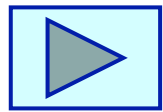


CS3230 Lecture 1

“Algorithms & Motivation”

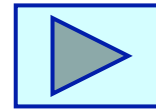
□ Lecture Topics and Readings



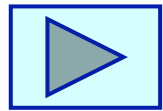
❖ **Algorithms is Cool**

[CLRS]-C1

❖ **Stable Marriage Problem**



[KT06]-C1



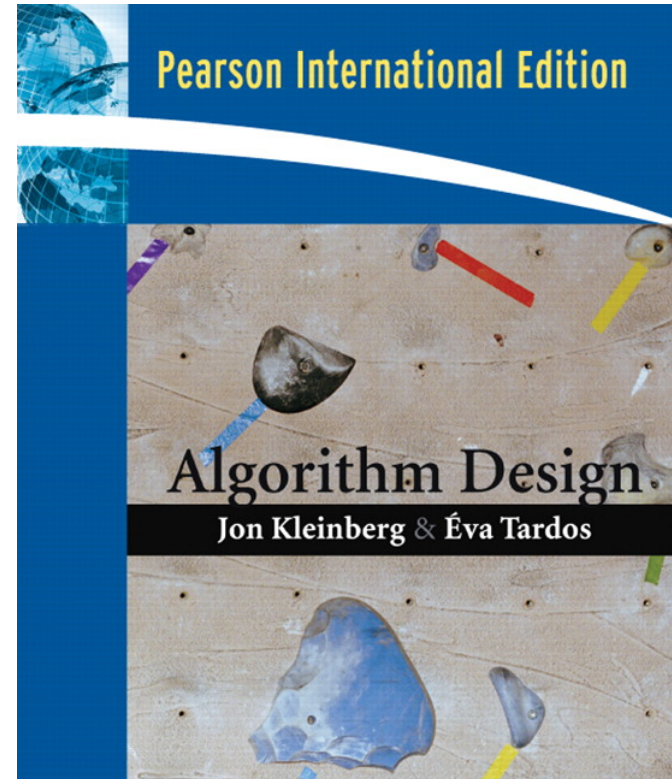
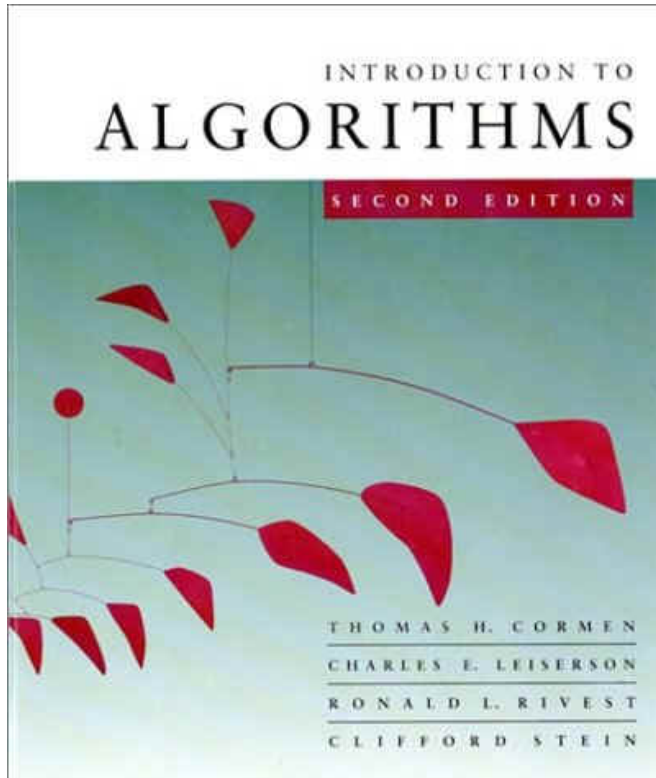
❖ **Some Sample Problems**

[KT06]-C1

□ **Assignment:** HW0 – Due: Fri, 15-Aug (< 12nn)
in drop-box outside my office, COM1-03-17

