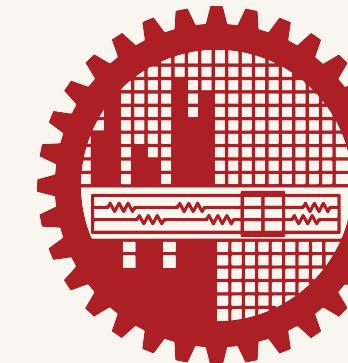

Reinforcement Learning in Age of Large Scale Foundation Models

Invited Lecturer :
Zarif Ikram



NUS
National University
of Singapore

Lecture 6

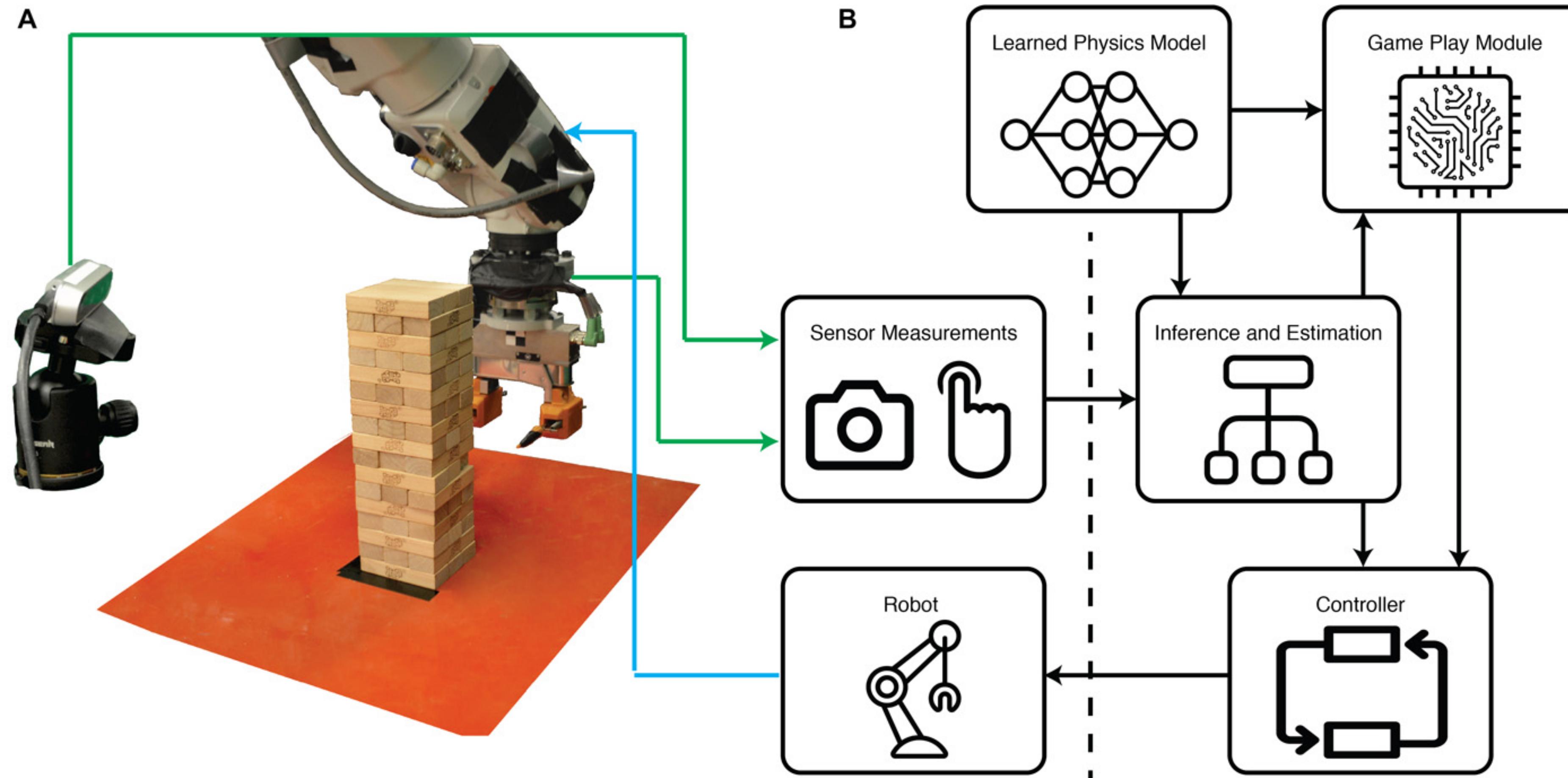
How to Train Your
World Models

Introduction

Why World Models?

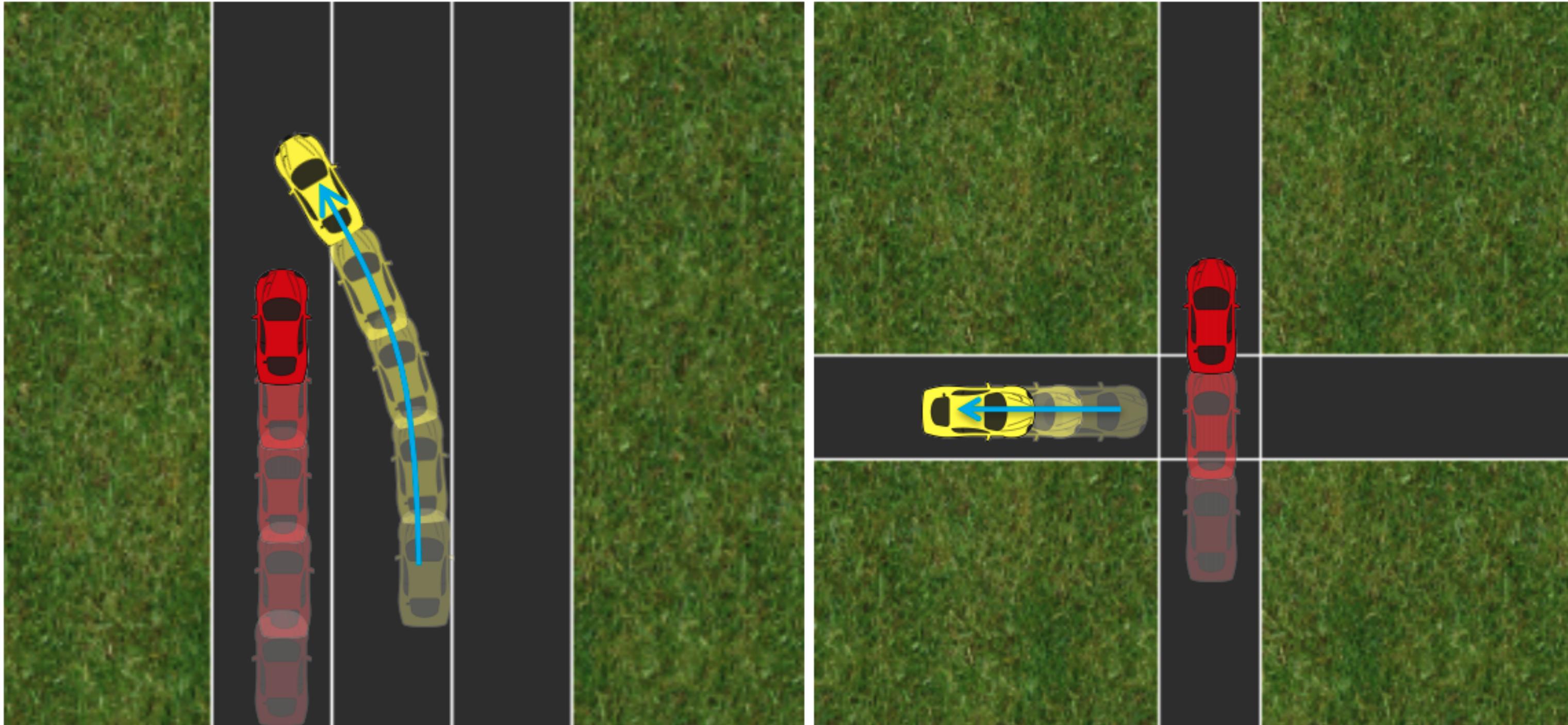
- ❖ Model Predictive Control (MPC)
- ❖ Model Based Reinforcement Learning (MBRL)
- ❖ Model Based Reasoning

Model-based reasoning for robotic control



Fazeli et al. (2019). See, feel, act: Hierarchical learning for complex manipulation skills with multisensory fusion. *Science Robotics*, 4(26).

Model-based reasoning for human-AI interaction

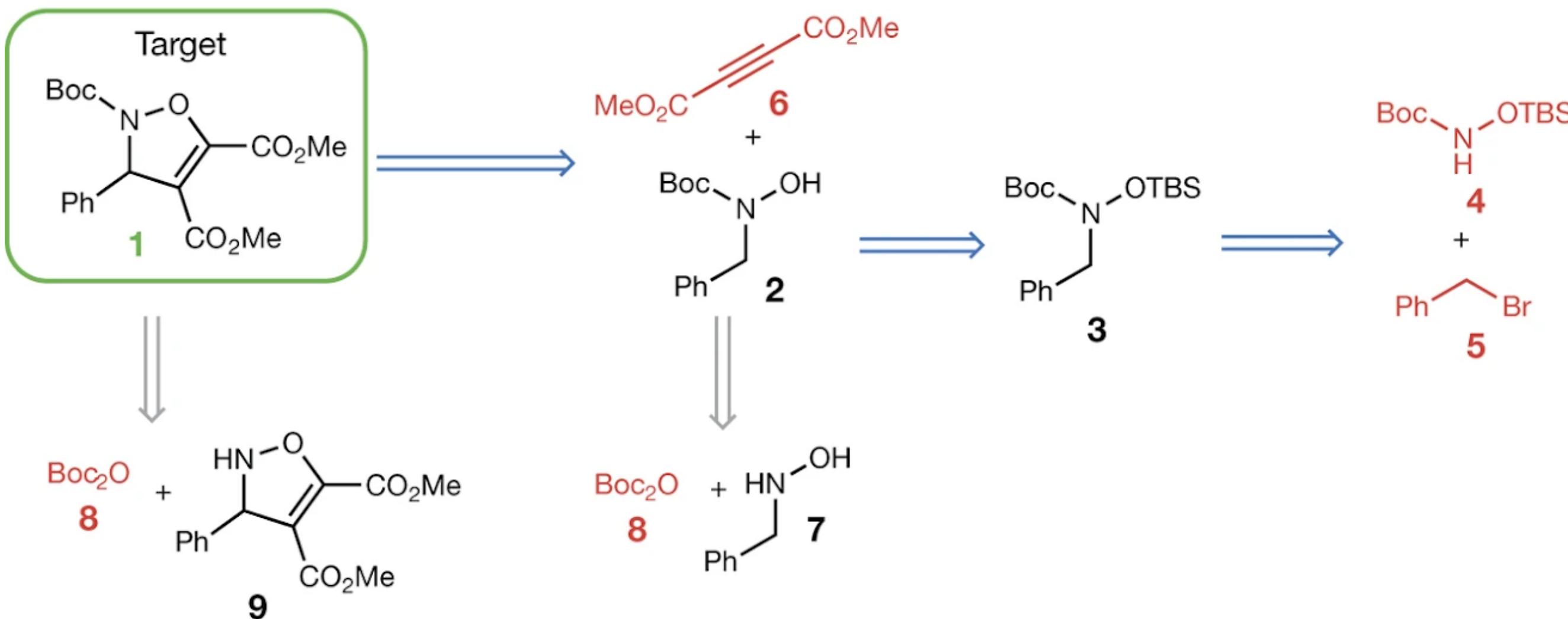


(a) Car merges *ahead* of human;
anticipates human *braking*

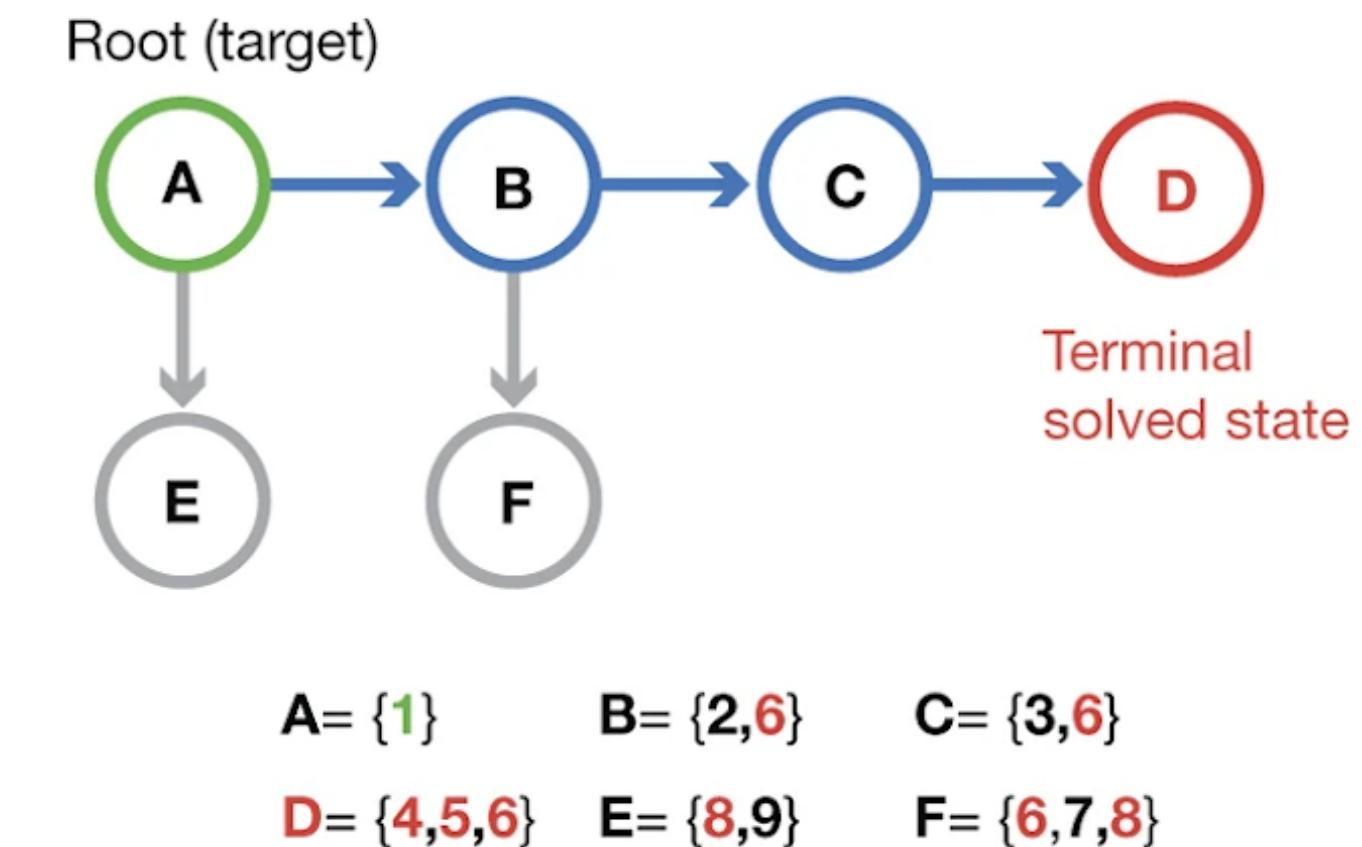
(b) Car *backs up* at 4way stop;
anticipates human *proceeding*

