.1193	4.3918	6.0586	9.0936	12.248		40	1.4064	1.5505	1.6906	1.8737	2.0125
	6	2.7383	3.6976	4.8934	6.9513	8.9772		45	1.3803	1.5135	1.6420	1.8087	1.9342
	7	2.4884	3.2600	4.1877	5.7199	7.1700		50	1.3590	1.4835	1.6029	1.7567	1.8719
	8	2.3115	2.9591	3.7165	4.9287	6.0422		60	1.3264	1.4377	1.5435	1.6784	1.7785
	9	2.1793	2.7394	3.3801	4.3805	5.2778		70	1.3024	1.4042	1.5003	1.6220	1.7116
	10	2.0766	2.5718	3.1280	3.9792	4.7280		80	1.2839	1.3786	1.4674	1.5792	1.6611
	11	1.9942	2.4394	2.9320	3.6730	4.3147		100	1.2571	1.3416	1.4203	1.5184	1.5897
	12	1.9266	2.3322	2.7750	3.4319	3.9930		120	1.2385	1.3162	1.3880	1.4770	1.5413
	13 14	$1.8701 \\ 1.8220$	2.2434 $2.1686$	2.6465 $2.5392$	3.2371 $3.0764$	3.7357 $3.5254$		$\frac{150}{200}$	1.2193 $1.1991$	$1.2899 \\ 1.2626$	1.3548 $1.3204$	$1.4347 \\ 1.3912$	1.4921 $1.4416$
	15	1.7805	2.1030 $2.1046$	2.3392 $2.4482$	$\frac{3.0704}{2.9415}$	3.3501		500	1.1591 $1.1598$	1.2020 $1.2096$	1.3204 $1.2543$	1.3912 $1.3081$	1.3459
	16	1.7444	2.1040 $2.0492$	2.3700	2.8267	3.2019		$+\infty$	1.1301	1.1700	1.2043 $1.2053$	1.2472	1.2763
	17	1.7126	2.0008	2.3020	2.7276	3.0748							
	18	1.6843	1.9581	2.2423	2.6413	2.9647	500	1	63.264	254.06	1017.2	6359.5	25439
	19	1.6590	1.9200	2.1895	2.5654	2.8683		2	9.4892	19.494	39.496	99.497	199.50
	20	1.6363	1.8860	2.1424	2.4981	2.7832		$\frac{3}{4}$	5.1358 $3.7642$	8.5320 $5.6353$	13.913 8.2698	26.148 13.486	$41.867 \\ 19.359$
	$\frac{20}{21}$	1.6363 $1.6157$	1.8552	2.1424 $2.1001$	2.4961 $2.4379$	2.7032 $2.7075$		4 5	3.7042	5.6353 4.3731	6.0283	9.0424	19.359 $12.175$
	22	1.5969	1.8273	2.0618	2.3839	2.6396		6	2.7270	$\frac{4.5751}{3.6775}$	4.8625	6.9015	8.9088
	23	1.5797	1.8019	2.0271	2.3350	2.5785		7	2.4761	3.2389	4.0525 $4.1560$	5.6707	7.1044
	24	1.5640	1.7787	1.9954	2.2906	2.5232		8	2.2983	2.9371	3.6842	4.8799	5.9782
	25	1.5494	1.7573	1.9664	2.2501	2.4727		9	2.1653	2.7166	3.3471	4.3317	5.2148
	30	1.4907	1.6717	1.8510	2.0905	2.2758		10	2.0618	2.5481	3.0944	3.9302	4.6656
	35	1.4482	1.6102	1.7691	1.9787	2.1391		11	1.9788	2.4151	2.8977	3.6238	4.2525
	40	1.4157	1.5637	1.7076	1.8956	2.0383		12	1.9106	2.3071	2.7401	3.3823	3.9309
						$\rightarrow$							$\rightarrow$

$ u_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995
500	13	1.8535	2.2176	2.6109	3.1871	3.6735
	14	1.8048	2.1422	2.5030	3.0260	3.4630
	15	1.7628	2.0776	2.4114	2.8906	3.2875
	16	1.7262	2.0217	2.3326	2.7752	3.1389
	17	1.6939	1.9727	2.2640	2.6757	3.0115
	18	1.6651	1.9294	2.2038	2.5889	2.9010
	19	1.6394	1.8909	2.1504	2.5124	2.8042
	20	1.6162	1.8562	2.1027	2.4446	2.7186
	21	1.5952	1.8250	2.1027 $2.0599$	2.3840	2.7100 $2.6425$
	22	1.5760	1.7966	2.0333 $2.0211$	2.3294	2.5742
	23	1.5585	1.7708	1.9859	2.3294 $2.2800$	2.5142 $2.5126$
	$\frac{26}{24}$	1.5423	1.7470	1.9537	2.2351	2.4568
	25	1.5274	1.7252	1.9242	2.1941	2.4059
	30	1.4670	1.6375	1.8065	2.0321	2.2066
	35	1.4229	1.5742	1.7224	1.9180	2.0676
	40	1.3890	1.5260	1.6590	1.8329	1.9647
	45	1.3621	1.4879	1.6092	1.7666	1.8850
	50	1.3400	1.4569	1.5689	1.7133	1.8214
	60	1.3060	1.4093 $1.3743$	1.5075	1.6327	1.7256
	70	1.2807		1.4625	1.5743	1.6565
	80	1.2611 $1.2324$	1.3472 $1.3079$	1.4280 $1.3781$	1.5296 $1.4656$	1.6041 $1.5291$
	$\frac{100}{120}$	1.2324 $1.2122$		1.3434	1.4050 $1.4215$	
	$120 \\ 150$	1.2122 $1.1910$	1.2804 $1.2516$	1.3454 $1.3073$	1.4215 $1.3757$	1.4778 $1.4248$
	200	1.1910 $1.1683$	1.2310 $1.2211$	1.3673 $1.2691$	1.3757 $1.3277$	1.4246 $1.3694$
	500	1.1216	1.2211 $1.1587$	1.1918	1.3277 $1.2317$	1.3094 $1.2596$
	$+\infty$	1.0819	1.1063	1.1918 $1.1277$	1.2517 $1.1530$	1.2590 $1.1704$
$+\infty$	1	63.328	254.31	1018.3	6365.9	25464
	2	9.4912	19.496	39.498	99.499	199.50
	3	5.1337	8.5264	13.902	26.125	41.828
	4	3.7607	5.6281	8.2573	13.463	19.325
	5 c	3.1050	4.3650 $3.6689$	6.0153	9.0204	12.144
	6	2.7222		4.8491	6.8800	8.8793 $7.0760$
	7 8	2.4708 $2.2926$	3.2298 $2.9276$	4.1423 $3.6702$	5.6495 $4.8588$	5.9506
	9	2.2920 $2.1592$	2.7067	3.3329	4.3105	5.9500 $5.1875$
	10	2.0554	2.5379	3.0798	3.9090	4.6385
	11	1.9721	2.4045	2.8828	3.6024	4.2255
	12	1.9036	2.2962	2.7249	3.3608	3.9039
	13	1.8462	2.2064	2.5955	3.1654	3.6465
	14	$1.7973 \\ 1.7551$	2.1307	2.4872	3.0040	3.4359
	15		2.0658	2.3953	2.8684	3.2602
	$\frac{16}{17}$	$1.7182 \\ 1.6856$	2.0096 $1.9604$	2.3163 $2.2474$	2.7528 $2.6530$	3.1115 $2.9839$
	18	1.6567	1.9168	2.1869	2.5660	2.8732
	19	1.6308	1.8780	2.1333	2.4893	2.7762
	20	1.6074	1.8432	2.0853	2.4212	2.6904
	21	1.5862	1.8117	2.0422	2.3603	2.6140
	22	1.5668	1.7831	2.0032	2.3055	2.5455
	23	1.5490	1.7570	1.9677	2.2558	2.4837
	24	1.5327	1.7330	1.9353	2.2107	2.4276
	$\frac{25}{30}$	1.5176	1.7110	1.9055	2.1694	2.3765
	$\frac{30}{35}$	1.4564 $1.4115$	1.6223 $1.5580$	$1.7867 \\ 1.7016$	2.0062 $1.8910$	2.1760 $2.0359$
	33 40	1.4115 $1.3769$	1.5089	1.7016 $1.6371$	1.8910 $1.8047$	2.0339 1.9318
	45	1.3493	1.4700	1.5864	1.7374	1.9516 $1.8510$
	50	1.3267	1.4383	1.5452	1.6831	1.7863
	60	1.2915	1.3893	1.4821	1.6006	1.6885
	70	1.2652	1.3529	1.4357	1.5404	1.6176
	80 100	1.2446	1.3247	1.3997	1.4942	1.5634
	100	1.2142	1.2832	1.3473	1.4272	1.4853
	120	1.1926	1.2539	1.3104	1.3805	1.4311

