323.25 Project 5: Kruskal MST

Student: Jingshi Liu

Due Date: 3/27/2022

# **Algorithm Steps for the Project:**

```
Step 0: inFile, outFile1, outFile2 < - open via args[] as given in the above
       numNodes < - inFile
       numSets < - numNodes
       whichSet <- allocate space, size of numNodes + 1, set whichSet[i] to i, i from 1 to
       numNodes+1 edgeHead <-get a dummy edge <0,0,0, null>
       mstHead <- get a dummy edge<0,0,0, null>
       totalMSTCost <- 0
Step 1: <Ni, Nj, cost> <-read from inFile newEdge <-get a new edge (Ni, Nj, cost)
Step 2: insert (newEdge, edgeHead)
Step 3: printList (edgeHead, outFile2)
Step 4: repeat step 1 to step 3 while inFile is not empty
Step 5: nextEdge < -- removeEdge (edgeHead)
Step 6: repeat Step 5 while whichSet [nextEdge.Ni] == whichSet [nextEdge.Nj] // Ni and Nj
cannot be in the same set
Step 7: push (nextEdge, mstHead)
       totalMSTCost += nextEdge.cost
       merge2Sets (nextEdge,Ni, nextEdge.Nj)
       numSets --
Step 8: printAry(whichSet)
Step 9: printList (edgeHead, outFile2) // with caption indicating which edge list you are printing.
       printList (mstHead, outFile2) // with caption indicating which edge list you are printing.
Step 10: repeat step 5 – step 9 while numSets > 1
Step 11: printList (mstHead, outFile1)
Step 12: close all files.
```

## **Source Code:**

```
package com.company;
import java.io.*;
import java.util.Scanner;
class Edge{
    int Ni, Nj, cost;
    Edge next;
    Edge(int n1, int n2, int cost){
        Ni = n1;
        Nj = n2;
        this.cost = cost;
        next = null;
    }
    String printEdge(){
        return "<" + Ni + ", " + Nj + ", " + cost + "> -> ";
    }
}
class KruskalMST{
    int num_nodes;
    int[] which_set;
    int num_sets;
    int total_MST_cost;
    Edge edge_head = new Edge(0,0,0);
```

```
Edge mst_head = new Edge(0,0,0);
KruskalMST(int numNodes){
    num_nodes = numNodes;
    which_set = new int[num_nodes+1];
    for (int i = 0; i < which_set.length; i++) {</pre>
        which_set[i] = i;
    }
    num_sets = num_nodes;
}
void insert(Edge new edge){
    Edge spot = edge_head;
    while(spot.next != null && spot.next.cost < new_edge.cost){</pre>
        spot = spot.next;
    }
    new edge.next = spot.next;
    spot.next = new_edge;
}
Edge removeEdge(){
    if(edge_head.next == null)
        return null;
    Edge res = edge_head.next;
    edge_head.next = edge_head.next.next;
    res.next = null;
    return res;
```

```
}
void mergeSets(int Ni, int Nj){
    int set_of_Ni = which_set[Ni], set_of_Nj = which_set[Nj];
    if( set of Ni > set of Nj)
        for (int i = 0; i < which_set.length; i++) {</pre>
            if(which_set[i] == set of Ni)
                which_set[i] = set_of_Nj;
        }
    else
        for (int i = 0; i < which_set.length; i++) {</pre>
            if(which_set[i] == set of Nj)
                which_set[i] = set of Ni;
        }
}
void push(Edge nextEdge){
    nextEdge.next = mst_head.next;
    mst_head.next = nextEdge;
}
void printArray(BufferedWriter outFile) throws IOException {
    String res = "Which Set: ";
    for(int i: which_set)
        res += i + " ";
    outFile.write(res + "\n");
}
```

```
void printList(BufferedWriter outFile, Edge head) throws
IOException {
        Edge pointer;
        String res = "";
        if(head == edge_head){
            pointer = edge_head;
            res += "Edge List: ";
        }else {
            pointer = mst_head;
            res += "MST List: ";
        }
        while(pointer != null){
            res += pointer.printEdge();
            pointer = pointer.next;
        }
        outFile.write(res + " null\n");
    }
}
public class Main {
    public static void main(String[] args) throws IOException {
         Scanner input = new Scanner(new File(args[0]));
        BufferedWriter outFile1 = new BufferedWriter(new
FileWriter(args[1], true));
```

```
BufferedWriter outFile2 = new BufferedWriter(new
FileWriter(args[2], true));
        int num nodes = input.nextInt();
        KruskalMST kruskalMST = new KruskalMST(num nodes);
        outFile2.write("Reading:\n");
        int n1, n2, cost;
        try{
            while(input.hasNextLine()){
                n1 = input.nextInt();
                n2 = input.nextInt();
                cost = input.nextInt();
                kruskalMST.insert(new Edge(n1, n2, cost));
                kruskalMST.printList(outFile2, kruskalMST.edge head);
            }
        }catch (Exception ignored){
        }
        outFile2.write("\n\nConstructing Minimum Spanning Tree:\n");
        Edge nextEdge;
        while(kruskalMST.num_sets > 1){
            do{
                nextEdge = kruskalMST.removeEdge();
            }while(nextEdge != null &&
kruskalMST.which_set[nextEdge.Ni] ==
kruskalMST.which_set[nextEdge.Nj]);
```

```
if(nextEdge == null)
                break;
            kruskalMST.push(nextEdge);
            kruskalMST.total_MST_cost += nextEdge.cost;
            kruskalMST.mergeSets(nextEdge.Ni, nextEdge.Nj);
            kruskalMST.num sets--;
            kruskalMST.printArray(outFile2);
            kruskalMST.printList(outFile2, kruskalMST.edge_head);
            kruskalMST.printList(outFile2, kruskalMST.mst_head);
            outFile2.write("\n");
        }
        kruskalMST.printList(outFile1, kruskalMST.mst_head);
        outFile1.write("Total cost is: " + kruskalMST.total MST cost);
       outFile1.close();
        outFile2.close();
    }
}
```