Model-based reasoning for science

a Chemical representation of the synthesis plan

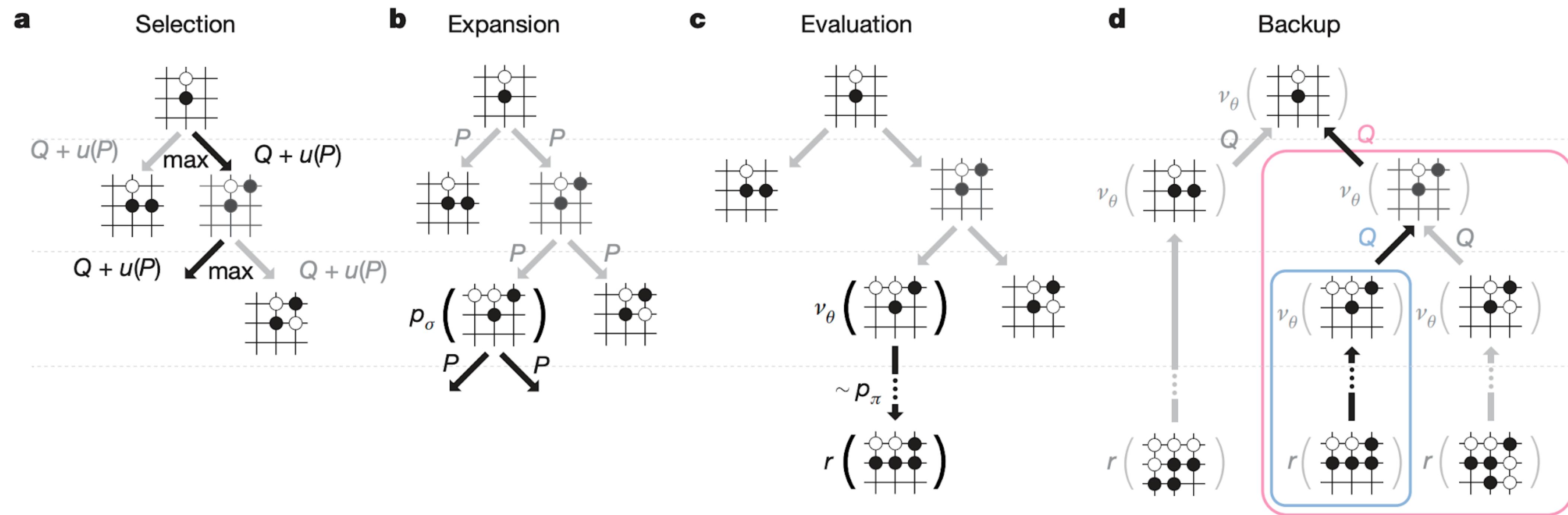


b Search tree representation



Segler, Preuss, & Waller (2018). Planning chemical syntheses with deep neural networks and symbolic AI. *Nature*, 555(7698).

Model-based reasoning for games



Silver et al. (2016). Mastering the game of Go with deep neural networks and tree search. Nature, 529(7587), 484.

Model, View, Controller

At each time step, our agent receives an **observation** from the environment.

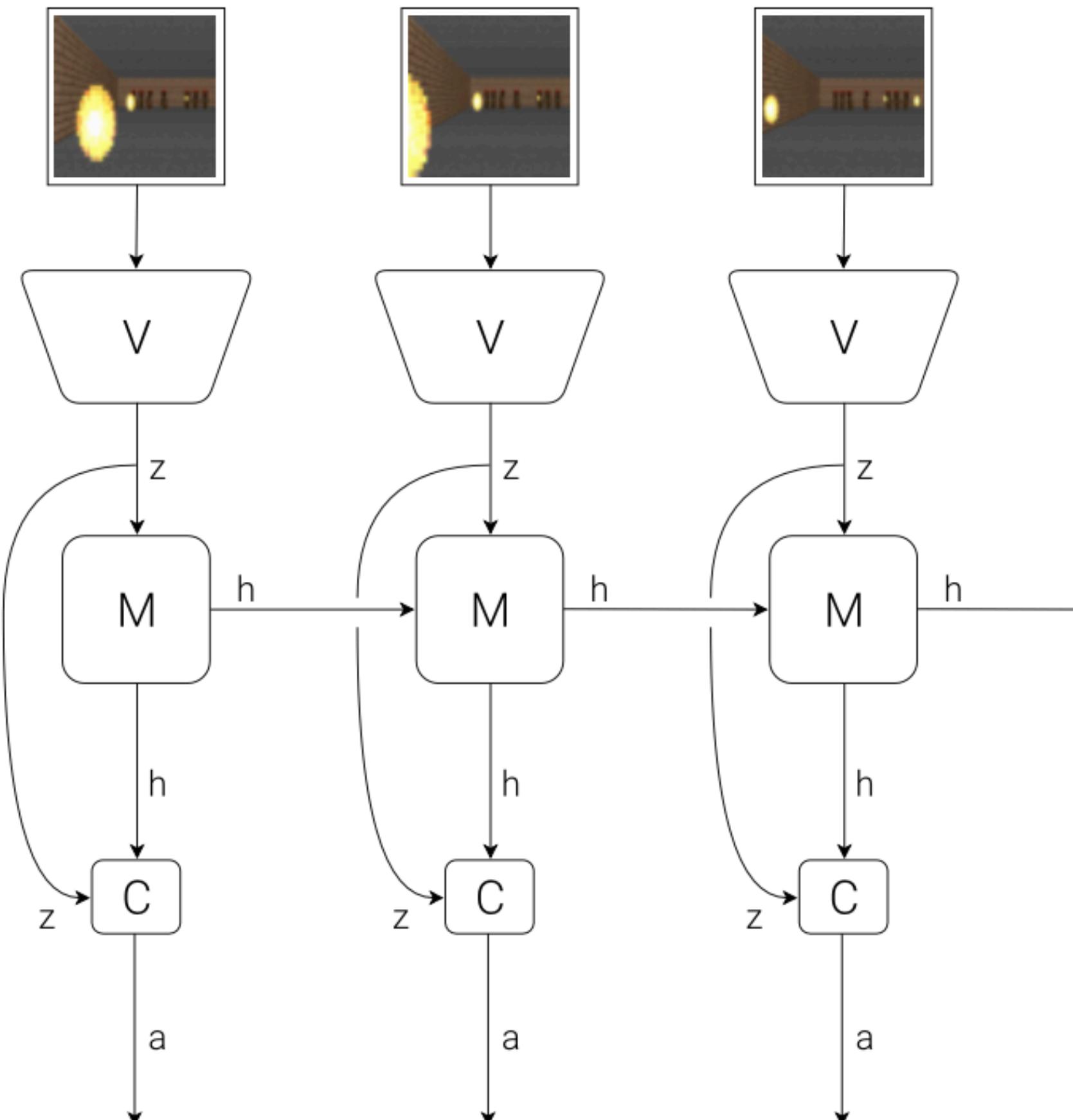
World Model

The **Vision Model (V)** encodes the high-dimensional observation into a low-dimensional latent vector.

The **Memory RNN (M)** integrates the historical codes to create a representation that can predict future states.

A small **Controller (C)** uses the representations from both **V** and **M** to select good actions.

The agent performs **actions** that go back and affect the environment.



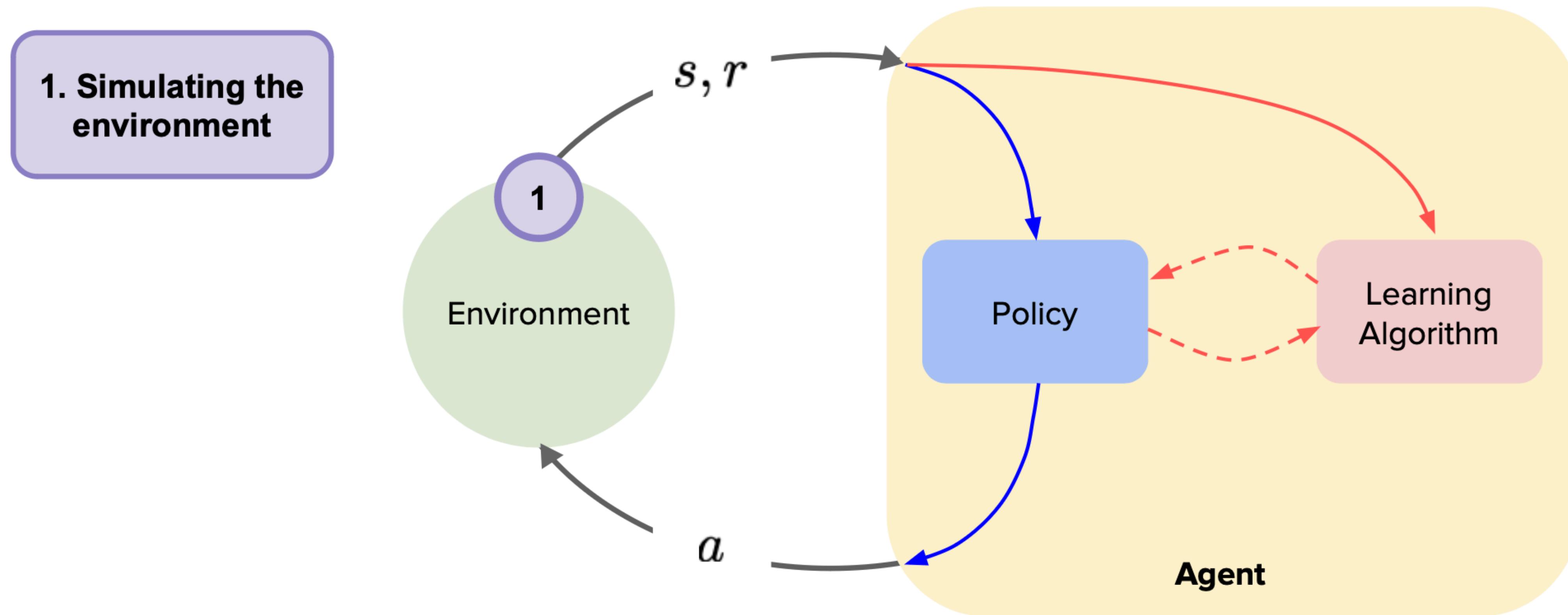
What is a model?

- ❖ Definition: a model is a representation that explicitly encodes knowledge about the structure of the environment and task.

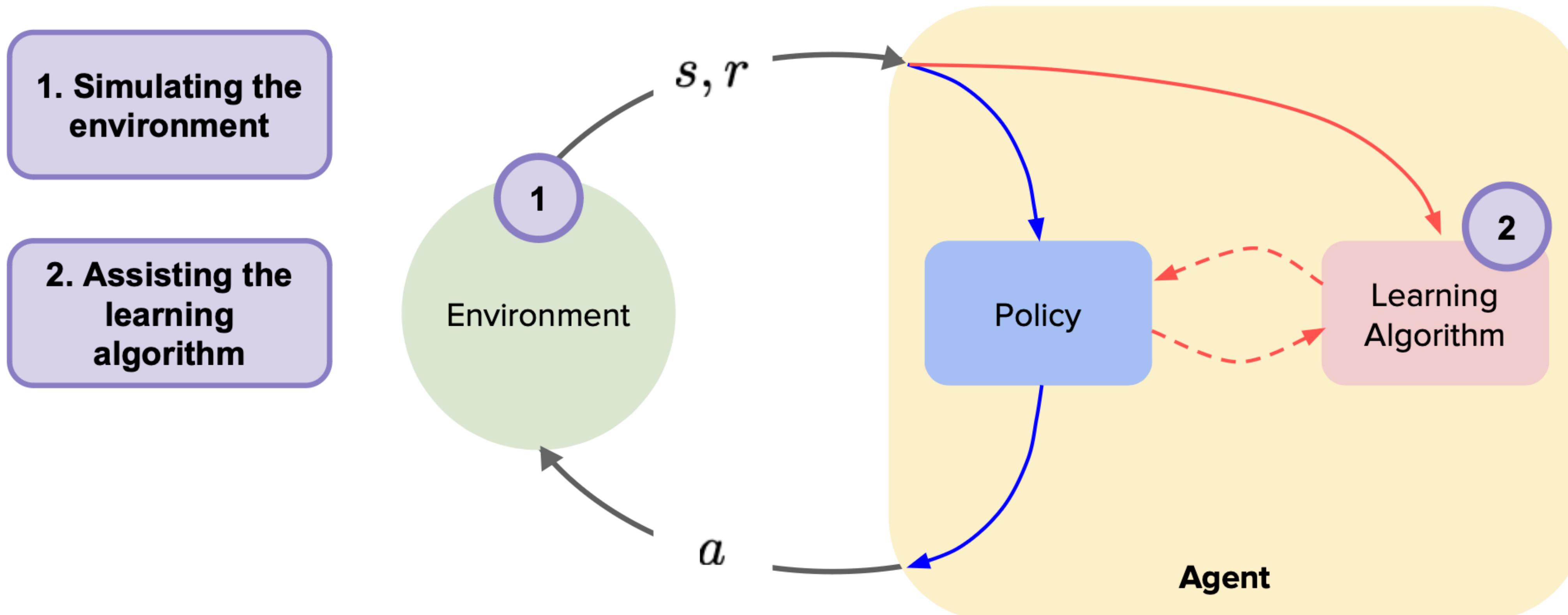
- A transition/dynamics model: $s_{t+1} = f_s(s_t, a_t)$
- A model of rewards: $r_{t+1} = f_r(s_t, a_t)$
- An inverse transition/dynamics model: $a_t = f_s^{-1}(s_t, s_{t+1})$
- A model of distance: $d_{ij} = f_d(s_i, s_j)$
- A model of future returns: $G_t = Q(s_t, a_t)$ or $G_t = V(s_t)$

Typically what is meant by
the model in model-based RL

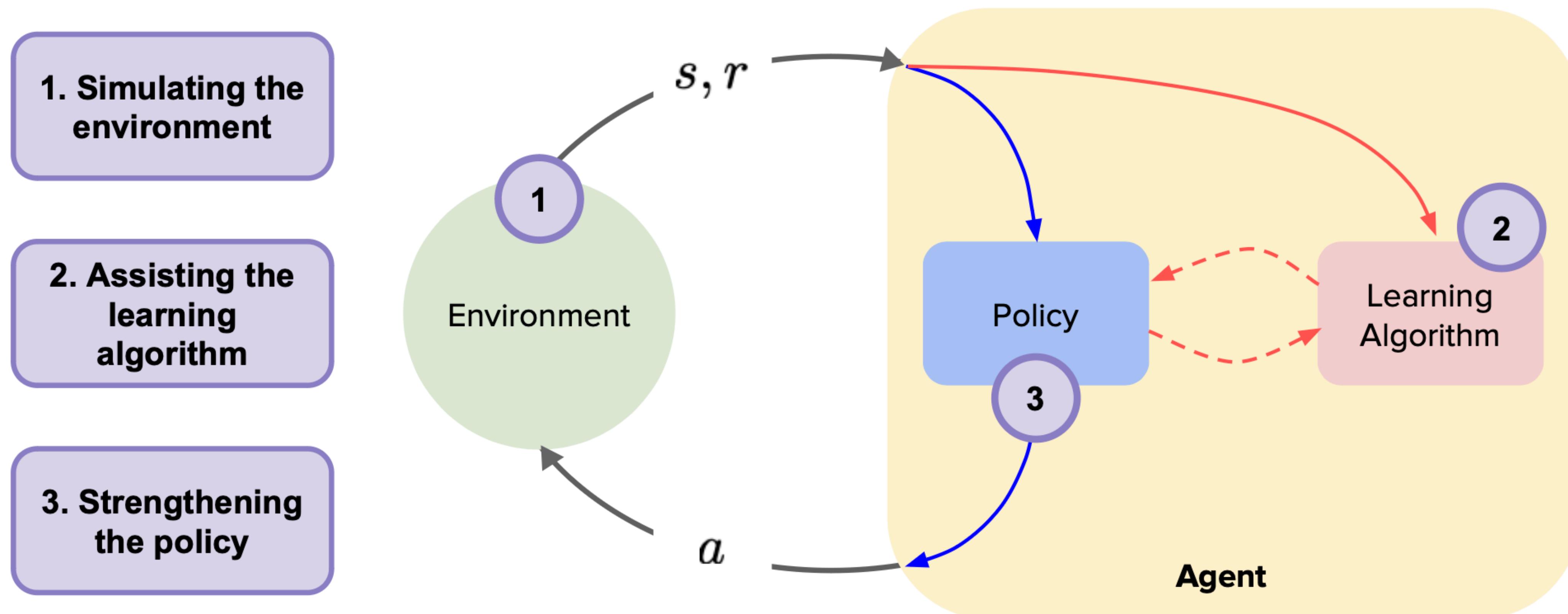
Where does the model fit into the picture?



