323.25 Project 4: Dijkstra's Algorithm for Single Source Shortest Path

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Algorithm Steps for the Project:

```
Step 0: open inFile, SSSfile, deBugFile
       numNodes ← get from inFile
      Allocate and initialize all members in the DijktraSSS class accordingly
Step 1: loadCostMatrix (inFile)
       sourceNode ← 1
Step 2: setBestAry (sourceNode)
      setParentAry (sourceNode)
      setToDoAry (sourceNode)
Step 3: minNode ← findMinNode (...)
       ToDoAry[minNode] \leftarrow 0
       debugPrint (...)
Step 4: for(childNode = 1; childNode <= numNodes; childNode++)
           if (todoArray[childNode] == 1 and bestArray[childNode] > computeCost(childNode)
              parentArray[childNode] = minNode
              bestArray[childNode] = newCost
              debuggingPrint()
Step 5: Repeat step 3 and 4 until todoArray contains no 1's
Step 6: printShortestPath()
Step 7:sourceNode ++
Step 8: Repeat Step 2 to Step 7 while sourceNode <= numNodes
```

Source Code:

```
//
//
   main.cpp
   320Project 4
//
//
// Created by Jingshi Liu on 3/7/22.
#include <iostream>
#include <fstream>
using namespace std;
class DijkstraSSS{
public:
    int numNodes;
    int sourceNode;
    int minNode;
    int currentNode;
    int newCost;
    int** costMatrix;
    int* parentArray;
    int* todoArray;
    int* bestArray;
    DijkstraSSS(int num nodes){
        numNodes = num_nodes;
        // Allocate rows of costMatrix
        costMatrix = new int*[numNodes+1];
        // Allocate memory for 3 arrays below
        parentArray = new int[numNodes+1];
        todoArray = new int[numNodes+1];
        bestArray = new int[numNodes+1];
        for(int i = 0; i < numNodes+1; i++){
            //Current pointer in 1D array now pointing to newly
allocated 1D array, this makes costMatrix a 2D array
            costMatrix[i] = new int[numNodes+1];
            // Initialize arrays below
            todoArray[i] = 1;
            bestArray[i] = 99999;
            for(int j = 0; j < numNodes+1; j++){
                costMatrix[i][j] = 99999;
            }
            // Change the diagonal index in the matrix to 0
            costMatrix[i][i] = 0;
        }
    }
```

```
void loadCostMatrix(ifstream& inFile){
        int startingVertex, endingVertex, cost;
        while(inFile >> startingVertex && inFile >> endingVertex &&
inFile >> cost){
            costMatrix[startingVertex][endingVertex] = cost;
    }
    void setBestArray(){
        for(int i = 1; i < numNodes+1; i++)</pre>
            bestArray[i] = costMatrix[sourceNode][i];
        bestArray[0] = 99999;
    }
    void setParentArray(){
        for(int i = 0; i < numNodes+1; i++)
            parentArray[i] = sourceNode;
    }
    void setToDoArray(){
        for(int i = 1; i < numNodes+1; i++)</pre>
            todoArray[i] = 1;
        todoArray[sourceNode] = 0;
        todoArray[0] = 0;
    }
    int findMinNode(){
        // Min cost by default is 99999 bc best bestArray[0] was
initialized to 99999
        int minNode = 0;
        for(int i = 1; i < numNodes+1; i++){</pre>
            if(todoArray[i] == 1 && bestArray[i] < bestArray[minNode])</pre>
                minNode = i;
        todoArray[minNode] = 0;
        this->minNode = minNode;
        return minNode:
    }
    int computeCost(int node){
        this->newCost = bestArray[minNode] + costMatrix[minNode]
[node];
        return this->newCost;
    }
    bool checkToDoArray(){
        for(int i = 1; i < numNodes+1; i++)</pre>
            if(todoArray[i] == 1)
                return true:
```

```
return false:
    }
    void debuggingPrint(ostream& debuggingFile){
        debuggingFile << "Source Node</pre>
                                             : "<<sourceNode;
        debuggingFile << "\nParent Array</pre>
        for(int i = 1; i < numNodes+1; i++)
            debuggingFile << parentArray[i]<< " ";</pre>
        debuggingFile << "\nTo Do Array</pre>
        for(int i = 1; i < numNodes+1; i++)
            debuggingFile << todoArray[i] << " ";</pre>
        debuggingFile << "\nBest Cost Array : ";</pre>
        for(int i = 1; i < numNodes+1; i++)</pre>
            debuggingFile << bestArray[i] << " ";</pre>
        debuggingFile <<</pre>
"\n\n\n******************************\n\n\n";
    }
    void printShortestPath(ostream& sssFile){
        int current_node = 1, cost = 0;
        string shortestPath = "";
        sssFile <<
"========\nSource node =
"<<sourceNode<<"\n\n":
        for(int i = 1; i < numNodes+1; i++){
            current node = i;
            shortestPath = to string(current node);
            cost = 0;
            while(current node != sourceNode){
                shortestPath = to_string(parentArray[current_node]) +
" -> " + shortestPath;
                cost += costMatrix[parentArray[current node]]
[current node];
                current_node = parentArray[current_node];
            sssFile << shortestPath << " Cost = " << cost <<"\n";</pre>
        }
    }
};
int main(int argc, const char * argv[]) {
    ifstream inFile;
    ofstream sssFile, debuggingFile;
    DijkstraSSS* dijkstra;
```

```
inFile.open(argv[1]);
    sssFile.open(argv[2]);
    debuggingFile.open(argv[3]);
    int numNodes = 0;
    inFile >> numNodes;
    dijkstra = new DijkstraSSS(numNodes);
    // Load Cost Matrix
    dijkstra->loadCostMatrix(inFile);
    for(int source_node = 1; source_node <= dijkstra->numNodes;
source_node++){
        dijkstra->sourceNode = source_node;
        dijkstra->setBestArray();
        dijkstra->setParentArray();
        dijkstra->setToDoArray();
        while(dijkstra->checkToDoArray()){
            dijkstra->findMinNode();
            for(int i = 1; i <= dijkstra->numNodes; i++){
                if(dijkstra->todoArray[i] == 1 && dijkstra-
>bestArray[i] > dijkstra->computeCost(i)){
                    dijkstra->parentArray[i] = dijkstra->minNode;
                    dijkstra->bestArray[i] = dijkstra->newCost;
                    dijkstra->debuggingPrint(debuggingFile);
                }
            }
        dijkstra->printShortestPath(sssFile);
    }
    inFile.close();
    sssFile.close();
    debuggingFile.close();
    return 0;
}
```

