

COMP SCI 524 - Homework 3

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Q1

```
In [12]: using JuMP, NamedArrays

availability =
[ 0 0 1 1 0 0 0 1 1 0 0 0 0
  0 1 1 0 0 0 0 0 1 1 0 0 0
  0 0 0 1 1 0 1 1 0 1 1 1 1
  0 0 0 1 1 1 1 1 1 1 1 1 0
  0 0 0 0 0 0 1 1 1 0 0 0 0
  0 1 1 0 0 0 0 0 1 1 0 0 0
  0 0 0 1 1 1 1 0 0 0 0 0 0
  1 1 0 0 0 0 0 0 0 0 1 1 1
  1 1 1 0 0 0 0 0 0 1 1 0 0
  0 0 0 0 0 0 0 1 1 0 0 0 0
  0 0 0 0 0 0 1 1 1 0 0 0 0
  1 1 0 0 0 1 1 1 1 0 0 1 1
  1 1 1 0 1 1 0 0 0 0 0 1 1
  0 1 1 1 0 0 0 0 0 0 0 0 0
  1 1 0 0 1 1 0 0 0 0 0 0 0 ]

TIMES = ["10:00", "10:20", "10:40", "11:00", "11:20", "11:40", "lunch", "1:00", "1:20", "1:40", "2:00", "2:20", "2:40"]
NAMES = [:Manuel, :Luca, :Jule, :Michael, :Malte, :Chris, :Spyros, :Mirjam, :Matt, :Florian, :Josep, :Joel, :Tom, :Daniel, :Anne]
times = NamedArray(availability, (NAMES, TIMES), ("NAME", "TIME"))
```

Out[12]: 15×13 Named Array{Int64,2}

| NAME \ TIME | 10:00 | 10:20 | 10:40 | 11:00 | ... | 1:40 | 2:00 | 2:20 | 2:40 |
|-------------|-------|-------|-------|-------|-----|------|------|------|------|
| :Manuel | 0 | 0 | 1 | 1 | ... | 0 | 0 | 0 | 0 |
| :Luca | 0 | 1 | 1 | 0 | | 1 | 0 | 0 | 0 |
| :Jule | 0 | 0 | 0 | 1 | | 1 | 1 | 1 | 1 |
| :Michael | 0 | 0 | 0 | 1 | | 1 | 1 | 1 | 0 |
| :Malte | 0 | 0 | 0 | 0 | | 0 | 0 | 0 | 0 |
| :Chris | 0 | 1 | 1 | 0 | | 1 | 0 | 0 | 0 |
| :Spyros | 0 | 0 | 0 | 1 | | 0 | 0 | 0 | 0 |
| :Mirjam | 1 | 1 | 0 | 0 | | 0 | 1 | 1 | 1 |
| :Matt | 1 | 1 | 1 | 0 | | 1 | 1 | 0 | 0 |
| :Florian | 0 | 0 | 0 | 0 | | 0 | 0 | 0 | 0 |
| :Josep | 0 | 0 | 0 | 0 | | 0 | 0 | 0 | 0 |
| :Joel | 1 | 1 | 0 | 0 | | 0 | 0 | 1 | 1 |
| :Tom | 1 | 1 | 1 | 0 | | 0 | 0 | 1 | 1 |
| :Daniel | 0 | 1 | 1 | 1 | | 0 | 0 | 0 | 0 |
| :Anne | 1 | 1 | 0 | 0 | ... | 0 | 0 | 0 | 0 |

```
In [26]: using JuMP, Clp

m = Model(Clp.Optimizer)

@variable(m, 0 <= x[1:15,1:13] <= 1)

# meet candidate at some time slot for each senior
for i in 1:15
    @constraint(m, sum(x[i,:]) == 1)
end

# only one senior at each time slot except for lunch
for j in 1:6
    @constraint(m, sum(x[:,j]) == 1)
end

@constraint(m, sum(x[:,7]) == 3)

for j in 8:13
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@constraint(m, sum(x[:,j]) == 1)
end

@objective(m, Max, sum(x[i,j]*times[i,j] for i in 1:15, j in 1:13))

optimize!(m)
println(termination_status(m))

assignment = NamedArray( [ (value.(x[i,j])) for i in 1:15, j in 1:13 ], (NAMES, TIMES), ("NAME"
println(assignment)