Where does the model fit into the picture?



Where does the model fit into the picture?



Why do we want to learn a model?



Planning with real robots
(too expensive, too risky)

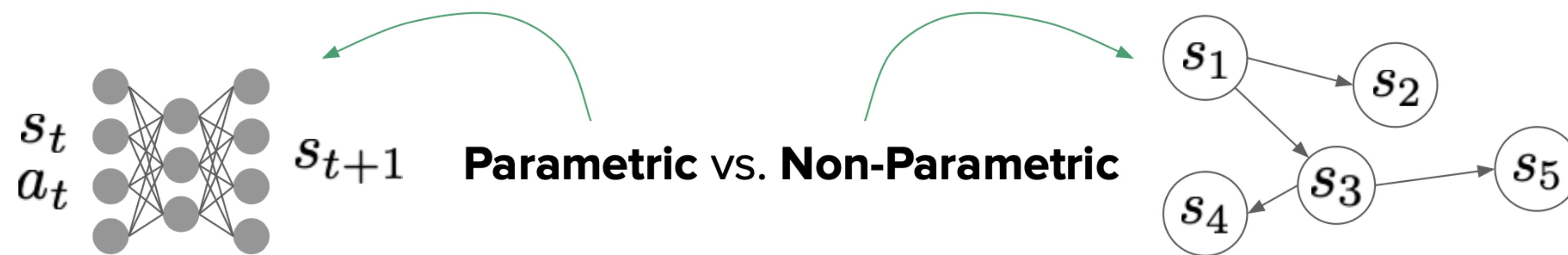
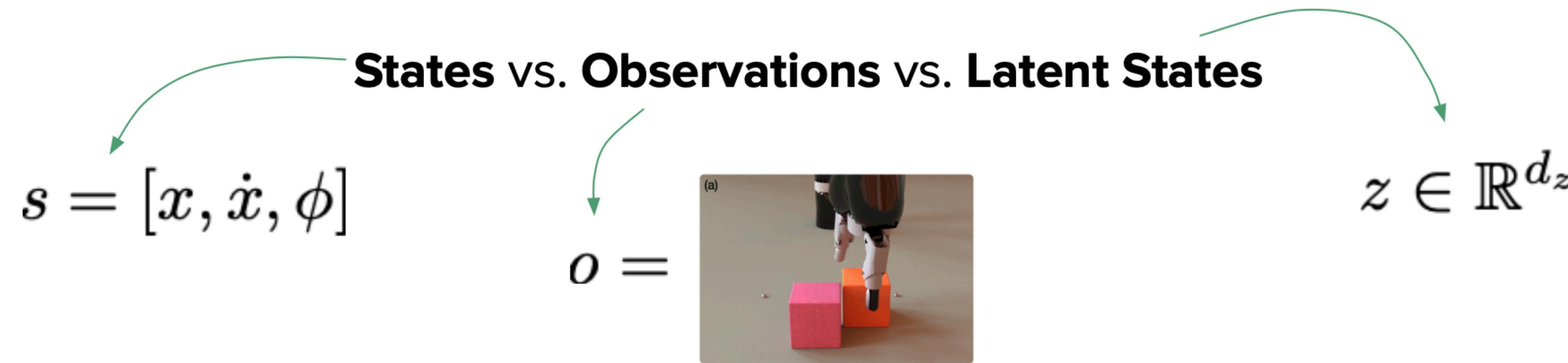


**Simulating complex
physical dynamics**
(too expensive)



Interactions with humans
(no access)

V-View



Why View?

- ❖ Observation o_t can high dimensional
- ❖ Compresses each o_t it receives at time step t into a low dimensional latent vector z_t
- ❖ This compressed representation can be used to reconstruct the original \hat{o}_t

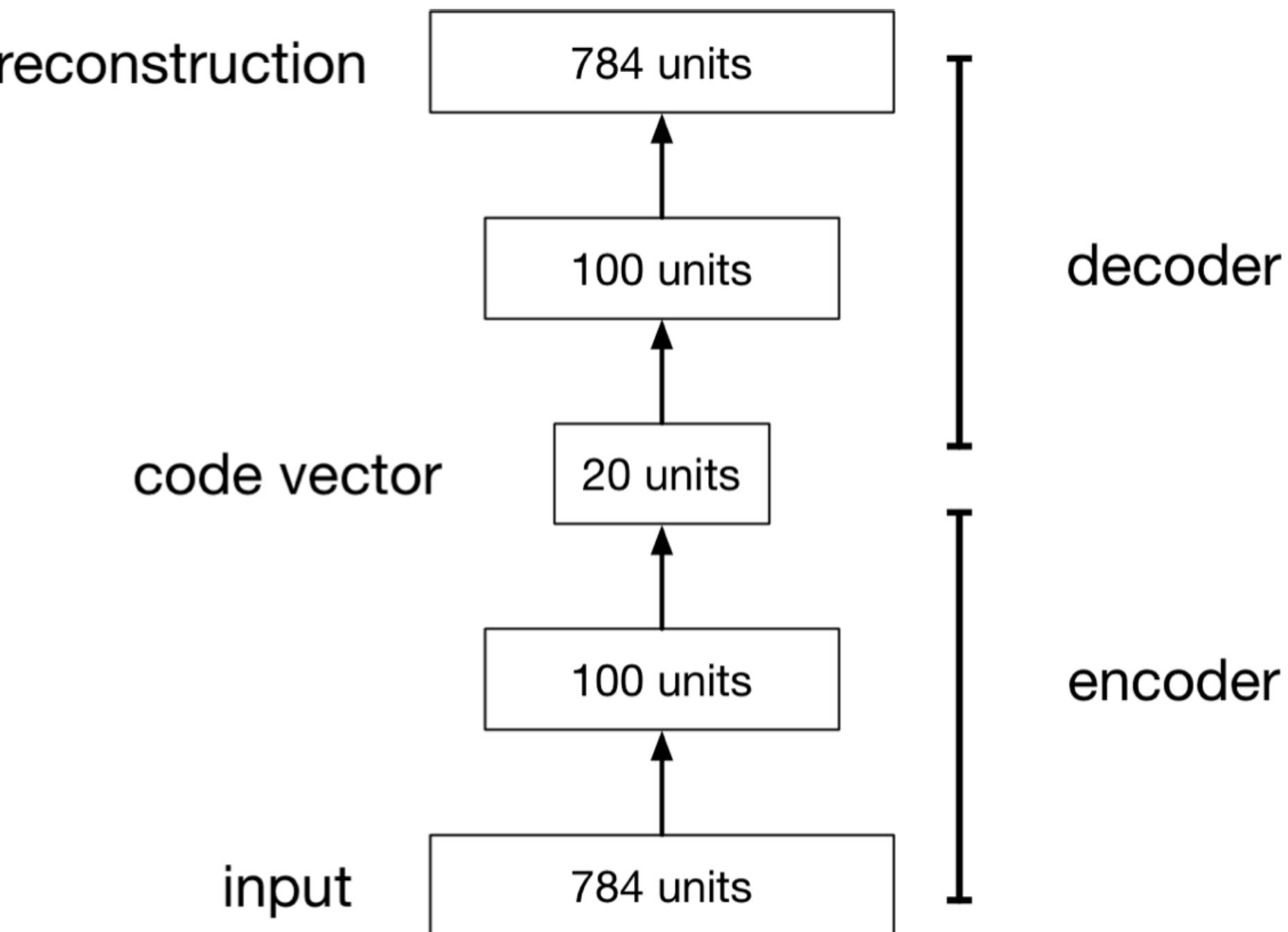
C-Controller

- ❖ The Controller (C) model is responsible for determining the course of actions to take in order to maximize the expected cumulative reward of the agent during a rollout of the environment.
- ❖ It uses V and M to rollout the environment
 - ❖ Like a dream!
 - ❖ Can be (almost) any RL algorithm

Preliminaries

Autoencoders

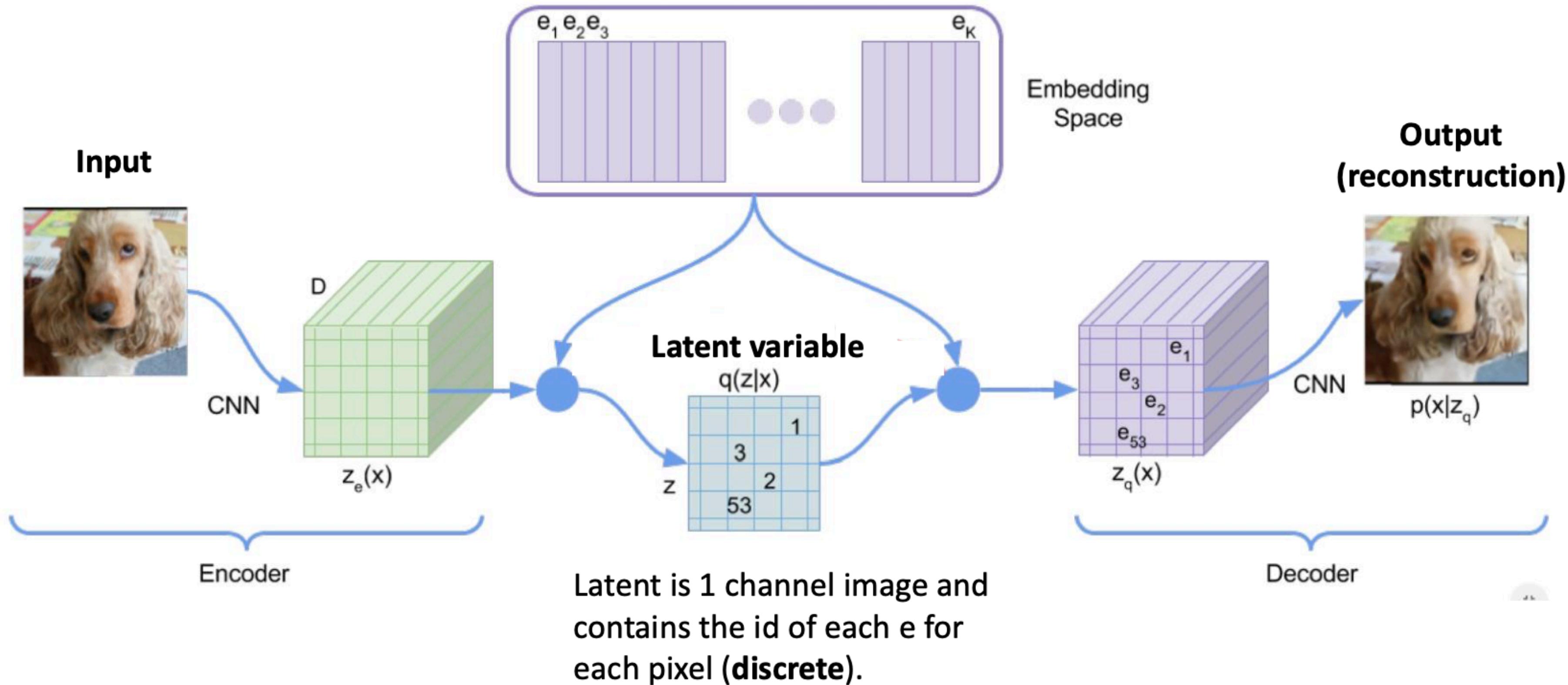
- An **autoencoder** is a feed-forward neural net whose job it is to take an input x and predict x .
- To make this non-trivial, we need to add a **bottleneck layer** whose dimension is much smaller than the input.



Why Autoencoders?

- Map high-dimensional data to two dimensions for visualization
- Compression (i.e. reducing the file size)
 - Note: this requires a VAE, not just an ordinary autoencoder.
- Learn abstract features in an unsupervised way so you can apply them to a supervised task
 - Unlabeled data can be much more plentiful than labeled data
- Learn a semantically meaningful representation where you can, e.g., interpolate between different images.

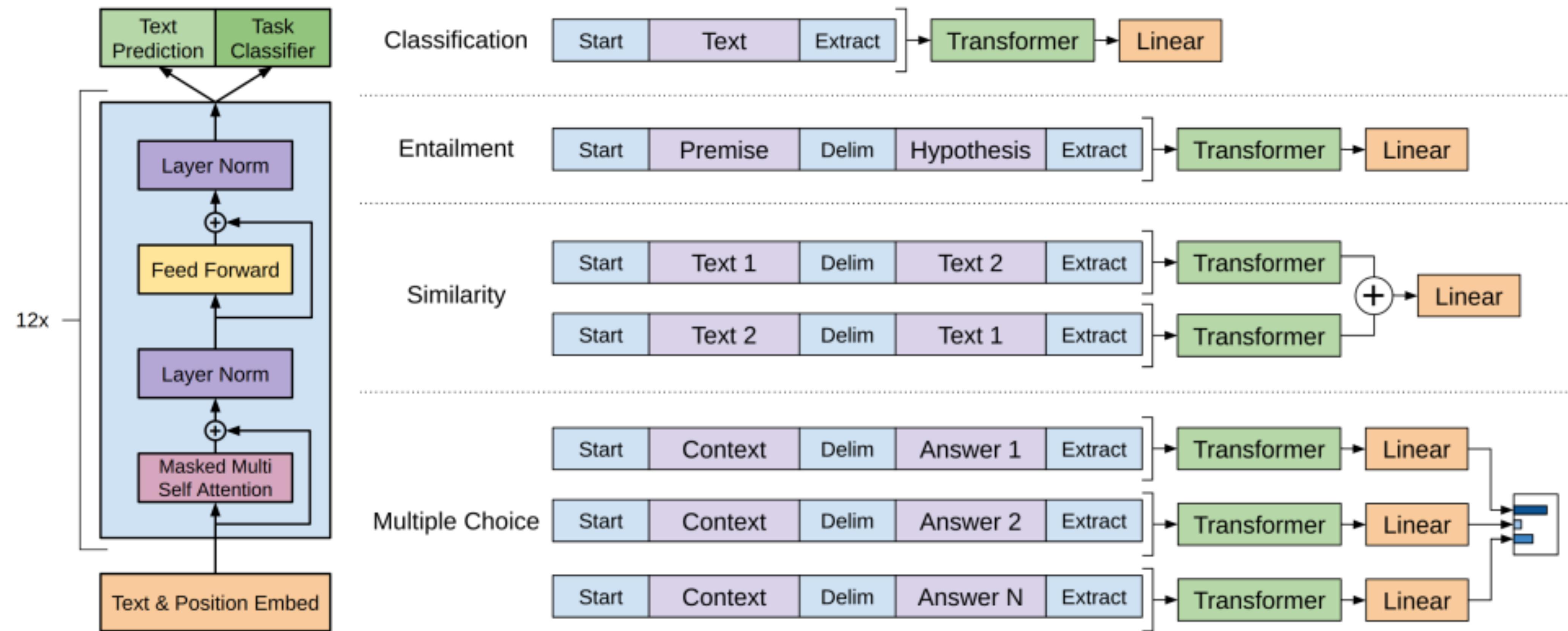
VQ-VAE



Why are they useful?