Output:

Data 1, SSSFile1, and debuggingFile1

Data 1:

1 3 70

SSSFile for data 1:

4 -> 3 -> 5 Cost = 30

```
______
Source node = 1
1 Cost = 0
1 -> 2 Cost = 10
1 -> 4 -> 3 Cost = 50
1 -> 4  Cost = 30
1 -> 4 -> 3 -> 5 Cost = 60
______
Source node = 2
2 -> 3 -> 5 -> 1 Cost = 100
2 \quad Cost = 0
2 -> 3 Cost = 50
2 -> 3 -> 5 -> 1 -> 4 Cost = 130
2 -> 3 -> 5 Cost = 60
______
Source node = 3
3 -> 5 -> 1 Cost = 50
3 -> 5 -> 1 -> 2 Cost = 60
3 \quad Cost = 0
3 -> 5 -> 1 -> 4 Cost = 80
3 -> 5 Cost = 10
_____
Source node = 4
4 \rightarrow 3 \rightarrow 5 \rightarrow 1 Cost = 70
4 -> 3 -> 5 -> 1 -> 2 Cost = 80
4 -> 3 Cost = 20
4 Cost = 0
```

Source node = 5

5 -> 1 Cost = 40 5 -> 1 -> 2 Cost = 50 5 -> 1 -> 4 -> 3 Cost = 90 5 -> 1 -> 4 Cost = 70 5 Cost = 0

debuggingFile2 for data 1:

