

# STAT 35510

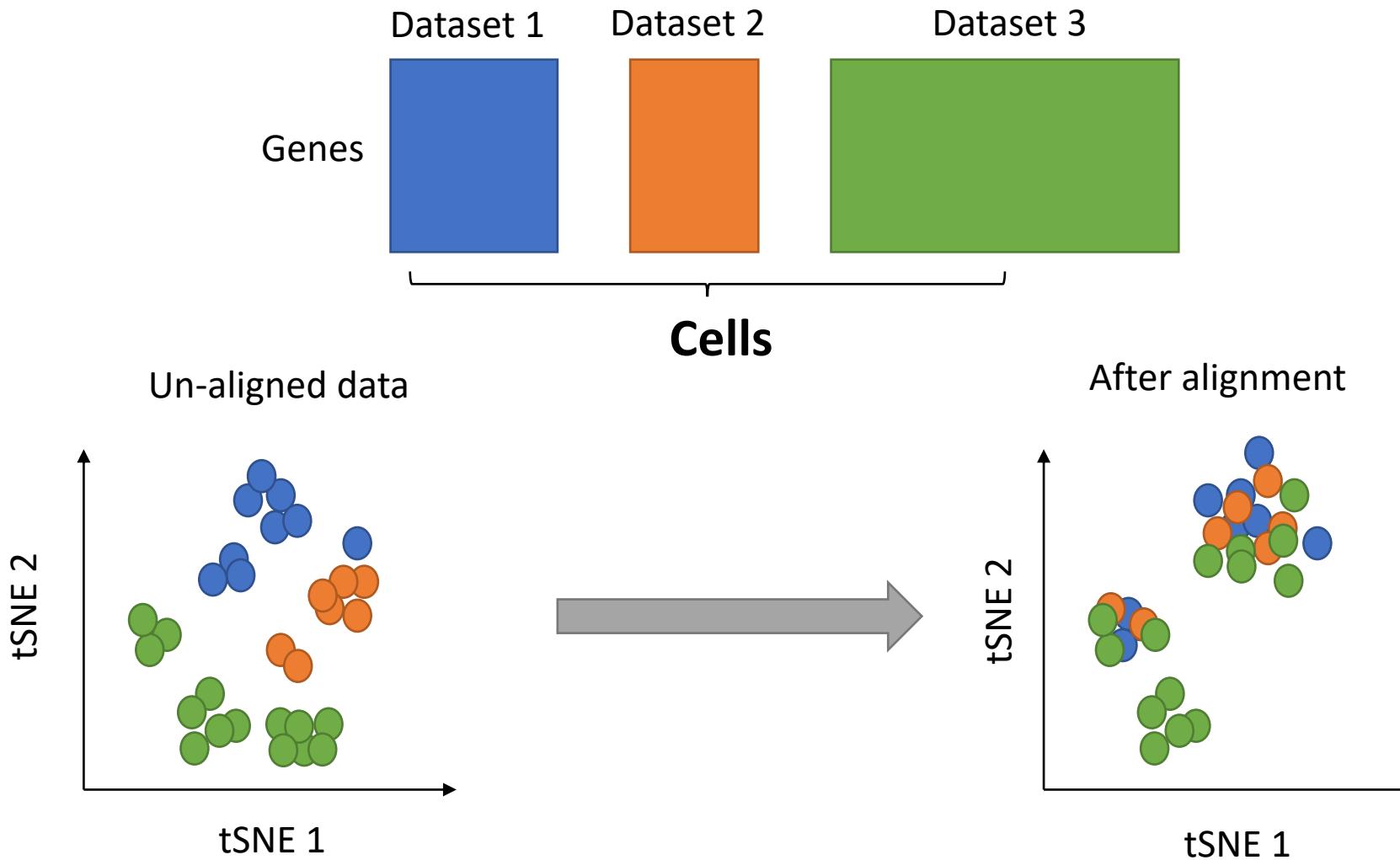
## Lecture 8

*Spring, 2024*  
Jingshu Wang

# Outline

- scRNA-seq data integration and batch correction
  - Three types of integration for single-cell multi-omics data
  - Factor model-based methods
    - Linear models
    - Variational autoencoders
  - Cell-similarity based methods
  - Comparison between different methods

# What is data integration/alignment?

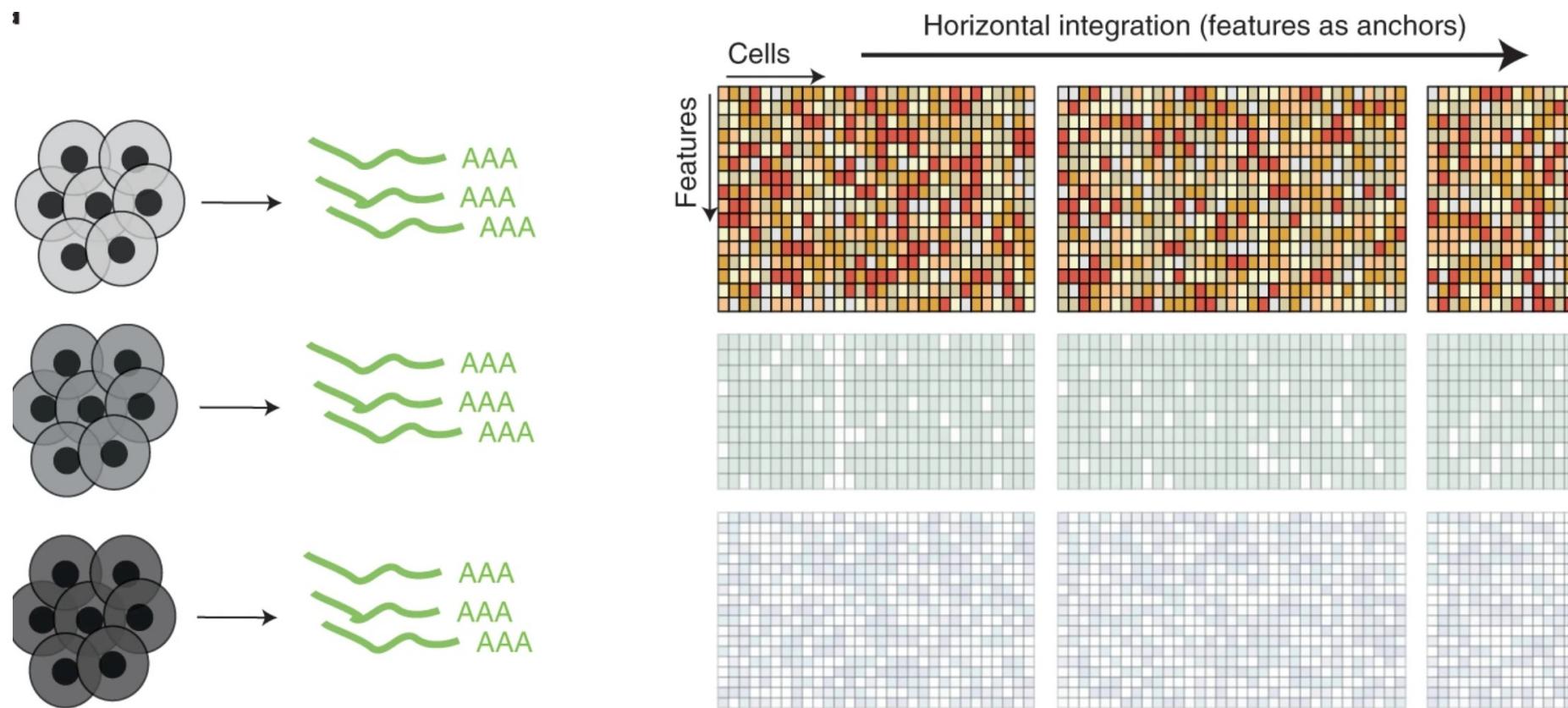


- Data integration may serve as the first step before any down-stream analyses
  - Double dipping: cells are not longer independent anymore after integration
  - Observations are no longer counts, or only obtain low-dimensional features

# Three types of data integration for single-cell multiomics data

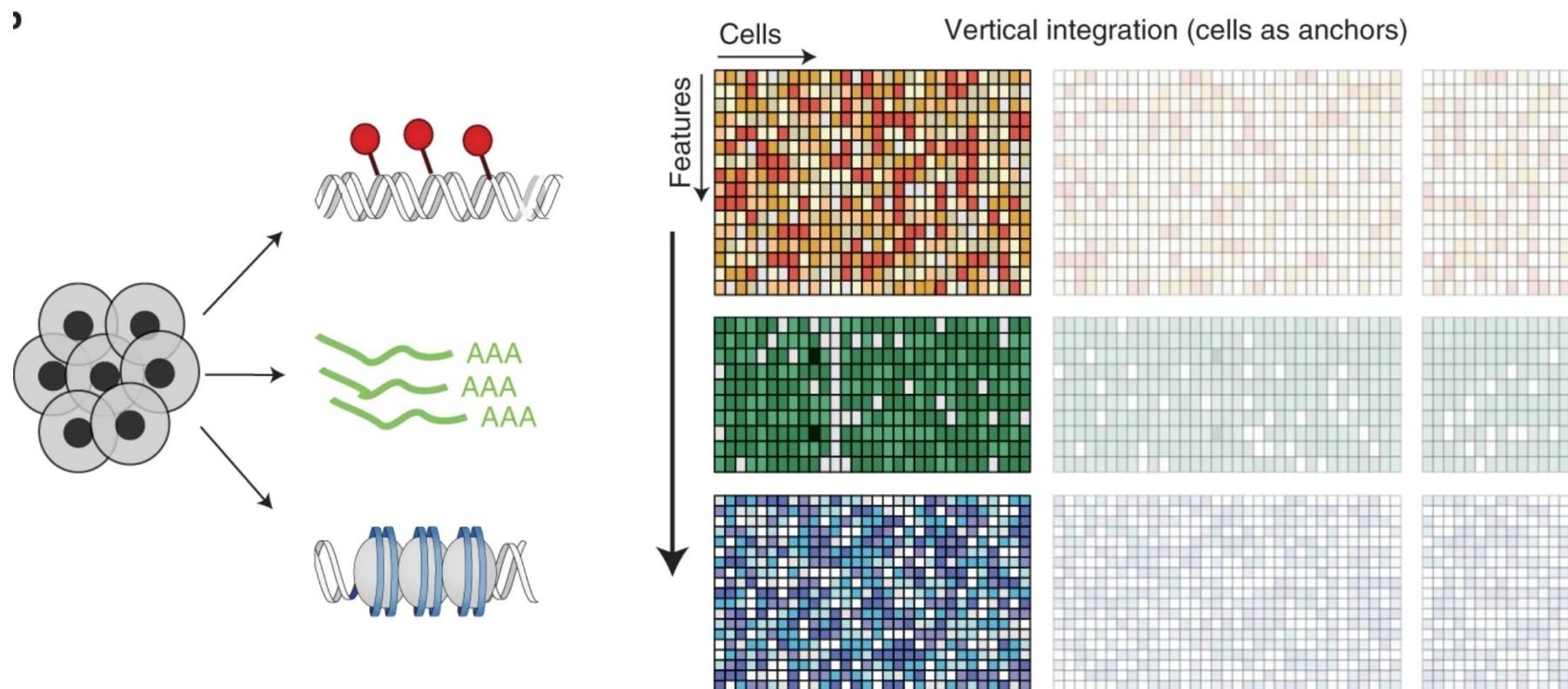
[Argelaguet et. al., Nature Biotech 2021]