## **Output:**

#### Data1:

6

126

131

143

235

3 4 2

254

356

363

462

566

## **OutFile1 for Data 1:**

MST List: <0, 0, 0> -> <2, 3, 5> -> <2, 5, 4> -> <3, 4, 2> -> <4, 6, 2> -> <1, 3, 1> -> null

Total cost is: 14

# OutFile2 (Debugging) for Data 2:

#### Reading:

Edge List: <0, 0, 0> -> <1, 2, 6> -> null

Edge List: <0, 0, 0> -> <1, 3, 1> -> <1, 2, 6> -> null

Edge List: <0, 0, 0> -> <1, 3, 1> -> <1, 4, 3> -> <1, 2, 6> -> null

Edge List: <0, 0, 0> -> <1, 3, 1> -> <1, 4, 3> -> <2, 3, 5> -> <1, 2, 6> -> null

Edge List: <0, 0, 0> -> <1, 3, 1> -> <3, 4, 2> -> <1, 4, 3> -> <2, 3, 5> -> <1, 2, 6> -> null

Edge List: <0, 0, 0> -> <1, 3, 1> -> <3, 4, 2> -> <1, 4, 3> -> <2, 5, 4> -> <2, 3, 5> -> <1, 2, 6> -> null

Edge List: <0, 0, 0> -> <1, 3, 1> -> <3, 4, 2> -> <1, 4, 3> -> <2, 5, 4> -> <2, 3, 5> -> <3, 5, 6> -> <1, 2, 6> -> null

Edge List: <0, 0, 0> -> <1, 3, 1> -> <3, 4, 2> -> <3, 6, 3> -> <1, 4, 3> -> <2, 5, 4> -> <2, 3, 5> -> <3, 5, 6> -> <1, 2, 6> -> null

Edge List: <0, 0, 0> -> <1, 3, 1> -> <4, 6, 2> -> <3, 4, 2> -> <3, 6, 3> -> <1, 4, 3> -> <2, 5, 4> -> <2, 3, 5> -> <3, 5, 6> -> <1, 2, 6> -> null

Edge List: <0, 0, 0> -> <1, 3, 1> -> <4, 6, 2> -> <3, 4, 2> -> <3, 6, 3> -> <1, 4, 3> ->