Source Node : 1
Parent Array : 1 1 2 1 1
To Do Array : 0 0 1 1 1

Best Cost Array: 0 10 60 30 99999

Source Node : 1 Parent Array : 1 1 4 1 1 To Do Array : 0 0 1 0 1

Best Cost Array: 0 10 50 30 99999

Source Node : 1
Parent Array : 1 1 4 1 4
To Do Array : 0 0 1 0 1

Best Cost Array: 0 10 50 30 90

Source Node : 1
Parent Array : 1 1 4 1 3
To Do Array : 0 0 0 0 1

Best Cost Array: 0 10 50 30 60

Source Node : 2 Parent Array : 2 2 2 2 3 To Do Array : 1 0 0 1 1

Best Cost Array: 99999 0 50 99999 60

Source Node : 2 Parent Array : 5 2 2 2 3 To Do Array : 1 0 0 1 0

Best Cost Array: 100 0 50 99999 60

Source Node : 2 Parent Array : 5 2 2 1 3 To Do Array : 0 0 0 1 0

Best Cost Array: 100 0 50 130 60

Source Node : 3 Parent Array : 5 3 3 3 3 To Do Array : 1 1 0 1 0

Best Cost Array: 50 99999 0 99999 10

Source Node : 3 Parent Array : 5 1 3 3 3 To Do Array : 0 1 0 1 0

Best Cost Array: 50 60 0 99999 10

Source Node : 3 Parent Array : 5 1 3 1 3 To Do Array : 0 1 0 1 0

Best Cost Array : 50 60 0 80 10

Source Node : 4 Parent Array : 4 4 4 4 3 To Do Array : 1 1 0 0 1

Best Cost Array: 99999 99999 20 0 30

Source Node : 4 Parent Array : 5 4 4 4 3 To Do Array : 1 1 0 0 0

Best Cost Array: 70 99999 20 0 30

Source Node : 4
Parent Array : 5 1 4 4 3
To Do Array : 0 1 0 0 0
Best Cost Array : 70 80 20 0 30

Source Node : 5 Parent Array : 5 1 5 5 5 To Do Array : 0 1 1 1 0

Best Cost Array: 40 50 99999 99999 0

Source Node : 5 Parent Array : 5 1 1 5 5 To Do Array : 0 1 1 1 0

Best Cost Array: 40 50 110 99999 0

Source Node : 5 Parent Array : 5 1 1 1 5 To Do Array : 0 1 1 1 0

Best Cost Array: 40 50 110 70 0

Source Node : 5 Parent Array : 5 1 2 1 5 To Do Array : 0 0 1 1 0

Best Cost Array: 40 50 100 70 0

Source Node : 5
Parent Array : 5 1 4 1 5
To Do Array : 0 0 1 0 0

Best Cost Array: 40 50 90 70 0

Data 2, SSSFile2, and debuggingFile2

Data 2:

2 7 40 2 3 35

```
2 1 25
6 2 5
6 3 20
4 7 25
4 8 20
```

SSSFile for data 2:

```
______
Source node = 1
1 \quad Cost = 0
1 -> 3 -> 2 Cost = 7
1 -> 3 Cost = 5
1 -> 3 -> 4 Cost = 10
1 -> 3 -> 4 -> 5 Cost = 15
1 -> 3 -> 4 -> 6 Cost = 13
1 -> 3 -> 2 -> 8 -> 7 Cost = 11
1 -> 3 -> 2 -> 8 Cost = 9
______
Source node = 2
2 -> 8 -> 1 Cost = 8
2 \quad Cost = 0
2 -> 8 -> 1 -> 3 Cost = 13
2 -> 8 -> 7 -> 4 Cost = 8
2 -> 8 -> 7 -> 4 -> 5 Cost = 13
2 -> 8 -> 7 -> 6 Cost = 7
2 -> 8 -> 7 Cost = 4
2 -> 8  Cost = 2
_____
Source node = 3
3 -> 2 -> 8 -> 1 Cost = 10
3 -> 2  Cost = 2
3 \quad Cost = 0
3 -> 4  Cost = 5
3 -> 4 -> 5 Cost = 10
3 -> 4 -> 6 Cost = 8
3 -> 2 -> 8 -> 7 Cost = 6
3 -> 2 -> 8 Cost = 4
______
Source node = 4
4 -> 6 -> 1 Cost = 8
4 -> 6 -> 2 Cost = 8
4 \rightarrow 6 \rightarrow 1 \rightarrow 3 Cost = 13
4 Cost = 0
4 -> 5 Cost = 5
4 -> 6 Cost = 3
4 -> 6 -> 7 Cost = 5
4 -> 5 -> 8 Cost = 8
```

```
______
Source node = 5
5 -> 8 -> 1 Cost = 9
5 -> 2 \quad Cost = 10
5 -> 8 -> 1 -> 3 Cost = 14
5 -> 8 -> 7 -> 4 Cost = 9
5 Cost = 0
5 -> 8 -> 7 -> 6 Cost = 8
5 -> 8 -> 7 Cost = 5
5 -> 8 \quad Cost = 3
Source node = 6
6 -> 1  Cost = 5
6 -> 2 \quad Cost = 5
6 -> 1 -> 3 Cost = 10
6 -> 7 -> 4 Cost = 6
6 -> 7 -> 4 -> 5 Cost = 11
6 Cost = 0
6 -> 7 \quad Cost = 2
6 -> 2 -> 8 Cost = 7
Source node = 7
7 -> 6 -> 1 Cost = 8
7 -> 6 -> 2 Cost = 8
7 -> 6 -> 1 -> 3 Cost = 13
7 -> 4  Cost = 4
7 -> 4 -> 5 Cost = 9
7 -> 6 Cost = 3
7 Cost = 0
7 -> 6 -> 2 -> 8 Cost = 10
______
Source node = 8
8 -> 1  Cost = 6
8 -> 7 -> 6 -> 2 Cost = 10
8 -> 1 -> 3 Cost = 11
8 -> 7 -> 4 Cost = 6
8 -> 7 -> 4 -> 5 Cost = 11
8 -> 7 -> 6 Cost = 5
8 -> 7 \quad Cost = 2
8 Cost = 0
```