- ❖ Provides low dimensional latent
 - ❖ Useful for V!
- ❖ Provides discrete representations
 - ❖ Useful for M
 - ❖ We'll see soon

GPT

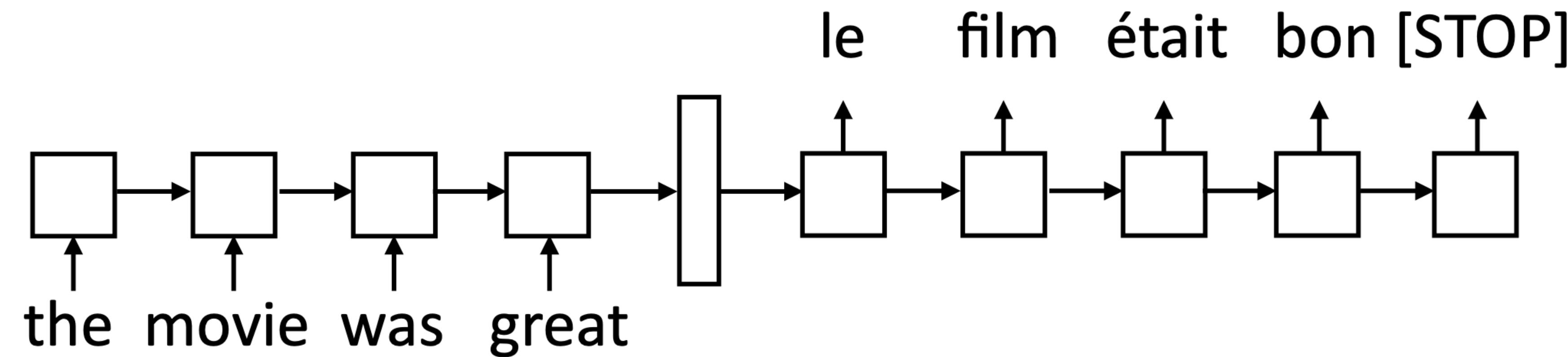


GPT Training

- ❖ Assume a set of N tokens
- ❖ Given a T length sequence
 - ❖ Take a $0:t-1$ sequence
 - ❖ Pass it through the model
 - ❖ Predict $1:t$ sequence through a softmax layer

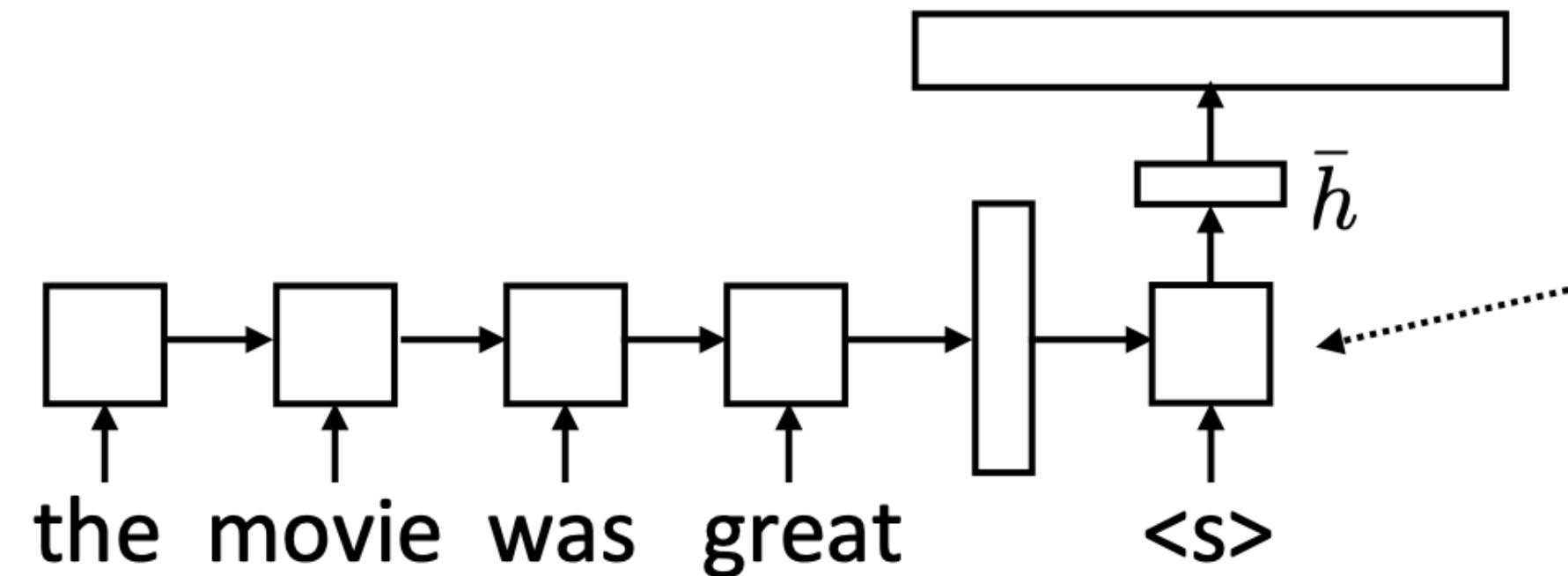
GPT From Encoder-Decoder View

Encode a sequence into a fixed-sized vector



GPT From Encoder-Decoder View

- ▶ Generate next word conditioned on previous word as well as hidden state
- ▶ W size is $|\text{vocab}| \times |\text{hidden state}|$, softmax over entire vocabulary



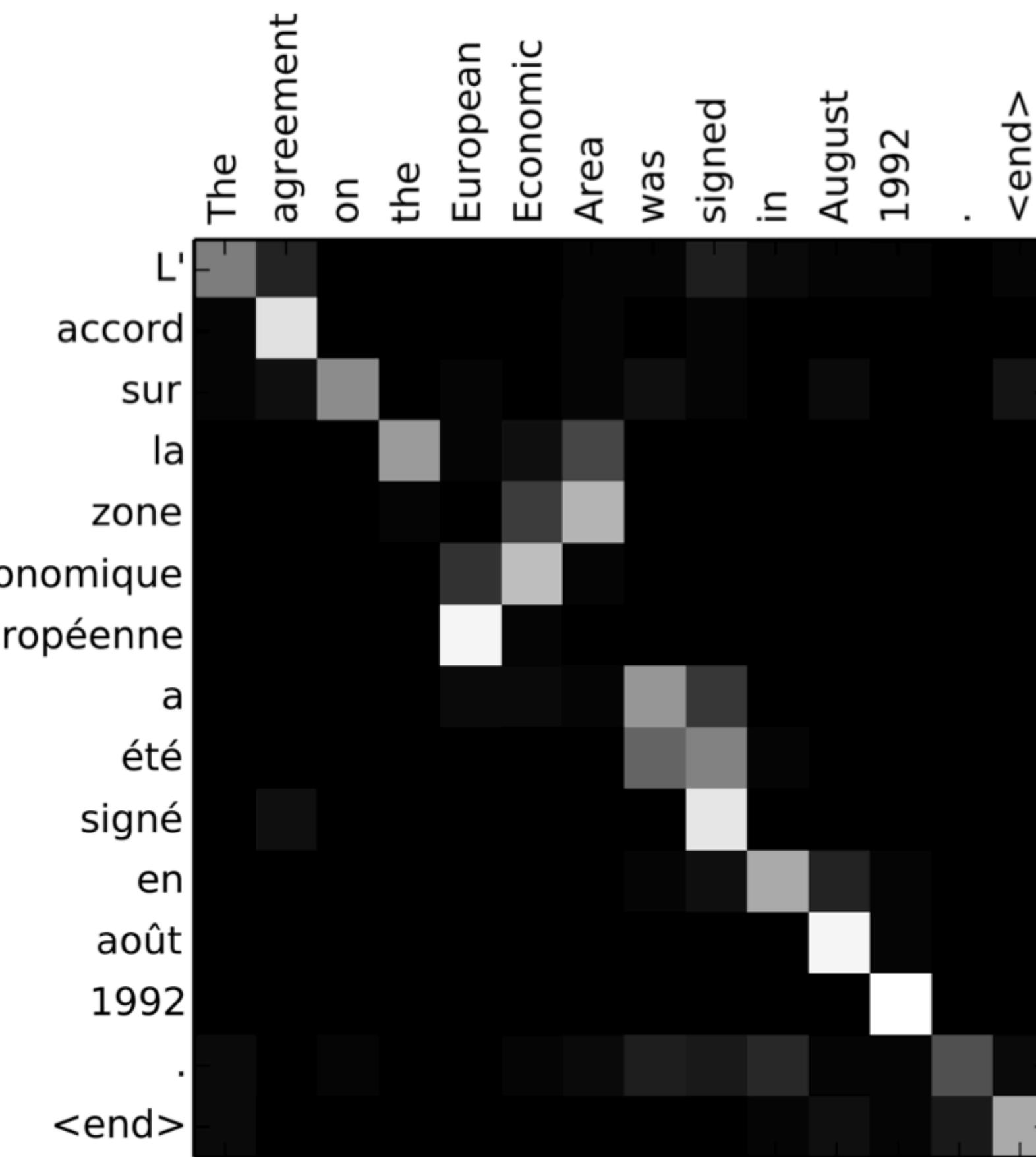
$$P(y_i|\mathbf{x}, y_1, \dots, y_{i-1}) = \text{softmax}(W\bar{h})$$

$$P(\mathbf{y}|\mathbf{x}) = \prod_{i=1}^n P(y_i|\mathbf{x}, y_1, \dots, y_{i-1})$$

Decoder has separate parameters from encoder, so this can learn to be a language model (produce a plausible next word given current one)

Inference - Let's talk about attention

- ▶ Encoder hidden states capture contextual source word identity
- ▶ Decoder hidden states are now mostly responsible for selecting what to attend to
- ▶ Doesn't take a complex hidden state to walk monotonically through a sentence and spit out word-by-word translations

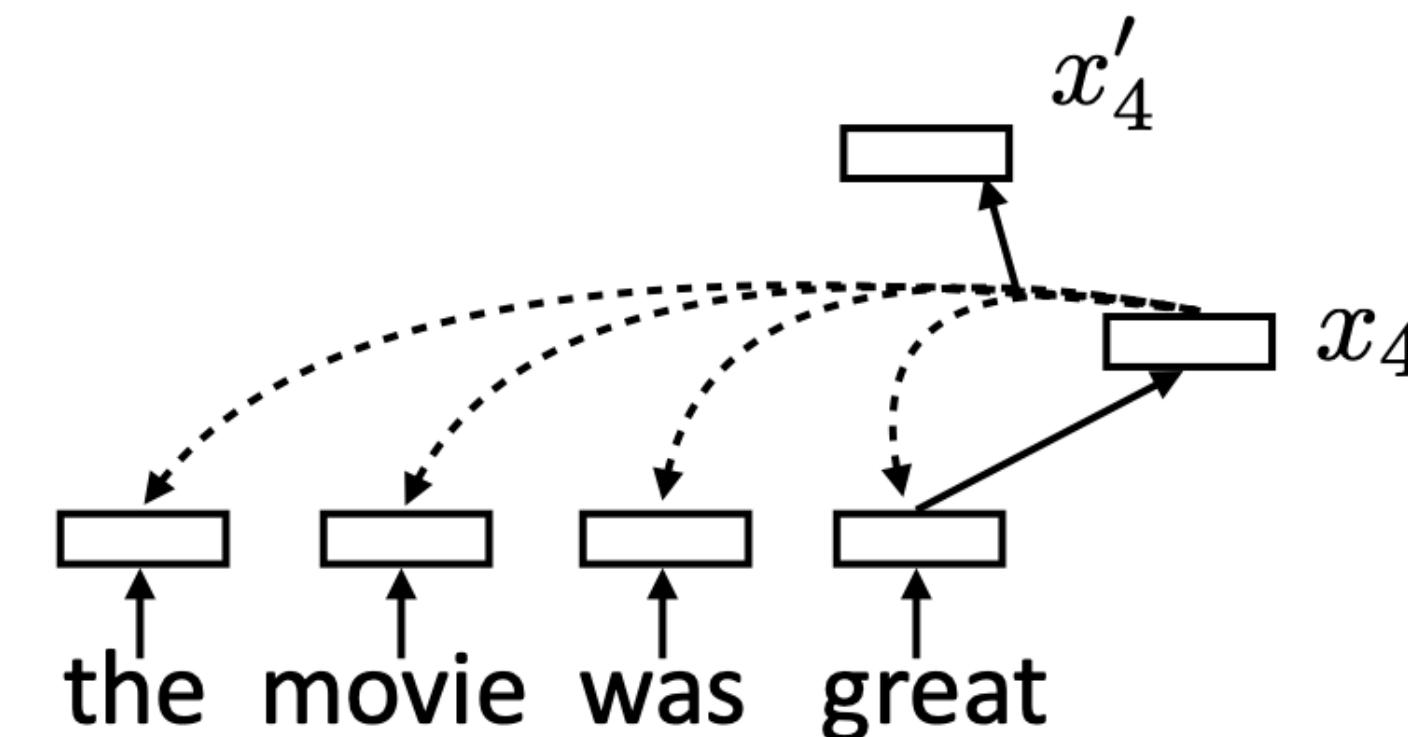


Self-attention

- ▶ Each word forms a “query” which then computes attention over each word

$$\alpha_{i,j} = \text{softmax}(x_i^\top x_j) \quad \text{scalar}$$

$$x'_i = \sum_{j=1}^n \alpha_{i,j} x_j \quad \text{vector} = \text{sum of scalar * vector}$$