- Same sets of features, different datasets
  - Main challenge: batch effects



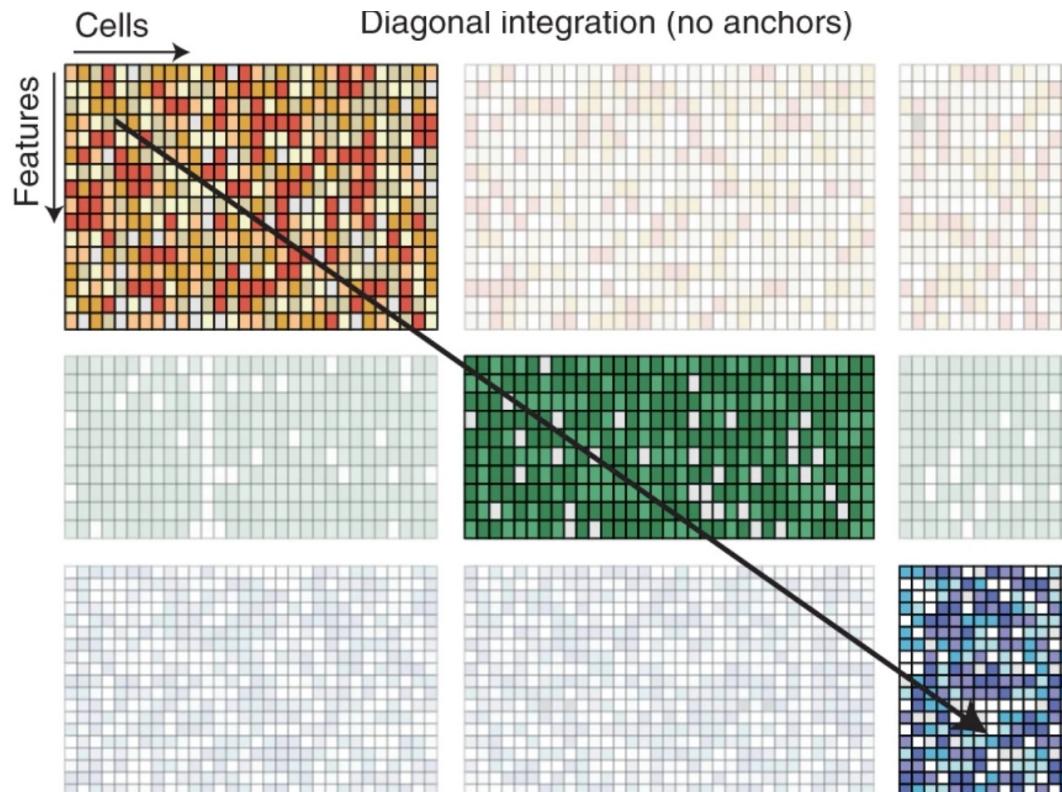
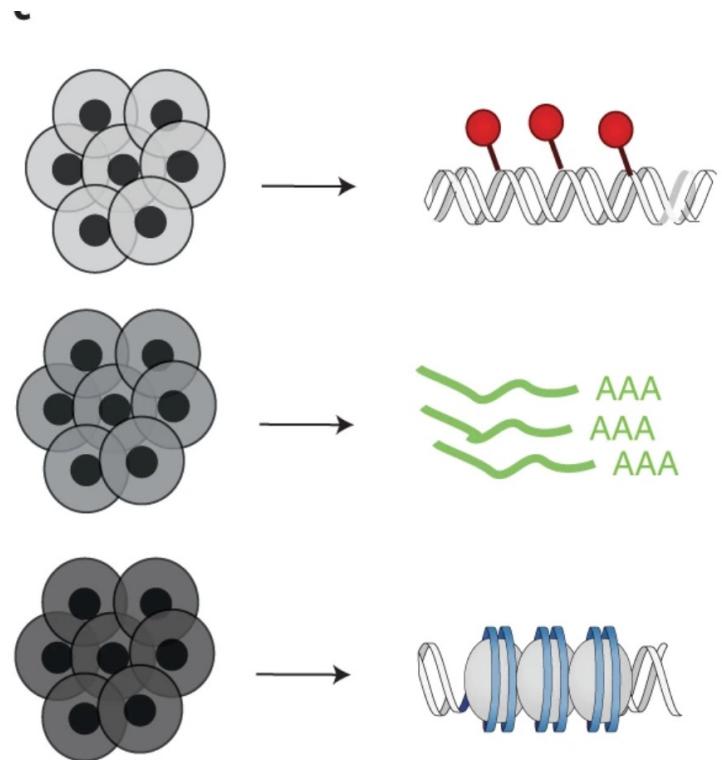
# Three types of data integration for single-cell multiomics data

- Same cell, different types of features (multimodal data)
  - Combine different types of features to understand cell-cell similarity
  - Missing modality in some datasets



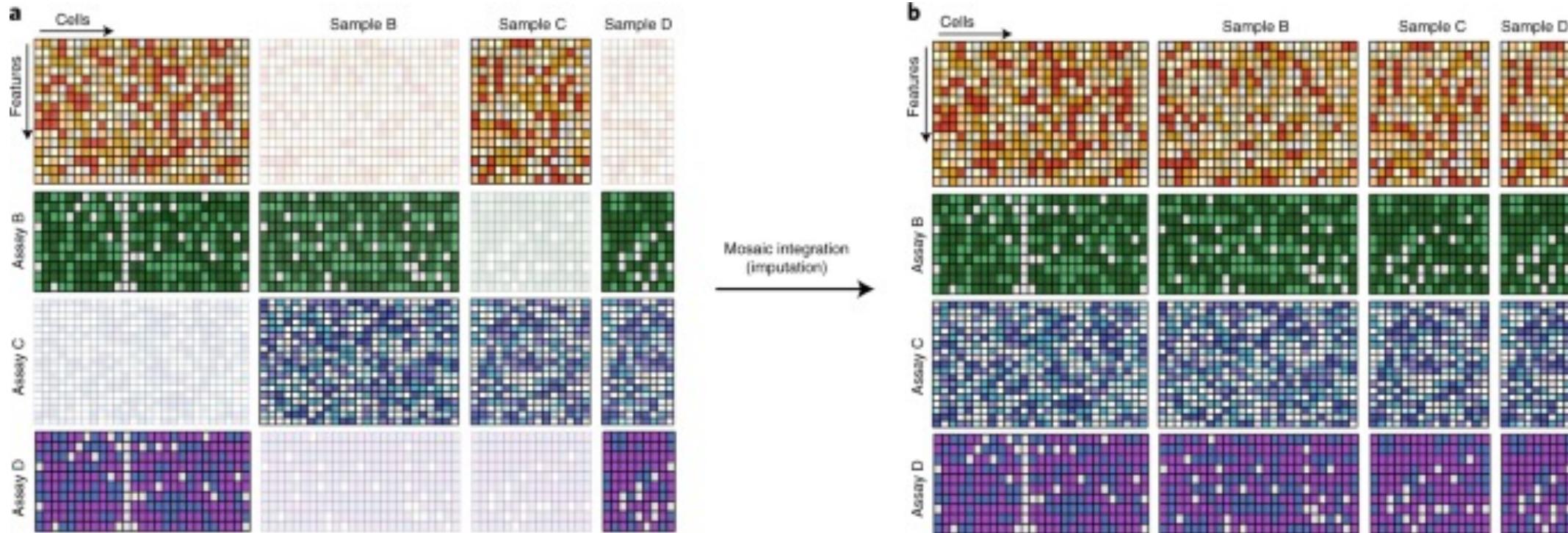
# Three types of data integration for single-cell multiomics data

- Different cells, different types of features
  - What is the basis for integration?
    - Extra information about feature connections
    - Use subset of cells with overlapping features as “bridges”



# Three types of data integration for single-cell multiomics data

- Mosaic integration between the second and third types



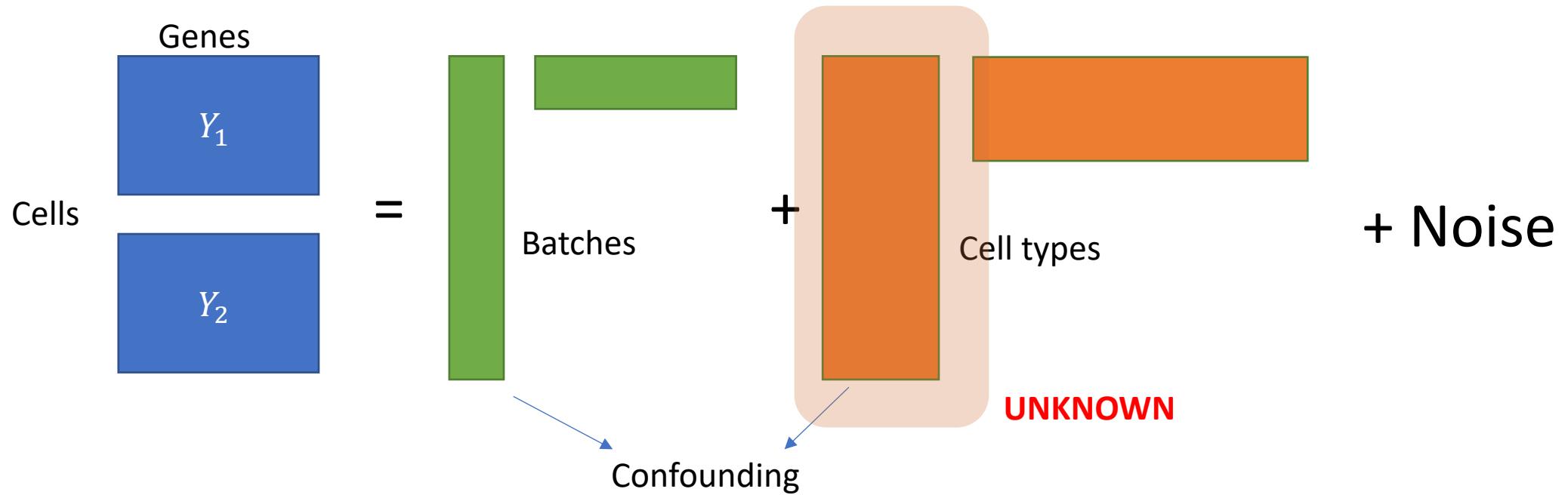
# Integration for scRNA-seq data = batch correction?