DebuggingFile for data 2:

Source Node : 1

Parent Array : 1 3 1 1 1 1 1 1 To Do Array : 0 1 0 1 1 1 1 1

Best Cost Array: 0 7 5 20 30 99999 99999 20

Source Node : 1

Parent Array : 1 3 1 3 1 1 1 1 To Do Array : 0 1 0 1 1 1 1 1

Best Cost Array: 0 7 5 10 30 99999 99999 20

Source Node : 1

Parent Array : 1 3 1 3 1 1 3 1 To Do Array : 0 1 0 1 1 1 1 1

Best Cost Array: 0 7 5 10 30 99999 35 20

Source Node : 1

Parent Array : 1 3 1 3 1 1 3 3 To Do Array : 0 1 0 1 1 1 1 1

Best Cost Array: 0 7 5 10 30 99999 35 15

Source Node : 1

Parent Array : 1 3 1 3 1 1 3 2 To Do Array : 0 0 0 1 1 1 1 1

Best Cost Array: 0 7 5 10 30 99999 35 9

Source Node : 1 Parent Array : 1 3 1 3 1 8 3 2 To Do Array : 0 0 0 1 1 1 1 0

Best Cost Array: 0 7 5 10 30 16 35 9

Source Node : 1

Parent Array : 1 3 1 3 1 8 8 2 To Do Array : 0 0 0 1 1 1 1 0 Best Cost Array: 0 7 5 10 30 16 11 9

Source Node : 1

Parent Array : 1 3 1 3 4 8 8 2 To Do Array : 0 0 0 0 1 1 1 0 Best Cost Array: 0 7 5 10 15 16 11 9

Source Node : 1

Parent Array : 1 3 1 3 4 4 8 2 To Do Array : 0 0 0 0 1 1 1 0

Best Cost Array: 0 7 5 10 15 13 11 9

Source Node : 2

Parent Array : 8 2 2 2 2 2 2 2 To Do Array : 10111110

Best Cost Array: 8 0 35 99999 99999 99999 40 2

Source Node : 2

Parent Array : 8 2 2 2 2 8 2 2 To Do Array : 1 0 1 1 1 1 1 0

Best Cost Array: 8 0 35 99999 99999 9 40 2

Source Node : 2 Parent Array : 8 2 2 2 2 8 8 2 To Do Array : 10111110

Best Cost Array: 8 0 35 99999 99999 9 4 2

Source Node : 2

Parent Array : 8 2 2 7 2 8 8 2 To Do Array : 1 0 1 1 1 1 0 0

Best Cost Array: 8 0 35 8 99999 9 4 2

Source Node : 2

Parent Array : 8 2 2 7 7 8 8 2 To Do Array : 10111100 Best Cost Array: 8 0 35 8 34 9 4 2

