

# §13.5 卡诺过程

地热发电厂



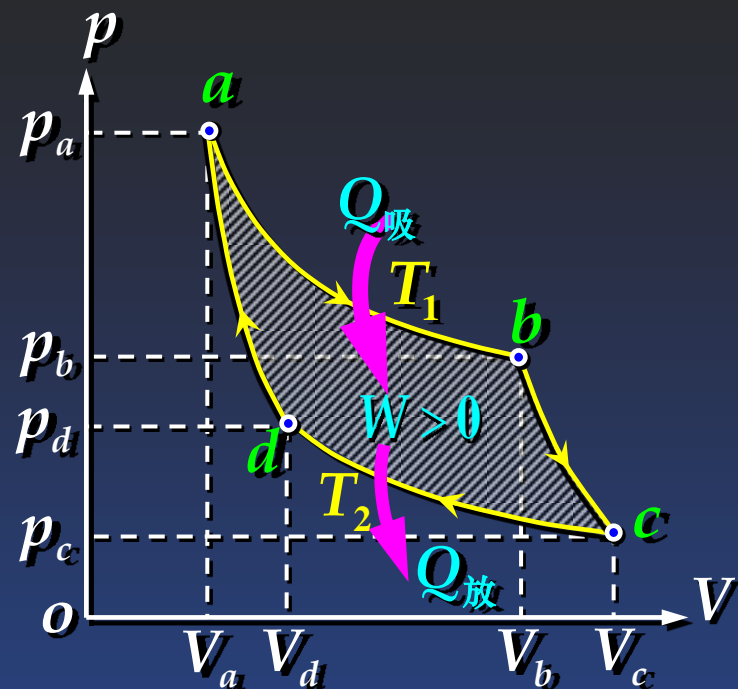
# 一、卡诺正循环

$a \rightarrow b$ : 等温膨胀 ( $T_1$ )

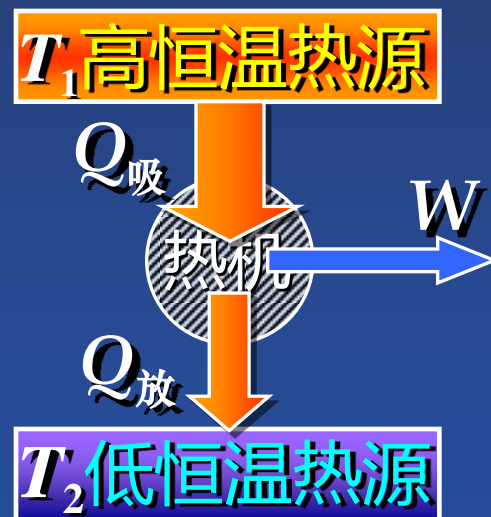
$b \rightarrow c$ : 绝热膨胀

$c \rightarrow d$ : 等温压缩 ( $T_2$ )