$\nu_1$	$\nu_2$	0.9	0.95	0.975	0.99	0.995
$+\infty$	150	1.1694	1.2226	1.2714	1.3314	1.3744
	200	1.1439	1.1885	1.2290	1.2785	1.3137
	500	1.0871	1.1132	1.1365	1.1644	1.1840
	$+\infty$	1.0000	1.0000	1.0000	1.0000	1.0000

34 7. Non-parametric tests

#### 7 Non-parametric tests

#### Rejection regions of the Wilcoxon signed-rank test (one sample)

The table below contains the end points of the rejection regions for the Wilcoxon signed-rank test for inference about the median  $\eta$  of a symmetric distribution.

Denote by  $w_-$  the rank sum of the observations less than  $\eta_0$ , and denote by  $w_+$  the rank sum of the observations greater than  $\eta_0$ .

 $H_0$ :  $\eta \le \eta_0$  vs.  $H_1 \eta > \eta_0$  (one-sided): Reject  $H_0$  if  $w_-$  is not larger than the tabulated value.

 $H_0$ :  $\eta \ge \eta_0$  vs.  $H_1 \eta < \eta_0$  (one-sided): Reject  $H_0$  if  $w_+$  is not larger than the tabulated value.

 $H_0$ :  $\eta = \eta_0$  vs.  $H_1 \eta \neq \eta_0$  (two-sided): Reject  $H_0$  if  $\min\{w_+, w_-\}$  is not larger than the tabulated value.

"-" indicates that  $H_0$  is never rejected for the chosen size  $\alpha$  and sample size n.

	S	ize $\alpha$ (or	ne-sided	l)		S	size $\alpha$ (or	ne-sided	1)			size $\alpha$ (o	ne-sided	)
	5%	2.5%	1%	0.5%		5%	2.5%	1%	0.5%		5%	2.5%	1%	0.5%
	S	ize $\alpha$ (tv	vo-sided	1)		S	size $\alpha$ (tv	vo-sideo	d)		:	size $\alpha$ (ty	vo-sided	)
n	10%	5%	2%	1%	n	10%	5%	2%	1%	n	10%	5%	2%	1%
1	_	_	_		31	163	147	130	118	61	715	672	623	589
2	_	_	_	_	32	175	159	140	128	62	741	697	646	611
3	_	_	_	_	33	187	170	151	138	63	767	721	669	634
4	_	_	_	_	34	200	182	162	148	64	793	747	693	657
5	0	_	_	_	35	213	195	173	159	65	820	772	718	681
6	2	0	_	_	36	227	208	185	171	66	847	798	742	705
7	3	2	0	_	37	241	221	198	182	67	875	825	768	729
8	5	3	1	0	38	256	235	211	194	68	903	852	793	754
9	8	5	3	1	39	271	249	224	207	69	931	879	819	779
10	10	8	5	3	40	286	264	238	220	70	960	907	846	805
11	13	10	7	5	41	302	279	252	233	71	990	936	873	831
12	17	13	9	7	42	319	294	266	247	72	1020	964	901	858
13	21	17	12	9	43	336	310	281	261	73	1050	994	928	884
14	25	21	15	12	44	353	327	296	276	74	1081	1023	957	912
15	30	25	19	15	45	371	343	312	291	75	1112	1053	986	940
16	35	29	23	19	46	389	361	328	307	76	1144	1084	1015	968
17	41	34	27	23	47	407	378	345	322	77	1176	1115	1044	997
18	47	40	32	27	48	426	396	362	339	78	1209	1147	1075	1026
19	53	46	37	32	49	446	415	379	355	79	1242	1179	1105	1056
20	60	52	43	37	50	466	434	397	373	80	1276	1211	1136	1086
21	67	58	49	42	51	486	453	416	390	81	1310	1244	1168	1116
22	75	65	55	48	52	507	473	434	408	82	1345	1277	1200	1147
23	83	73	62	54	53	529	494	454	427	83	1380	1311	1232	1178
24	91	81	69	61	54	550	514	473	445	84	1415	1345	1265	1210
25	100	89	76	68	55	573	536	493	465	85	1451	1380	1298	1242
26	110	98	84	75	56	595	557	514	484	86	1487	1415	1332	1275
27	119	107	92	83	57	618	579	535	504	87	1524	1451	1366	1308
28	130	116	101	91	58	642	602	556	525	88	1561	1487	1400	1342
29	140	126	110	100	59	666	625	578	546	89	1599	1523	1435	1376
30	151	137	120	109	60	690	648	600	567	90	1638	1560	1471	1410

#### Rejection regions of the Mann-Whitney/Wilcoxon two-sample test

The table below contains the end points of the rejection regions for the Mann-Whitney test for inference about the medians  $\eta_1$  and  $\eta_2$  of two translated symmetric distributions based on two samples of size  $n_1$  and  $n_2$ , respectively.