<2, 5, 4> -> <2, 3, 5> -> <5, 6, 6> -> <3, 5, 6> -> <1, 2, 6> -> null

## Constructing Minimum Spanning Tree:

Which Set: 0 1 2 1 4 5 6

Edge List: <0, 0, 0> -> <4, 6, 2> -> <3, 4, 2> -> <3, 6, 3> -> <1, 4, 3> -> <2, 5, 4> -> <2, 3, 5> -> <5, 6, 6> -> <3, 5, 6> -> <1, 2, 6> -> null

MST List: <0, 0, 0> -> <1, 3, 1> -> null

```
Which Set: 0 1 2 1 4 5 4
```

Edge List: <0, 0, 0> -> <3, 4, 2> -> <3, 6, 3> -> <1, 4, 3> -> <2, 5, 4> -> <2, 3, 5> -> <5, 6, 6> -> <3, 5, 6> -> <1, 2, 6> -> null

MST List: <0, 0, 0> -> <4, 6, 2> -> <1, 3, 1> -> null

### Which Set: 0 1 2 1 1 5 1

Edge List: <0, 0, 0> -> <3, 6, 3> -> <1, 4, 3> -> <2, 5, 4> -> <2, 3, 5> -> <5, 6, 6> ->

<3, 5, 6> -> <1, 2, 6> -> null

MST List: <0, 0, 0> -> <3, 4, 2> -> <4, 6, 2> -> <1, 3, 1> -> null

#### Which Set: 0 1 2 1 1 2 1

Edge List: <0, 0, 0> -> <2, 3, 5> -> <5, 6, 6> -> <3, 5, 6> -> <1, 2, 6> -> null MST List: <math><0, 0, 0> -> <2, 5, 4> -> <3, 4, 2> -> <4, 6, 2> -> <1, 3, 1> -> null

## Which Set: 0 1 1 1 1 1 1

Edge List: <0, 0, 0> -> <5, 6, 6> -> <3, 5, 6> -> <1, 2, 6> -> null

MST List: <0, 0, 0> -> <2, 3, 5> -> <2, 5, 4> -> <3, 4, 2> -> <4, 6, 2> -> <1, 3, 1> ->