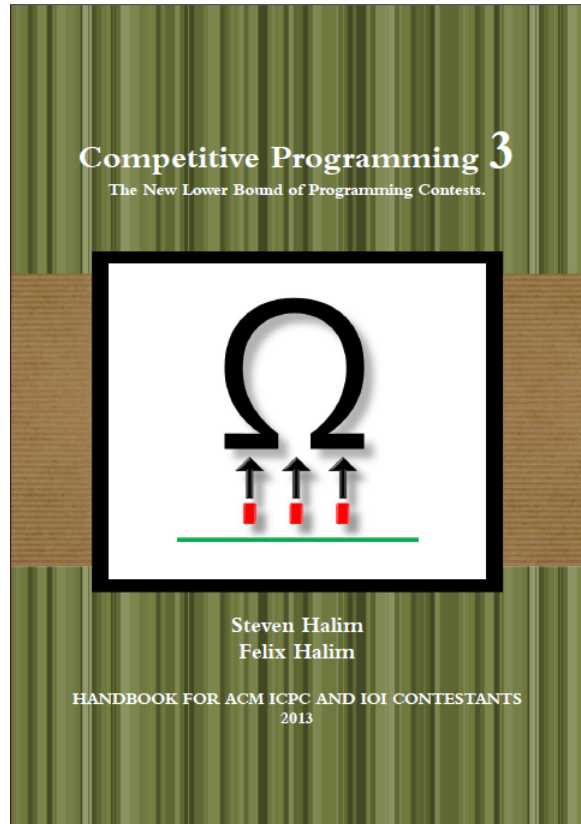
*Algorithms is Cool,
Stable Marriage is “easy” with algorithm*

[CLRS] and [KT06]

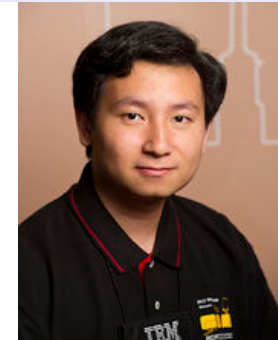


Two good books on
algorithm design and analysis.

[CP13]



Good book on
competitive programming.
By our very own
Steven Halim and Felix Halim



Stable Marriage → Nobel Prize

Put theory into practice;
implemented, tested, deploy

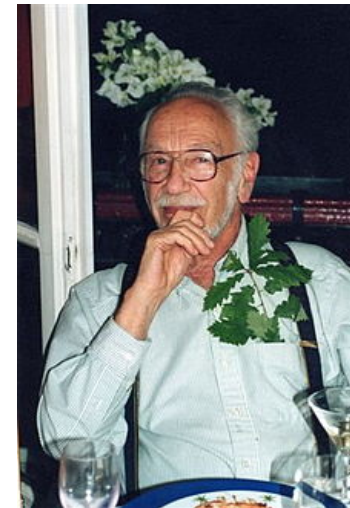


Alvin E. Roth



Lloyd S. Shapley

Developed theory & algorithm
(Gale-Shapley algorithm)



David Gale
(1921-2008)

Alvin Roth & Lloyd Shapley
(Nobel Prize, Economics, 2012)

http://www.nobelprize.org/nobel_prizes/economic-sciences/laureates/2012/

“Algorithms is Cool”

- ❑ Where do we use Algorithms
- ❑ Analysis of Algorithms & Why it is important
- ❑ Sample Computational Problems

Why Algorithm is Cool:

Algorithms is Anywhere & Everywhere.

Motivation

□ Where do we use Algorithms?

- ❖ Computer Science, Engineering
- ❖ Business, Operations Research
- ❖ Finance, Social Sciences, ... , Everywhere

□ Why is Performance Important?

