

1. Give a factor  $1/2$  approximation algorithm for the MAX-CUT.
2. Let  $P \in F[x_1, x_2, \dots, x_n]$  be a non-zero polynomial of total degree  $d \geq 0$  over a field,  $F$ . Let  $S$  be a finite subset of  $F$  and let  $r_1, r_2, \dots, r_n$  be selected at random independently and uniformly from  $S$ . Prove that

$$\Pr[P(r_1, r_2, \dots, r_n) = 0] \leq \frac{d}{|S|}.$$