null

#### Data 2:

12

643

12 7 4

6 12 7

10 12 7

9 10 4

2 4 1

9 11 5

325

575

163

862

982

8 10 1

5 4 2

433

126

1 11 6

3 5 4

672

#### OutFile1 for Data 2:

MST List: <0, 0, 0> -> <9, 11, 5> -> <12, 7, 4> -> <6, 4, 3> -> <1, 6, 3> -> <4, 3, 3> -> <8, 6, 2> -> <9, 8, 2> -> <5, 4, 2> -> <6, 7, 2> -> <2, 4, 1> -> <8, 10, 1> -> null Total cost is: 28

```
OutFile 2 for Data 2:
Reading:
Edge List: <0, 0, 0> -> <6, 4, 3> ->  null
Edge List: <0, 0, 0> -> <6, 4, 3> -> <12, 7, 4> ->  null
Edge List: <0, 0, 0> -> <6, 4, 3> -> <12, 7, 4> -> <6, 12, 7> -> null
Edge List: <0, 0, 0> -> <6, 4, 3> -> <12, 7, 4> -> <10, 12, 7> -> <6, 12, 7> -> null
Edge List: <0, 0, 0> -> <6, 4, 3> -> <9, 10, 4> -> <12, 7, 4> -> <10, 12, 7> -> <6, 12, 7>
-> null
Edge List: <0, 0, 0> -> <2, 4, 1> -> <6, 4, 3> -> <9, 10, 4> -> <12, 7, 4> -> <10, 12, 7>
-><6, 12, 7>->  null
Edge List: <0, 0, 0> -> <2, 4, 1> -> <6, 4, 3> -> <9, 10, 4> -> <12, 7, 4> -> <9, 11, 5> -
> <10, 12, 7> -> <6, 12, 7> -> null
Edge List: <0, 0, 0> -> <2, 4, 1> -> <6, 4, 3> -> <9, 10, 4> -> <12, 7, 4> -> <3, 2, 5> ->
<9, 11, 5> -> <10, 12, 7> -> <6, 12, 7> -> null
Edge List: <0, 0, 0> -> <2, 4, 1> -> <6, 4, 3> -> <9, 10, 4> -> <12, 7, 4> -> <5, 7, 5> ->
<3, 2, 5> -> <9, 11, 5> -> <10, 12, 7> -> <6, 12, 7> -> null
Edge List: <0, 0, 0> -> <2, 4, 1> -> <1, 6, 3> -> <6, 4, 3> -> <9, 10, 4> -> <12, 7, 4> ->
<5, 7, 5> -> <3, 2, 5> -> <9, 11, 5> -> <10, 12, 7> -> <6, 12, 7> -> null
Edge List: <0, 0, 0> -> <2, 4, 1> -> <8, 6, 2> -> <1, 6, 3> -> <6, 4, 3> -> <9, 10, 4> ->
<12, 7, 4> -> <5, 7, 5> -> <3, 2, 5> -> <9, 11, 5> -> <10, 12, 7> -> <6, 12, 7> -> null
Edge List: <0, 0, 0> -> <2, 4, 1> -> <9, 8, 2> -> <8, 6, 2> -> <1, 6, 3> -> <6, 4, 3> ->
<9, 10, 4> -> <12, 7, 4> -> <5, 7, 5> -> <3, 2, 5> -> <9, 11, 5> -> <10, 12, 7> -> <6,
12, 7 > - > \text{null}
Edge List: <0, 0, 0> -> <8, 10, 1> -> <2, 4, 1> -> <9, 8, 2> -> <8, 6, 2> -> <1, 6, 3> ->
<6, 4, 3> -> <9, 10, 4> -> <12, 7, 4> -> <5, 7, 5> -> <3, 2, 5> -> <9, 11, 5> -> <10, 12,
7 > - > < 6, 12, 7 > - >  null
Edge List: <0, 0, 0> -> <8, 10, 1> -> <2, 4, 1> -> <5, 4, 2> -> <9, 8, 2> -> <8, 6, 2> ->
<1, 6, 3> -> <6, 4, 3> -> <9, 10, 4> -> <12, 7, 4> -> <5, 7, 5> -> <3, 2, 5> -> <9, 11, 5>
-> <10, 12, 7> -> <6, 12, 7> -> null
Edge List: <0, 0, 0> -> <8, 10, 1> -> <2, 4, 1> -> <5, 4, 2> -> <9, 8, 2> -> <8, 6, 2> ->
<4, 3, 3> -> <1, 6, 3> -> <6, 4, 3> -> <9, 10, 4> -> <12, 7, 4> -> <5, 7, 5> -> <3, 2, 5>
-> <9, 11, 5> -> <10, 12, 7> -> <6, 12, 7> -> null
Edge List: <0, 0, 0> -> <8, 10, 1> -> <2, 4, 1> -> <5, 4, 2> -> <9, 8, 2> -> <8, 6, 2> ->
<4, 3, 3> -> <1, 6, 3> -> <6, 4, 3> -> <9, 10, 4> -> <12, 7, 4> -> <5, 7, 5> -> <3, 2, 5>
-> <9, 11, 5> -> <1, 2, 6> -> <10, 12, 7> -> <6, 12, 7> -> null
Edge List: <0, 0, 0> -> <8, 10, 1> -> <2, 4, 1> -> <5, 4, 2> -> <9, 8, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 6, 2> -> <8, 
<4, 3, 3> -> <1, 6, 3> -> <6, 4, 3> -> <9, 10, 4> -> <12, 7, 4> -> <5, 7, 5> -> <3, 2, 5>
-> <9, 11, 5> -> <1, 11, 6> -> <1, 2, 6> -> <10, 12, 7> -> <6, 12, 7> -> null
Edge List: <0, 0, 0> -> <8, 10, 1> -> <2, 4, 1> -> <5, 4, 2> -> <9, 8, 2> -> <8, 6, 2> ->
<4, 3, 3> -> <1, 6, 3> -> <6, 4, 3> -> <3, 5, 4> -> <9, 10, 4> -> <12, 7, 4> -> <5, 7, 5>
-> <3, 2, 5> -> <9, 11, 5> -> <1, 11, 6> -> <1, 2, 6> -> <10, 12, 7> -> <6, 12, 7> ->
```