- ❖ Exponential-size solution space
- ❖ NP-completeness

□ Problem Size Explosion

- ❖ Computer Chip Complexity,
- ❖ Database Sizes,
- ❖ Human Genome Project, WWW (Google),

Diverse Applications

- ❖ **Design the next generation computer chip**
 - ◆ *how to design optimally (wrt speed, power, area)*
- ❖ **Internet (WWW)**
 - ◆ *how to manage, manipulate large volume of data*
- ❖ **e-Commerce**
 - ◆ *how to manage transaction (secure, private)*
- ❖ **Logistics**
 - ◆ *how to manage transport/transfer of goods, people*
- ❖ **Human Genome Project**
 - ◆ *how to analyze huge volume of DNA/protein data*

Analysis of algorithms

The theoretical study of computer-program performance and resource usage.

What's often more important than *performance*?

- modularity
- correctness
- maintainability
- functionality
- robustness
- user-friendliness
- programmer time
- simplicity
- extensibility
- reliability

Why study algorithms and performance?

- ❑ Algorithms help us to understand *scalability*.
- ❑ Performance often draws the line between what is *feasible* and what is *impossible*.
- ❑ Algorithmic mathematics provides a *language* for talking about program behavior.
- ❑ Performance is the *currency* of computing.
- ❑ The lessons of program performance *generalize* to other computing resources.
- ❑ Speed is *fun*!

Design and Analysis of Algorithms

□ Given a problem P ,

❖ Can it be solved?

Computability

□ If “Yes”, given an algorithm A for solving P ,

❖ Is algorithm A correct ?

Verification

❖ How good is algorithm A ?

Efficiency

❖ Can find a better algorithm A' ?

□ How do we define good?

❖ How much time it takes.

Time Complexity

❖ How much space it uses.

Space Complexity

Complexity

□ Given an algorithm A for problem P ,

□ How to do better?

Complexity of Algorithm

- ❖ Is the time complexity of A polynomial ?
- ❖ Can we design faster algorithm A' ?
- ❖ Can we design algorithm A'' that uses less space

□ Can we do better?

Complexity of Problem

- ❖ Is the problem NP-complete?
- ❖ Can we establish lower bounds
- ❖ Is the algorithm “*best possible*”



***Too boring?
is it useful?***

Testing * operation in a CPU

Q: How to test that the “*” operation of your CPU is correct?

A: Check exhaustively. for all a, b
Check $a * b = c$

Q: How long will it take?

A: Any guesses?



Testing * operation in a CPU

Q: How long will it take?

Assume we use a 100 G-Flop CPU
can take 100B operations per sec.

a is a 32-bit number (2^{32} cases)

b is a 32-bit number (2^{32} cases)

So, $(a * b)$ there are (2^{64} cases)

Time taken = $(2^{64} / 100 \times 10^9)$ sec

≈ 6 years!



$2^{64} / 100 \times 10^9$ seconds



Examples Random

Assuming seconds of time for "seconds" | Use **seconds of arc** instead

<http://www.wolframalpha.com/input/?i=2^64+%2F+100x10^9+seconds> ←- URL

Input interpretation:

$$\frac{2^{64}}{100 \times 10^9} \text{ seconds}$$

Unit conversions:

More

3.074×10^6 minutes

51 241 hours

2135 days

305 weeks

70.19 months

Testing * operation in a CPU

Q: What if we have $(n \lg n)$ algorithm?

Assume we use a 100G-Flop CPU
can take 100B operations per sec.

a is a 32-bit number (2^{32} cases)

b is a 32-bit number (2^{32} cases)

When $n = 2^{32}$, with $(n \lg n)$ algorithm

Time taken = $(2^{32} * 32 / 100 \times 10^9)$ sec

< 2 sec!