Un-alignment between datasets

- Biological differences:
  - Different cell population (tissue, individual, species)
  - Different cell types
- Technical differences:
  - batch effects
  - different sequencing depth
- Jointly analyze of multiple datasets
  - Remove batch effects
  - Remove unwanted/not interesting biological differences  
‘uninteresting’ differences between individuals, species
  - Keep meaningful biological difference between datasets (such as new cell type or true differential expression of cell type marker genes between conditions)
- Challenge: “unknown” Confounding between batches and cell types

# Unsupervised Batch Effect Removal

- Confounding between batches and unknown cell types



- Batches can be confounded with other important biological signals

# Batch correction with linear model: Limma (Ritchie et. al. , NAR 2015)

- The overall gene expression matrix (mean matrix):  $\mu_g \times 1_n^T$
- Batch corrected data:  $X - R_s D_s$
- Developed for bulk RNA-seq data where differential testing across conditions is the primary goal
- $(D_c^T, D_s^T)$  needs to be full rank. For scRNA-seq, conditions and batches can be perfectly confounded
- Batches can also be confounded with cell types, trajectories in scRNA-seq

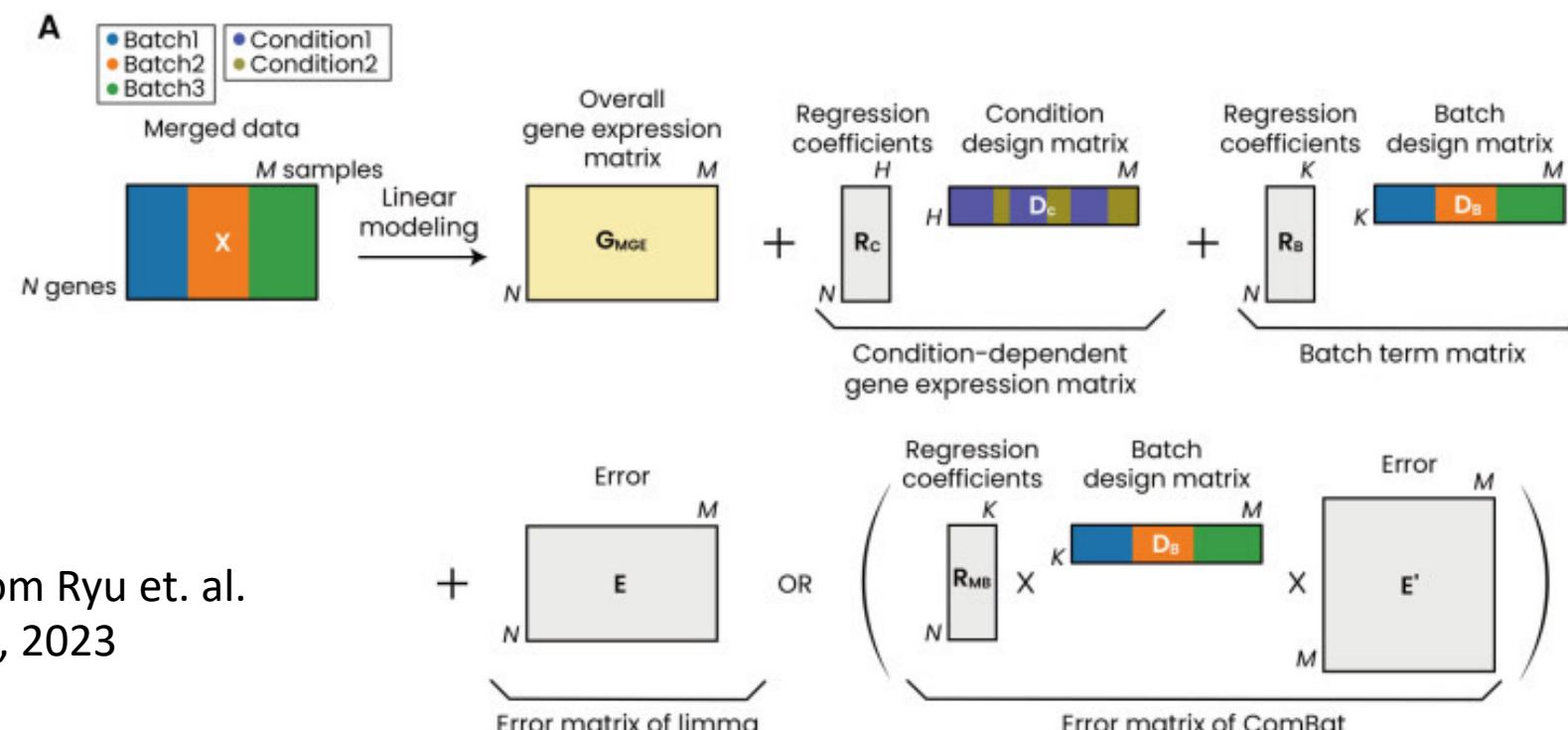
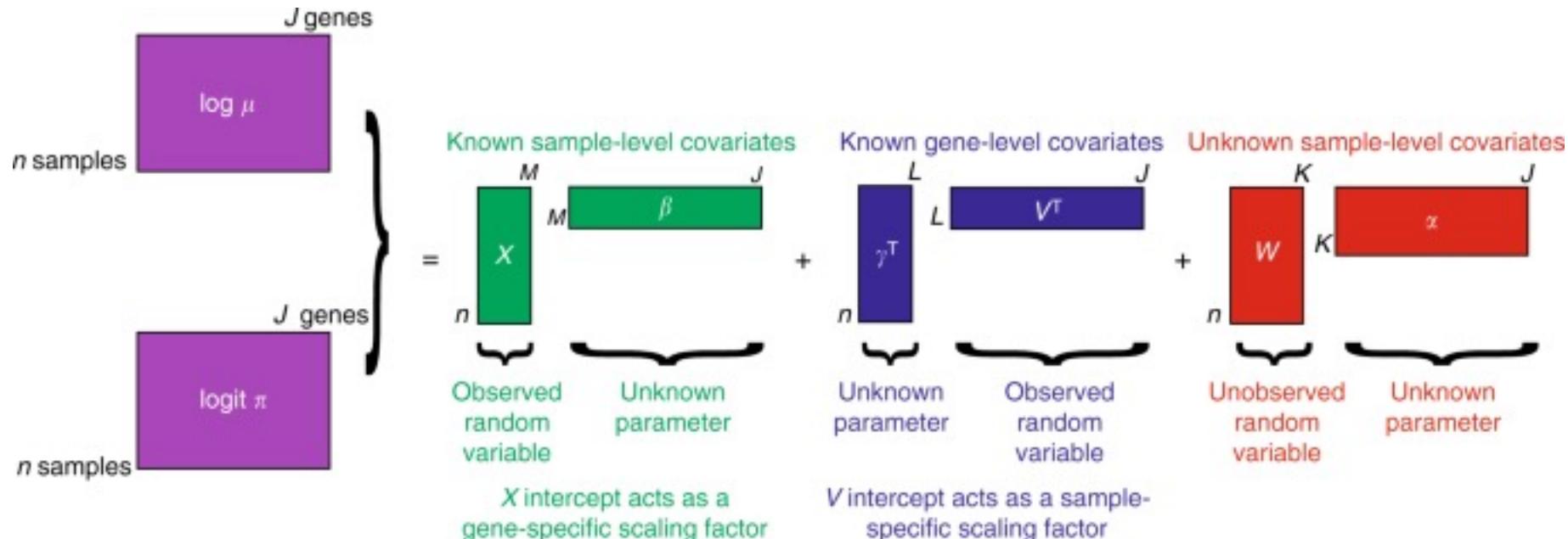


Figure from Ryu et. al.  
Mol Cells, 2023

# Challenges for batch correction in scRNA-seq

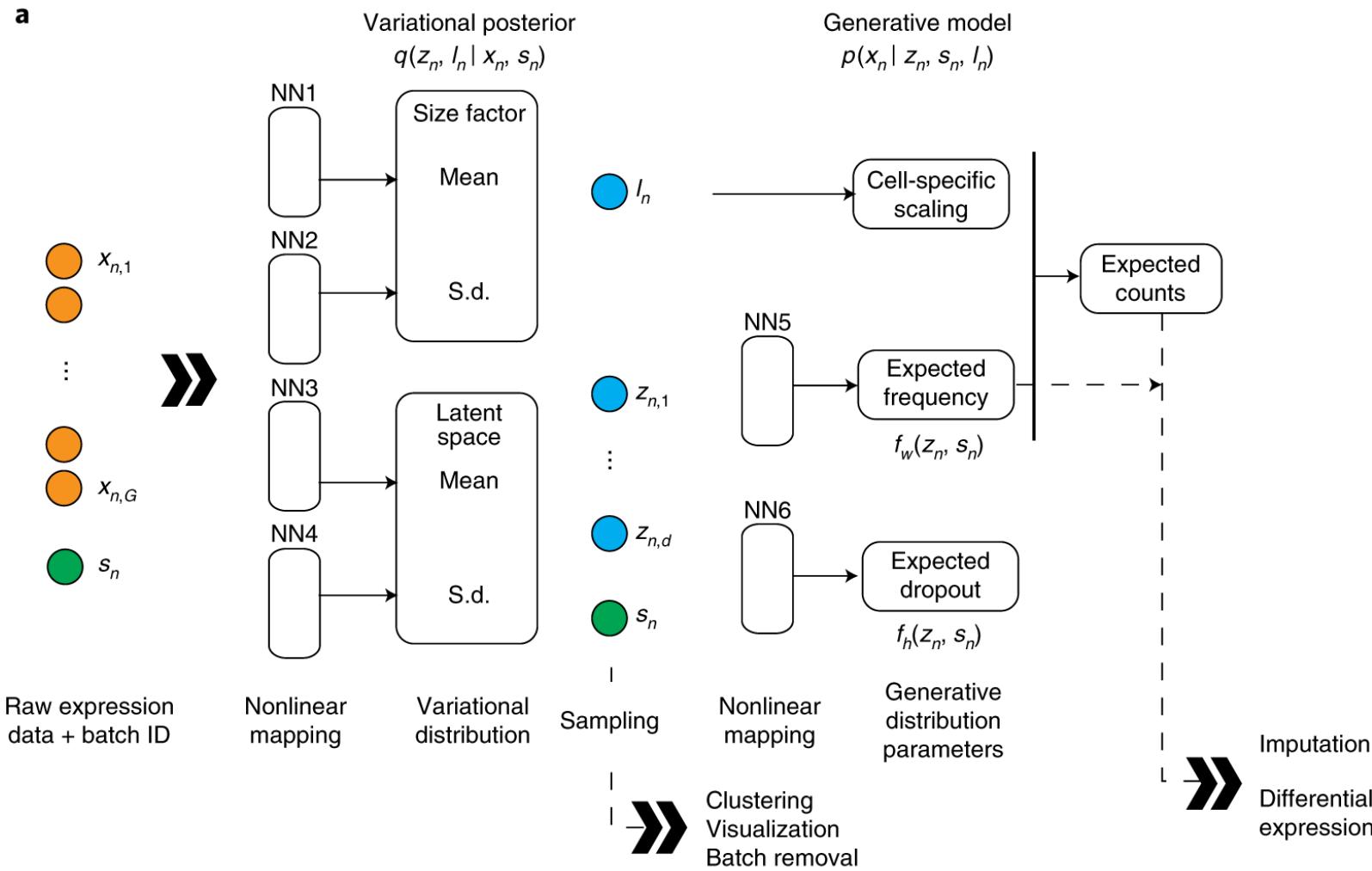
- Batch effects may not be linear
- If Batches are confounded with hidden factors of the data (like clustering structure), then batch effects are not identifiable
  - $Y_{\text{cells*genes}} = ZV^T + X_{\text{batch}}\beta + \text{error}$ ,  $\beta$  is not identifiable if the latent factors  $Z$  and  $X_{\text{batch}}$  can be arbitrarily correlated
  - One possible identifiability condition: within the same cell type, cells are biologically homogenous across batches
    - If cell types are already known, what is the purpose of integration?
  - Another possible identifiability condition (implicitly assumed in many similarity based methods):  $X_{\text{batch}}\beta$  is small compared to  $ZV^T$ , similar cells in batch 2 to a cell in batch 1 keep the same with/without batches
- Current batch correction methods tend to overcorrect batches effects (Argelaguet et. al., Nature Biotech 2021). Differential testing between conditions may tend to be conservative after correction