$d \rightarrow a$ : 绝热压缩

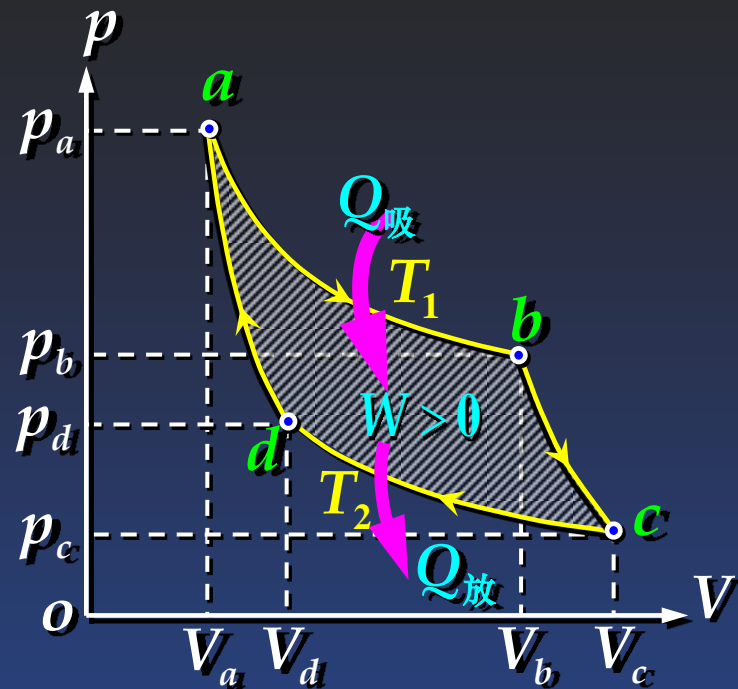


$$\left. \begin{aligned} Q_{\text{吸}} &= \nu RT_1 \ln \frac{V_b}{V_a} \\ Q_{\text{放}} &= \nu RT_2 \ln \frac{V_d}{V_c} \end{aligned} \right\} \eta_{\text{卡诺}} = 1 - \frac{|Q_{\text{放}}|}{Q_{\text{吸}}}$$



$$\eta_{\text{卡诺}} = 1 - \frac{T_2}{T_1} \frac{\ln(V_c/V_d)}{\ln(V_b/V_a)}$$

$$\left. \begin{aligned} T_1 V_b^{\gamma-1} &= T_2 V_c^{\gamma-1} \\ T_1 V_a^{\gamma-1} &= T_2 V_d^{\gamma-1} \end{aligned} \right\} \frac{V_b}{V_a} = \frac{V_c}{V_d}$$



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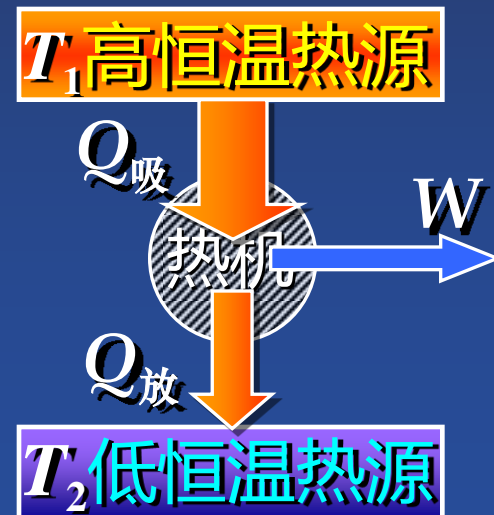
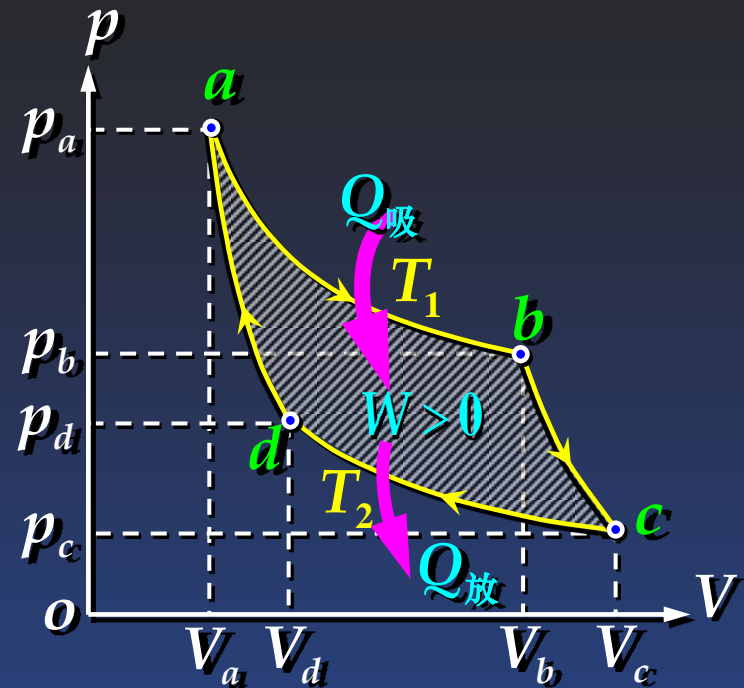
$$\eta_{\text{卡诺}} = 1 - \frac{T_2}{T_1} \frac{\ln(V_c/V_d)}{\ln(V_b/V_a)}$$