Moral of the story

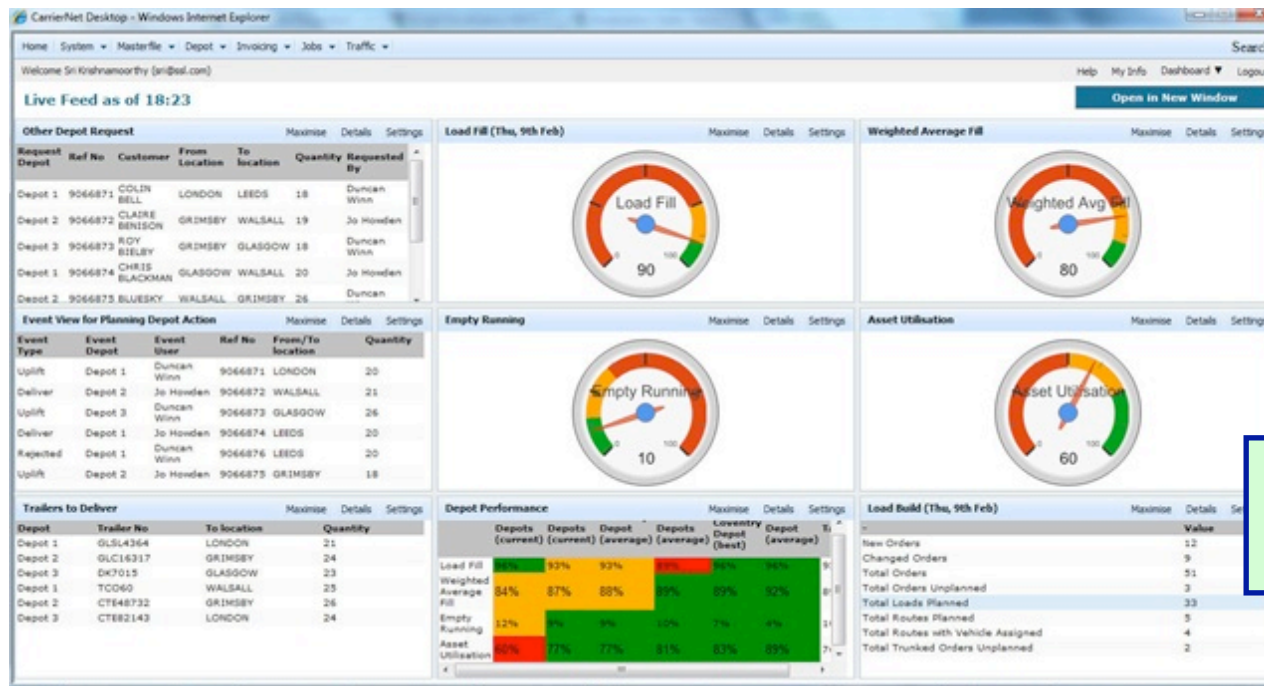
Analysis of algorithms
help us make *predictions*.

Analysis of algorithms
help us *prepare for the worst case*.

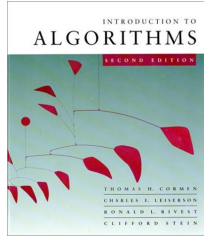
Story of Algorithms in Action

Credit card processing centre in SG (Sci Park):

- monitor showing servers load for diff. countries, green, orange alert (sends SMS), RED alert (urgent!) → deploy more servers!



Note: Picture is not so good. But is “demos” my point. Will find a better one.



Why study algorithms and performance?

- Algorithms help us to understand *scalability*.
- Performance often draws the line between what is feasible and what is impossible.
- Algorithmic mathematics provides a *language* for talking about program behavior.
- Performance is the *currency* of computing.
- The lessons of program performance generalize to other computing resources.
- Speed is fun!

Thank you.