Denote by  $r_1$  and  $r_2$  the rank sums obtained for the observations from the first and the second sample. Define  $u_1 = r_1 - \frac{n_1(n_1+1)}{2}$  and  $u_2 = r_2 - \frac{n_2(n_2+1)}{2}$ .

 $H_0$ :  $\eta_1 \le \eta_2$  vs.  $H_1 \eta_1 > \eta_2$  (one-sided): Reject  $H_0$  if  $u_2$  is not larger than the tabulated value.

 $H_0$ :  $\eta_1 \ge \eta_2$  vs.  $H_1 \eta_1 < \eta_2$  (one-sided): Reject  $H_0$  if  $u_1$  is not larger than the tabulated value.

 $H_0$ :  $\eta_1 = \eta_2$  vs.  $H_1 \eta_1 \neq \eta_2$  (two-sided): Reject  $H_0$  if  $\min\{u_1, u_2\}$  is not larger than the tabulated value.

The corresponding tables are shown on pages 35 and 36.

<sup>&</sup>quot;-" indicates that  $H_0$  is never rejected for the chosen size  $\alpha$  and sample sizes  $n_1$  and  $n_2$ .

# Rejection regions of the Mann-Whitney/Wilcoxon two-sample test (size $\alpha$ : 5% one-sided, 10% two-sided)

	$n_2$																							
$n_1$	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25
2	_	_	_	0	0	0	1	1	1	1	2	2	2	3	3	3	4	4	4	5	5	5	6	6
3	_	_	0	1	2	2	3	3	4	5	5	6	7	7	8	9	9	10	11	11	12	13	13	14
4	_	0	1	2	3	4	5	6	7	8	9	10	11	12	14	15	16	17	18	19	20	21	22	23
5	0	1	2	4	5	6	8	9	11	12	13	15	16	18	19	20	22	23	25	26	28	29	30	32
6	0	2	3	5	7	8	10	12	14	16	17	19	21	23	25	26	28	30	32	34	36	37	39	41
7	0	2	4	6	8	11	13	15	17	19	21	24	26	28	30	33	35	37	39	41	44	46	48	50
8	1	3	5	8	10	13	15	18	20	23	26	28	31	33	36	39	41	44	47	49	52	54	57	60
9	1	3	6	9	12	15	18	21	24	27	30	33	36	39	42	45	48	51	54	57	60	63	66	69
10	1	4	7	11	14	17	20	24	27	31	34	37	41	44	48	51	55	58	62	65	68	72	75	79
11	1	5	8	12	16	19	23	27	31	34	38	42	46	50	54	57	61	65	69	73	77	81	85	89
12	2	5	9	13	17	21	26	30	34	38	42	47	51	55	60	64	68	72	77	81	85	90	94	98
13	2	6	10	15	19	24	28	33	37	42	47	51	56	61	65	70	75	80	84	89	94	98	103	108
14	2	7	11	16	21	26	31	36	41	46	51	56	61	66	71	77	82	87	92	97	102	107	113	118
15	3	7	12	18	23	28	33	39	44	50	55	61	66	72	77	83	88	94	100	105	111	116	122	128
16	3	8	14	19	25	30	36	42	48	54	60	65	71	77	83	89	95	101	107	113	119	125	131	137
17	3	9	15	20	26	33	39	45	51	57	64	70	77	83	89	96	102	109	115	121	128	134	141	147
18	4	9	16	22	28	35	41	48	55	61	68	75	82	88	95	102	109	116	123	130	136	143	150	157
19	4	10	17	23	30	37	44	51	58	65	72	80	87	94	101	109	116	123	130	138	145	152	160	167
20	4	11	18	25	32	39	47	54	62	69	77	84	92	100	107	115	123	130	138	146	154	161	169	177
21	5	11	19	26	34	41	49	57	65	73	81	89	97	105	113	121	130	138	146	154	162	170	179	187
22	5	12	20	28	36	44	52	60	68	77	85	94	102	111	119	128	136	145	154	162	171	179	188	197
23	5	13	21	29	37	46	54	63	72	81	90	98	107	116	125	134	143	152	161	170	179	189	198	207
24	6	13	22	30	39	48	57	66	75	85	94	103	113	122	131	141	150	160	169	179	188	198	207	217
25	6	14	23	32	41	50	60	69	79	89	98	108	118	128	137	147	157	167	177	187	197	207	217	227

# Rejection regions of the Mann-Whitney/Wilcoxon two-sample test (size $\alpha$ : 2.5% one-sided, 5% two-sided)

														$n_2$										
$n_1$	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25
2	_	_	_	_	_	_	0	0	0	0	1	1	1	1	1	2	2	2	2	3	3	3	3	3
3	_	_	_	0	1	1	2	2	3	3	4	4	5	5	6	6	7	7	8	8	9	9	10	10
4	_	_	0	1	2	3	4	4	5	6	7	8	9	10	11	11	12	13	14	15	16	17	17	18
5	_	0	1	2	3	5	6	7	8	9	11	12	13	14	15	17	18	19	20	22	23	24	25	27
6	_	1	2	3	5	6	8	10	11	13	14	16	17	19	21	22	24	25	27	29	30	32	33	35
7	_	1	3	5	6	8	10	12	14	16	18	20	22	24	26	28	30	32	34	36	38	40	42	44
8	0	2	4	6	8	10	13	15	17	19	22	24	26	29	31	34	36	38	41	43	45	48	50	53
9	0	2	4	7	10	12	15	17	20	23	26	28	31	34	37	39	42	45	48	50	53	56	59	62
10	0	3	5	8	11	14	17	20	23	26	29	33	36	39	42	45	48	52	55	58	61	64	67	71
11	0	3	6	9	13	16	19	23	26	30	33	37	40	44	47	51	55	58	62	65	69	73	76	80
12	1	4	7	11	14	18	22	26	29	33	37	41	45	49	53	57	61	65	69	73	77	81	85	89
13	1	4	8	12	16	20	24	28	33	37	41	45	50	54	59	63	67	72	76	80	85	89	94	98
14	1	5	9	13	17	22	26	31	36	40	45	50	55	59	64	69	74	78	83	88	93	98	102	107
15	1	5	10	14	19	24	29	34	39	44	49	54	59	64	70	75	80	85	90	96	101	106	111	117
16	1	6	11	15	21	26	31	37	42	47	53	59	64	70	75	81	86	92	98	103	109	115	120	126
17	2	6	11	17	22	28	34	39	45	51	57	63	69	75	81	87	93	99	105	111	117	123	129	135
18	2	7	12	18	24	30	36	42	48	55	61	67	74	80	86	93	99	106	112	119	125	132	138	145
19	2	7	13	19	25	32	38	45	52	58	65	72	78	85	92	99	106	113	119	126	133	140	147	154
20	2	8	14	20	27	34	41	48	55	62	69	76	83	90	98	105	112	119	127	134	141	149	156	163
21	3	8	15	22	29	36	43	50	58	65	73	80	88	96	103	111	119	126	134	142	150	157	165	173
22	3	9	16	23	30	38	45	53	61	69	77	85	93	101	109	117	125	133	141	150	158	166	174	182
23	3	9	17	24	32	40	48	56	64	73	81	89	98	106	115	123	132	140	149	157	166	175	183	192
24	3	10	17	25	33	42	50	59	67	76	85	94	102	111	120	129	138	147	156	165	174	183	192	201
25	3	10	18	27	35	44	53	62	71	80	89	98	107	117	126	135	145	154	163	173	182	192	201	211