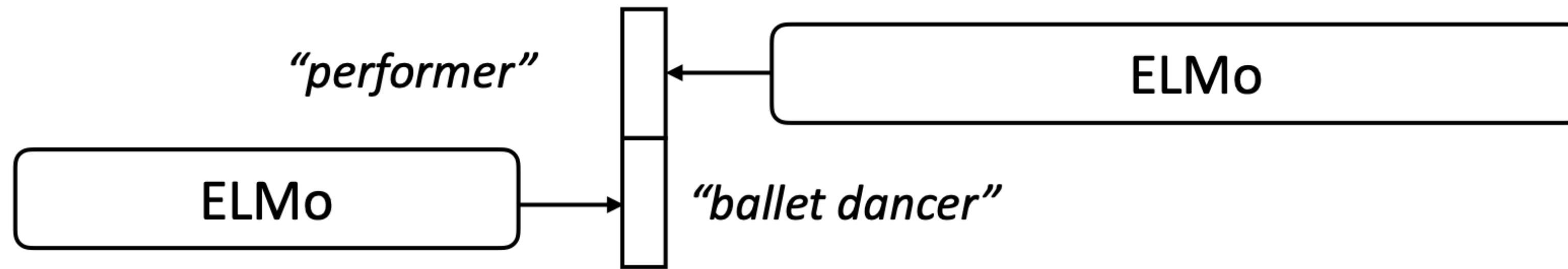


- ▶ Multiple “heads” analogous to different convolutional filters. Use parameters W_k and V_k to get different attention values + transform vectors

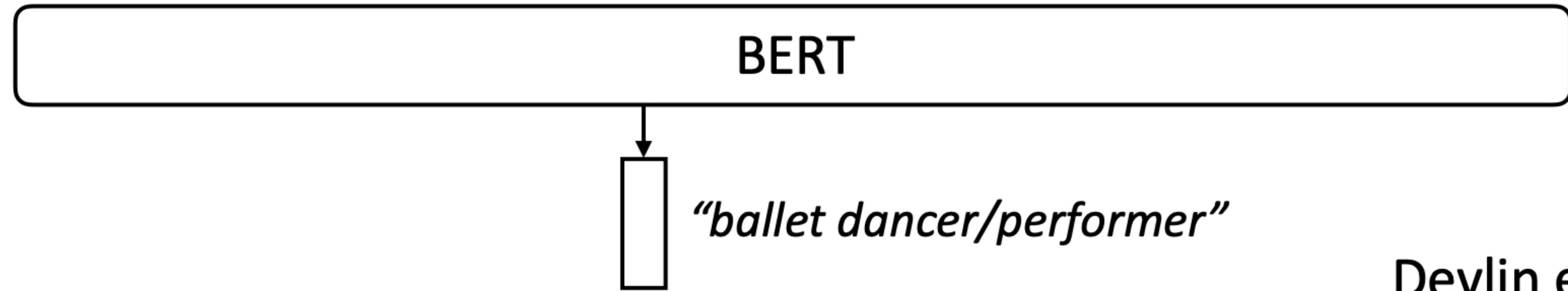
Vaswani et al. (2017)

Bidirectional Encoder Representations from Transformers(BERT)

- ▶ ELMo is a unidirectional model (as is GPT): we can concatenate two unidirectional models, but is this the right thing to do?
- ▶ ELMo reprs look at each direction in isolation; BERT looks at them jointly



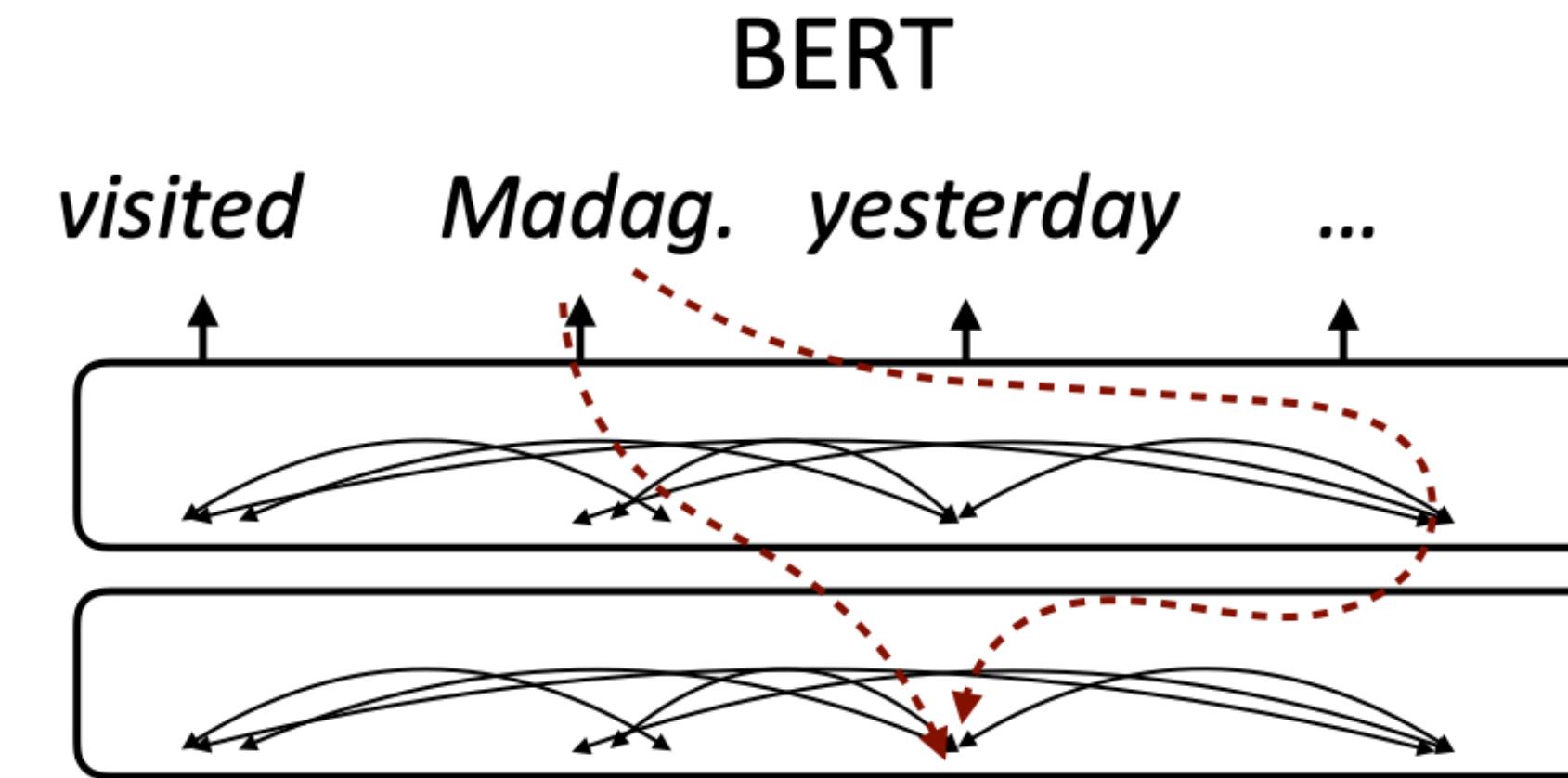
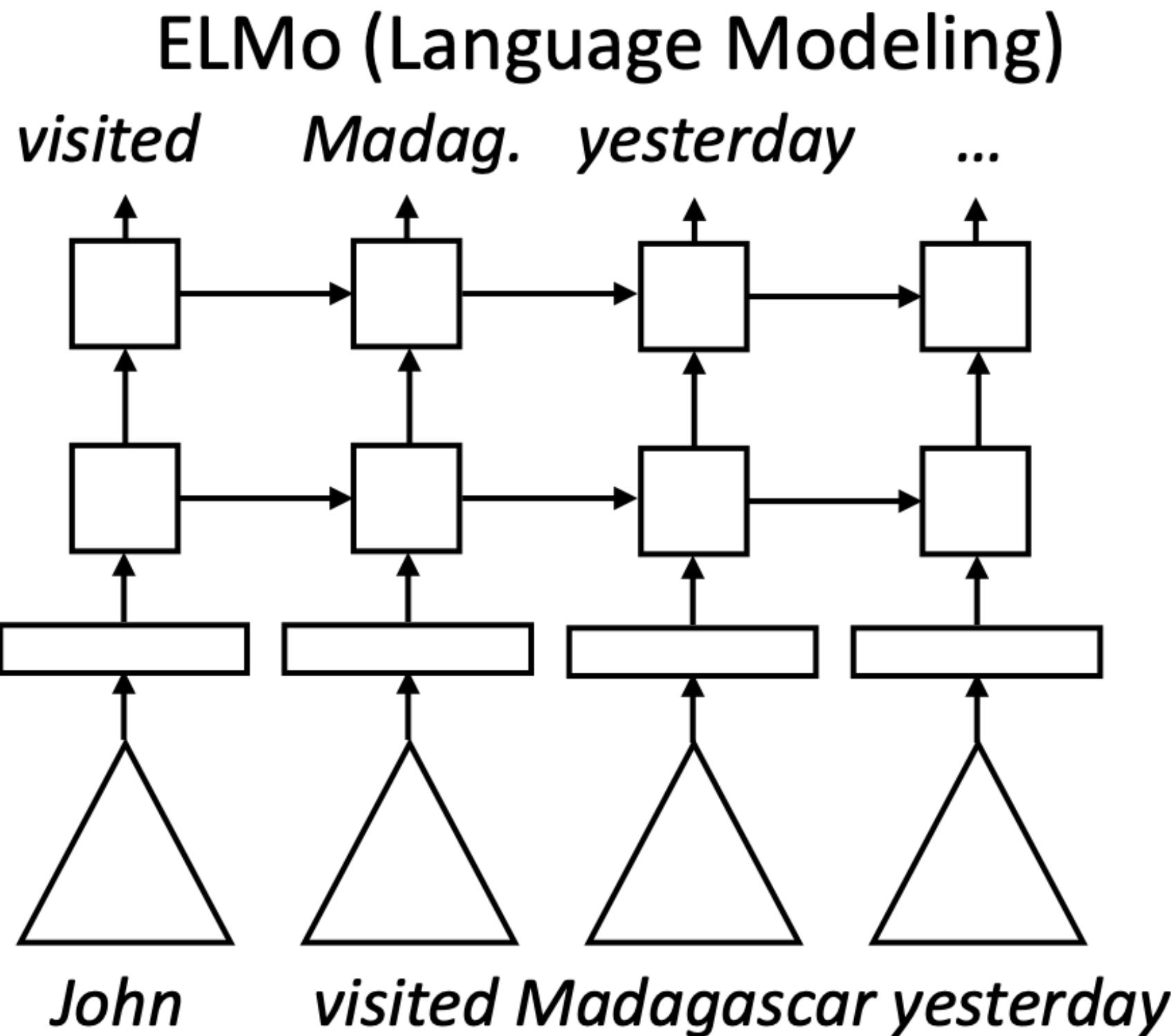
A stunning ballet dancer, Copeland is one of the best performers to see live.



Devlin et al. (2019)

Bidirectional Encoder Representations from Transformers(BERT)

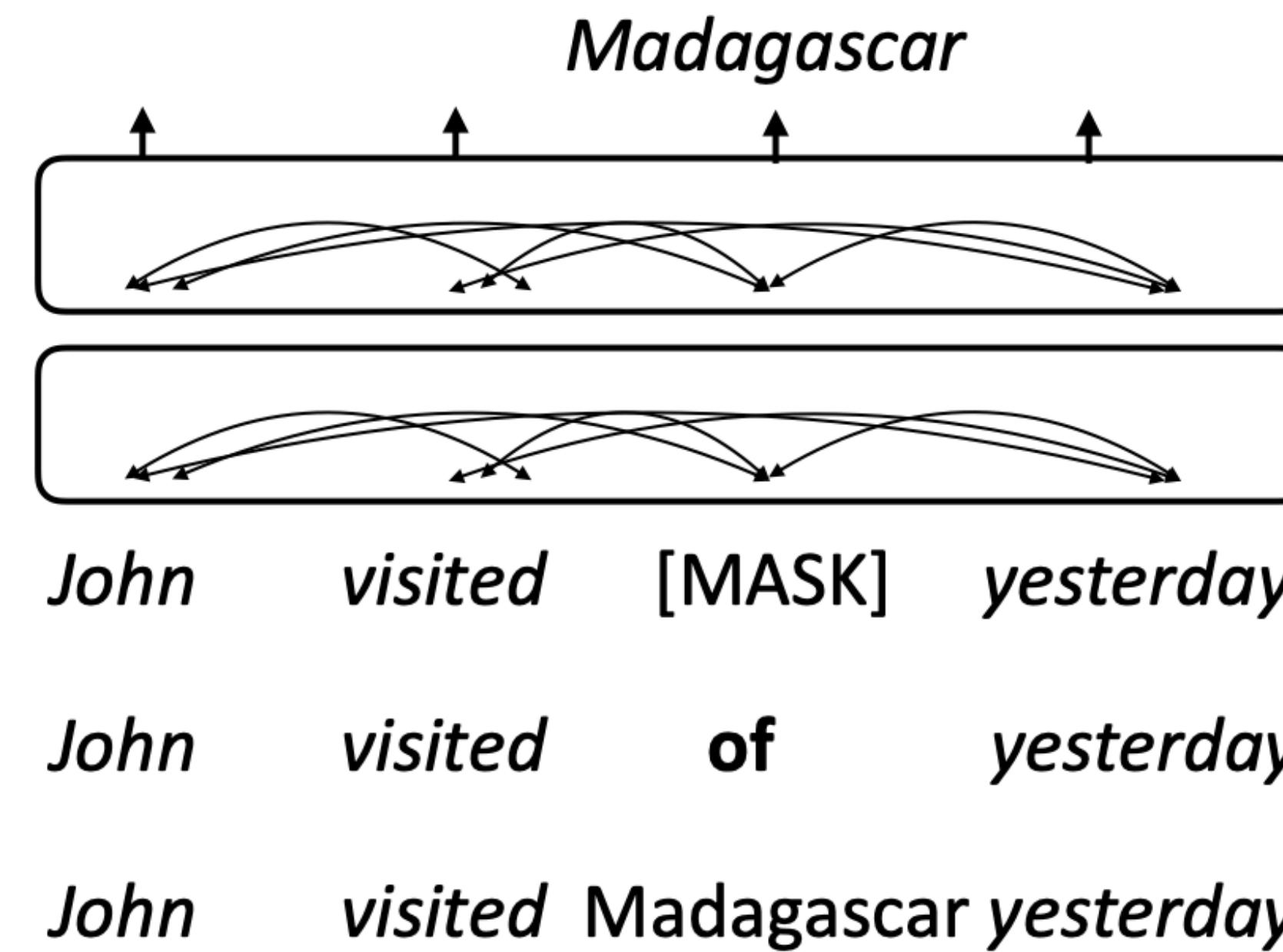
- ▶ How to learn a “deeply bidirectional” model? What happens if we just replace an LSTM with a transformer?