Q & A



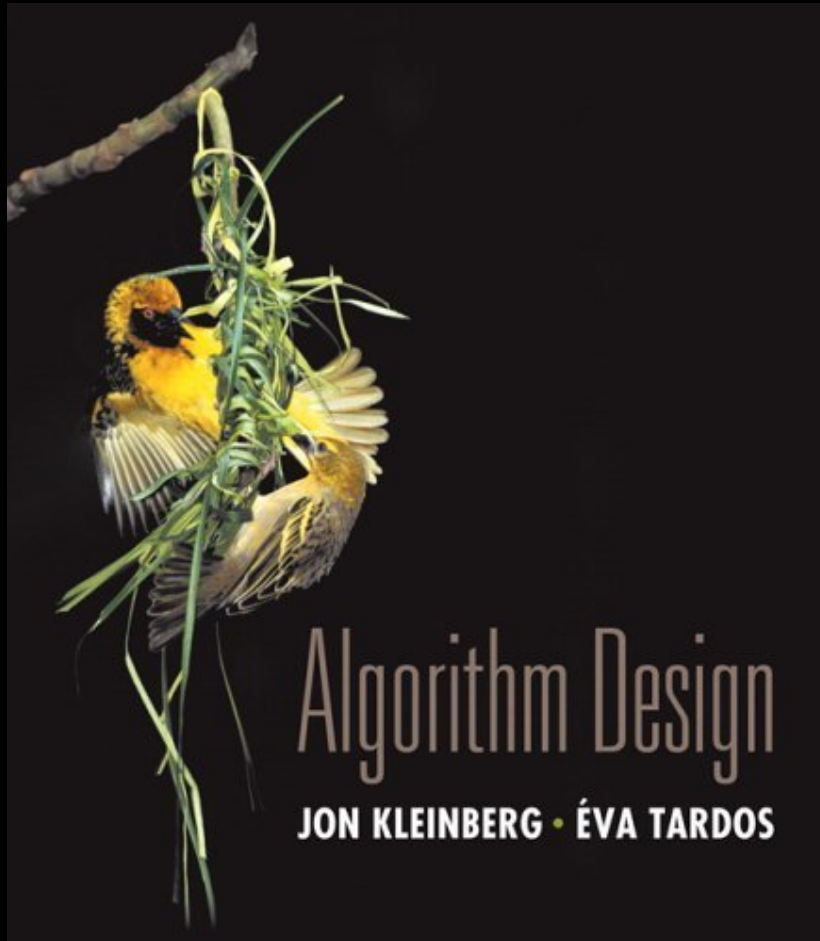
For CS3230 (Fall 2013)

For CS3230, we will only cover

- * Basics of Stable Matching Problem (Slides 3-17, 25)
- * Five Sample Problems (Slides 27-33)

The extensions to “Men Optimality and Women Pessimality” are **fun**, but they are outside the scope of CS3230 and optional.

The same for Extensions to “Matching Residents to Hospital” and the extra slides.



Chapter 1

Introduction: Some Representative Problems



Slides by Kevin Wayne.
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1.1 A First Problem: Stable Matching

Matching Residents to Hospitals

Goal. Given a set of preferences among hospitals and medical school students, design a **self-reinforcing** admissions process.

Unstable pair: applicant x and hospital y are **unstable** if:

- x prefers y to its assigned hospital.
- y prefers x to one of its admitted students.

Stable assignment. Assignment with no unstable pairs.

- Natural and desirable condition.
- Individual self-interest will prevent any applicant/hospital deal from being made.

Stable Matching Problem

Goal. Given n men and n women, find a "suitable" matching.

- Participants rate members of opposite sex.
- Each man lists women in order of preference from best to worst.
- Each woman lists men in order of preference from best to worst.

	favorite ↓ 1 st	2 nd	least favorite ↓ 3 rd
Xavier	Amy	Bertha	Clare
Yancey	Bertha	Amy	Clare
Zeus	Amy	Bertha	Clare

Men's Preference Profile

	favorite ↓ 1 st	2 nd	least favorite ↓ 3 rd
Amy	Yancey	Xavier	Zeus
Bertha	Xavier	Yancey	Zeus
Clare	Xavier	Yancey	Zeus

Women's Preference Profile

Stable Matching Problem

Perfect matching: everyone is matched monogamously.

- Each man gets exactly one woman.
- Each woman gets exactly one man.

Stability: no incentive for some pair of participants to undermine assignment by joint action.

- In matching M , an unmatched pair m - w is **unstable** if man m and woman w prefer each other to current partners.
- Unstable pair m - w could each improve by eloping.