# ZINB-WaVE (Risso et. al., Nature Comm 2018)



- The batches are sample-level covariates
- Gene-level covariates can include gene features such as gene length and GC content
- $W$  is the batch adjusted latent representation of cells
- Implicitly assume that the latent factors and batches are uncorrelated
  - They used an L2 penalization on  $W$  in the loss function
  - The algorithm does not force latent factors and batches to be uncorrelated
- Assume that the observed counts follow ZINB model

# scVI (Lopez et. al. Nature Methods 2018)



- Use variational autoencoder (next page)
- Main feature: add batch information as extra nodes in both the input and bottleneck layer
- Implicitly assumes that latent factors  $Z$  and  $X_{\text{batch}}$  are uncorrelated as  $X_{\text{batch}}$  is fixed and  $Z$  has prior  $Z \sim N(0, I)$
- Under linear model  

$$Y_{\text{cells} \times \text{genes}} = UV^T + X_{\text{batch}}\beta + E$$
estimated  $Z$  and  $X_{\text{batch}}$  are uncorrelated
- Estimated  $Z$  can be correlated with  $X_{\text{batch}}$  in scVI because of using VAE

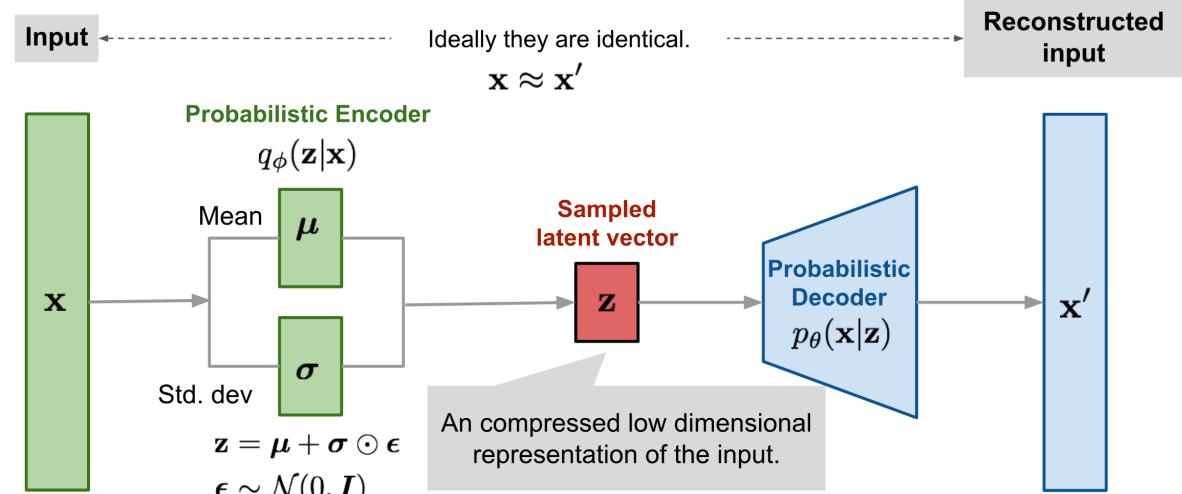
# Details of scVI model

## Variational autoencoder

- Assume that the latent variables  $Z \sim N(0, I)$
- Approximate the posterior of  $Z$  given input data by Gaussian distribution
- Encoder: posterior mean and variance of  $Z$  as non-linear functions of input data
- Decoder: non-linear mapping from  $Z$  to the observed data
- Generalization of linear probabilistic factor model to nonlinear probabilistic factor models
- scVI assumes a ZINB model on the observed data
  - Both posterior distributions of  $Z$  and mapping from  $Z$  to the observed data depend on the batches

## Final output of scVI

- Use latent factors for visualization and clustering
- Use output layer for denoising (imputation)



$$\begin{aligned}
z_n &\sim \text{Normal}(0, I) \\
\ell_n &\sim \text{log normal}(\ell_\mu, \ell_\sigma^2) \\
\rho_n &= f_w(z_n, s_n) \\
w_{ng} &\sim \text{Gamma}(\rho_n^g, \theta) \\
y_{ng} &\sim \text{Poisson}(\ell_n w_{ng}) \\
h_{ng} &\sim \text{Bernoulli}(f_h^g(z_n, s_n)) \\
x_{ng} &= \begin{cases} y_{ng} & \text{if } h_{ng} = 0 \\ 0 & \text{otherwise} \end{cases}
\end{aligned}$$

# scGen (Lotfollahi et. al. Nature Methods, 2019)

- Originally designed to perturbation prediction but can also be used for batch correction
- scGen also used VAE, not sure if batches are inputs in the VAE as in scVI
- Batch correction is done to each cell type separately
  - Requires cell type information as input data (may not be applicable in practice)
  - In the latent space, for each cell type, calculate
$$\delta = \text{avg}(z_{\text{condition}=1}) - \text{avg}(z_{\text{condition}=0})$$
    - Add  $\delta$  to the corresponding latent vectors so cells within the same cell type are mixed
    - Get the corrected gene expression matrix
    - Sounds like applying Limma on the latent space for each cell type separately

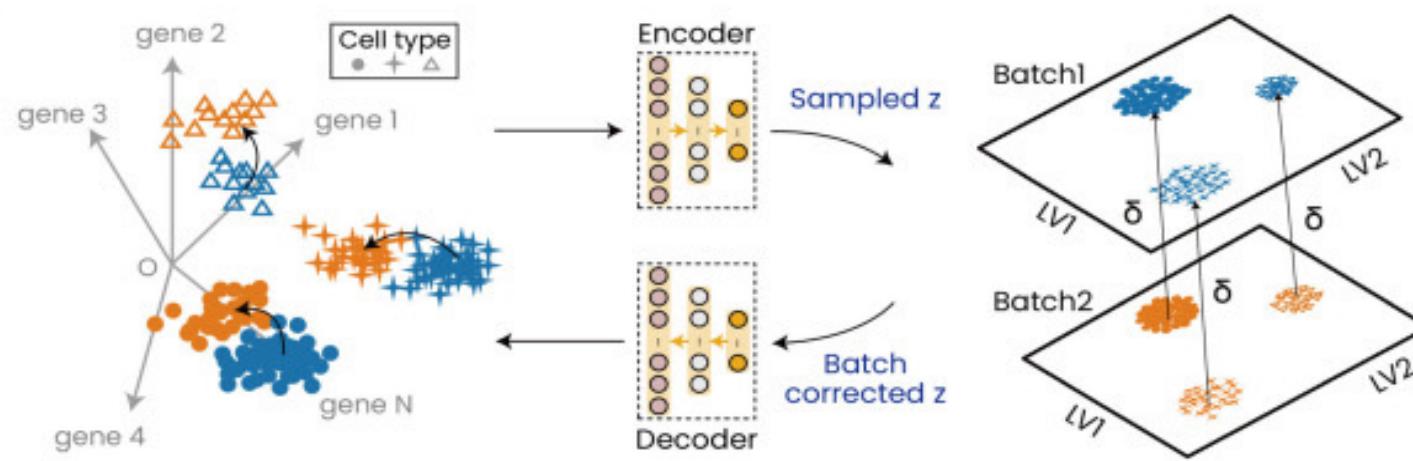
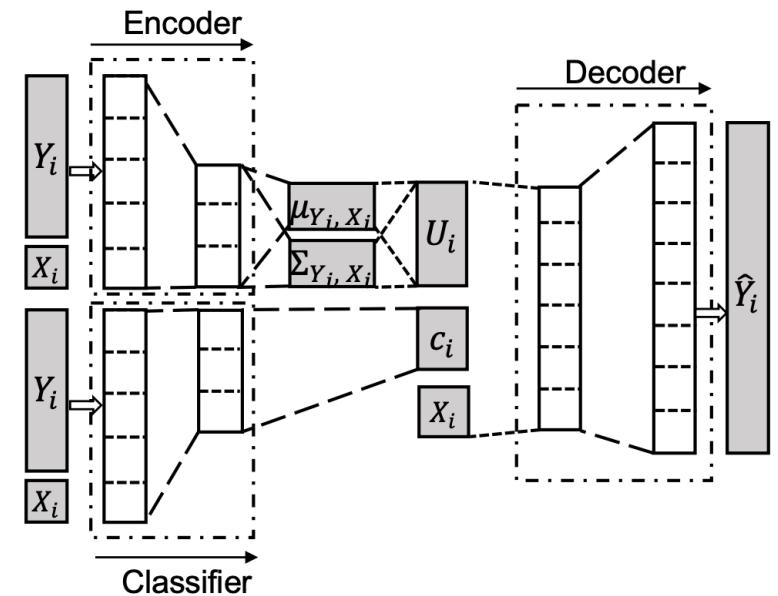