- ▶ Transformer LMs have to be “one-sided” (only attend to previous tokens), not what we want

Masked Sequence Modelling

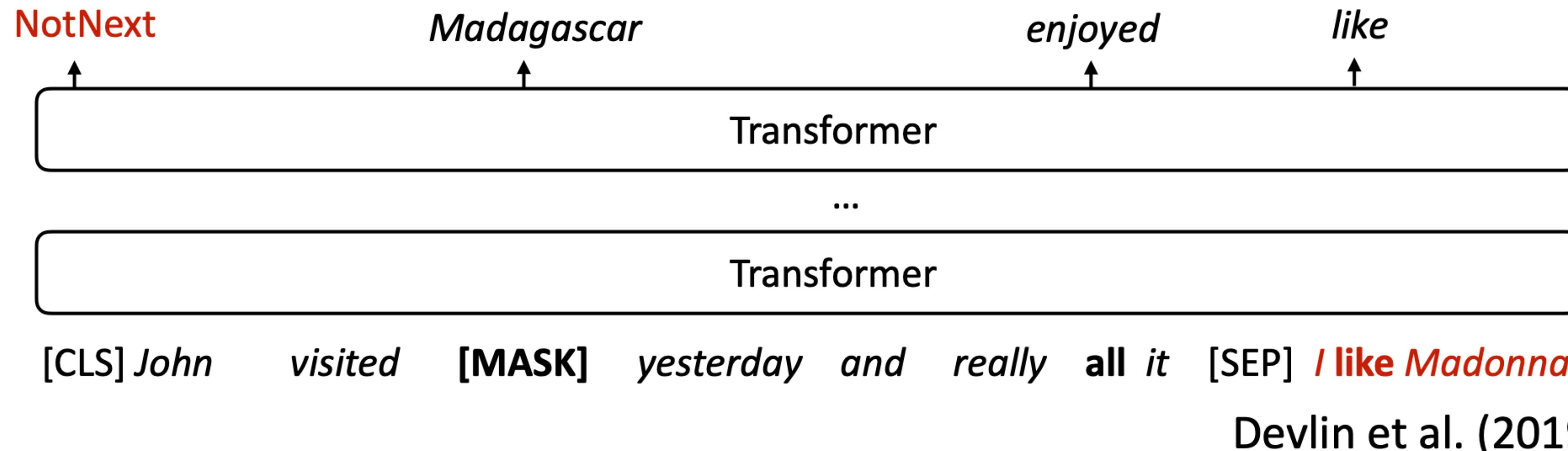
- ▶ How to prevent cheating? Next word prediction fundamentally doesn't work for bidirectional models, instead do *masked language modeling*
- ▶ BERT formula: take a chunk of text, predict 15% of the tokens
 - ▶ For 80% (of the 15%), replace the input token with [MASK]
 - ▶ For 10%, replace w/random
 - ▶ For 10%, keep same



Devlin et al. (2019)

Masked Sequence Modelling

- ▶ Input: [CLS] Text chunk 1 [SEP] Text chunk 2
- ▶ 50% of the time, take the true next chunk of text, 50% of the time take a random other chunk. Predict whether the next chunk is the “true” next
- ▶ BERT objective: masked LM + next sentence prediction



Devlin et al. (2019)

Why are we learning this?

- ❖ Different ways of sequence modeling
 - ❖ Important for model - M
- ❖ Different ways have different drawbacks
 - ❖ Engineering decisions!

How to train your world model?

Dreamer



encode images



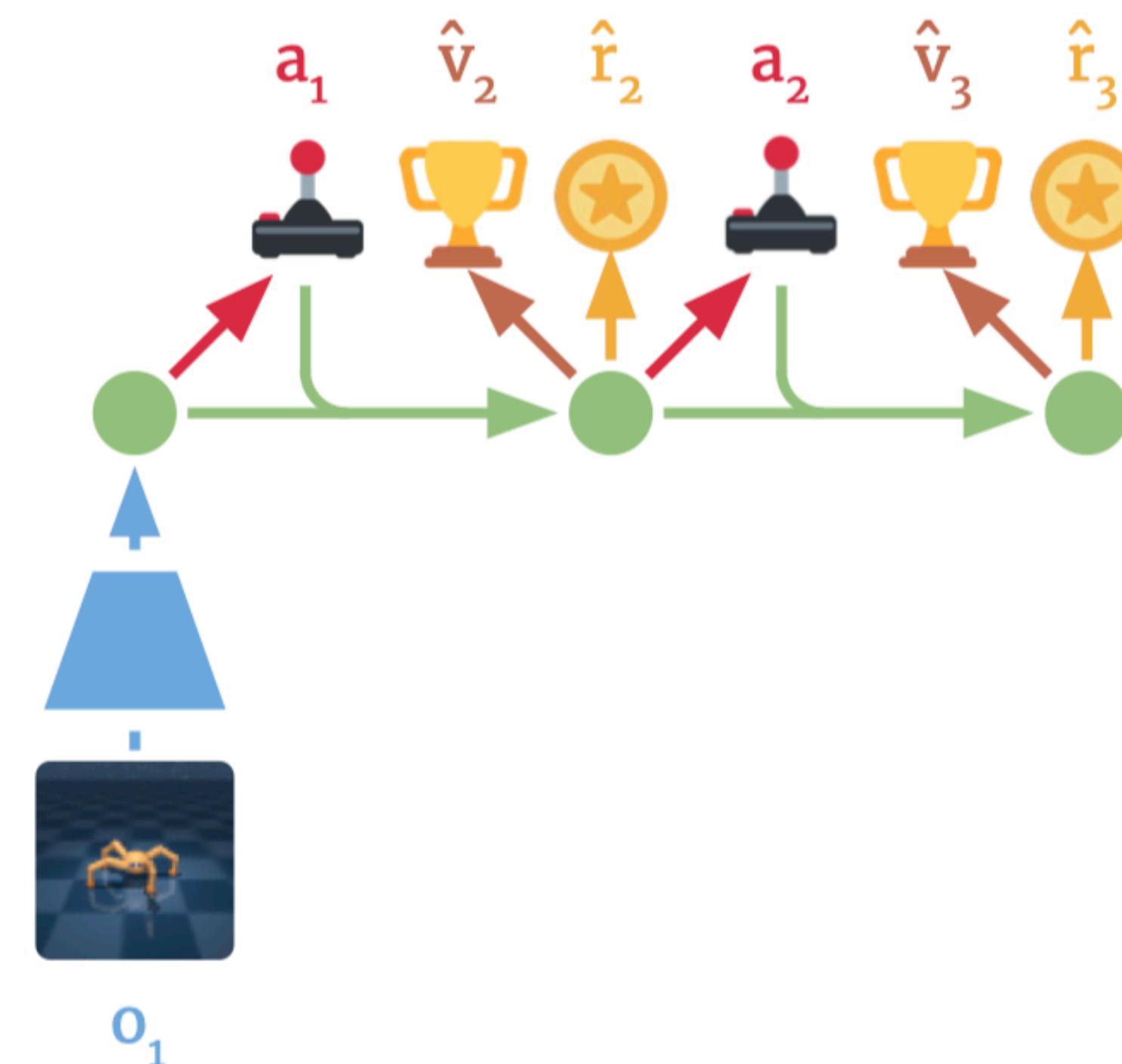
imagine ahead



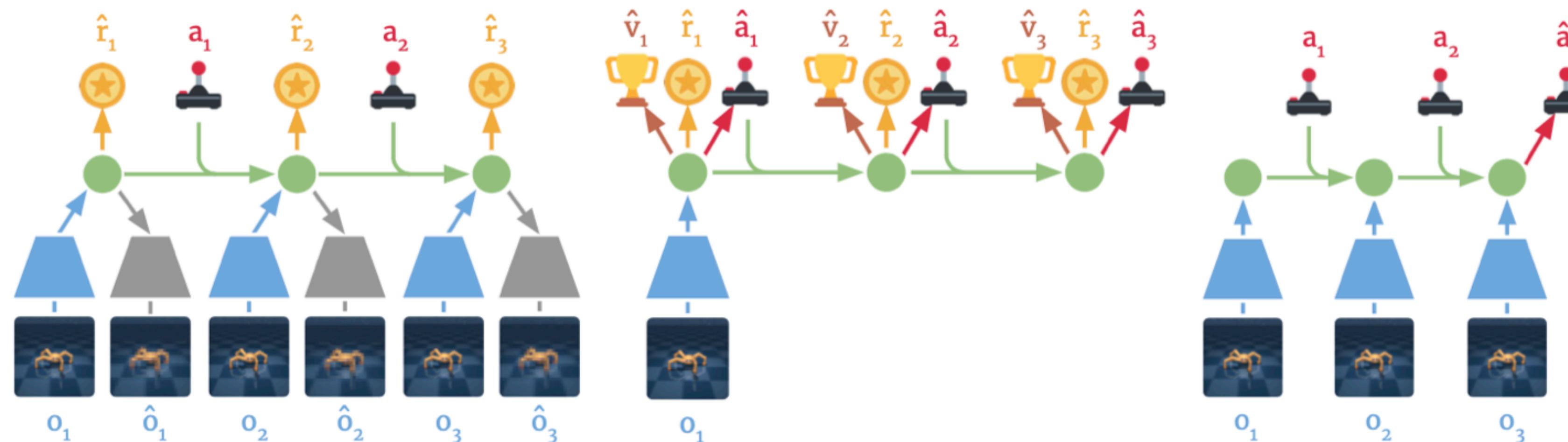
predict rewards



predict values



Dreamer



Dreamer

Initialize policy θ, ϕ, ψ randomly and D_{env} with random trajectories $\{(o_t^{(i)}, a_t^{(i)}, r_t^{(i)})_{t=1}^T\}$.

1. Dynamics learning:

1. Sample trajectories from D_{env} and infer states from observations using the representation model: $s_t \sim p_\theta(s_t | s_{t-1}, a_{t-1}, o_t)$.
2. Train the dynamics model using variational inference and update θ .

2. Actor-critic learning from imagined rollouts:

1. Imagine trajectories seeded from $s_t : \{s_\tau, r_\tau, a_\tau, v_\tau\}_{\tau=t}^{t+H}$
2. Compute value targets $V_\lambda(s_\tau)$.
3. Update actor $\phi \rightarrow \phi + \alpha \nabla_\phi \sum_{\tau}^H V_\lambda(s_\tau)$
4. Update critic: $\psi \rightarrow \psi - \alpha \nabla_\psi \sum_{\tau}^H \|v_\psi - V_\lambda(s_\tau)\|$

3. Environment interaction

1. Deploy the actor in the environment adding exploration noise to the predicted actions and update D_{env}

Dreamer

Initialize policy θ, ϕ, ψ randomly and D_{env} with random trajectories $\{(o_t^{(i)}, a_t^{(i)}, r_t^{(i)})_{t=1}^T\}$.

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3. Environment interaction

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Dreamer

Algorithm 1: Dreamer

```

Initialize dataset  $\mathcal{D}$  with  $S$  random seed episodes.
Initialize neural network parameters  $\theta, \phi, \psi$  randomly.
while not converged do
    for update step  $c = 1..C$  do
        // Dynamics learning
        Draw  $B$  data sequences  $\{(a_t, o_t, r_t)\}_{t=k}^{k+L} \sim \mathcal{D}$ .
        Compute model states  $s_t \sim p_\theta(s_t | s_{t-1}, a_{t-1}, o_t)$ .
        Update  $\theta$  using representation learning.

        // Behavior learning
        Imagine trajectories  $\{(s_\tau, a_\tau)\}_{\tau=t}^{t+H}$  from each  $s_t$ .
        Predict rewards  $E(q_\theta(r_\tau | s_\tau))$  and values  $v_\psi(s_\tau)$ .
        Compute value estimates  $V_\lambda(s_\tau)$  via Equation 6.
        Update  $\phi \leftarrow \phi + \alpha \nabla_\phi \sum_{\tau=t}^{t+H} V_\lambda(s_\tau)$ .
        Update  $\psi \leftarrow \psi - \alpha \nabla_\psi \sum_{\tau=t}^{t+H} \frac{1}{2} \|v_\psi(s_\tau) - V_\lambda(s_\tau)\|^2$ .

        // Environment interaction
         $o_1 \leftarrow \text{env.reset}()$ 
        for time step  $t = 1..T$  do
            Compute  $s_t \sim p_\theta(s_t | s_{t-1}, a_{t-1}, o_t)$  from history.
            Compute  $a_t \sim q_\phi(a_t | s_t)$  with the action model.
            Add exploration noise to action.
             $r_t, o_{t+1} \leftarrow \text{env.step}(a_t)$ .
            Add experience to dataset  $\mathcal{D} \leftarrow \mathcal{D} \cup \{(o_t, a_t, r_t)_{t=1}^T\}$ .

```

Model components

Representation	$p_\theta(s_t s_{t-1}, a_{t-1}, o_t)$
Transition	$q_\theta(s_t s_{t-1}, a_{t-1})$
Reward	$q_\theta(r_t s_t)$
Action	$q_\phi(a_t s_t)$
Value	$v_\psi(s_t)$

Hyper parameters

Seed episodes	S
Collect interval	C
Batch size	B
Sequence length	L
Imagination horizon	H
Learning rate	α

Dreamer - What's there?

- ❖ M - latent state space model
- ❖ V - latent state space model
- ❖ C - actor critic model

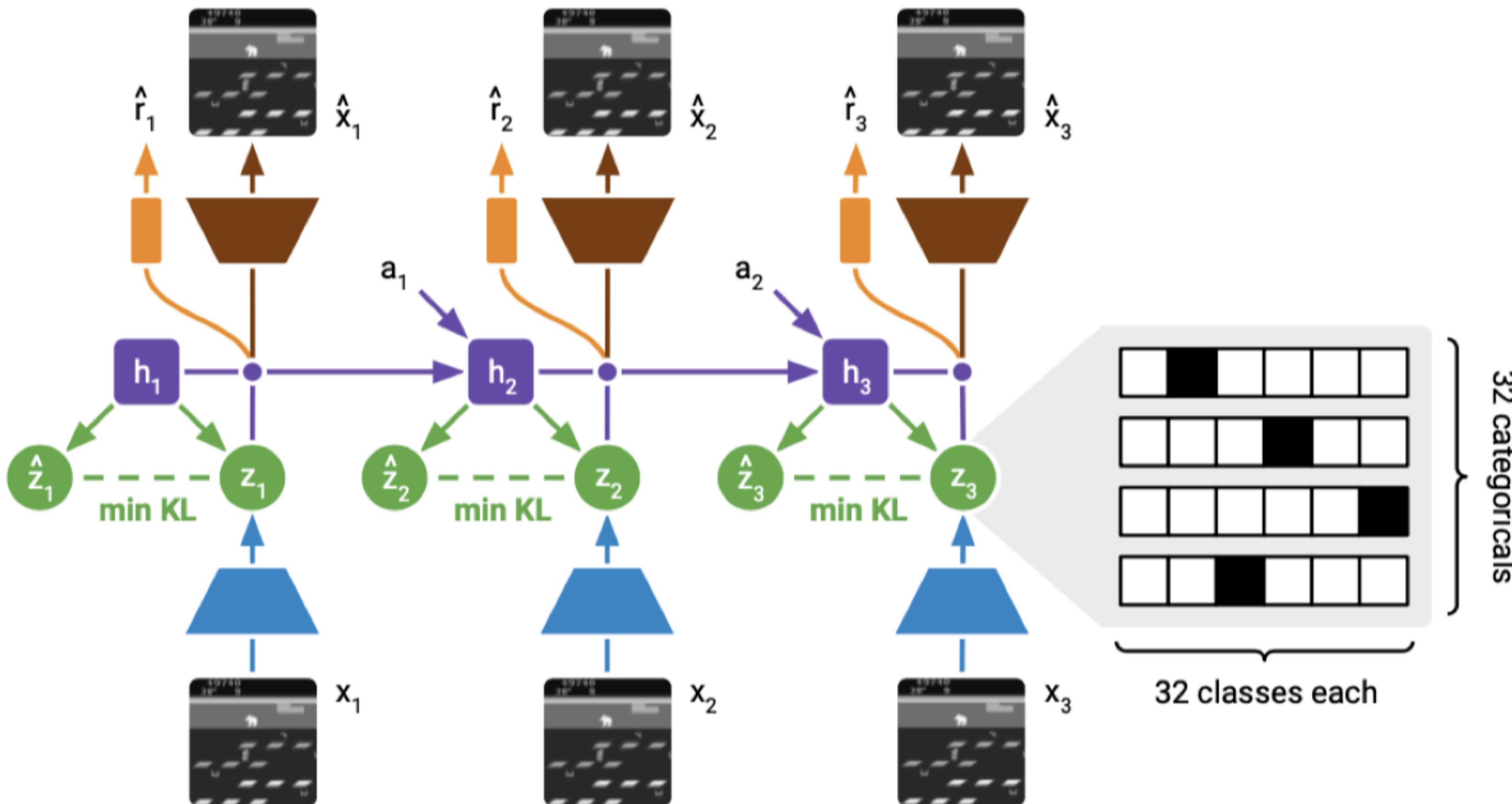
Dreamer - What's missing?