$$\left. \begin{aligned} T_1 V_b^{\gamma-1} &= T_2 V_c^{\gamma-1} \\ T_1 V_a^{\gamma-1} &= T_2 V_d^{\gamma-1} \end{aligned} \right\} \frac{V_b}{V_a} = \frac{V_c}{V_d}$$

$$\longrightarrow \eta_{\text{卡诺}} = 1 - \frac{T_2}{T_1}$$

注意

☺ 卡诺热机效率只与高、低温热源的温度有关，与工质无关！



## 二、卡诺逆循环

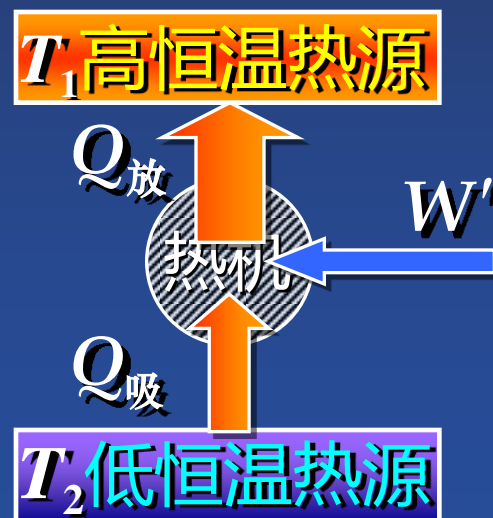
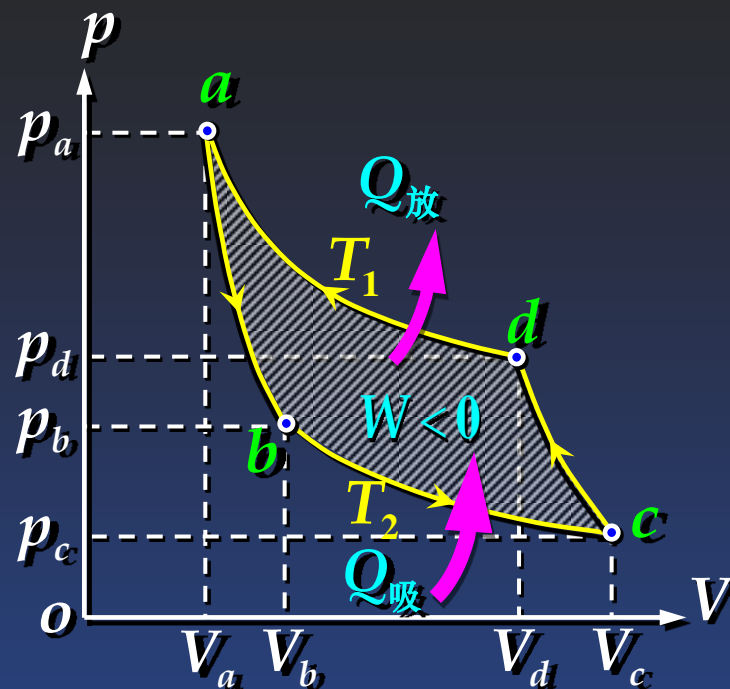
$$w_{\text{卡诺}} = \frac{Q_{\text{吸}}}{W'} = \frac{T_2}{T_1 - T_2}$$

