# Exercises for MI

### Exercise sheet 6

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When you have finished with the exercises, you should continue with the exam sheet from the previous years, which can be found at the course's home page.

#### Exercise 1\*

For the Bayesian network on slide 6.16:

- define (somewhat) reasonable conditional probability tables for the five nodes of the network (use only probability values 0,0.1,0.2,...,0.9,1 in order to facilitate the subsequent computations)
- perform the variable elimination computations of slide 6.17 to determine the conditional probability  $P(MC \mid B = t)$  according to the numbers you specified.

Exercise 2\* Complete Exercise 8.10 in PM.

**Exercise 3** Consider the network defined by the two binary variables A and B, where A is the parent of B. Assume that the conditional probability tables are given as P(A) = (0.1, 0.9) and

$$\begin{array}{c|cc} & A \\ & a_1 & a_2 \\ \hline b_1 & 0.05 & 0.2 \\ b_2 & 0.95 & 0.8 \\ \end{array}$$

- Assume that you want to estimate  $P(b_1)$  using sampling. How many samples would be required if you only accept an error larger than 0.15 in 10% of the cases?
- Implement the network above in Hugin and use Hugin to sample the number of cases that you have just calculated; use the function 'Simulate cases' under 'File'.
- Use the sampled cases to estimate  $P(b_1)$  and compare the result with Hugin. Feel free to use a spreadsheet for the counting.

**Exercise 4**\* Consider again the network in the exercise above, and assume that you want to use rejection sampling to estimate  $P(A|B=b_1)$ . How many samples do you expect you would have to generate in order to end up (after rejection) with a sample set of 1000 cases for estimating the probability.

# Exercise 5

Complete Exercise 8.6(a-b) in PM.

### Exercise 6

Continue with the exercises from last time.