- ❖ No discrete representation
 - ❖ We saw discrete representation in VQ-VAE!

Dreamer V2

- ❖ Adds stochasticity through discrete latents
- ❖ Two representation for states s_t
 - ❖ Deterministic part (from previous approaches)
 - ❖ Stochastic part
 - ❖ 32 vectors from 32 values
- ❖ Combination of reinforce and straight-through gradients
- ❖ KL balancing

Dreamer V2



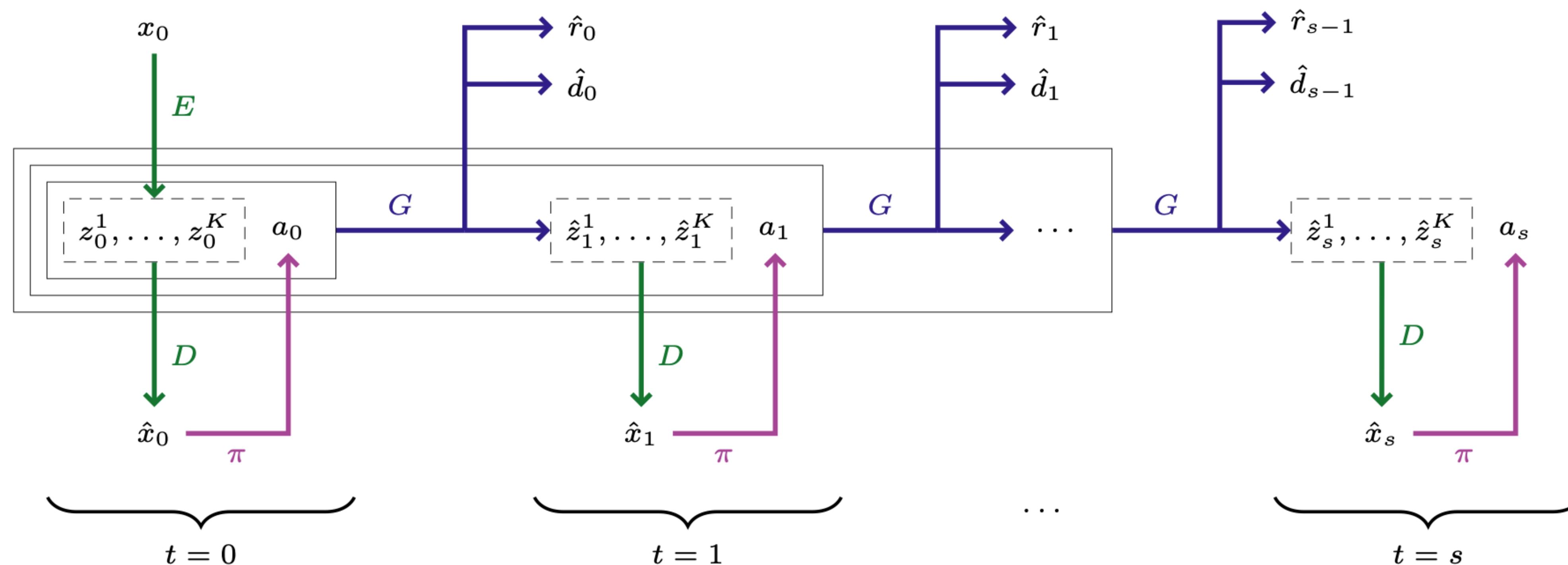
IRIS

- ❖ We saw discrete representations
- ❖ Can we use GPT? 

Transformers are sample efficient world models

- ❖ Encode observations in a discrete space
- ❖ Use 0..T-1 discrete tokens and actions to generate token at T, and predict reward and termination
- ❖ Using the WM, learn a policy on the decoded observation

Transformers are sample efficient world models



IRIS - What's there?

- ❖ M - GPT2
- ❖ V - VAE
- ❖ C - Actor critic model

IRIS - Issues

- ❖ Slow Imagine step
 - ❖ Imagine step has $N * H$ steps where
 - ❖ Next token prediction for N tokens ($1 \text{ obs/state} = N \text{ tokens}$)
 - ❖ Next state prediction for H states
- ❖ Does not retain any state information

Faster imagination - two approaches

- ❖ Less number of tokens for imagination
- ❖ Non-autoregressive generation

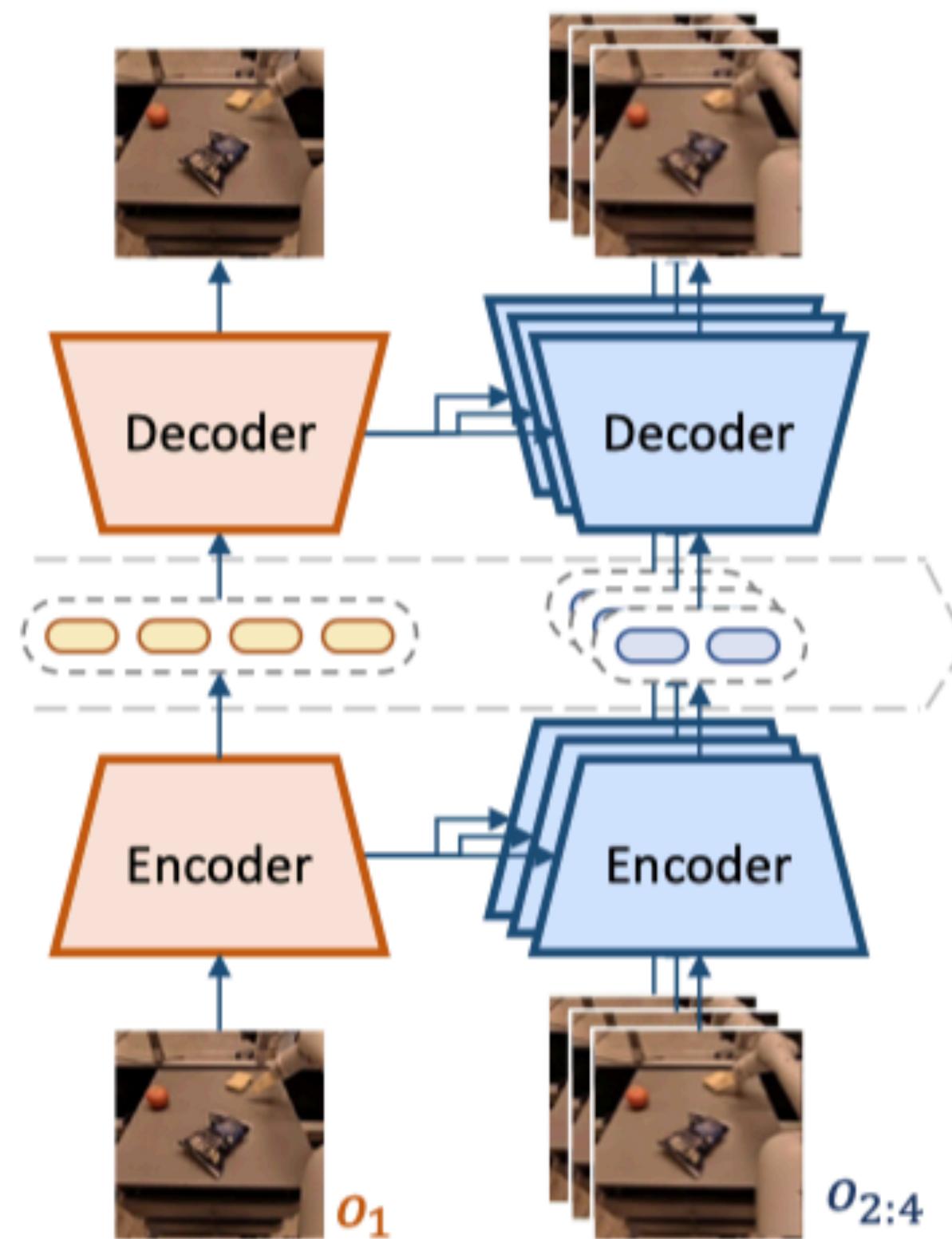
iVideoGPT | View (V)

- Context encoder and decoder
 - $N = 16$ tokens for $1 : T_0$ observation
 - $z_t^{1:N} = E_c(o_t)$
 - Uses larger token numbers to learn the underlying structure (e.g., physics, motion, etc.)
- Dynamics encoder and decoder
 - Used for tokenizing observations for $t > T_0$
 - $N = 4$ tokens for $T_0 + 1 : T$ observations
 - $z_t^{1:n} = E_p(o_t | o_{1:T_0})$, we condition on context observations
 - Uses cross-attention to achieve conditioning

iVideoGPT | View (V)

- Context encoder and decoder
 - $N = 16$ tokens for $1 : T_0$ observation
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 - Used for tokenizing observations for $t > T_0$
 - $N = 4$ tokens for $T_0 + 1 : T$ observations $\mathcal{L}_{\text{tokenizer}} = \sum_{t=1}^{T_0} \mathcal{L}_{\text{VQGAN}}(o_t; E_c(\cdot), D_c(\cdot)) + \sum_{t=T_0+1}^T \mathcal{L}_{\text{VQGAN}}(o_t; E_p(\cdot|o_{1:T_0}), D_p(\cdot|o_{1:T_0}))$
 - $z_t^{1:n} = E_p(o_t | o_{1:T_0})$, we condition on context observations
 - Uses cross-attention to achieve conditioning

iVideoGPT | View (V)

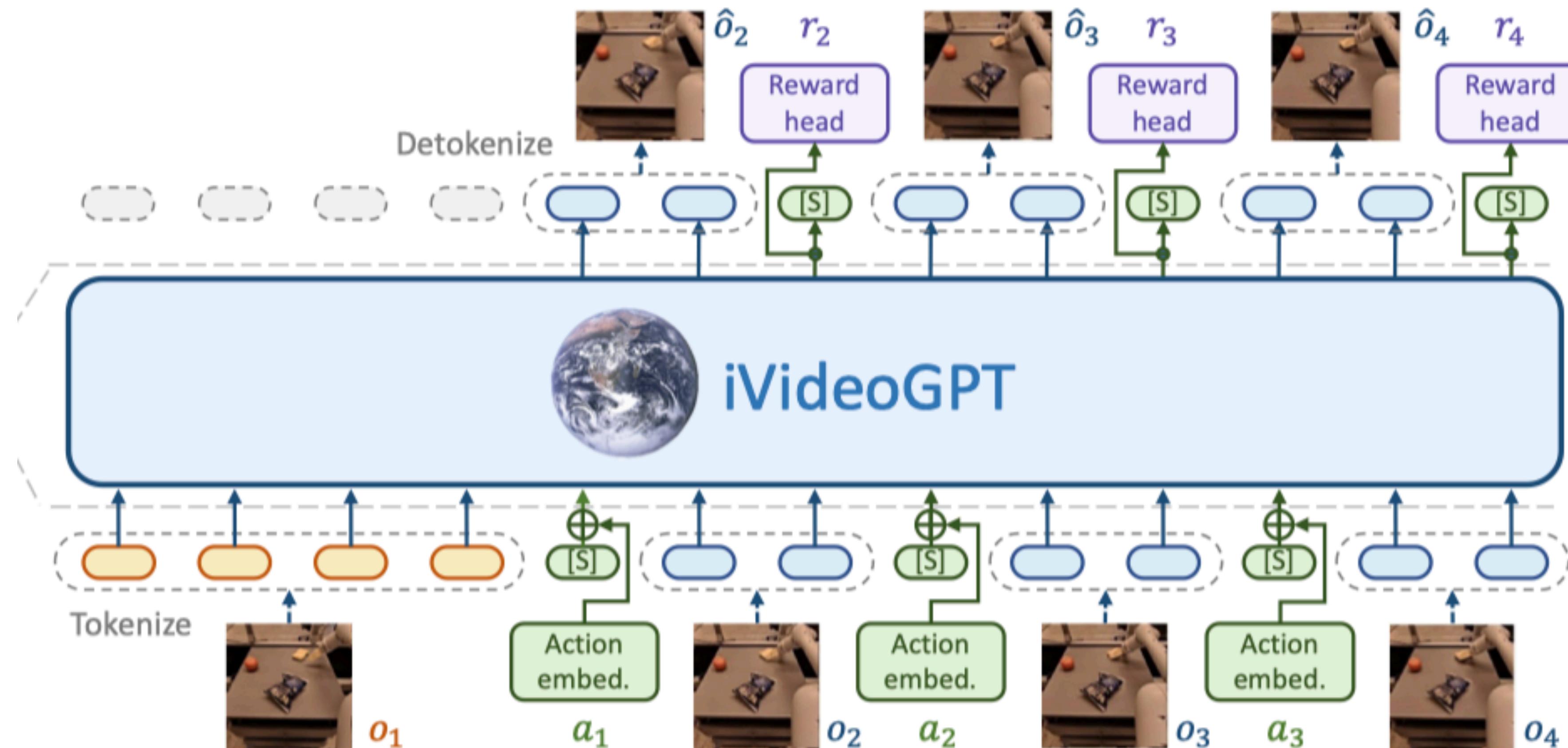


(a) Compressive tokenization

iVideoGPT | Model (M)

- ❖ N tokens for each context observation
- ❖ n tokens for each dynamics observation
- ❖ One extra ‘slot’ token for each observation
- ❖ Total tokens = $(N + 1)T_0 + (n + 1)(T - T_0) - 1$

iVideoGPT | Model (M)



iVideoGPT - What's there?