Source Node : 2

Parent Array : 8 2 2 7 7 7 8 2 To Do Array : 1 0 1 1 1 1 0 0 Best Cost Array: 8 0 35 8 34 7 4 2

Source Node : 2

Parent Array : 8 2 6 7 7 7 8 2 To Do Array : 10111000 Best Cost Array: 8 0 27 8 34 7 4 2

Source Node : 2

Parent Array : 8 2 1 7 7 7 8 2 To Do Array : 0 0 1 1 1 0 0 0 Best Cost Array: 8 0 13 8 34 7 4 2

Source Node : 2 Parent Array : 8 2 1 7 4 7 8 2 To Do Array : 0 0 1 0 1 0 0 0 Best Cost Array: 8 0 13 8 13 7 4 2

Source Node : 3

Parent Array : 2 3 3 3 3 3 3 3 To Do Array : 1 0 0 1 1 1 1 1

Best Cost Array: 27 2 0 5 99999 99999 30 10

Source Node : 3

Parent Array : 2 3 3 3 3 3 3 2 To Do Array : 10011111

Best Cost Array: 27 2 0 5 99999 99999 30 4

Source Node : 3

Parent Array : 8 3 3 3 3 3 3 2 To Do Array : 1 0 0 1 1 1 1 0

Best Cost Array: 10 2 0 5 99999 99999 30 4

Source Node : 3

Parent Array : 8 3 3 3 3 8 3 2 To Do Array : 10011110

Best Cost Array: 10 2 0 5 99999 11 30 4

Source Node : 3

Parent Array : 8 3 3 3 3 8 8 2 To Do Array : 1 0 0 1 1 1 1 0

Best Cost Array: 10 2 0 5 99999 11 6 4

Source Node : 3 Parent Array : 8 3 3 3 4 8 8 2 To Do Array : 10001110 Best Cost Array: 10 2 0 5 10 11 6 4

Source Node : 3

Parent Array : 8 3 3 3 4 4 8 2 To Do Array : 1 0 0 0 1 1 1 0 Best Cost Array: 10 2 0 5 10 8 6 4

Source Node : 4

Parent Array : 6 4 4 4 4 4 4 4 To Do Array : 1 1 1 0 1 0 1 1

Best Cost Array: 8 99999 99999 0 5 3 25 20

Source Node : 4

Parent Array : 6 6 4 4 4 4 4 4 4 To Do Array : 1 1 1 0 1 0 1 1

Best Cost Array: 8 8 99999 0 5 3 25 20

Source Node : 4

Parent Array : 6 6 6 4 4 4 4 4 To Do Array : 1 1 1 0 1 0 1 1 Best Cost Array: 8 8 23 0 5 3 25 20

Source Node : 4

Parent Array : 6 6 6 4 4 4 6 4 To Do Array : 1 1 1 0 1 0 1 1 Best Cost Array: 8 8 23 0 5 3 5 20

Source Node : 4 Parent Array : 6 6 6 4 4 4 6 5 To Do Array : 1 1 1 0 0 0 1 1 Best Cost Array: 8 8 23 0 5 3 5 8

Source Node : 4

Parent Array : 6 6 1 4 4 4 6 5 To Do Array : 0 1 1 0 0 0 0 1 Best Cost Array: 8 8 13 0 5 3 5 8

Source Node : 5

Parent Array : 8 5 5 5 5 5 5 5 To Do Array : 111110110

Best Cost Array: 9 10 99999 99999 0 15 99999 3

Source Node : 5

Parent Array : 8 5 5 5 5 8 5 5 To Do Array : 1 1 1 1 0 1 1 0

Best Cost Array: 9 10 99999 99999 0 10 99999 3

Source Node : 5

Parent Array : 8 5 5 5 5 8 8 5 To Do Array : 111110110

Best Cost Array: 9 10 99999 99999 0 10 5 3

Source Node : 5

Parent Array : 8 5 5 7 5 8 8 5 To Do Array : 1 1 1 1 0 1 0 0

Best Cost Array: 9 10 99999 9 0 10 5 3

Source Node : 5 Parent Array : 8 5 5 7 5 7 8 5 To Do Array : 1 1 1 1 0 1 0 0

Best Cost Array: 9 10 99999 9 0 8 5 3

Source Node : 5

Parent Array : 8 5 6 7 5 7 8 5 To Do Array : 1 1 1 1 0 0 0 0 Best Cost Array: 9 10 28 9 0 8 5 3