# Rejection regions of the Mann-Whitney/Wilcoxon two-sample test (size $\alpha$ : 1% one-sided, 2% two-sided)

	$n_2$																							
$n_1$	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25
2	_	_	_	_	_	_	_	_	_	_	_	0	0	0	0	0	0	1	1	1	1	1	1	1
3	_	_	_	_	_	0	0	1	1	1	2	2	2	3	3	4	4	4	5	5	5	6	6	7
4	_	_	_	0	1	1	2	3	3	4	5	5	6	7	7	8	9	9	10	11	11	12	13	13
5	_	_	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21
6	_	_	1	2	3	4	6	7	8	9	11	12	13	15	16	18	19	20	22	23	24	26	27	29
7	_	0	1	3	4	6	7	9	11	12	14	16	17	19	21	23	24	26	28	30	31	33	35	36
8	_	0	2	4	6	7	9	11	13	15	17	20	22	24	26	28	30	32	34	36	38	40	42	45
9	_	1	3	5	7	9	11	14	16	18	21	23	26	28	31	33	36	38	40	43	45	48	50	53
10	_	1	3	6	8	11	13	16	19	22	24	27	30	33	36	38	41	44	47	50	53	55	58	61
11	_	1	4	7	9	12	15	18	22	25	28	31	34	37	41	44	47	50	53	57	60	63	66	70
12	_	2	5	8	11	14	17	21	24	28	31	35	38	42	46	49	53	56	60	64	67	71	75	78
13	0	2	5	9	12	16	20	23	27	31	35	39	43	47	51	55	59	63	67	71	75	79	83	87
14	0	2	6	10	13	17	22	26	30	34	38	43	47	51	56	60	65	69	73	78	82	87	91	95
15	0	3	7	11	15	19	24	28	33	37	42	47	51	56	61	66	70	75	80	85	90	94	99	104
16	0	3	7	12	16	21	26	31	36	41	46	51	56	61	66	71	76	82	87	92	97	102	108	113
17	0	4	8	13	18	23	28	33	38	44	49	55	60	66	71	77	82	88	93	99	105	110	116	122
18	0	4	9	14	19	24	30	36	41	47	53	59	65	70	76	82	88	94	100	106	112	118	124	130
19	1	4	9	15	20	26	32	38	44	50	56	63	69	75	82	88	94	101	107	113	120	126	133	139
20	1	5	10	16	22	28	34	40	47	53	60	67	73	80	87	93	100	107	114	121	127	134	141	148
21	1	5	11	17	23	30	36	43	50	57	64	71	78	85	92	99	106	113	121	128	135	142	150	157
22	1	5	11	18	24	31	38	45	53	60	67	75	82	90	97	105	112	120	127	135	143	150	158	166
23	1	6	12	19	26	33	40	48	55	63	71	79	87	94	102	110	118	126	134	142	150	158	167	175
24	1	6	13	20	27	35	42	50	58	66	75	83	91	99	108	116	124	133	141	150	158	167	175	184
25	1	7	13	21	29	36	45	53	61	70	78	87	95	104	113	122	130	139	148	157	166	175	184	192

# Rejection regions of the Mann-Whitney/Wilcoxon two-sample test (size $\alpha$ : 0.5% one-sided, 1% two-sided)

														$n_2$										
$n_1$	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25
2	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	_	0	0	0	0	0	0	0
3	_	_	_	_	_	_	_	0	0	0	1	1	1	2	2	2	2	3	3	3	4	4	4	5
4	_	_	_	_	0	0	1	1	2	2	3	3	4	5	5	6	6	7	8	8	9	9	10	10
5	_	_	_	0	1	1	2	3	4	5	6	7	7	8	9	10	11	12	13	14	14	15	16	17
6	_	_	0	1	2	3	4	5	6	7	9	10	11	12	13	15	16	17	18	19	21	22	23	24
7	_	_	0	1	3	4	6	7	9	10	12	13	15	16	18	19	21	22	24	25	27	29	30	32
8	_	_	1	2	4	6	7	9	11	13	15	17	18	20	22	24	26	28	30	32	34	35	37	39
9	_	0	1	3	5	7	9	11	13	16	18	20	22	24	27	29	31	33	36	38	40	43	45	47
10	_	0	2	4	6	9	11	13	16	18	21	24	26	29	31	34	37	39	42	44	47	50	52	55
11	_	0	2	5	7	10	13	16	18	21	24	27	30	33	36	39	42	45	48	51	54	57	60	63
12	_	1	3	6	9	12	15	18	21	24	27	31	34	37	41	44	47	51	54	58	61	64	68	71
13	_	1	3	7	10	13	17	20	24	27	31	34	38	42	45	49	53	57	60	64	68	72	75	79
14	_	1	4	7	11	15	18	22	26	30	34	38	42	46	50	54	58	63	67	71	75	79	83	87
15	_	2	5	8	12	16	20	24	29	33	37	42	46	51	55	60	64	69	73	78	82	87	91	96
16	_	2	5	9	13	18	22	27	31	36	41	45	50	55	60	65	70	74	79	84	89	94	99	104
17	_	2	6	10	15	19	24	29	34	39	44	49	54	60	65	70	75	81	86	91	96	102	107	112
18	_	2	6	11	16	21	26	31	37	42	47	53	58	64	70	75	81	87	92	98	104	109	115	121
19	0	3	7	12	17	22	28	33	39	45	51	57	63	69	74	81	87	93	99	105	111	117	123	129
20	0	3	8	13	18	24	30	36	42	48	54	60	67	73	79	86	92	99	105	112	118	125	131	138
21	0	3	8	14	19	25	32	38	44	51	58	64	71	78	84	91	98	105	112	118	125	132	139	146
22	0	4	9	14	21	27	34	40	47	54	61	68	75	82	89	96	104	111	118	125	133	140	147	155
23	0	4	9	15	22	29	35	43	50	57	64	72	79	87	94	102	109	117	125	132	140	148	155	163
24	0	4	10	16	23	30	37	45	52	60	68	75	83	91	99	107	115	123	131	139	147	155	164	172
25	0	5	10	17	24	32	39	47	55	63	71	79	87	96	104	112	121	129	138	146	155	163	172	180

8. Correlation 37

#### 8 Correlation

#### Critical values for the linear correlation coefficient

The table below contains the critical values for testing whether the linear correlation coefficient is 0. The test statistic used is the empirical correlation coefficient r computed from a sample of size n.