**例** 保持冰箱内温度为  $-3^{\circ}\text{C}$ ，  
则由于：

$$T_2 = 273 - 3 = 270(\text{K})$$

$$T_1 = 273 + 27 = 300(\text{K})$$

$$w_{\text{卡诺}} = \frac{T_2}{T_1 - T_2} = 9$$

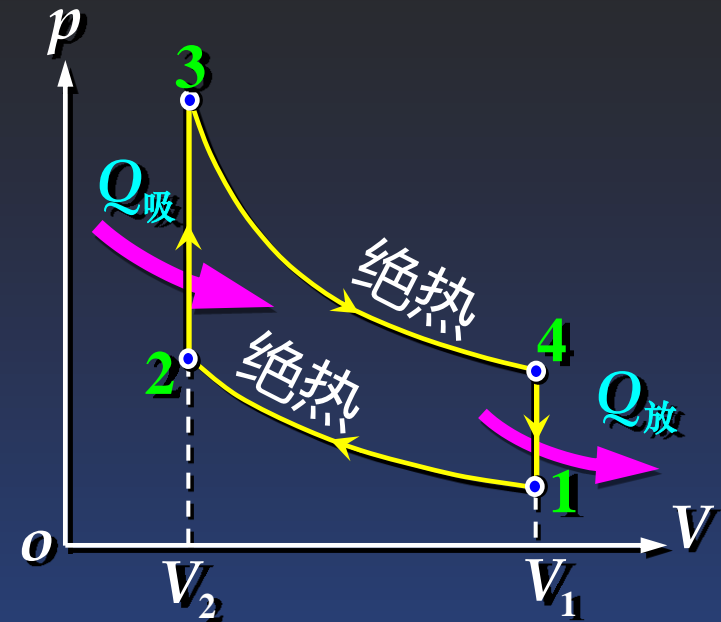


### 三、其他循环

☺ 奥托循环 (Otto cycle):

$$\eta_{\text{otto}} = 1 - q^{1-\gamma}$$

$q = V_1/V_2$ : 绝热压缩比



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$$T_1 = 273 + 27 = 300(\text{K})$$

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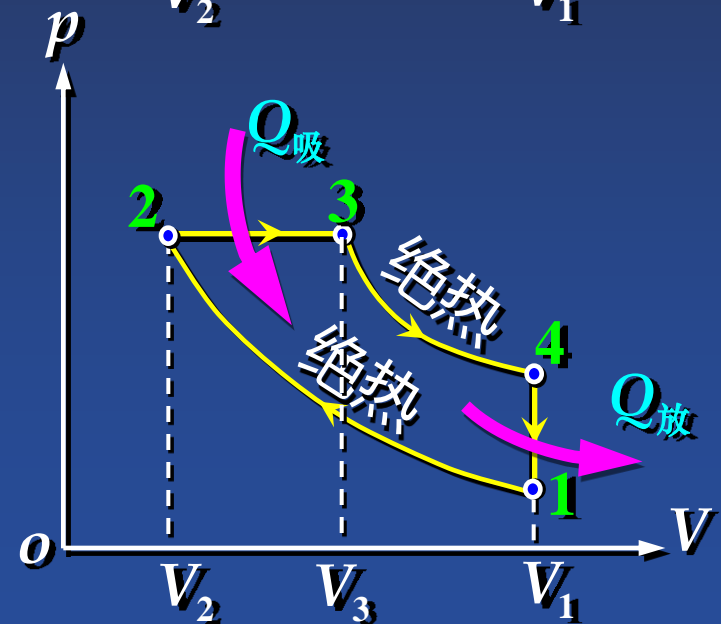
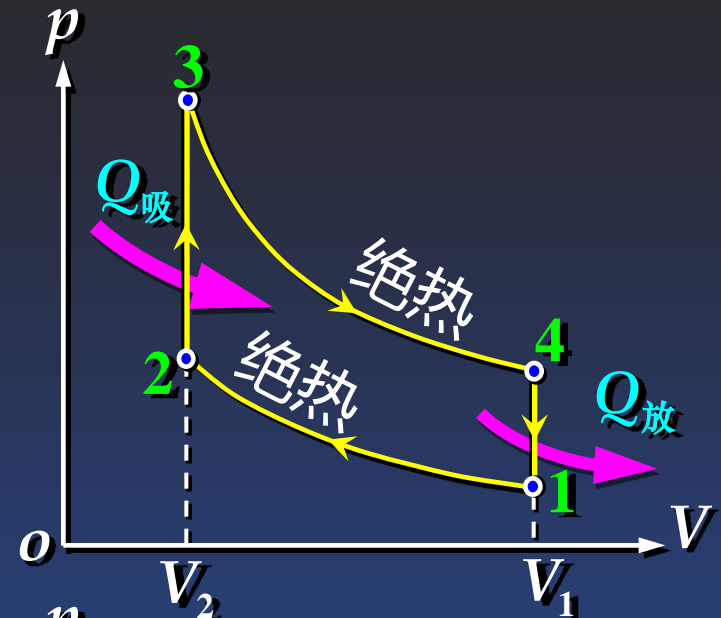
$$\eta_{otto} = 1 - q^{1-\gamma}$$