Figure from Ryu et.  
al. Mol Cells, 2023

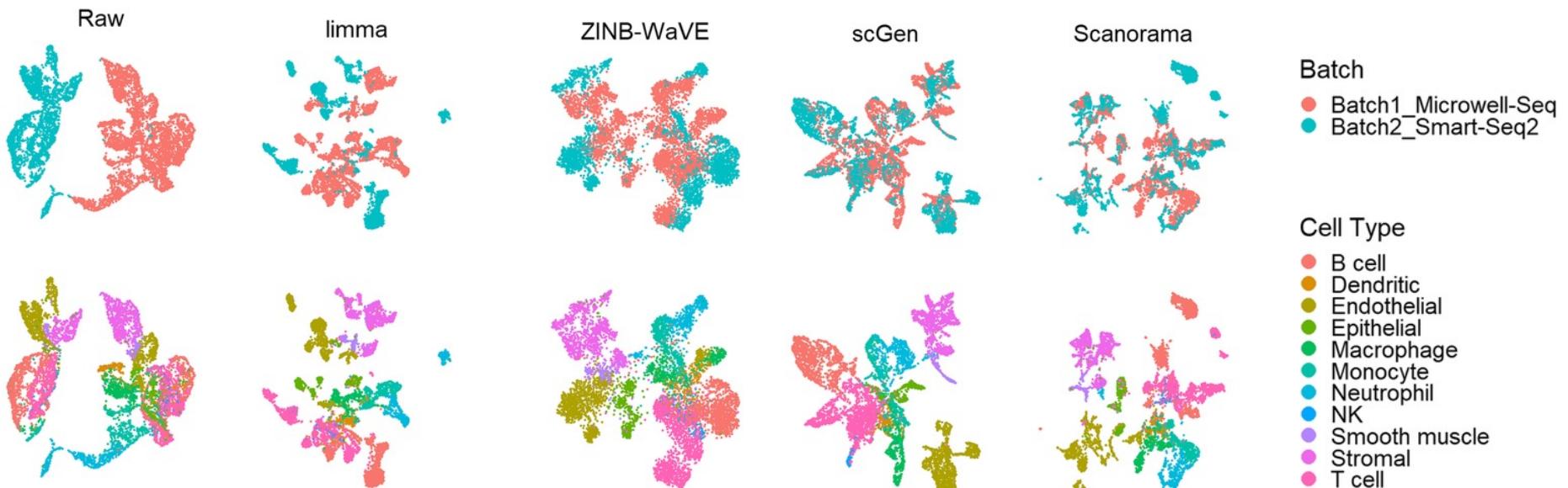
# SCANVI (Xu et. al. Mol Syst Biol, 2021)

- Perform automatic cell type annotation by integrating cells with cell type labels and cells without cell type labels
- Other assumptions are the same as scVI
  - More complicated encoders for representing posterior distribution of the latent space
    - Cells without labels: posterior distribution of Z given observed data and batch
    - Cells with labels: posterior distribution of Z given observed data, batch and cell type
  - Specific algorithm and neural network design:
    - Details not provided, claim following Kingma et. al., NeurIPS 2014
    - A guess of the neural network structure based on (Kingma et. al., NeurIPS 2014) model M2
- What if there are unseen cell types in the unlabeled data?
  - Common problem in automatic cell type annotation as discussed earlier

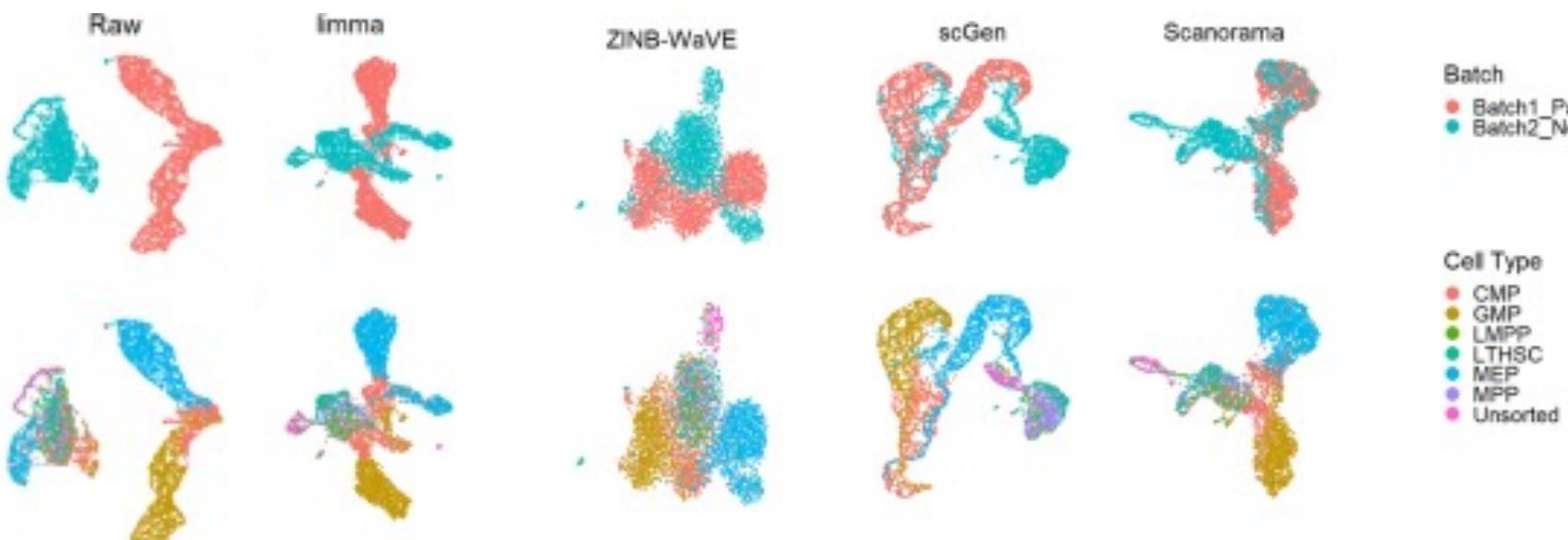


# Some benchmarking results (Tran et. al. Genome Biology 2018)

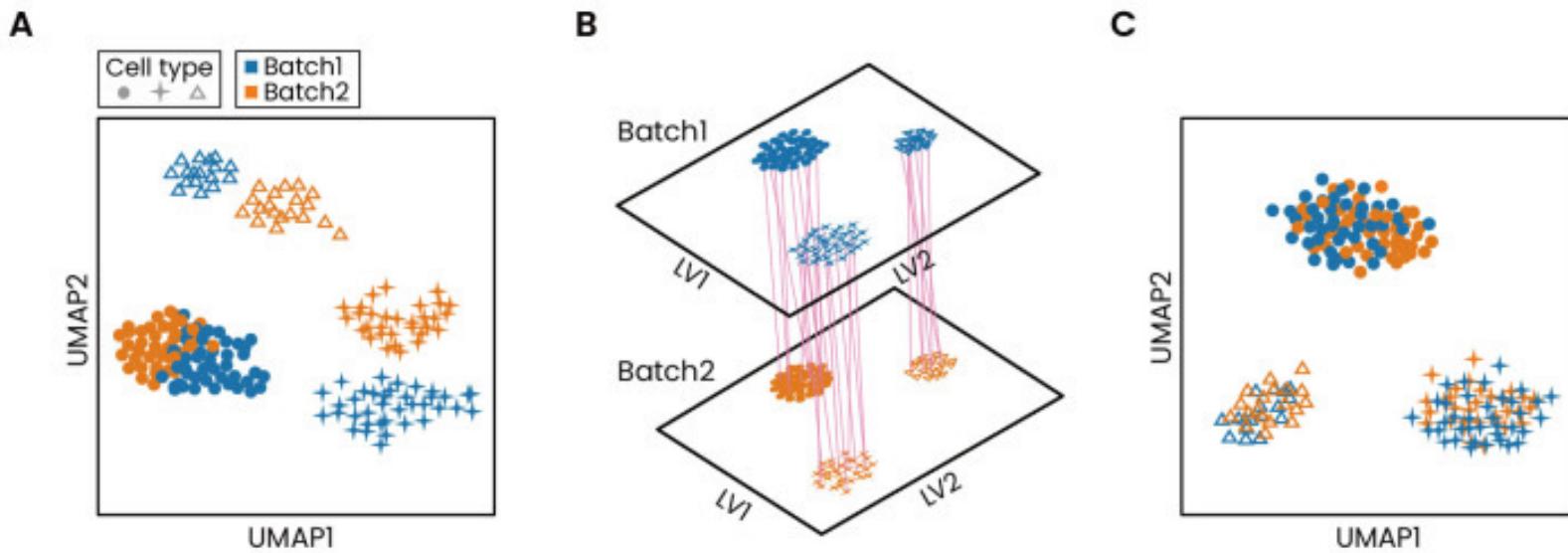
Identical cell types, different technologies



Non identical cell types



# Similarity-based batch correction methods



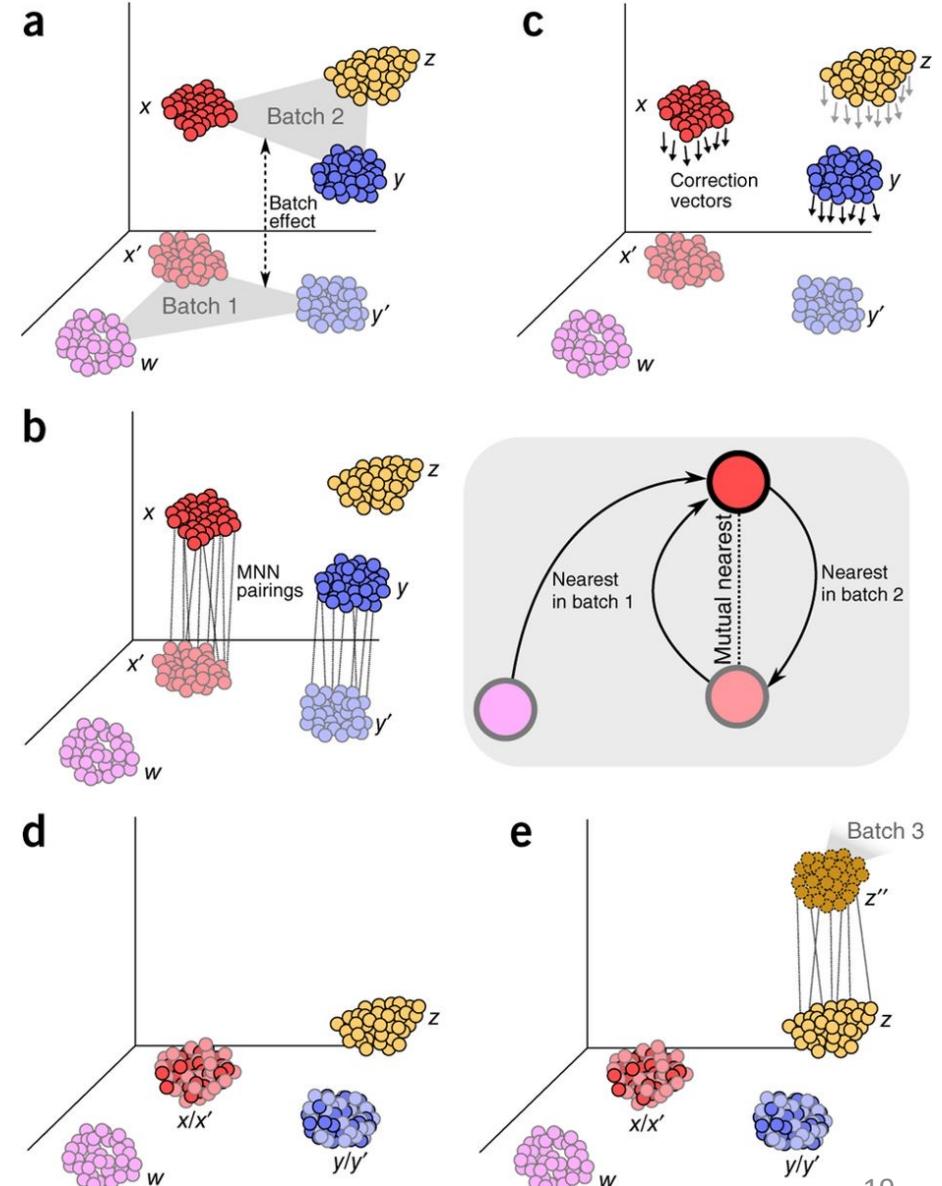
Common steps:

- Project the merged datasets onto a low-dimensional space
- Identify similar cells (pairs of cells) between batches
- Correction: correct batch effects so that cells pairs are together on the low-dimensional space
- Batch correction is only performed on low-dimensional space
  - Previous factor-model-based methods provide batch corrected gene expressions

# MNNcorrect / fast MNN (Hadhverdi L. et. al., Nature Biotech, 2018)

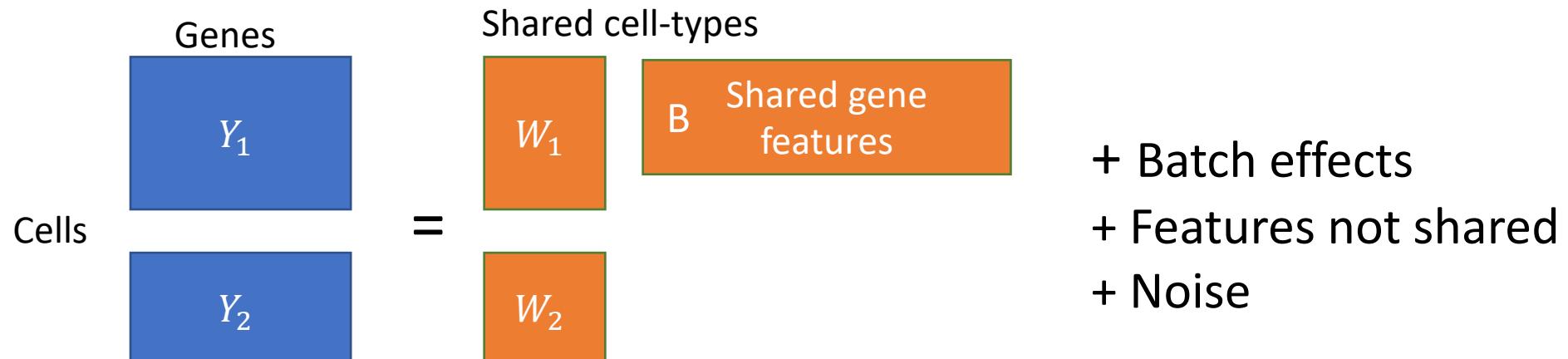
- Steps:

- Measure cell similarity (Euclidean distance after normalization)
- Find paired cells from two batches
  - Identify KNN of each cell in batch 1 (2) in the other batch 2 (1)
  - Keep the pair of cells if they are both KNN of each other
- Batch correction:
  - Compute pair-specific differences
  - Use Gaussian kernel smoothing (weights) to compute the correction vector of each cell
    - The cell-specific correction vector is a weighted average of the pair-specific correction vectors
- Critical assumption
  - Batch effects are relatively small



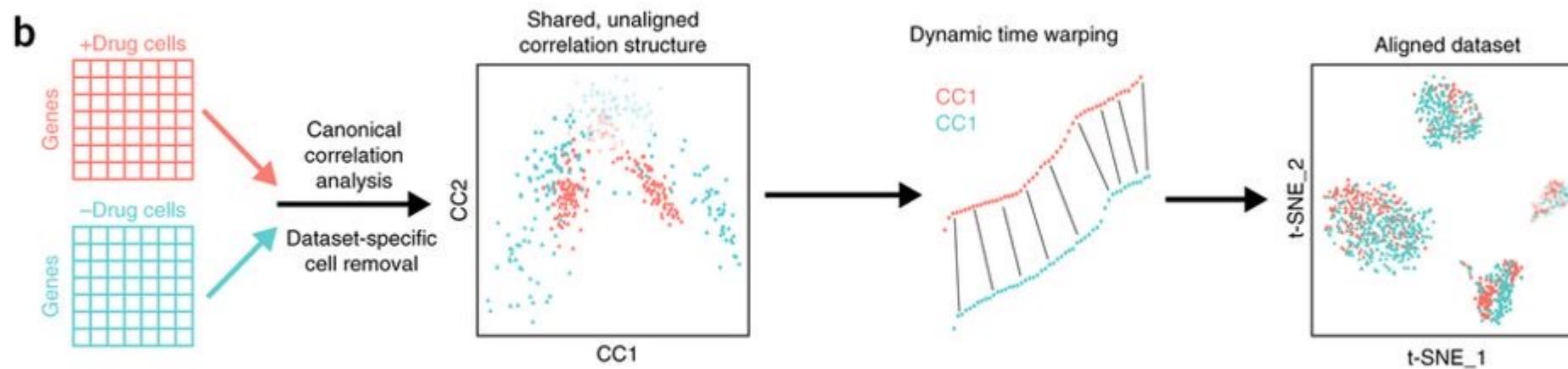
# Use Canonical correlation analysis (CCA) for scRNA-seq alignment

- CCA: originally used to find best combination of two sets of variables that have largest correlation
  - For scRNA-seq, treat each cell as a “feature”, each gene as an “observation”
  - Compute weighted combination of cells within each batch so that the combined cells have best correlation between the two batches
  - Essentially solving SVD of  $Y_1^T Y_2$ 
    - Left and right eigenvectors of  $Y_1^T Y_2$  are estimates of  $W_1$  and  $W_2$
  - Treat CCA as a dimension reduction step that minimize the effect of batches



# Seurat CCA

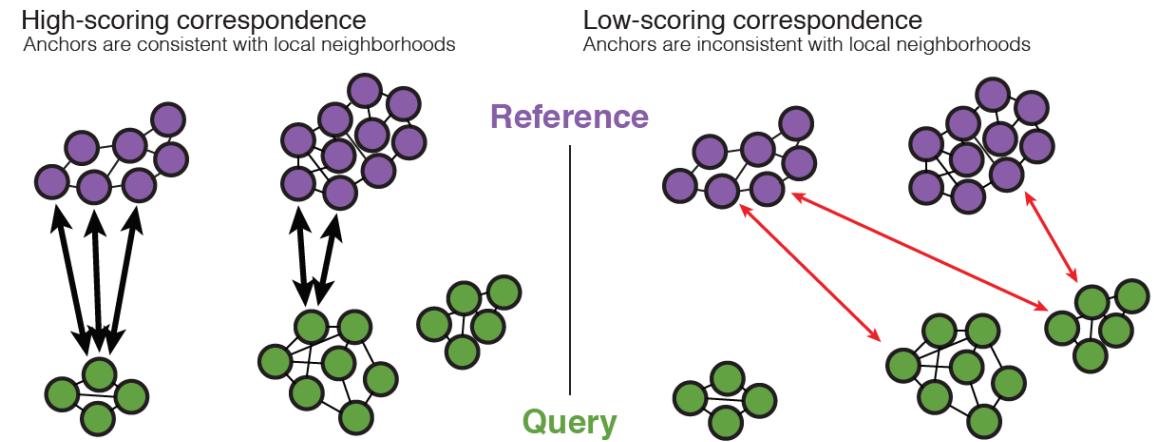
- MultiCCA (v1) (Butler et. al. Nature Biotech 2018) further uses dynamic time wrapping to further align the CC vectors to remove remaining batch effects



- They later have developed multiCCA (v2) which is hybrid between multiCCA (v1) and MNNCorrect

# MultiCCA v2 (Stuart et. al. Cell, 2019)

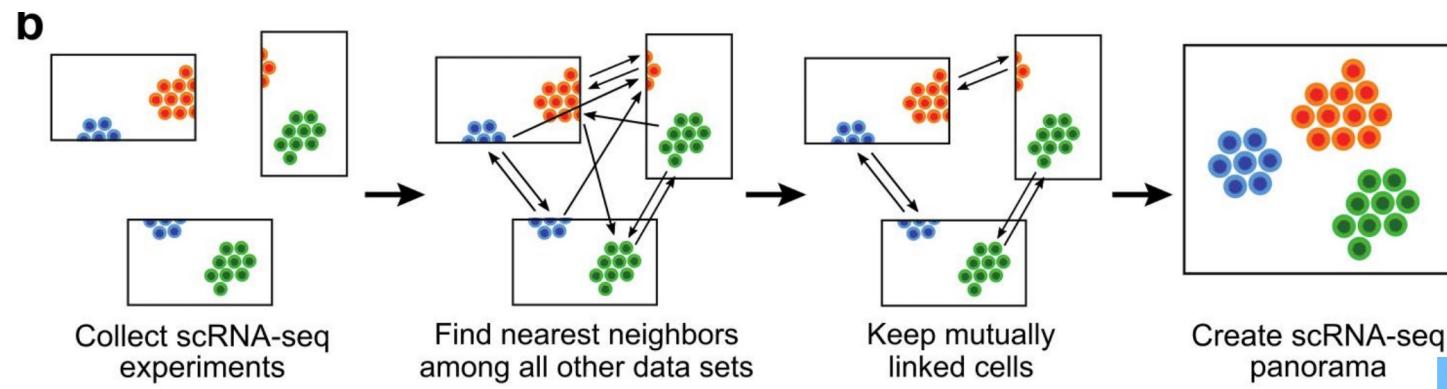
- Steps
  - CCA as in MultiCCA V1 to project both datasets into lower dimensions
    - PCA may amplify differences between two datasets and focus on variation directions that are unique to one dataset
  - Identify anchor cells using MNN
    - Give each cell an anchor score
      - Check MNN also in the original space to improve robustness
      - **Anchors scoring:** find consistency of KNNs within each dataset and with other datasets
      - **Anchor weighting  $W$ :** a matrix of anchors by cells in  $Y_2$ 
        - Weights depend on cell-cell distance, only use k nearest anchors
      - **Alignment:**  $\hat{Y}_2 = Y_2 + (Y_{1,A} - Y_{2,A})W$
      - Multiple datasets: align sequentially
  - Label transfer and feature imputation