The test is based on the same assumptions as the simple linear model, i.e.  $Y_i|X_i=x_i\sim N(\beta_0+\beta_1x_i,\sigma^2)$  with the  $Y_i$  being independent. This assumption for example holds when  $(X_i,Y_i)$  are i.i.d. realisations from a bivariate normal distribution.

 $H_0$ :  $\rho \le 0$  vs.  $H_1 \rho > 0$  (one-sided): Reject  $H_0$  if r is greater than the tabulated value.

 $H_0$ :  $\rho \ge 0$  vs.  $H_1 \rho < 0$  (one-sided): Reject  $H_0$  if -r is greater than the tabulated value.

 $H_0$ :  $\rho=0$  vs.  $H_1$   $\rho\neq 0$  (two-sided): Reject  $H_0$  if |r| is greater than the tabulated value.

			ne-sided)	
•	5%	2.5%	1%	0.5%
-			wo-sided)	
n	10%	5%	2%	1%
3	0.9877	0.9969	0.9995	0.9999
4	0.9000	0.9500	0.9800	0.9900
5	0.8054	0.8783	0.9343	0.9587
6	0.7293	0.8114	0.8822	0.9172
7	0.6694	0.7545	0.8329	0.8745
8	0.6215	0.7067	0.7887	0.8343
9	0.5822	0.6664	0.7498	0.7977
10	0.5494	0.6319	0.7155	0.7646
11	0.5214	0.6021	0.6851	0.7348
12	0.4973	0.5760	0.6581	0.7079
13	0.4762	0.5529	0.6339	0.6835
14	0.4575	0.5324	0.6120	0.6614
15	0.4409	0.5140	0.5923	0.6411
16	0.4259	0.4973	0.5742	0.6226
17	0.4124	0.4821	0.5577	0.6055
18	0.4000	0.4683	0.5425	0.5897
19	0.3887	0.4555	0.5285	0.5751
20	0.3783	0.4438	0.5155	0.5614
21	0.3687		0.5133 $0.5034$	0.5014 $0.5487$
$\frac{21}{22}$	0.3598	0.4329 $0.4227$	0.3034 $0.4921$	0.5368
23	0.3598 $0.3515$	0.4227 $0.4132$	0.4921 $0.4815$	0.5256
$\frac{23}{24}$	0.3438	0.4132 $0.4044$	0.4815 $0.4716$	0.5250 $0.5151$
$\frac{24}{25}$	0.3438 $0.3365$	0.4044 $0.3961$	0.4716 $0.4622$	0.5151 $0.5052$
26 27	0.3297	0.3882	0.4534	0.4958
27	0.3233	0.3809	0.4451	0.4869
28	0.3172	0.3739	0.4372	0.4785
29	0.3115	0.3673	0.4297	0.4705
30	0.3061	0.3610	0.4226	0.4629
31	0.3009	0.3550	0.4158	0.4556
32	0.2960	0.3494	0.4093	0.4487
33	0.2913	0.3440	0.4032	0.4421
34	0.2869	0.3388	0.3972	0.4357
35	0.2826	0.3338	0.3916	0.4296
36	0.2785	0.3291	0.3862	0.4238
37	0.2746	0.3246	0.3810	0.4182
38	0.2709	0.3202	0.3760	0.4128
39	0.2673	0.3160	0.3712	0.4076

Note that confidence intervals and tests for the linear correlation coefficient can also be constructed using Fisher's z-transform, which is tabulated in section 9.