$q = V_1/V_2$ : 绝热压缩比

☺ 狄塞尔循环 (Diesel cycle):

$$\eta_{diesel} = 1 - \frac{1}{\gamma} q^{1-\gamma} \cdot \frac{\beta^{\gamma} - 1}{\beta - 1}$$

$\beta = V_3/V_2$ : 定压膨胀比



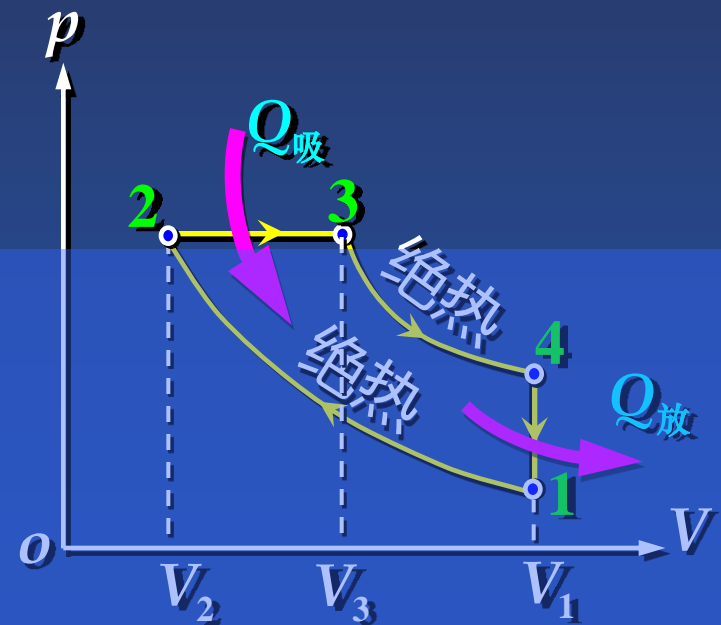
归纳:

$$\text{☺} \quad \eta_{\text{卡诺}} = 1 - \frac{|Q_{\text{放}}|}{Q_{\text{吸}}} = 1 - \frac{T_2}{T_1}$$

$$\text{☺} \quad w_{\text{卡诺}} = \frac{T_2}{T_1 - T_2}$$

$$\eta_{\text{diesel}} = 1 - \frac{1}{\gamma} q^{1-\gamma} \cdot \frac{\beta^\gamma - 1}{\beta - 1}$$

$\beta = V_3/V_2$ : 定压膨胀比





归纳:

☺  $\eta_{\text{卡诺}} = 1 - \frac{|Q_{\text{放}}|}{Q_{\text{吸}}} = 1 - \frac{T_2}{T_1}$

☺  $w_{\text{卡诺}} = \frac{T_2}{T_1 - T_2}$

☺  $\eta \leq \eta_{\text{卡诺}} = 1 - T_2 / T_1$

(The end)