```

OPTIMAL

15×13 Named Array{Float64,2}

NAME \ TIME | 10:00 10:20 10:40 11:00 ... 1:40 2:00 2:20 2:40

| | 10:00 | 10:20 | 10:40 | 11:00 | ... | 1:40 | 2:00 | 2:20 | 2:40 |
|----------|-------|-------|-------|-------|-----|------|------|------|------|
| :Manuel | 0.0 | 0.0 | 0.0 | 0.0 | ... | 0.0 | 0.0 | 0.0 | 0.0 |
| :Luca | 0.0 | 1.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0.0 | 0.0 |
| :Jule | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0.0 | 1.0 |
| :Michael | 0.0 | 0.0 | 0.0 | 1.0 | | 0.0 | 0.0 | 0.0 | 0.0 |
| :Malte | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0.0 | 0.0 |
| :Chris | 0.0 | 0.0 | 0.0 | 0.0 | | 1.0 | 0.0 | 0.0 | 0.0 |
| :Spyros | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0.0 | 0.0 |
| :Mirjam | 1.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0.0 | 0.0 |
| :Matt | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 1.0 | 0.0 | 0.0 |
| :Florian | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0.0 | 0.0 |
| :Josep | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0.0 | 0.0 |
| :Joel | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 0.0 | 0.0 |
| :Tom | 0.0 | 0.0 | 0.0 | 0.0 | | 0.0 | 0.0 | 1.0 | 0.0 |
| :Daniel | 0.0 | 0.0 | 1.0 | 0.0 | | 0.0 | 0.0 | 0.0 | 0.0 |
| :Anne | 0.0 | 0.0 | 0.0 | 0.0 | ... | 0.0 | 0.0 | 0.0 | 0.0 |

Coin0506I Presolve 28 (0) rows, 195 (0) columns and 390 (0) elements

Clp0006I 0 Obj 0 Primal inf 29.999997 (28) Dual inf 72.999993 (73)

Clp0006I 41 Obj 22 Primal inf 54.999998 (24)

Clp0006I 72 Obj 15 Primal inf 0.9999999 (1)

Clp0006I 73 Obj 15

Clp0000I Optimal - objective value 15

Clp0032I Optimal objective 15 - 73 iterations time 0.002

Q2

In this problem, I need to determine the internal transfer of cars among 10 agencies. $x[i, j]$ denotes the number of cars transferred from agency i to agency j , where $i = 2, 5, 8, 9, j = 1, 3, 4, 6, 7, 10$.

```

In [46]: using JuMP, Clp

m1 = Model(Clp.Optimizer)

cars_in = [1,3,4,6,7,10]
cars_out = [2,5,8,9]

xcoord = [0 20 18 30 35 33 5 5 11 2]
ycoord = [0 20 10 12 0 25 27 10 0 15]

@variable(m1, x[1:4, 1:6] >= 0)

# cars in
@constraint(m1, sum(x[:,1]) >= 2) #j=1
@constraint(m1, sum(x[:,2]) >= 4) #j=3
@constraint(m1, sum(x[:,3]) >= 3) #j=4
@constraint(m1, sum(x[:,4]) >= 5) #j=6
@constraint(m1, sum(x[:,5]) >= 1) #j=7
@constraint(m1, sum(x[:,6]) >= 5) #j=10

#cars out
@constraint(m1, sum(x[1,:]) <= 7) #i=2
@constraint(m1, sum(x[2,:]) <= 3) #i=5
@constraint(m1, sum(x[3,:]) <= 4) #i=8
@constraint(m1, sum(x[4,:]) <= 7) #i=9

```

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@objective(m1, Min, sum( 0.5*x[i, j]*1.3*sqrt((xcoord[cars_out[i]]-xcoord[cars_in[j]])^2
+ (ycoord[cars_out[i]]-ycoord[cars_in[j]])^2) for i in 1:4, j in 1:6))

optimize!(m1)
println("The total minimum cost incurred for transport: ", objective_value(m1))
println("The movement is shown below (i is the vertical index, j is the horizontal index):")
for i in 1:4
    for j in 1:6
        print(getvalue(x[i, j]), " ")
    end
    println()
end
end

```

```

The total minimum cost incurred for transport: 152.63901632295628
The movement is shown below (i is the vertical index, j is the horizontal index):
0.0  1.0  0.0  5.0  1.0  0.0
0.0  0.0  3.0  0.0  0.0  0.0
0.0  0.0  0.0  0.0  0.0  4.0
2.0  3.0  0.0  0.0  0.0  1.0
Coin0506I Presolve 10 (0) rows, 24 (0) columns and 48 (0) elements
Clp0006I 0 Obj 0 Primal inf 19.999999 (6)
Clp0006I 10 Obj 152.63902
Clp0000I Optimal - objective value 152.63902
Clp0032I Optimal objective 152.6390163 - 10 iterations time 0.002

```

Q3

(a)

```

In [47]: tasks = 1:18
durations = [2 16 9 8 10 6 2 2 9 5 3 2 1 7 4 3 9 1]
predecessors = ( [], [1], [2], [2], [3], [4,5], [4], [6], [4,6], [4], [6], [9], [7], [2], [4,14],
pred_dict = Dict{zip(tasks, predecessors)}; # dictionary mapping tasks --> predecessors.

```