Edge List: <0, 0, 0> -> <8, 10, 1> -> <2, 4, 1> -> <6, 7, 2> -> <5, 4, 2> -> <9, 8, 2> -> <8, 6, 2> -> <4, 3, 3> -> <1, 6, 3> -> <6, 4, 3> -> <3, 5, 4> -> <9, 10, 4> -> <12, 7, 4>

-> <5, 7, 5> -> <3, 2, 5> -> <9, 11, 5> -> <1, 11, 6> -> <1, 2, 6> -> <10, 12, 7> -> <6, 12, 7> -> null

## Constructing Minimum Spanning Tree:

Which Set: 0 1 2 3 4 5 6 7 8 9 8 11 12

Edge List: <0, 0, 0> -> <2, 4, 1> -> <6, 7, 2> -> <5, 4, 2> -> <9, 8, 2> -> <8, 6, 2> -> <4, 3, 3> -> <1, 6, 3> -> <6, 4, 3> -> <3, 5, 4> -> <9, 10, 4> -> <12, 7, 4> -> <5, 7, 5> -> <3, 2, 5> -> <9, 11, 5> -> <1, 11, 6> -> <1, 2, 6> -> <10, 12, 7> -> <6, 12, 7> -> null

MST List: <0, 0, 0> -> <8, 10, 1> -> null

## Which Set: 0 1 2 3 2 5 6 7 8 9 8 11 12

Edge List: <0, 0, 0> -> <6, 7, 2> -> <5, 4, 2> -> <9, 8, 2> -> <8, 6, 2> -> <4, 3, 3> -> <1, 6, 3> -> <6, 4, 3> -> <3, 5, 4> -> <9, 10, 4> -> <12, 7, 4> -> <5, 7, 5> -> <3, 2, 5> -> <9, 11, 5> -> <1, 11, 6> -> <1, 2, 6> -> <10, 12, 7> -> <6, 12, 7> -> null MST List: <math><0, 0, 0> -> <2, 4, 1> -> <8, 10, 1> -> null

## Which Set: 0 1 2 3 2 5 6 6 8 9 8 11 12

Edge List: <0, 0, 0> -> <5, 4, 2> -> <9, 8, 2> -> <8, 6, 2> -> <4, 3, 3> -> <1, 6, 3> -> <6, 4, 3> -> <3, 5, 4> -> <9, 10, 4> -> <12, 7, 4> -> <5, 7, 5> -> <3, 2, 5> -> <9, 11, 5> -> <1, 11, 6> -> <1, 2, 6> -> <10, 12, 7> -> <6, 12, 7> -> null MST List: <math><0, 0, 0> -> <6, 7, 2> -> <2, 4, 1> -> <8, 10, 1> -> null

#### Which Set: 0 1 2 3 2 2 6 6 8 9 8 11 12

Edge List: <0, 0, 0> -> <9, 8, 2> -> <8, 6, 2> -> <4, 3, 3> -> <1, 6, 3> -> <6, 4, 3> -> <3, 5, 4> -> <9, 10, 4> -> <12, 7, 4> -> <5, 7, 5> -> <3, 2, 5> -> <9, 11, 5> -> <1, 11, 6> -> <1, 2, 6> -> <10, 12, 7> -> <6, 12, 7> -> null MST List: <math><0, 0, 0> -> <5, 4, 2> -> <6, 7, 2> -> <2, 4, 1> -> <8, 10, 1> -> null

#### Which Set: 0 1 2 3 2 2 6 6 8 8 8 11 12

Edge List: <0, 0, 0> -> <8, 6, 2> -> <4, 3, 3> -> <1, 6, 3> -> <6, 4, 3> -> <3, 5, 4> -> <9, 10, 4> -> <12, 7, 4> -> <5, 7, 5> -> <3, 2, 5> -> <9, 11, 5> -> <1, 11, 6> -> <1, 2, 6> -> <10, 12, 7> -> <6, 12, 7> -> null MST List: <math><0, 0, 0> -> <9, 8, 2> -> <5, 4, 2> -> <6, 7, 2> -> <2, 4, 1> -> <8, 10, 1> -> null