Stable matching: perfect matching with no unstable pairs.

Stable matching problem. Given the preference lists of n men and n women, find a stable matching if one exists.

Stable Matching Problem

Q. Is assignment X-C, Y-B, Z-A stable?

	favorite ↓		least favorite ↓
	1 st	2 nd	3 rd
Xavier	Amy	Bertha	Clare
Yancey	Bertha	Amy	Clare
Zeus	Amy	Bertha	Clare

Men's Preference Profile

	favorite ↓		least favorite ↓
	1 st	2 nd	3 rd
Amy	Yancey	Xavier	Zeus
Bertha	Xavier	Yancey	Zeus
Clare	Xavier	Yancey	Zeus

Women's Preference Profile

Stable Matching Problem

Q. Is assignment X-C, Y-B, Z-A stable?

A. No. Bertha and Xavier will hook up.

	favorite ↓		least favorite ↓
	1 st	2 nd	3 rd
Xavier	Amy	Bertha	Clare
Yancey	Bertha	Amy	Clare
Zeus	Amy	Bertha	Clare

Men's Preference Profile

	favorite ↓		least favorite ↓
	1 st	2 nd	3 rd
Amy	Yancey	Xavier	Zeus
Bertha	Xavier	Yancey	Zeus
Clare	Xavier	Yancey	Zeus

Women's Preference Profile

Stable Matching Problem

Q. Is assignment X-A, Y-B, Z-C stable?

A. Yes.

	favorite ↓		least favorite ↓
	1 st	2 nd	3 rd
Xavier	Amy	Bertha	Clare
Yancey	Bertha	Amy	Clare
Zeus	Amy	Bertha	Clare

Men's Preference Profile

	favorite ↓		least favorite ↓
	1 st	2 nd	3 rd
Amy	Yancey	Xavier	Zeus
Bertha	Xavier	Yancey	Zeus
Clare	Xavier	Yancey	Zeus

Women's Preference Profile

A Related Problem: Stable Roommate Problem

Q. Do stable matchings always exist?

A. Not obvious a priori.

↖
is core of market nonempty?

Stable roommate problem. [Closely related, but not the same]

- $2n$ people; each person ranks others from 1 to $2n-1$.
- Assign roommate pairs so that no unstable pairs.

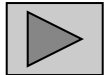
	1 st	2 nd	3 rd
Adam	B	C	D
Bob	C	A	D
Chris	A	B	D
Doofus	A	B	C

$A-B, C-D \Rightarrow B-C$ unstable
 $A-C, B-D \Rightarrow A-B$ unstable
 $A-D, B-C \Rightarrow A-C$ unstable

Observation. Stable matchings do not always exist for the stable roommate problem.

Propose-And-Reject Algorithm

Propose-and-reject algorithm. [Gale-Shapley 1962] Intuitive method that guarantees to find a stable matching.



```
Initialize each person to be free.
while (some man is free and hasn't proposed to every woman) {
    Choose such a man m
    w = 1st woman on m's list to whom m has not yet proposed
    if (w is free)
        assign m and w to be engaged
    else if (w prefers m to her fiancé m')
        assign m and w to be engaged, and m' to be free
    else
        w rejects m
}
```

Proof of Correctness: Termination

Observation 1. Men propose to women in decreasing order of preference.

Observation 2. Once a woman is matched, she never becomes unmatched; she only "trades up."

Claim. Algorithm terminates after at most n^2 iterations of while loop.

Pf. Each time through the while loop a man proposes to a new woman. There are only n^2 possible proposals. ■

	1 st	2 nd	3 rd	4 th	5 th
Victor	A	B	C	D	E
Wyatt	B	C	D	A	E
Xavier	C	D	A	B	E
Yancey	D	A	B	C	E
Zeus	A	B	C	D	E

	1 st	2 nd	3 rd	4 th	5 th
Amy	W	X	Y	Z	V
Bertha	X	Y	Z	V	W
Clare	Y	Z	V	W	X
Diane	Z	V	W	X	Y
Erika	V	W	X	Y	Z

$n(n-1) + 1$ proposals required

Proof of Correctness: Perfection

Claim. All men and women get matched.