```

Out[47]: Dict{Int64,Array{T,1} where T} with 18 entries:
 18 => [17]
  2 => [1]
 16 => [8, 11, 14]
 11 => [6]
  7 => [4]
  9 => [4, 6]
 10 => [4]
 17 => [12]
  8 => [6]
  6 => [4, 5]
  4 => [2]
  3 => [2]
  5 => [3]
 13 => [7]
 14 => [2]
 15 => [4, 14]
 12 => [9]
  1 => Any[]

```

```

In [60]: using JuMP, Clp
m2 = Model(Clp.Optimizer)

@variable(m2, tstart[tasks]>=0)

for i in tasks
    for j in pred_dict[i]
        @constraint(m2, tstart[i] >= tstart[j] + durations[j])
    end
end
@constraint(m2, tstart[1] == 0)
@objective(m2, Min, tstart[18] + durations[18])

optimize!(m2)
println("Earliest possible completion date: ", getobjectivevalue(m2))
for i in tasks

```

```
println("Task ", i, " date of completion: ", getvalue(tstart[i]))
end
```

```
Earliest possible completion date: 64.0
Task 1 date of completion: 0.0
Task 2 date of completion: 2.0
Task 3 date of completion: 18.0
Task 4 date of completion: 18.0
Task 5 date of completion: 27.0
Task 6 date of completion: 37.0
Task 7 date of completion: 26.0
Task 8 date of completion: 43.0
Task 9 date of completion: 43.0
Task 10 date of completion: 26.0
Task 11 date of completion: 43.0
Task 12 date of completion: 52.0
Task 13 date of completion: 28.0
Task 14 date of completion: 18.0
Task 15 date of completion: 26.0
Task 16 date of completion: 46.0
Task 17 date of completion: 54.0
Task 18 date of completion: 63.0
Coin0506I Presolve 0 (-23) rows, 0 (-18) columns and 0 (-45) elements
Clp3002W Empty problem - 0 rows, 0 columns and 0 elements
Clp0000I Optimal - objective value 64
Coin0511I After Postsolve, objective 64, infeasibilities - dual 0 (0), primal 0 (0)
Clp0032I Optimal objective 64 - 0 iterations time 0.002, Presolve 0.00
```

(b)

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In [67]: # additional columns of data (maximum reduction possible )
max_reduction = [0, 3, 1, 2, 2, 1, 1, 0, 2, 1, 1, 0, 0, 2, 2, 1, 3, 0] # max reduction
cost_reduction = [0, 30, 26, 12, 17, 15, 8, 0, 42, 21, 18, 0, 0, 22, 12, 6, 16, 0] # cost of reduction
bonus_amount = 30 # bonus for expediting the project ($1,000/week )
```

Out[67]: 30

```
In [68]: using JuMP, Clp
m3 = Model(Clp.Optimizer)

@variable(m3, tstart[tasks] >= 0)
@variable(m3, treduct[tasks] >= 0)

for i in tasks
    @constraint(m3, treduct[i] <= max_reduction[i])
end

for i in tasks
    for j in pred_dict[i]
        @constraint(m3, tstart[i] >= tstart[j] + durations[j] - treduct[i])
    end
end
@constraint(m3, tstart[1] == 0)
@objective(m3, Max, bonus_amount*(64-tstart[18]-durations[18])-sum(cost_reduction[i]*treduct[i]

optimize!(m3)
println("Maximum profit: ", getobjectivevalue(m3))
println("Earliest date of completion: ", getvalue(tstart[18]) + durations[18])
for i in tasks
    println("Task ", i, " date of completion: ", getvalue(tstart[i]))
end
```

```
Maximum profit: 87.0
Earliest date of completion: 57.0
Task 1 date of completion: 0.0
Task 2 date of completion: 2.0
Task 3 date of completion: 17.0
Task 4 date of completion: 18.0
Task 5 date of completion: 24.0
Task 6 date of completion: 33.0
Task 7 date of completion: 26.0
Task 8 date of completion: 39.0
```

Task 9 date of completion: 39.0
Task 10 date of completion: 26.0
Task 11 date of completion: 39.0
Task 12 date of completion: 48.0
Task 13 date of completion: 28.0
Task 14 date of completion: 18.0
Task 15 date of completion: 26.0
Task 16 date of completion: 42.0
Task 17 date of completion: 47.0
Task 18 date of completion: 56.0
Coin0506I Presolve 5 (-36) rows, 9 (-27) columns and 18 (-67) elements
Clp0006I 0 Obj 273 Primal inf 11.199997 (3)
Clp0006I 3 Obj 87
Clp0000I Optimal - objective value 87
Coin0511I After Postsolve, objective 87, infeasibilities - dual 0 (0), primal 0 (0)
Clp0032I Optimal objective 87 - 3 iterations time 0.002, Presolve 0.00