Inner Minkowski Dimension of a Fractal String

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: $D_{\Omega} = \inf \{ \alpha \geq 0 \mid V(\epsilon) = O(\epsilon^{1-\alpha}) \text{ as } \epsilon \to 0^+ \}$



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Cantor String Dimension: $D_{cs} = \log_3 2$