38 9. Fisher's z-transform

### 9 Fisher's z-transform

#### Fisher's z-transform

The function tabulated below is Fisher's z-transform

$$z(r) \equiv \tanh^{-1}(r) = \frac{1}{2} \log \left( \frac{1+r}{1-r} \right).$$

					1	r				
r	□.□□0	□.□□1	$\Box.\Box\Box 2$	□.□□3	□.□□4	□.□□5	□.□□6	o.oo7	□.□□8	□.□□9
0.00□	0.0000	0.0010	0.0020	0.0030	0.0040	0.0050	0.0060	0.0070	0.0080	0.0090
0.01□	0.0100	0.0110	0.0120	0.0130	0.0140	0.0150	0.0160	0.0170	0.0180	0.0190
0.02□	0.0200	0.0210	0.0220	0.0230	0.0240	0.0250	0.0260	0.0270	0.0280	0.0290
0.03□	0.0300	0.0310	0.0320	0.0330	0.0340	0.0350	0.0360	0.0370	0.0380	0.0390
0.04□	0.0400	0.0410	0.0420	0.0430	0.0440	0.0450	0.0460	0.0470	0.0480	0.0490
0.05□	0.0500	0.0410 $0.0510$	0.0420 $0.0520$	0.0530	0.0541	0.0450 $0.0551$	0.0561	0.0470 $0.0571$	0.0581	0.0490 $0.0591$
0.06□	0.0601	0.0611	0.0620	0.0631	0.0641	0.0651	0.0661	0.0671	0.0681	0.0691
0.07□	0.0701	0.0711	0.0021 $0.0721$	0.0031 $0.0731$	0.0741	0.0051 $0.0751$	0.0761	0.0071 $0.0772$	0.0782	0.0091 $0.0792$
0.08□	0.0802	0.0812	0.0822	0.0832	0.0842	0.0852	0.0862	0.0872	0.0882	0.0892
0.09□	0.0902	0.0012	0.0923	0.0933	0.0943	0.0953	0.0963	0.0973	0.0983	0.0993
$0.10\Box$	0.1003	0.1013	0.1024	0.1034	0.1044	0.1054	0.1064	0.1074	0.1084	0.1094
0.11	0.1104	0.1115	0.1125	0.1135	0.1145	0.1155	0.1165	0.1175	0.1186	0.1196
$0.12\square$	0.1206	0.1216	0.1226	0.1236	0.1246	0.1257	0.1267	0.1277	0.1287	0.1297
0.13	0.1307	0.1318	0.1328	0.1338	0.1348	0.1358	0.1368	0.1379	0.1389	0.1399
0.14	0.1409	0.1419	0.1430	0.1440	0.1450	0.1460	0.1471	0.1481	0.1491	0.1501
$0.15\square$	0.1511	0.1522	0.1532	0.1542	0.1552	0.1563	0.1573	0.1583	0.1593	0.1604
$0.16\square$	0.1614	0.1624	0.1634	0.1645	0.1655	0.1665	0.1676	0.1686	0.1696	0.1706
$0.17\Box$	0.1717	0.1727	0.1737	0.1748	0.1758	0.1768	0.1779	0.1789	0.1799	0.1809
$0.18\Box$	0.1820	0.1830	0.1841	0.1851	0.1861	0.1872	0.1882	0.1892	0.1903	0.1913
0.19	0.1923	0.1934	0.1944	0.1955	0.1965	0.1975	0.1986	0.1996	0.2007	0.2017
$0.20\Box$	0.2027	0.2038	0.2048	0.2059	0.2069	0.2079	0.2090	0.2100	0.2111	0.2121
0.21	0.2132	0.2142	0.2153	0.2163	0.2174	0.2184	0.2195	0.2205	0.2216	0.2226
0.22	0.2237	0.2247	0.2258	0.2268	0.2279	0.2289	0.2300	0.2310	0.2321	0.2331
0.23	0.2342	0.2352	0.2363	0.2374	0.2384	0.2395	0.2405	0.2416	0.2427	0.2437
0.24	0.2448	0.2458	0.2469	0.2480	0.2490	0.2501	0.2512	0.2522	0.2533	0.2543
0.25	0.2554	0.2565	0.2575	0.2586	0.2597	0.2608	0.2618	0.2629	0.2640	0.2650
$0.26 \square$	0.2661	0.2672	0.2683	0.2693	0.2704	0.2715	0.2726	0.2736	0.2747	0.2758
0.27	0.2769	0.2779	0.2790	0.2801	0.2812	0.2823	0.2833	0.2844	0.2855	0.2866
$0.28 \square$	0.2877	0.2888	0.2899	0.2909	0.2920	0.2931	0.2942	0.2953	0.2964	0.2975
0.29	0.2986	0.2997	0.3008	0.3018	0.3029	0.3040	0.3051	0.3062	0.3073	0.3084
0.30□	0.3095	0.3106	0.3117	0.3128	0.3139	0.3150	0.3161	0.3172	0.3183	0.3194
0.31□	0.3205	0.3217	0.3228	0.3239	0.3250	0.3261	0.3272	0.3283	0.3294	0.3305
0.32□	0.3316	0.3328	0.3339	0.3350	0.3361	0.3372	0.3383	0.3395	0.3406	0.3417
0.33□	0.3428	0.3440	0.3451	0.3462	0.3473	0.3484	0.3496	0.3507	0.3518	0.3530
0.34	0.3541	0.3552	0.3564	0.3575	0.3586	0.3598	0.3609	0.3620	0.3632	0.3643
$0.35\square$	0.3654	0.3666	0.3677	0.3689	0.3700	0.3712	0.3723	0.3734	0.3746	0.3757
0.36□	0.3769	0.3780	0.3792	0.3803	0.3815	0.3826	0.3838	0.3850	0.3861	0.3873
0.37	0.3884	0.3896	0.3907	0.3919	0.3931	0.3942	0.3954	0.3966	0.3977	0.3989
$0.38\square$	0.4001	0.4012	0.4024	0.4036	0.4047	0.4059	0.4071	0.4083	0.4094	0.4106
0.39	0.4118	0.4130	0.4142	0.4153	0.4165	0.4177	0.4189	0.4201	0.4213	0.4225
0.40□	0.4236	0.4248	0.4260	0.4272	0.4284	0.4296	0.4308	0.4320	0.4332	0.4344
0.40□	0.4250 $0.4356$	0.4248 $0.4368$	0.4200 $0.4380$	0.4212 $0.4392$	0.4204 $0.4404$	0.4250 $0.4416$	0.4308 $0.4428$	0.4320 $0.4441$	0.4352 $0.4453$	0.4344 $0.4465$
$0.41$ $\square$	0.4350 $0.4477$	0.4308 $0.4489$	0.4500 $0.4501$	0.4592 $0.4513$	0.4404 $0.4526$	0.4416 $0.4538$	0.4428 $0.4550$	0.4441 $0.4562$	0.4455 $0.4574$	0.4465 $0.4587$
0.42□	0.4477 $0.4599$	0.4469 $0.4611$	0.4501 $0.4624$	0.4513 $0.4636$	0.4520 $0.4648$	0.4558 $0.4660$	0.4673	0.4502 $0.4685$	0.4574 $0.4698$	0.4567 $0.4710$
0.43□	0.4399 $0.4722$	0.4011 $0.4735$	0.4024 $0.4747$	0.4030 $0.4760$	0.4048 $0.4772$	0.4000 $0.4784$	0.4073 $0.4797$	0.4809	0.4098 $0.4822$	0.4710 $0.4834$
0.44	0.4722 $0.4847$	0.4755 $0.4860$	0.4747 $0.4872$	0.4760 $0.4885$	0.4772 $0.4897$	0.4784 $0.4910$	0.4797 $0.4922$	0.4809 $0.4935$	0.4822 $0.4948$	0.4854 $0.4960$
0.45□	0.4847 $0.4973$	0.4860 $0.4986$	0.4872 $0.4999$	0.4865 $0.5011$	0.4897 $0.5024$	0.4910 $0.5037$	0.4922 $0.5049$	0.4955 $0.5062$	0.4948 $0.5075$	0.4900 $0.5088$
0.46⊔ 0.47□	0.4973 $0.5101$	0.4986 $0.5114$	0.4999 $0.5126$	0.5011 $0.5139$	0.5024 $0.5152$	0.5037 $0.5165$	0.5049 $0.5178$	0.5062 $0.5191$	0.5075 $0.5204$	0.5088 $0.5217$
0.47□	0.5101 $0.5230$	0.5114 $0.5243$	0.5126 $0.5256$	0.5159 $0.5269$	0.5152 $0.5282$	0.5105 $0.5295$	0.5178 $0.5308$	0.5191 $0.5321$	0.5204 $0.5334$	0.5217 $0.5347$
0.48□	0.5250 $0.5361$	0.5245 $0.5374$	0.5250 $0.5387$	0.5209 $0.5400$	0.5282 $0.5413$	0.5427	0.5308 $0.5440$	0.5321 $0.5453$	0.5354 $0.5466$	0.5347 $0.5480$
0.4∂⊔	0.0001	0.0014	0.0001	0.0400	0.0410	0.0441	0.0440	0.0400	0.0400	0.0400