Source Node : 5

Parent Array : 8 5 1 7 5 7 8 5 To Do Array : 0 1 1 1 0 0 0 0 Best Cost Array: 9 10 14 9 0 8 5 3

Source Node : 6

Parent Array : 6 6 6 7 6 6 6 6 To Do Array : 1 1 1 1 1 0 0 1

Best Cost Array: 5 5 20 6 99999 0 2 99999

Source Node : 6

Parent Array : 6 6 6 7 7 6 6 6 To Do Array : 1 1 1 1 1 0 0 1

Best Cost Array: 5 5 20 6 32 0 2 99999

Source Node : 6

Parent Array : 6 6 1 7 7 6 6 6 To Do Array : 0 1 1 1 1 0 0 1

Best Cost Array: 5 5 10 6 32 0 2 99999

Source Node : 6 Parent Array : 6 6 1 7 7 6 6 1 To Do Array : 0 1 1 1 1 0 0 1 Best Cost Array: 5 5 10 6 32 0 2 25

Source Node : 6

Parent Array : 6 6 1 7 7 6 6 2 To Do Array : 0 0 1 1 1 0 0 1 Best Cost Array: 5 5 10 6 32 0 2 7

Source Node : 6

Parent Array : 6 6 1 7 4 6 6 2 To Do Array : 0 0 1 0 1 0 0 1 Best Cost Array: 5 5 10 6 11 0 2 7

Source Node : 7

Parent Array : 6777777 To Do Array : 11111001

Best Cost Array: 8 99999 99999 4 30 3 0 99999

Source Node : 7

Parent Array : 6 6 7 7 7 7 7 To Do Array : 1 1 1 1 1 0 0 1

Best Cost Array: 8 8 99999 4 30 3 0 99999

Source Node : 7

Parent Array : 6 6 6 7 7 7 7 7 To Do Array : 1 1 1 1 1 0 0 1

Best Cost Array: 8 8 23 4 30 3 0 99999

Source Node : 7 Parent Array : 6 6 6 7 4 7 7 7 To Do Array : 1 1 1 0 1 0 0 1

Best Cost Array: 8 8 23 4 9 3 0 99999

Source Node : 7

Parent Array : 6 6 6 7 4 7 7 4 To Do Array : 1 1 1 0 1 0 0 1 Best Cost Array: 8 8 23 4 9 3 0 24

Source Node : 7

Parent Array : 6 6 1 7 4 7 7 4 To Do Array : 0 1 1 0 1 0 0 1 Best Cost Array: 8 8 13 4 9 3 0 24

Source Node : 7

Parent Array : 6 6 1 7 4 7 7 2 To Do Array : 0 0 1 0 1 0 0 1 Best Cost Array: 8 8 13 4 9 3 0 10

Source Node : 8

Parent Array : 8 8 8 7 8 8 8 8 To Do Array : 11111100

Best Cost Array: 6 99999 99999 6 99999 7 2 0

Source Node : 8

Parent Array : 8 8 8 7 7 8 8 8 To Do Array : 1 1 1 1 1 1 0 0

Best Cost Array: 6 99999 99999 6 32 7 2 0

Source Node : 8 Parent Array : 8 8 8 7 7 7 8 8 To Do Array : 1 1 1 1 1 1 0 0

Best Cost Array: 6 99999 99999 6 32 5 2 0

Source Node : 8

Parent Array : 8 6 8 7 7 7 8 8 To Do Array : 1 1 1 1 1 0 0 0

Best Cost Array: 6 10 99999 6 32 5 2 0

Source Node : 8

Parent Array : 8 6 6 7 7 7 8 8 To Do Array : 1 1 1 1 1 0 0 0 Best Cost Array: 6 10 25 6 32 5 2 0

Source Node : 8

Parent Array : 8 6 1 7 7 7 8 8
To Do Array : 0 1 1 1 1 0 0 0
Best Cost Array : 6 10 11 6 32 5 2 0

Source Node : 8
Parent Array : 8 6 1 7 4 7 8 8
To Do Array : 0 1 1 0 1 0 0 0 Best Cost Array: 6 10 11 6 11 5 2 0