

1. Temperature-dependent material properties of UO₂

(1) Density (kg/m³) ^[1]

$$\rho_u = 10960(a + bT + cT^2 + dT^3)^{-3}$$

Where, T represents the temperature (K).

Table 1: Material parameter values for the density.

Parameter	$T \leq 923K$	$T > 923K$
a	0.99734	0.99672
b	9.802×10^{-6}	1.179×10^{-5}
c	-2.705×10^{-10}	-2.429×10^{-9}
d	4.391×10^{-11}	1.219×10^{-12}

(2) Thermal conductivity (W / m / K) ^[2]

$$k_u = k_{95} \cdot f_d \cdot f_p \cdot f_{pro} \cdot f_x \cdot f_r$$

k_{95} refers to the thermal conductivity of unirradiated uranium dioxide at 95% theoretical density (W / m / K) ; f_d is the soluble fission product correction factor; f_p is the insoluble fission product correction factor; f_{pro} is the porosity correction factor; f_x represents the deviation from stoichiometry, taken as 1.0 in this case; and f_r is the irradiation effect correction factor.

The temperature range for this model is 298~3120K, and the specific forms of these correction factors are as follows:

$$k_{95} = \frac{100}{7.5408 + 17.692 \cdot T^{-3} + 3.6142 \cdot T^{-6}} + \frac{6400}{T^{15/2}} \exp\left(-\frac{16.35}{T^{-3}}\right)$$

$$f_d = \left(\frac{1.09}{Bu^{3.265}} + 0.0643 \cdot \sqrt{\frac{T}{Bu}} \right) \times \arctan \left(\frac{1.0}{\frac{1.09}{Bu^{3.265}} + 0.0643 \cdot \sqrt{\frac{T}{Bu}}} \right)$$

$$f_p = 1.0 + \left(\frac{0.019Bu}{3.0 - 0.019Bu} \right) \times \left(\frac{1.0}{1.0 + \exp\left(\frac{-T + 1200}{100}\right)} \right)$$

$$f_{por} = \frac{1.0 - p}{1.0 + 0.5p}$$

$$f_r = 1.0 - \frac{0.2}{1.0 + \exp\left(\frac{T - 900}{80}\right)}$$

Where, Bu represents the burnup (%); p represents the fuel porosity (%).

(3) Specific heat capacity (J / kg / K) ^[3]

$$C_u = C_1 \left(\frac{\theta}{T} \right)^2 \exp\left(\frac{\theta}{T}\right) \left(\exp\left(\frac{\theta}{T}\right) - 1 \right)^{-2} + 2C_2T + C_3E_a \exp\left(\frac{-E_a}{T}\right) T^{-2}$$

Where C_1 , C_2 and C_3 are material parameters, with values of 302.27 J/kg/K , $8.463 \times 10^{-3} \text{ J/kg/K}$ and $8.741 \times 10^7 \text{ J/kg/K}$, respectively. θ is the Einstein temperature, with a value of 548.68 K ; E_a is the ratio of electronic activation energy to the Boltzmann constant, with a value of 18531.7 K .

- (4) Coefficient of thermal expansion ($1/\text{K}$)^[4]

$$\alpha_u = m + nT + jT^2 + kT^3$$

Table 2: Material parameter values for the coefficient of thermal expansion.

Parameter	$T \leq 923\text{K}$	$T > 923\text{K}$
m	9.28×10^{-6}	1.183×10^{-5}
n	-6.390×10^{-10}	-5.103×10^{-9}
j	1.33×10^{-12}	3.756×10^{-12}
k	-1.757×10^{-17}	-6.125×10^{-17}

- (5) Young's modulus (Pa)^[5]

$$E_u = 2.334 \times 10^{11} (1 - 2.752(1 - D))(1 - 1.0915 \times 10^{-4} T)$$

2. Temperature-dependent material properties of 316SS^[6]

- (1) Density (kg/m^3)

$$\rho = 8084 - 0.4209T - 3.894 \times 10^{-5} T^2$$

- (2) Thermal conductivity (W/m/K)

$$k = 9.248 + 0.01571T$$

- (3) Specific heat capacity (J/kg/K)

$$c_p = 462 + 0.134T$$

- (4) Coefficient of thermal expansion ($1/\text{K}$)

$$\alpha_c(T) = 1.789 \times 10^{-5} + 2.398 \times 10^{-9} T + 3.269 \times 10^{-13} T^2$$

- (5) Young's modulus (Pa)

$$E = 2.15946 \times 10^{11} - 7.07727 \times 10^7 T$$

- (6) Melting point: 1700K

- (7) Yield strength (MPa)

$$\sigma_{0.2\%} = \begin{cases} 555.5 - 0.25T & \text{if } T < 600^\circ\text{C} \\ 405.5 - 0.775(T - 600) & \text{if } 600^\circ\text{C} < T < 1000^\circ\text{C} \\ 345.5 - 0.25T & \text{if } T > 1000^\circ\text{C} \end{cases}$$

The material parameters listed above are primarily sourced from the referenced literature, with some modifications based on experiments conducted by the Nuclear Power Institute of China.

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