Homework 5

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1 Problem 1

1.对一个问题,找个多多的分类器。这个雕化较踢2、磨曲的弱学习算法产生一组分类器,依次针对前面到中比较难苦的部分数据3、曲达一级淡器故要来分类新数据

2 Problem 2

- ①将数据集分成长份.
- ②.将其中分作为测试集,东下上1份作训练棒训练口,测试等到错误率
- ③、对数据题的k份中每一份进行②、得到k分,k个错误率,
- 图将所得可结起来(比如选最大错误举对应的新)、

3 Problem 3

3. 中
$$\mathcal{U}_{1}=(2.5,4.5)$$
 $\mathcal{U}_{2}=(2.5,0.5)$
则对 \mathcal{U}_{1} $\overset{*}{=}$ $\overset{*$

··对标题是1e,</br>
小对标题程序行列发展1,15m1=15m21</br>
// 5m1, 故1,2种划分较好。

4 Programming Problem 1

4.1 Result

Clastur No.	center	Number of samples
1	200	(5.93835690, 4.47548968)
2	201	(5.47541305, -4.52601645)
3	200	(1.02155866, -0.93527395)
4	199	(1.07159471, 4.01702333)
5	200	(9.00870491, -0.04025460)

4.2 Code

#!/usr/bin/python # coding=utf-8 import numpy as np

```
import matplotlib.pyplot as plt
Sigma = [[1, 0], [0, 1]]
gen_means = [[1, -1], [5.5, -4.5], [1, 4], [6, 4.5], [9, 0]]
EPS = 1E-4
def gen_points():
    x, y = [],[]
    for mean in gen_means:
        x[len(x):len(x)], y[len(y):len(y)] =
            np.random.multivariate_normal(mean, Sigma, 200).T
    return x, y
def get_samples(x, y):
    samples = []
    for i in range(len(x)):
        samples.append([x[i], y[i]])
    return samples
def get_rand_mean(x, y, size):
    x_min = np.min(x)
    x_max = np.max(x)
    y_min = np.min(y)
    y_max = np.max(y)
    means = np.random.random((size, 2))
    # print (means)
    for xy in means:
        xy[0] = (x_max - x_min) * xy[0] + x_min
        xy[1] = (y_{max} - y_{min}) * xy[1] + y_{min}
    return means
def vector_add(a, b):
    c = []
    c [0:0] = a
    for i in range(len(a)):
        c[i] += b[i]
    return c
def vector_add_inplace(a, b):
    for i in range(len(a)):
        a[i] += b[i]
    return a
def vector_sub(a, b):
    c = []
    c[0:0] = a
    for i in range(len(a)):
        c[i] -= b[i]
    return c
def k_means(samples, means):
    # print(sums, cnt)
    changed = True
    \# str = ""
    while changed:
        sums = []
```

```
for i in range(len(means)):
            sums.append ([0, 0])
        cnt = [0] * len(means)
        for sample in samples:
            mi = 0
            \min_{l} = 1E10
            for i in range (len (means)):
                 dif = np.array(vector_sub(sample, means[i]))
                 l = np.sqrt(dif.dot(dif))
                 if l < min_l:
                     mi = i
                     \min_{-1} = 1
            vector_add_inplace(sums[mi], sample)
            cnt[mi] += 1
        changed = False
        print("cnt:", cnt)
        # print("sum:", np.array(sums))
        for i in range(len(means)):
            if cnt[i] > 0:
                 for j in range(len(sums[i])):
                     sums [ i ] [ j ] /= cnt [ i ]
             if np.max(np.abs(vector_sub(means[i], sums[i]))) > EPS:
                 changed = True
            means[i] = sums[i]
        # print("means:", np.array(means))
    return means
def rand_k_mins(x, y, samples, times):
    for cnt in range (times):
        means = get_rand_mean(x, y, 5)
        print ( means )
        new_means = k_means(samples, means)
        print(new_means)
if \ \_\_name\_\_ = '\_\_main\_\_':
    x, y = gen_points()
    \# plt.scatter(x, y)
    # plt.show()
    samples = get_samples(x, y)
    rand_k_mins(x, y, samples, 1)
    \# means = gen\_means
    \# new\_means = k\_means(samples, means)
    \# print(new\_means)
    plt.scatter(x, y)
    plt.show()
```

