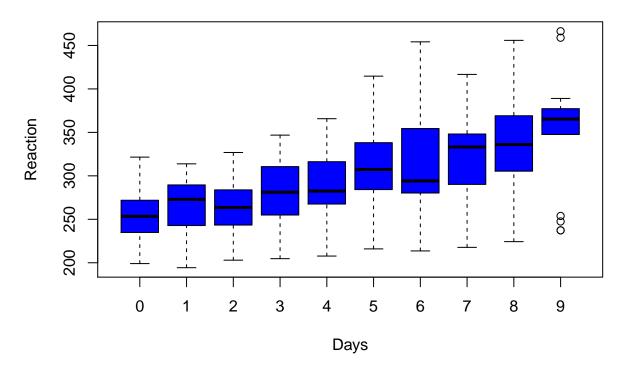
Comparison of P values from linear and linear mixed models

This is provided by the lmerTest package as illustrated fully with the documentation example here.

Reaction by Days

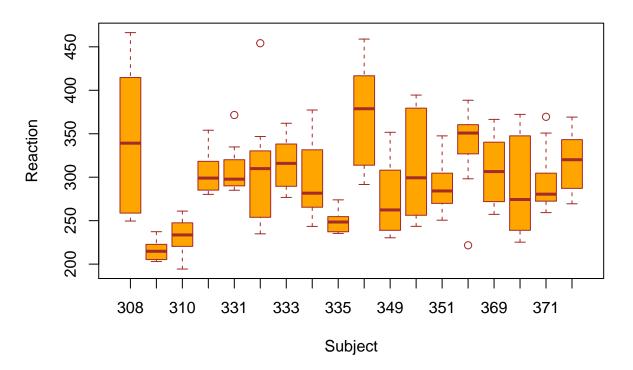


We see a trend of Reaction by Days, so it is reasonable to fit a simple linear regression,

```
1 <- lm(Reaction ~ Days, sleepstudy)</pre>
s <- summary(1)
s
##
## Call:
## lm(formula = Reaction ~ Days, data = sleepstudy)
##
## Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
  -110.848 -27.483
                         1.546
                                 26.142
                                         139.953
##
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 251.405
                              6.610
                                     38.033 < 2e-16 ***
                 10.467
                              1.238
                                      8.454 9.89e-15 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

```
##
## Residual standard error: 47.71 on 178 degrees of freedom
## Multiple R-squared: 0.2865, Adjusted R-squared: 0.2825
## F-statistic: 71.46 on 1 and 178 DF, p-value: 9.894e-15
names(s)
    [1] "call"
##
                         "terms"
                                         "residuals"
                                                          "coefficients"
##
    [5] "aliased"
                         "sigma"
                                                          "r.squared"
    [9] "adj.r.squared" "fstatistic"
                                         "cov.unscaled"
Now the Subject effect is treated as a random; from
boxplot(Reaction~Subject, data=sleepstudy, main="Reaction by Subject",
        xlab="Subject", ylab="Reaction", col="orange", border="brown")
```

Reaction by Subject



it is more approriate to fit a random effect model

```
f <- lme4::lmer(Reaction ~ Days + (Days | Subject), sleepstudy)
s <- summary(f)
s
## Linear mixed model fit by REML ['lmerMod']
  Formula: Reaction ~ Days + (Days | Subject)
##
      Data: sleepstudy
##
## REML criterion at convergence: 1743.6
##
## Scaled residuals:
##
       Min
                                 ЗQ
                1Q Median
                                        Max
```

```
## -3.9536 -0.4634 0.0231 0.4633 5.1793
##
## Random effects:
                          Variance Std.Dev. Corr
    Groups
             Name
##
    Subject (Intercept) 611.90
                                   24.737
##
                           35.08
                                     5.923
                                             0.07
             Days
                          654.94
                                    25.592
   Residual
## Number of obs: 180, groups: Subject, 18
##
## Fixed effects:
               Estimate Std. Error t value
                              6.824 36.843
## (Intercept) 251.405
                  10.467
                              1.546
                                       6.771
## Days
##
## Correlation of Fixed Effects:
##
        (Intr)
## Days -0.138
names(s)
   [1] "methTitle"
                        "objClass"
                                        "devcomp"
                                                        "isLmer"
##
   [5] "useScale"
                        "logLik"
                                        "family"
                                                        "link"
   [9] "ngrps"
                        "coefficients" "sigma"
                                                        "vcov"
## [13] "varcor"
                        "AICtab"
                                        "call"
                                                        "residuals"
## [17] "fitMsgs"
                        "optinfo"
We saw the same estimate of effect but a larger standard error for Days in the linear mixed model compared
to that in the linear regression model.
m <- lmerTest::lmer(Reaction ~ Days + (Days | Subject), sleepstudy)</pre>
class(m)
## [1] "lmerModLmerTest"
## attr(,"package")
## [1] "lmerTest"
s <-summary(m)
names(s)
                        "objClass"
   [1] "methTitle"
                                        "devcomp"
                                                        "isLmer"
##
   [5] "useScale"
                        "logLik"
                                        "family"
                                                        "link"
## [9] "ngrps"
                        "coefficients" "sigma"
                                                        "vcov"
## [13] "varcor"
                        "AICtab"
                                        "call"
                                                        "residuals"
## [17] "fitMsgs"
                        "optinfo"
with(s,coefficients)[,5]
## (Intercept)
                         Days
## 1.158238e-17 3.273014e-06
```