9. Fisher's z-transform

r	$\Box.\Box\Box 0$	$\Box.\Box\Box 1$	$\square.\square\square 2$	$\square.\square\square 3$	$\Box.\Box\Box 4$	$\Box.\Box\Box 5$	$\Box.\Box\Box 6$	$\Box.\Box\Box7$	$\Box.\Box\Box 8$	$\Box.\Box\Box 9$
0.50□	0.5493	0.5506	0.5520	0.5533	0.5547	0.5560	0.5573	0.5587	0.5600	0.5614
0.51	0.5627	0.5641	0.5654	0.5668	0.5682	0.5695	0.5709	0.5722	0.5736	0.5750
$0.52\Box$	0.5763	0.5777	0.5791	0.5805	0.5818	0.5832	0.5846	0.5860	0.5874	0.5888
0.53	0.5901	0.5915	0.5929	0.5943	0.5957	0.5971	0.5985	0.5999	0.6013	0.6027
$0.54\square$	0.6042	0.6056	0.6070	0.6084	0.6098	0.6112	0.6127	0.6141	0.6155	0.6169
$0.55\square$	0.6184	0.6198	0.6213	0.6227	0.6241	0.6256	0.6270	0.6285	0.6299	0.6314
$0.56 \square$	0.6328	0.6343	0.6358	0.6372	0.6387	0.6401	0.6416	0.6431	0.6446	0.6460
$0.57\Box$	0.6475	0.6490	0.6505	0.6520	0.6535	0.6550	0.6565	0.6580	0.6595	0.6610
$0.58\square$	0.6625	0.6640	0.6655	0.6670	0.6685	0.6700	0.6716	0.6731	0.6746	0.6761
$0.59 \square$	0.6777	0.6792	0.6807	0.6823	0.6838	0.6854	0.6869	0.6885	0.6900	0.6916
$0.60\Box$	0.6931	0.6947	0.6963	0.6978	0.6994	0.7010	0.7026	0.7042	0.7057	0.7073
0.61	0.7089	0.7105	0.7121	0.7137	0.7153	0.7169	0.7185	0.7201	0.7218	0.7234
0.62	0.7250	0.7266	0.7283	0.7299	0.7315	0.7332	0.7348	0.7365	0.7381	0.7398
0.63	0.7414	0.7431	0.7447	0.7464	0.7481	0.7498	0.7514	0.7531	0.7548	0.7565
0.64	0.7582	0.7599	0.7616	0.7633	0.7650	0.7667	0.7684	0.7701	0.7718	0.7736
$0.65 \square$	0.7753	0.7770	0.7788	0.7805	0.7823	0.7840	0.7858	0.7875	0.7893	0.7910
$0.66 \square$	0.7928	0.7946	0.7964	0.7981	0.7999	0.8017	0.8035	0.8053	0.8071	0.8089
$0.67 \square$	0.8107	0.8126	0.8144	0.8162	0.8180	0.8199	0.8217	0.8236	0.8254	0.8273
$0.68 \square$	0.8291	0.8310	0.8328	0.8347	0.8366	0.8385	0.8404	0.8423	0.8441	0.8460
0.69	0.8480	0.8499	0.8518	0.8537	0.8556	0.8576	0.8595	0.8614	0.8634	0.8653
$0.70\Box$	0.8673	0.8693	0.8712	0.8732	0.8752	0.8772	0.8792	0.8812	0.8832	0.8852
0.71	0.8872	0.8892	0.8912	0.8933	0.8953	0.8973	0.8994	0.9014	0.9035	0.9056
0.72	0.9076	0.9097	0.9118	0.9139	0.9160	0.9181	0.9202	0.9223	0.9245	0.9266
0.73	0.9287	0.9309	0.9330	0.9352	0.9373	0.9395	0.9417	0.9439	0.9461	0.9483
0.74	0.9505	0.9527	0.9549	0.9571	0.9594	0.9616	0.9639	0.9661	0.9684	0.9707
0.75	0.9730	0.9752	0.9775	0.9798	0.9822	0.9845	0.9868	0.9892	0.9915	0.9939
$0.76 \square$	0.9962	0.9986	1.0010	1.0034	1.0058	1.0082	1.0106	1.0130	1.0154	1.0179
$0.77\Box$	1.0203	1.0228	1.0253	1.0277	1.0302	1.0327	1.0352	1.0378	1.0403	1.0428
$0.78\square$	1.0454	1.0479	1.0505	1.0531	1.0557	1.0583	1.0609	1.0635	1.0661	1.0688
0.79	1.0714	1.0741	1.0768	1.0795	1.0822	1.0849	1.0876	1.0903	1.0931	1.0958
$0.80\Box$	1.0986	1.1014	1.1042	1.1070	1.1098	1.1127	1.1155	1.1184	1.1212	1.1241
$0.81 \Box$	1.1270	1.1299	1.1329	1.1358	1.1388	1.1417	1.1447	1.1477	1.1507	1.1538
0.82	1.1568	1.1599	1.1630	1.1660	1.1692	1.1723	1.1754	1.1786	1.1817	1.1849
0.83	1.1881	1.1914	1.1946	1.1979	1.2011	1.2044	1.2077	1.2111	1.2144	1.2178
$0.84\square$	1.2212	1.2246	1.2280	1.2315	1.2349	1.2384	1.2419	1.2454	1.2490	1.2526
$0.85\square$	1.2562	1.2598	1.2634	1.2671	1.2707	1.2745	1.2782	1.2819	1.2857	1.2895
$0.86 \square$	1.2933	1.2972	1.3011	1.3050	1.3089	1.3129	1.3169	1.3209	1.3249	1.3290
0.87	1.3331	1.3372	1.3414	1.3456	1.3498	1.3540	1.3583	1.3626	1.3670	1.3714
$0.88\square$	1.3758	1.3802	1.3847	1.3892	1.3938	1.3984	1.4030	1.4077	1.4124	1.4171
0.89	1.4219	1.4268	1.4316	1.4365	1.4415	1.4465	1.4516	1.4566	1.4618	1.4670
$0.90\Box$	1.4722	1.4775	1.4828	1.4882	1.4937	1.4992	1.5047	1.5103	1.5160	1.5217
0.91	1.5275	1.5334	1.5393	1.5453	1.5513	1.5574	1.5636	1.5698	1.5762	1.5826
0.92	1.5890	1.5956	1.6022	1.6089	1.6157	1.6226	1.6296	1.6366	1.6438	1.6510
0.93	1.6584	1.6658	1.6734	1.6811	1.6888	1.6967	1.7047	1.7129	1.7211	1.7295
0.94	1.7380	1.7467	1.7555	1.7645	1.7736	1.7828	1.7923	1.8019	1.8117	1.8216
0.95	1.8318	1.8421	1.8527	1.8635	1.8745	1.8857	1.8972	1.9090	1.9210	1.9333
0.96□	1.9459	1.9588	1.9721	1.9857	1.9996	2.0139	2.0287	2.0439	2.0595	2.0756
0.97	2.0923	2.1095	2.1273	2.1457	2.1649	2.1847	2.2054	2.2269	2.2494	2.2729
0.98□	2.2976	2.3235	2.3507	2.3796	2.4101	2.4427	2.4774	2.5147	2.5550	2.5987
0.99□	2.6467	2.6996	2.7587	2.8257	2.9031	2.9945	3.1063	3.2504	3.4534	3.8002