# Scanorama (Hie et. al. , Nature Biotech 2019)

Main advantage: computationally fast MNN

- Find KNN of a cell in one dataset from all other datasets
  - To reduce computational cost in finding KNN by approximation with random projection trees to make computational cost less than  $O(kn)$
- Anchor cells: keep a pair of cells if they are KNN to each other
  - Computational cost reduce from  $O(k^2 n_1 n_2)$  to  $O(k \min(n_1, n_2))$
- Batch correction from anchors using Gaussian kernel smoothing weights same as MNNCorrect/fastMNN
- Scanorama performs better than MNNCorrect/fastMNN in benchmarking studies
  - Only methodological difference between Scanorama and MNNCorrect/fastMNN seems to be the dimension reduction first step before finding KNN



# Harmony (Korsunsky et. al. Nature Methods, 2019)

## Steps

- PCA
- Iteratively perform
  - Soft k-means clustering
    - Penalize clusters that has less batch diversity

$$\min_{R,Y} \sum_{i,k} R_{ki} \|Z_i - Y_k\|^2 + \sigma R_{ki} \log R_{ki} + \sigma \theta R_{ki} \log \left( \frac{O_{ki}}{E_{ki}} \right) \phi_i$$

$$\text{s. t. } \forall_i \forall_k R_{ki} > 0, \forall_i \sum_{k=1}^K R_{ki} = 1$$

$O \in [0, 1]^{K \times B}$  The observed co-occurrence matrix of cells in clusters (rows) and batches (columns).

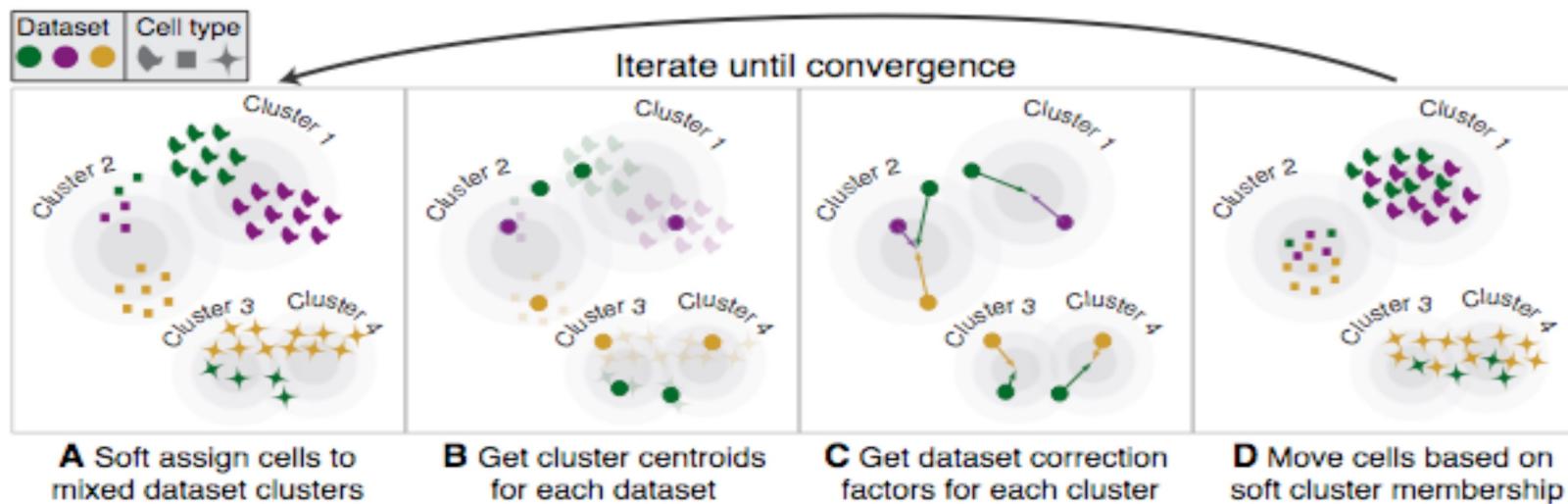
$E \in [0, 1]^{K \times B}$  The expected co-occurrence matrix of cells in clusters and batches, under the assumption of independence between cluster and batch assignment.

$Y \in [0, 1]^{d \times K}$  Cluster centroid locations in the  $k$ -means clustering algorithm.

# Harmony (Korsunsky et. al. Nature Methods, 2019)

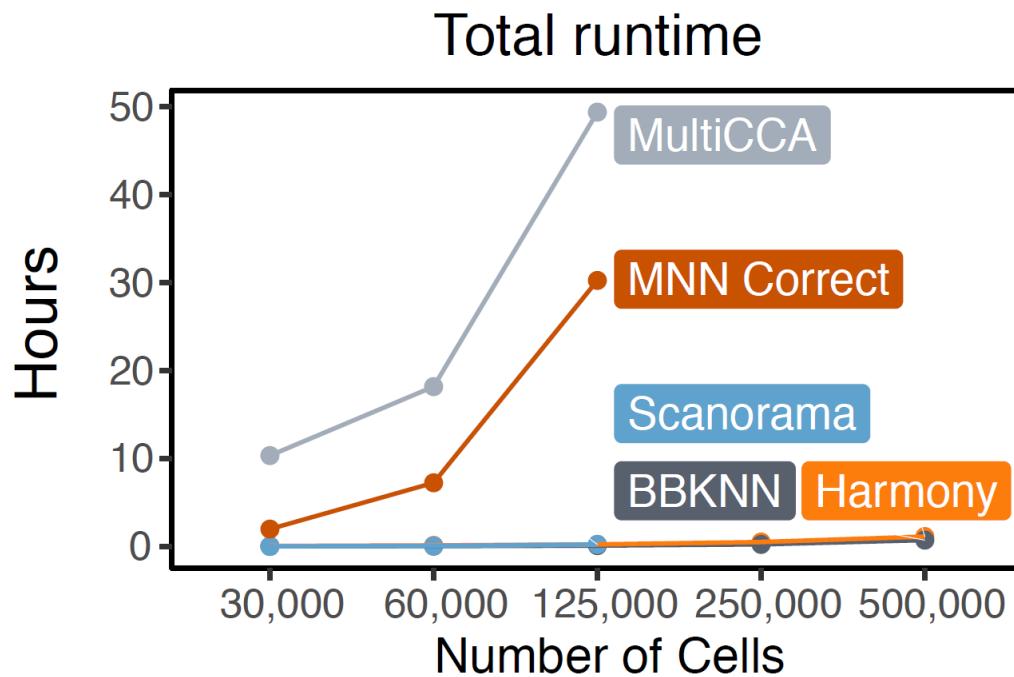
## Steps

- PCA
- Iteratively perform
  - Soft k-means clustering
    - Penalize clusters that has less batch diversity
    - Goal: make cells of the same cell type in each cluster
  - Mixture of experts model for correction
    - Compute cluster-specific batch correction by linear regression
      - Assume that the mean of each cell within each cluster linearly depend on the batch information
    - Move cells in each cluster by subtracting the batch and cluster specific mean effect