### Which Set: 0 1 2 3 2 2 6 6 6 6 6 11 12

Edge List: <0, 0, 0> -> <4, 3, 3> -> <1, 6, 3> -> <6, 4, 3> -> <3, 5, 4> -> <9, 10, 4> -> <12, 7, 4> -> <5, 7, 5> -> <3, 2, 5> -> <9, 11, 5> -> <1, 11, 6> -> <1, 2, 6> -> <10, 12, 7> -> <6, 12, 7> -> null MST List: <math><0, 0, 0> -> <8, 6, 2> -> <9, 8, 2> -> <5, 4, 2> -> <6, 7, 2> -> <2, 4, 1> -> <8, 10, 1> -> null

## Which Set: 0 1 2 2 2 2 6 6 6 6 6 11 12

Edge List: <0, 0, 0> -> <1, 6, 3> -> <6, 4, 3> -> <3, 5, 4> -> <9, 10, 4> -> <12, 7, 4> -> <5, 7, 5> -> <3, 2, 5> -> <9, 11, 5> -> <1, 11, 6> -> <1, 2, 6> -> <10, 12, 7> -> <6, 12, 7> -> null

MST List: <0, 0, 0> -> <4, 3, 3> -> <8, 6, 2> -> <9, 8, 2> -> <5, 4, 2> -> <6, 7, 2> -> <2, 4, 1> -> <8, 10, 1> -> null

## Which Set: 0 1 2 2 2 2 1 1 1 1 1 1 1 12

Edge List: <0, 0, 0> -> <6, 4, 3> -> <3, 5, 4> -> <9, 10, 4> -> <12, 7, 4> -> <5, 7, 5> -> <3, 2, 5> -> <9, 11, 5> -> <1, 11, 6> -> <1, 2, 6> -> <10, 12, 7> -> <6, 12, 7> -> null

MST List: <0, 0, 0> -> <1, 6, 3> -> <4, 3, 3> -> <8, 6, 2> -> <9, 8, 2> -> <5, 4, 2> -> <6, 7, 2> -> <2, 4, 1> -> <8, 10, 1> -> null

Which Set: 0 1 1 1 1 1 1 1 1 1 1 1 1 2

Edge List: <0, 0, 0> -> <3, 5, 4> -> <9, 10, 4> -> <12, 7, 4> -> <5, 7, 5> -> <3, 2, 5> -> <9, 11, 5> -> <1, 11, 6> -> <1, 2, 6> -> <10, 12, 7> -> <6, 12, 7> -> null MST List: <math><0, 0, 0> -> <6, 4, 3> -> <1, 6, 3> -> <4, 3, 3> -> <8, 6, 2> -> <9, 8, 2> -> <5, 4, 2> -> <6, 7, 2> -> <2, 4, 1> -> <8, 10, 1> -> null

Which Set: 0 1 1 1 1 1 1 1 1 1 1 1 1 1

Edge List: <0, 0, 0> -> <5, 7, 5> -> <3, 2, 5> -> <9, 11, 5> -> <1, 11, 6> -> <1, 2, 6> -> <10, 12, 7> -> <6, 12, 7> -> null MST List: <math><0, 0, 0> -> <12, 7, 4> -> <6, 4, 3> -> <1, 6, 3> -> <4, 3, 3> -> <8, 6, 2> -> <9, 8, 2> -> <5, 4, 2> -> <6, 7, 2> -> <2, 4, 1> -> <8, 10, 1> -> null

Which Set: 0 1 1 1 1 1 1 1 1 1 1 1

Edge List: <0, 0, 0> -> <1, 11, 6> -> <1, 2, 6> -> <10, 12, 7> -> <6, 12, 7> -> null MST List: <math><0, 0, 0> -> <9, 11, 5> -> <12, 7, 4> -> <6, 4, 3> -> <1, 6, 3> -> <4, 3, 3> -> <8, 6, 2> -> <9, 8, 2> -> <5, 4, 2> -> <6, 7, 2> -> <2, 4, 1> -> <8, 10, 1> -> null