40 Inverse z-transform 9. Fisher's z-transform

#### **Inverse z-transform**

The function tabulated below is the inverse of Fisher's z-transform

$$r(z) \equiv \tanh(z) = \frac{e^{2z} - 1}{e^{2z} + 1} = \frac{e^z - e^{-z}}{e^z + e^{-z}} = \frac{\sinh(z)}{\cosh(z)}.$$

	$oldsymbol{z}$									
z	$\Box.\Box 0$	□.□1	$\Box.\Box2$	□.□3	$\Box.\Box 4$	$\Box.\Box5$	□.□6	□.□7	□.□8	□.□9
0.0	0.0000	0.0100	0.0200	0.0300	0.0400	0.0500	0.0599	0.0699	0.0798	0.0898
$0.1\Box$	0.0997	0.1096	0.1194	0.1293	0.1391	0.1489	0.1586	0.1684	0.1781	0.1877
$0.2\Box$	0.1974	0.2070	0.2165	0.2260	0.2355	0.2449	0.2543	0.2636	0.2729	0.2821
$0.3\Box$	0.2913	0.3004	0.3095	0.3185	0.3275	0.3364	0.3452	0.3540	0.3627	0.3714
$0.4\Box$	0.3799	0.3885	0.3969	0.4053	0.4136	0.4219	0.4301	0.4382	0.4462	0.4542
$0.5\square$	0.4621	0.4699	0.4777	0.4854	0.4930	0.5005	0.5080	0.5154	0.5227	0.5299
$0.6\Box$	0.5370	0.5441	0.5511	0.5581	0.5649	0.5717	0.5784	0.5850	0.5915	0.5980
$0.7\Box$	0.6044	0.6107	0.6169	0.6231	0.6291	0.6351	0.6411	0.6469	0.6527	0.6584
$0.8\Box$	0.6640	0.6696	0.6751	0.6805	0.6858	0.6911	0.6963	0.7014	0.7064	0.7114
$0.9\Box$	0.7163	0.7211	0.7259	0.7306	0.7352	0.7398	0.7443	0.7487	0.7531	0.7574
$1.0\Box$	0.7616	0.7658	0.7699	0.7739	0.7779	0.7818	0.7857	0.7895	0.7932	0.7969
$1.1\Box$	0.8005	0.8041	0.8076	0.8110	0.8144	0.8178	0.8210	0.8243	0.8275	0.8306
$1.2\Box$	0.8337	0.8367	0.8397	0.8426	0.8455	0.8483	0.8511	0.8538	0.8565	0.8591
$1.3\Box$	0.8617	0.8643	0.8668	0.8692	0.8717	0.8741	0.8764	0.8787	0.8810	0.8832
$1.4\Box$	0.8854	0.8875	0.8896	0.8917	0.8937	0.8957	0.8977	0.8996	0.9015	0.9033
$1.5\Box$	0.9051	0.9069	0.9087	0.9104	0.9121	0.9138	0.9154	0.9170	0.9186	0.9201
$1.6\Box$	0.9217	0.9232	0.9246	0.9261	0.9275	0.9289	0.9302	0.9316	0.9329	0.9341
$1.7\Box$	0.9354	0.9366	0.9379	0.9391	0.9402	0.9414	0.9425	0.9436	0.9447	0.9458
$1.8\Box$	0.9468	0.9478	0.9488	0.9498	0.9508	0.9517	0.9527	0.9536	0.9545	0.9554
$1.9\Box$	0.9562	0.9571	0.9579	0.9587	0.9595	0.9603	0.9611	0.9618	0.9626	0.9633
$2.0\Box$	0.9640	0.9647	0.9654	0.9661	0.9667	0.9674	0.9680	0.9687	0.9693	0.9699
$2.1\Box$	0.9705	0.9710	0.9716	0.9721	0.9727	0.9732	0.9737	0.9743	0.9748	0.9753
$2.2\Box$	0.9757	0.9762	0.9767	0.9771	0.9776	0.9780	0.9785	0.9789	0.9793	0.9797
$2.3\Box$	0.9801	0.9805	0.9809	0.9812	0.9816	0.9820	0.9823	0.9827	0.9830	0.9833
$2.4\Box$	0.9837	0.9840	0.9843	0.9846	0.9849	0.9852	0.9855	0.9858	0.9861	0.9863
$2.5\square$	0.9866	0.9869	0.9871	0.9874	0.9876	0.9879	0.9881	0.9884	0.9886	0.9888
$2.6\Box$	0.9890	0.9892	0.9895	0.9897	0.9899	0.9901	0.9903	0.9905	0.9906	0.9908
$2.7\Box$	0.9910	0.9912	0.9914	0.9915	0.9917	0.9919	0.9920	0.9922	0.9923	0.9925
$2.8\Box$	0.9926	0.9928	0.9929	0.9931	0.9932	0.9933	0.9935	0.9936	0.9937	0.9938
$2.9\Box$	0.9940	0.9941	0.9942	0.9943	0.9944	0.9945	0.9946	0.9947	0.9949	0.9950
$3.0\Box$	0.9951	0.9952	0.9952	0.9953	0.9954	0.9955	0.9956	0.9957	0.9958	0.9959
3.1	0.9959	0.9960	0.9961	0.9962	0.9963	0.9963	0.9964	0.9965	0.9965	0.9966
$3.2\Box$	0.9967	0.9967	0.9968	0.9969	0.9969	0.9970	0.9971	0.9971	0.9972	0.9972
$3.3\Box$	0.9973	0.9973	0.9974	0.9974	0.9975	0.9975	0.9976	0.9976	0.9977	0.9977
$3.4\Box$	0.9978	0.9978	0.9979	0.9979	0.9979	0.9980	0.9980	0.9981	0.9981	0.9981
$3.5\Box$	0.9982	0.9982	0.9982	0.9983	0.9983	0.9984	0.9984	0.9984	0.9984	0.9985
$3.6\Box$	0.9985	0.9985	0.9986	0.9986	0.9986	0.9986	0.9987	0.9987	0.9987	0.9988
$3.7\Box$	0.9988	0.9988	0.9988	0.9988	0.9989	0.9989	0.9989	0.9989	0.9990	0.9990
$3.8\Box$	0.9990	0.9990	0.9990	0.9991	0.9991	0.9991	0.9991	0.9991	0.9991	0.9992
$3.9\Box$	0.9992	0.9992	0.9992	0.9992	0.9992	0.9993	0.9993	0.9993	0.9993	0.9993

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