CS4215 Project Report

Team Estepona - Abstract Abstract Machines

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1 Abstract

We implemented an abstract interpreter for a subset of source. By approximating program states, our abstract interpreter always terminates and can be used to analyse program behaviour and allow for code optimisation. Our interpreter also allows for visualisation of the abstract state-space for analysis.

2 Introduction

The objective of static program analysis is to determine the behaviour of a program without running it. This includes determining whether the program terminates, whether optimisations can be applied, and what states are reachable during program execution.

This is a difficult problem. The halting problem for example is undecidable. Data-flow analysis is also difficult to perform on languages such as Source which support higher-order functions.

A key difficulty is that a virtual machine executing a program might require an infinite number of states for a non-terminating program. However, by following the abstracting abstract machines approach [1], we are able to convert a concrete virtual machine into a non-deterministic abstract machine with finite states, with each abstract state representing multiple possible concrete states. As a result, we are able to soundly approximate program behaviour in finite time.

For example, if the concrete machine transitions from state A to state B, then the abstract machine must transition from some abstract state A' to some abstract state B', where A' and B' are the abstract states representing A and B. If the abstract machine always terminates, then so must the concrete machine.

We applied this approach to convert the Source virtual machine into an abstract interpreter which supports higher-order functions and conditionals. The interpreter provably terminates, returning a graph of abstract states reached that can be visualised by the user and potentially used to derive complier optimisations.

3 Implementation

Our abstract interpreter runs on the Source virtual machine code produced by the Source complier. We derived it from the original Source virtual machine by applying the technique of abstracting abstract machines [1]. Each state of our abstract interpreter is of the form:

Similar to the original Source virtual machine, PC is a number representing the program counter and OS is the operand stack itself, storing integers, booleans and closures. ENV maps the names of function parameters and local variables to addresses. Note that these names in practice are actually integers. STORE maps addresses to values. KONT is the address of the continuation. A continuation is similar to a stack frame and it stores the previous PC, OS, ENV, KONT, TIME and C. TIME is a string representing the current call stack. It is the concatenation of the locations of the CALL instructions in the call stack and is used to allocate new addresses. C is an incrementing counter that is used alongside TIME to allocate new addresses.

References

[1] David Van Horn and Matthew Might. Abstracting abstract machines. In Proceedings of the 15th ACM SIGPLAN international conference on $Functional\ programming,\ pages\ 51–62,\ 2010.$