- ❖ V - VQGAN for image tokenization
 - ❖ Context encoder and decoder
 - ❖ Dynamics encoder and decoder
- ❖ M - GPT
 - ❖ LLAMA architecture
 - ❖ GPT-2 model size

MaskGIT

- Autoregressive token generation is *not* the best for image
- Can we generate tokens taking advantage of the spatial multi-dimensionality?
 - Faster to sample
 - Better fidelity
- Can we use ideas from BERT? 🤔

MaskGIT Training

- Learn to tokenize using VQ-GAN
- Mask n out of N tokens and predict the tokens
 - There is a special [MASK] token
 - Loss -> CE only on the masked tokens
 - $n \in [0, N]$ and monotonous function of some ratio r

MaskGIT Inference

- Start with N [MASK] tokens
- For $t = 0$ to T
 - Predict the tokens using bidirectional transformer
 - Take n_t out N high confidence tokens ($n_T = N$)
 - Replace the mask tokens with these tokens

Draft and Revise

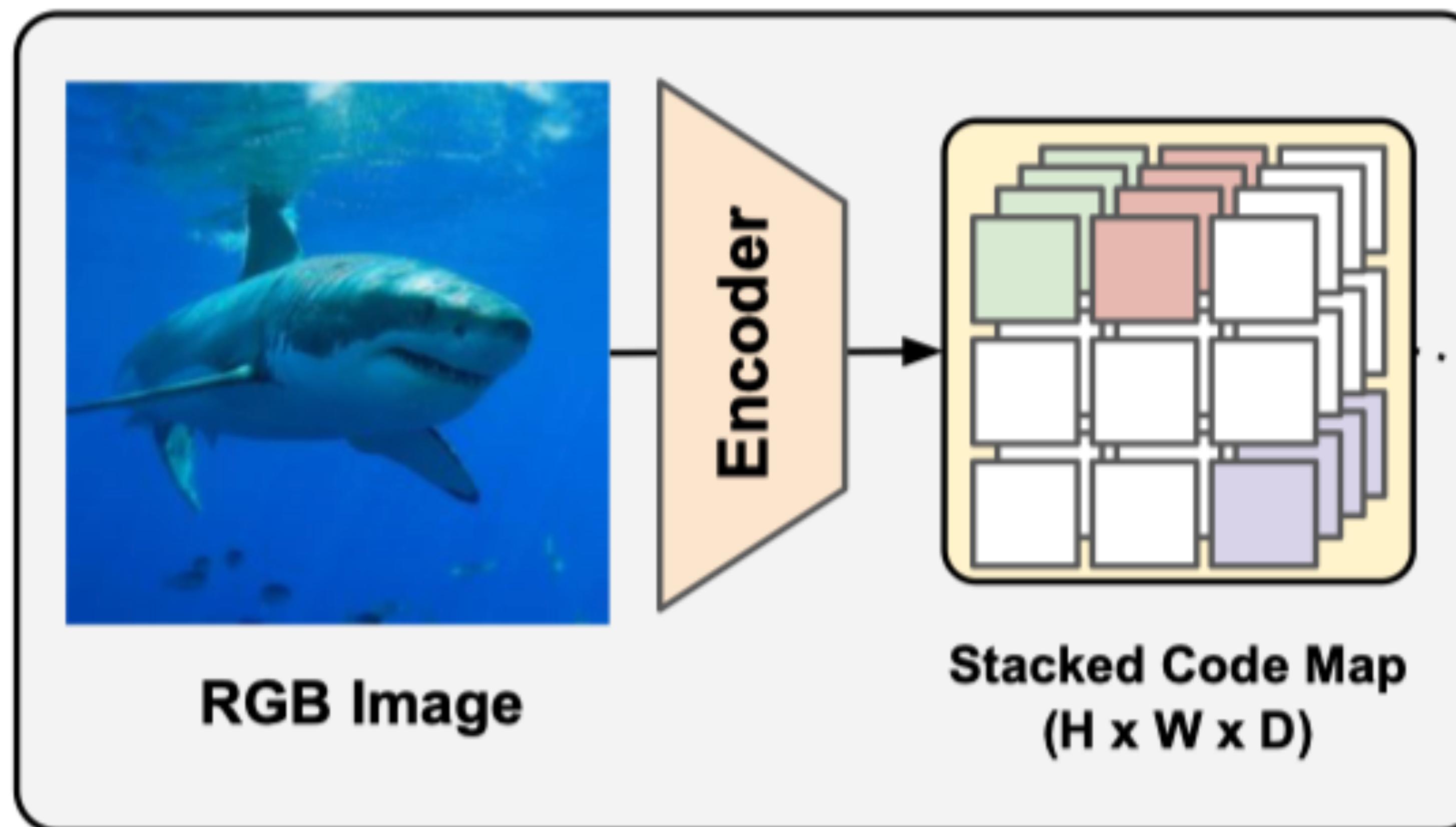
- ❖ Uses MaskGIT for model inference

Draft and Revise View (V)

- Step 1: Turn a image into $h \times w$ continuous latents
- Step 2: Turn those into discrete latents from codebook \mathcal{C}
- Step 3: Find the difference.
 - Go to step 2 if numbers of codes $< D$

Draft and Revise View (V)

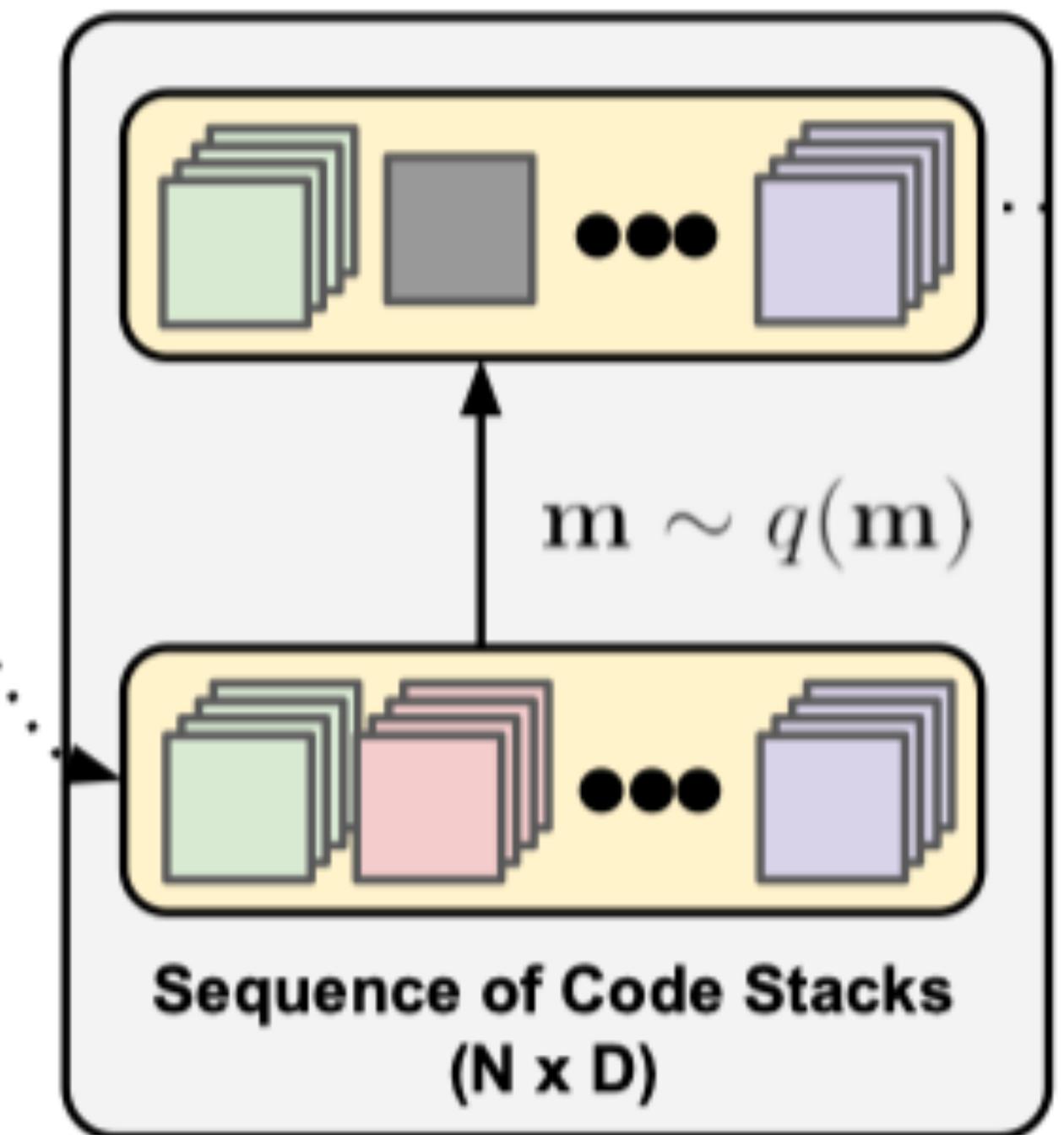
Tokenizing (RQ-VAE)



Draft and Revise Model (M)

- Similar to BERT training
- We construct a masked embedding sequence over time dimension
- The mask scheduling function is a strictly increasing function from $0 \rightarrow 1$
- The input to the transformer $\mathbf{u}_n = \text{PE}_N(n) + \begin{cases} \sum_{d=1}^D \mathbf{e}(\mathbf{S}_{nd}) & \text{if } \mathbf{m}_n = 0 \\ \mathbf{e}_{[\text{MASK}]} & \text{if } \mathbf{m}_n = 1 \end{cases}$
- The output $(\mathbf{h}_1, \dots, \mathbf{h}_N) = f_\theta^{\text{spatial}}(\mathbf{u}_1, \dots, \mathbf{u}_N)$.

Random Masking



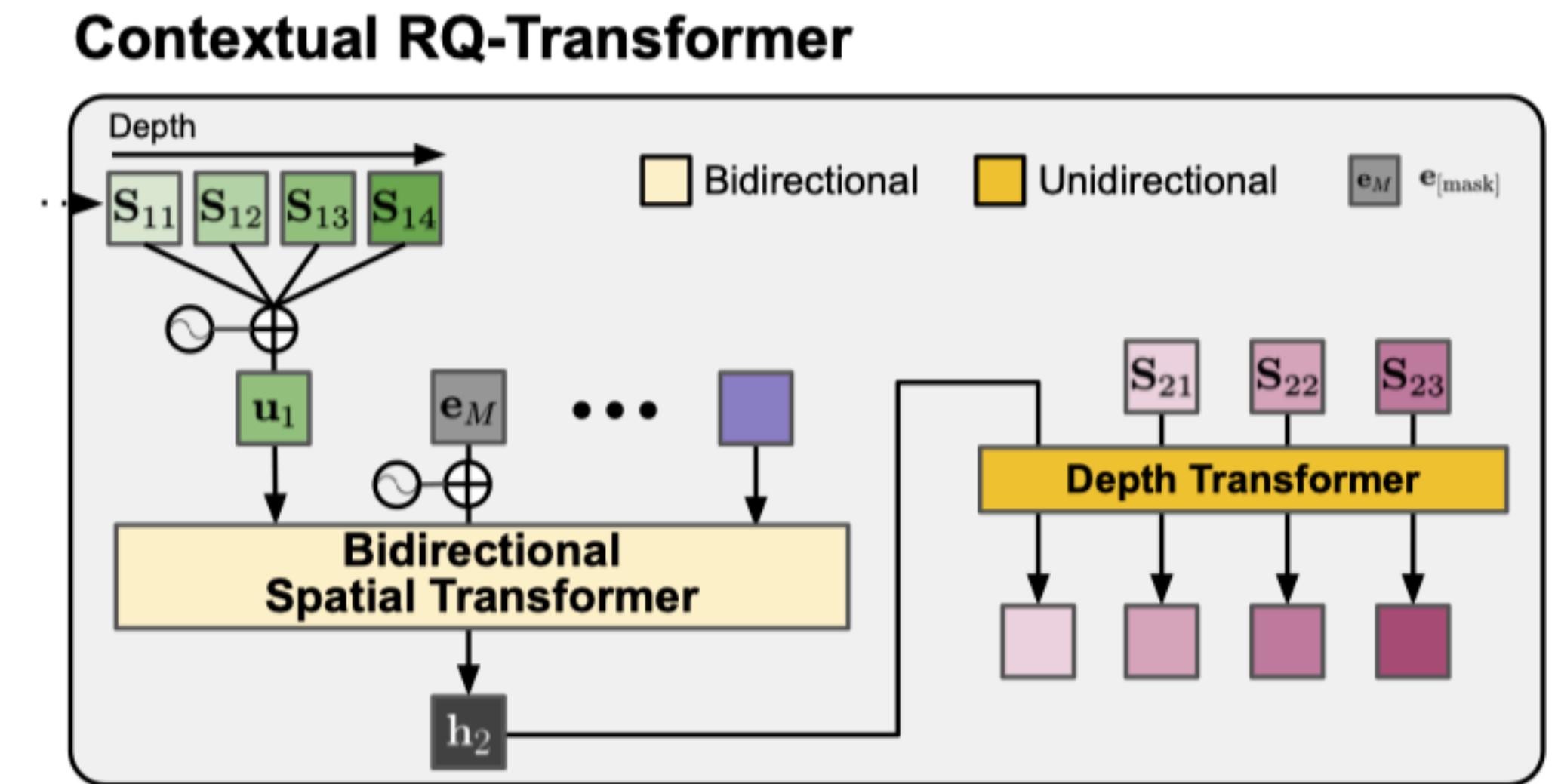
Draft and Revise Model (M)

Depth Transformer

- Autoregressive training
- We predict v_{nd} from $v_{n1, \dots, n(d-1)}$
- Input to the transformer $\mathbf{v}_{nd} = \text{PE}_D(d) + \begin{cases} \mathbf{h}_n & \text{if } d = 1 \\ \sum_{d'=1}^{d-1} \mathbf{e}(\mathbf{S}_{nd'}) & \text{if } d > 1 \end{cases}$
- Output of the transformer $\mathbf{p}_{nd} = f_\theta^{\text{depth}}(\mathbf{v}_{n1}, \dots, \mathbf{v}_{nd})$
- We find S_{nd} from sampling the softmax of p_{nd}

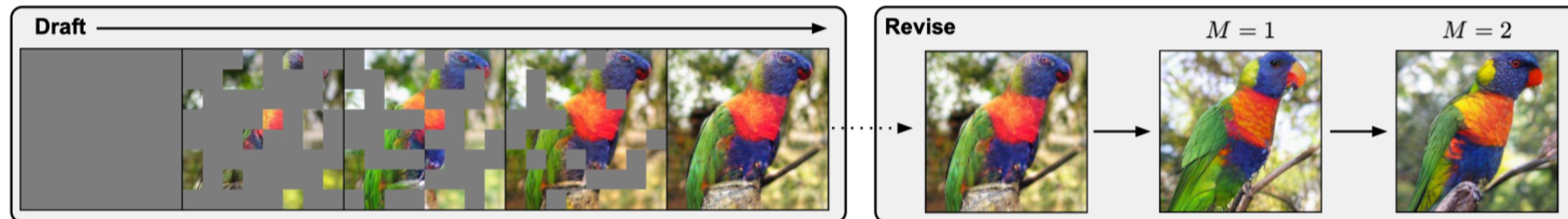
Draft and Revise Training

- Tokenize samples
- Sample masks
- Pass masked tokens and retrieve $\hat{S}_{11, \dots, N1}$
- From $\hat{S}_{11, \dots, N1}, \dots, \hat{S}_{1(t-1), \dots, N(t-1)}$, predict $\hat{S}_{1t, \dots, Nt}$
- Perform CE loss on masked code-stacks



Draft and Revise Inference

- Start with all masked positions
- **Draft:** Make a draft code-stack using bidirectional spatial transformer and depth transformer
- **Revise:** Update the code-stack conditioned on the previous one



Draft and Revise - What's there?

- ❖ V - RQ-VAE
- ❖ M - GPT and BERT

More...

- ❖ Better Model
 - ❖ Newer SSMs (S4, S5, etc.)
- ❖ Better representation for observations
 - ❖ CURL
 - ❖ STORM

More...

- ❖ Hierarchical World Modeling
 - ❖ Multi time scale world models using Gaussian marginalization and conditioning (MTS3)
- ❖ Hierarchical actors using goal-conditioning
 - ❖ Similar ideas as before
 - ❖ But, for more levels

Thank you

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