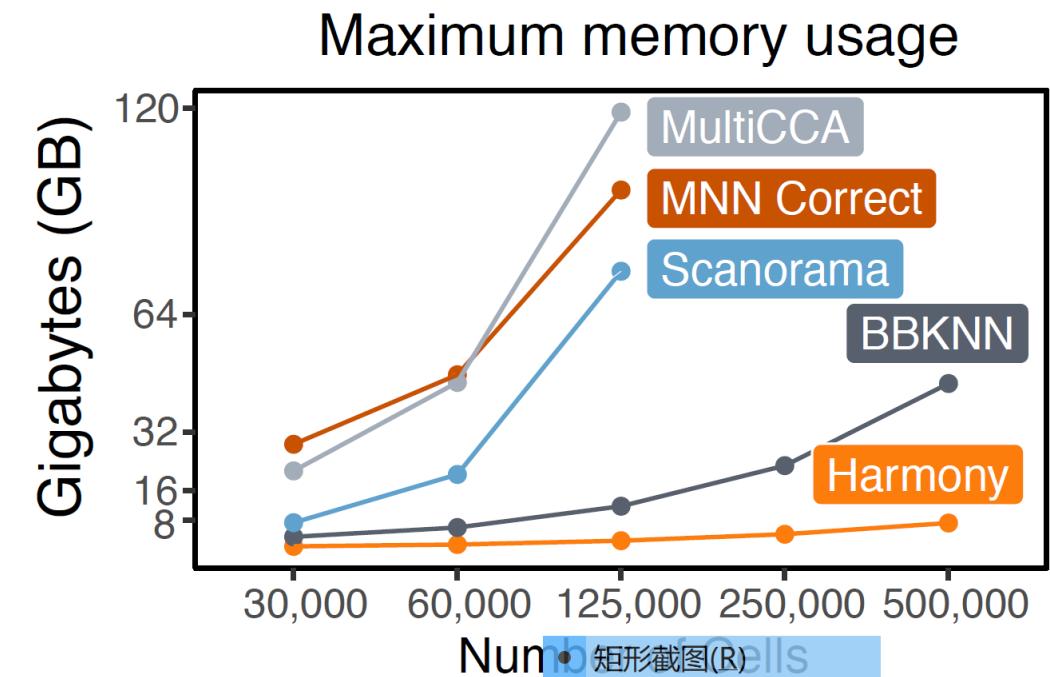


# Comparison of computational costs

A



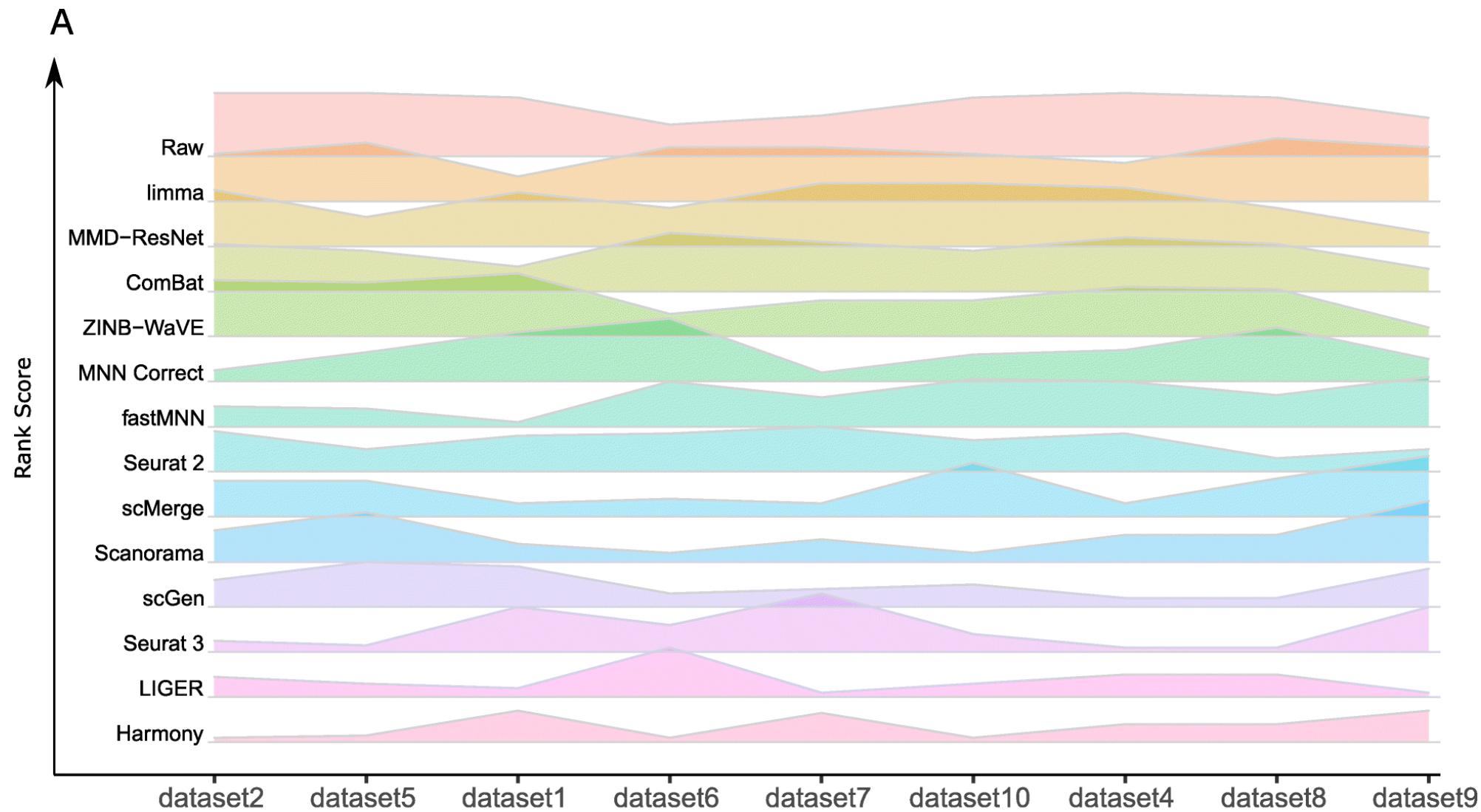
B



# Summary

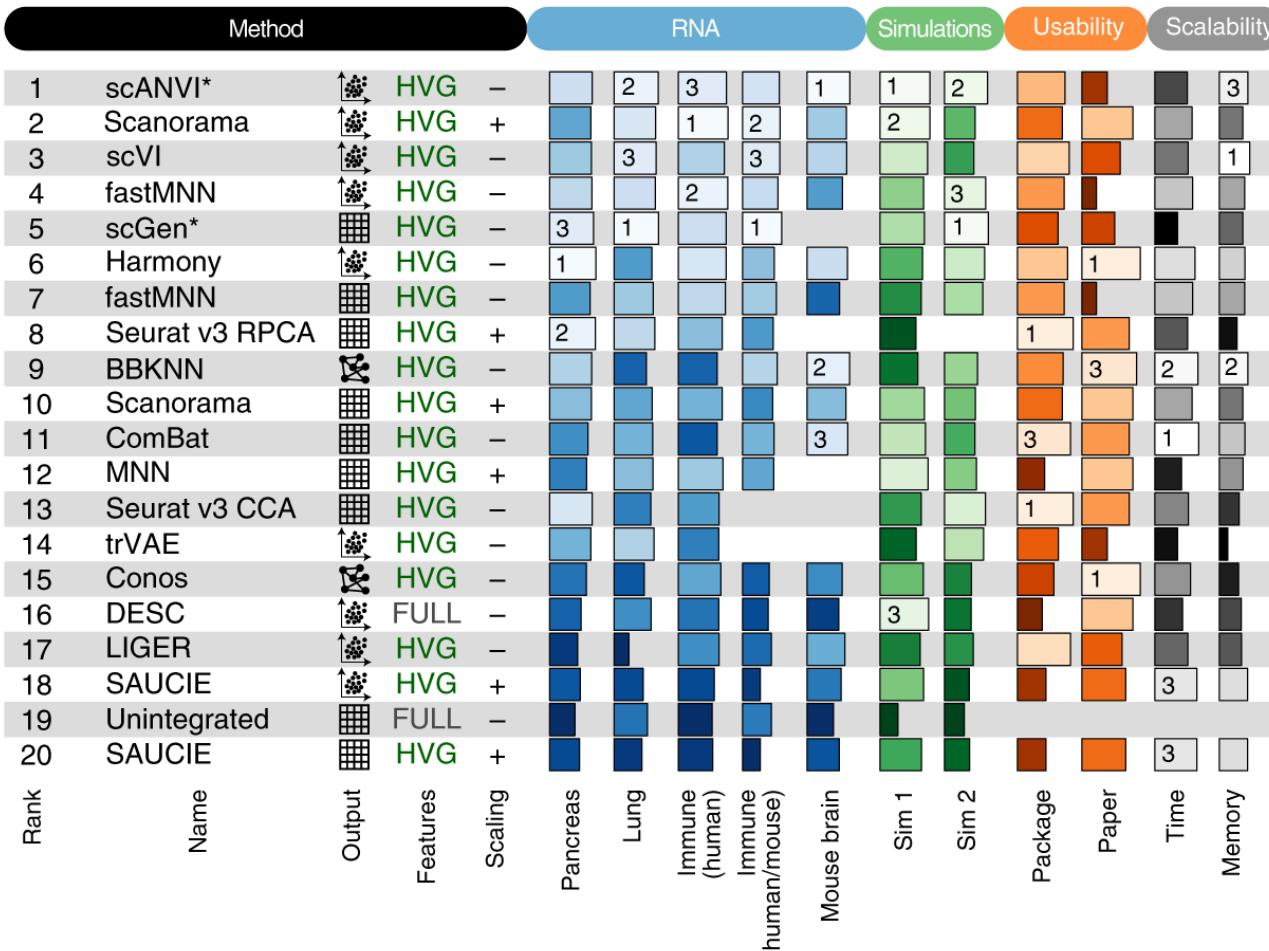
- Factor-model-based methods and cell-similarity based methods seem to be based on two different sets of assumptions on the batch effects
  - Factor-model-based: batch information and latent factors are nearly orthogonal to each other
  - Cell-similarity based: batch effect is very small compared to biological signals
  - The two assumptions seem quite different -> what is the consequence on performance?
- Factor-model-based methods can provide batch corrected gene expression matrix
  - May introduce false positives in down-stream differential testing
- Performance: Without using additional cell type information, cell-similarity based methods perform slightly better but the two strategies seem comparable

# Benchmarking results (Tran et. al. Genome Biology 2020)



# Benchmarking results (Luecken et. al. Nature Methods 2022)

**b**



Output  
 Genes  
 Embedding  
 Graph

Scaling  
+ Scaled  
- Unscaled

Ranking  
 1  
 20

# Related papers

- Argelaguet, R., Cuomo, A. S., Stegle, O., & Marioni, J. C. (2021). Computational principles and challenges in single-cell data integration. *Nature biotechnology*, 39(10), 1202-1215.
- Ritchie, M. E., Phipson, B., Wu, D. I., Hu, Y., Law, C. W., Shi, W., & Smyth, G. K. (2015). limma powers differential expression analyses for RNA-sequencing and microarray studies. *Nucleic acids research*, 43(7), e47-e47.
- Risso, D., Perraudeau, F., Gribkova, S., Dudoit, S., & Vert, J. P. (2018). A general and flexible method for signal extraction from single-cell RNA-seq data. *Nature communications*, 9(1), 284.
- Lopez, R., Regier, J., Cole, M. B., Jordan, M. I., & Yosef, N. (2018). Deep generative modeling for single-cell transcriptomics. *Nature methods*, 15(12), 1053-1058.
- Lotfollahi, M., Wolf, F. A., & Theis, F. J. (2019). scGen predicts single-cell perturbation responses. *Nature methods*, 16(8), 715-721.
- Xu, C., Lopez, R., Mehlman, E., Regier, J., Jordan, M. I., & Yosef, N. (2021). Probabilistic harmonization and annotation of single-cell transcriptomics data with deep generative models. *Molecular systems biology*, 17(1), e9620.
- Tran, H. T. N., Ang, K. S., Chevrier, M., Zhang, X., Lee, N. Y. S., Goh, M., & Chen, J. (2020). A benchmark of batch-effect correction methods for single-cell RNA sequencing data. *Genome biology*, 21, 1-32.
- Haghverdi, L., Lun, A. T., Morgan, M. D., & Marioni, J. C. (2018). Batch effects in single-cell RNA-sequencing data are corrected by matching mutual nearest neighbors. *Nature biotechnology*, 36(5), 421-427.
- Butler, A., Hoffman, P., Smibert, P., Papalexi, E., & Satija, R. (2018). Integrating single-cell transcriptomic data across different conditions, technologies, and species. *Nature biotechnology*, 36(5), 411-420.
- Stuart, T., Butler, A., Hoffman, P., Hafemeister, C., Papalexi, E., Mauck, W. M., ... & Satija, R. (2019). Comprehensive integration of single-cell data. *cell*, 177(7), 1888-1902.
- Hie, B., Bryson, B., & Berger, B. (2019). Efficient integration of heterogeneous single-cell transcriptomes using Scanorama. *Nature biotechnology*, 37(6), 685-691.
- Korsunsky, I., Millard, N., Fan, J., Slowikowski, K., Zhang, F., Wei, K., ... & Raychaudhuri, S. (2019). Fast, sensitive and accurate integration of single-cell data with Harmony. *Nature methods*, 16(12), 1289-1296.
- Luecken, M. D., Büttner, M., Chaichoompu, K., Danese, A., Interlandi, M., Müller, M. F., ... & Theis, F. J. (2022). Benchmarking atlas-level data integration in single-cell genomics. *Nature methods*, 19(1), 41-50.