5 Programming Problem 1

5.1 Result

Figure 1: Figure for Batch BP

5.2 Code

#!/usr/bin/python

```
\# coding=utf-8
import numpy as np
import matplotlib.pyplot as plt
from numpy import linalg as LA
data_file_path = './PP2.data'
sigma2 = 1**2
k_nearest = 5
k_{eigen_vectors} = 2
EPS = 1E-9
num\_of\_clusters = 2
def get_samples():
    samples = []
    with open(data_file_path, mode="r") as in_file:
        for line in in_file:
             row = line.split()
             xs = [float(a) for a in row]
             samples.append(xs)
    return samples
def get_wij(pa, pb):
    d2 = np.sum([(pa[i] - pb[i])**2  for i  in range(len(pa))])
    return np. \exp(-d2 / 2 / \text{sigma2})
\mathbf{def} \ \mathrm{get_-wij}(\mathrm{d}2):
    return np.\exp(-d2 / 2 / \text{sigma2})
def build_graph(samples):
    S = np.asarray(samples)
    N = len(samples)
    G = np.zeros([N, N])
    dis = np.zeros(N)
    for r in range (N):
        for c in range (N):
             if r = c:
                 dis[c] = 0
             else:
                 v = np.subtract(S[r], S[c])
                 dis[c] = np.sum([x**2 for x in v])
        indexes = np.argsort(dis)
        \# print(indexes[0:k+1])
        \# print(dis[0:11])
        # input()
        k = k_nearest
        for i in indexes [1:k+1]:
            G[r][i] = get_wij(dis[i])
    return G
def compute_L_sym(W):
    W_{mat} = np.asmatrix(W)
    W_{mat} = (W_{mat}.T + W) / 2
    D_half_rev = np.asmatrix(np.zeros(W.shape))
    \# print(D_half_rev)
    for r in range(len(D_half_rev)):
```

```
s = np.sum(W_mat[r])
        \# print(D_-half_-rev/r, r)
        D_half_rev[r, r] = 1 / np.sqrt(s)
   \# print(D_half_rev)
    I = np.identity(len(W_mat))
   L_sym = I - D_half_rev * W_mat * D_half_rev
    return L_sym
def normalize(v):
    s = v * v.T
    v \neq np.sqrt(s)
   return v
def compute_Accu(omega):
    dic = \{\}
    for i in range(num_of_clusters):
        dic[i] = 0
    for i in range (0, 100):
        dic [omega[i]] += 1
    n1 = max(dic.items(), key=lambda x: x[1])
    for i in range(num_of_clusters):
        dic[i] = 0
    for i in range (100, 200):
        dic [omega[i]] += 1
    n2 = max(dic.items(), key=lambda x: x[1])
    Accu = (n1[1] + n2[1]) / 200
    print (n1, n2, Accu)
    return Accu
def spectral_clustering (W):
    L_s = compute_L_{sym}(W)
   w, v = LA. eigh(L.s)
    f = 0 # first none-zero eigen column
    while np.abs(w[f]) < EPS:
        f += 1
   U = v[:, f:f + k_eigen_vectors]
   # Normalizing
    for row in U:
        normalize (row)
   # print("U: ", U)
    Accu = 0
    for cnt in range (5):
        omega = k_means(U, num_of_clusters)
        t = compute\_Accu(omega)
        Accu = max(Accu, t)
    return Accu
def dis2(a, b):
   d = np.subtract(a, b)
    return d * d.T
def k_means(samples, clusters):
   N = clusters
   S = np. asmatrix (samples)
   means = 2 * np.random.random(S.shape[1] * N) - 1
    means = means.reshape([clusters, S.shape[1]])
```

```
# print("initial means: ", means)
    changed = True
   omega = np.zeros(S.shape[0])
    while changed:
        changed = False
        sums = np.asmatrix(np.zeros(means.shape))
        cnt = np.zeros(means.shape[0])
        for s_i in range(len(S)):
            x = S[s_i]
            mean_i = np.argmin([dis2(x, mean) for mean in means])
            np.add(sums[mean_i], x, sums[mean_i])
            omega[s_i] = mean_i
            cnt[mean_i] += 1
        # print("cnt: ", cnt)
        for i in range(len(sums)):
            sums[i] /= cnt[i]
            diff = np.subtract(sums[i], means[i])
            if np.max(np.abs(diff)) > EPS:
                changed = True
            means[i] = sums[i]
        # print (means)
        # input()
    return omega
def frange(x, y, jump):
  while x < y:
    yield x
   x += jump
if _-name_- = '_-main_-':
    samples = get\_samples()
   # When sigma changes
   Accu = []
   x = []
    for sig in frange (1, 10, 0.5):
        x.append(sig)
        sigma2 = sig**2
       W = build_graph (samples)
        Accu.append(spectral_clustering(W))
    plt.plot(x, Accu)
    plt.show()
   # When k changes
    Accu = []
   x = []
    sigma2 = 1
    for k in range (1, 200, 10):
        x.append(k)
        k_nearest = k
       W = build_graph (samples)
        Accu.append(spectral_clustering(W))
    plt.plot(x, Accu)
    plt.show()
   \# Accu = spectral_-clustering(W)
   # print(Accu)
```