Pf. (by contradiction)

- Suppose, for sake of contradiction, that Zeus is not matched upon termination of algorithm.
- Then some woman, say Amy, is not matched upon termination.
- By Observation 2, Amy was never proposed to.
- But, Zeus proposes to everyone, since he ends up unmatched. ▪

Proof of Correctness: Stability

Claim. No unstable pairs.

Pf. (by contradiction)

- Suppose A - Z is an unstable pair: each prefers each other to partner in Gale-Shapley matching S^* .
- Case 1: Z never proposed to A .
 - $\Rightarrow Z$ prefers his GS partner to A .
 - $\Rightarrow A$ - Z is stable.
- Case 2: Z proposed to A .
 - $\Rightarrow A$ rejected Z (right away or later)
 - $\Rightarrow A$ prefers her GS partner to Z .
 - $\Rightarrow A$ - Z is stable.
- In either case A - Z is stable, a contradiction. ▪

men propose in decreasing
order of preference

S^*

Amy-Yancey

Bertha-Zeus

...

← women only trade up

Summary

Stable matching problem. Given n men and n women, and their preferences, find a stable matching if one exists.

Gale-Shapley algorithm. Guarantees to find a stable matching for **any** problem instance.

Q. How to implement GS algorithm efficiently?

Q. If there are multiple stable matchings, which one does GS find?

Efficient Implementation

Efficient implementation. We describe $O(n^2)$ time implementation.

Representing men and women.

- Assume men are named $1, \dots, n$.
- Assume women are named $1', \dots, n'$.

Engagements.

- Maintain a list of free men, e.g., in a queue.
- Maintain two arrays `wife[m]`, and `husband[w]`.
 - set entry to 0 if unmatched
 - if m matched to w then `wife[m]=w` and `husband[w]=m`

Men proposing.

- For each man, maintain a list of women, ordered by preference.
- Maintain an array `count[m]` that counts the number of proposals made by man m .

Efficient Implementation

Women rejecting/accepting.

- Does woman w prefer man m to man m' ?
- For each woman, create **inverse** of preference list of men.
- Constant time access for each query after $O(n)$ preprocessing.

Amy	1 st	2 nd	3 rd	4 th	5 th	6 th	7 th	8 th
Pref	8	3	7	1	4	5	6	2

Amy	1	2	3	4	5	6	7	8
Inverse	4 th	8 th	2 nd	5 th	6 th	7 th	3 rd	1 st

```
for i = 1 to n  
    inverse[pref[i]] = i
```

Amy prefers man 3 to 6
since $\text{inverse}[3] < \text{inverse}[6]$

2 7

Understanding the Solution (1)

Q. For a given problem instance, there may be several stable matchings. Do all executions of *Gale-Shapley* yield the same stable matching? If so, which one?

An instance with two stable matchings.

- A-X, B-Y, C-Z.
- A-Y, B-X, C-Z.

	1 st	2 nd	3 rd
Xavier	A	B	C
Yancey	B	A	C
Zeus	A	B	C

	1 st	2 nd	3 rd
Amy	Y	X	Z
Bertha	X	Y	Z
Clare	X	Y	Z

Understanding the Solution (2)

Q. For a given problem instance, there may be several stable matchings. Do all executions of *Gale-Shapley* yield the same stable matching? If so, which one?

Def. Man m is a **valid partner** of woman w if there exists some stable matching in which they are matched.

Def. **Man-optimal assignment.** Each man receives best valid partner.

Understanding the Solution (3)

Def. Man-optimal assignment. Each man receives best valid partner.

Claim. All executions of GS yield **man-optimal** assignment, which is a stable matching!

- No reason a priori to believe that man-optimal assignment is perfect, let alone stable.
- Simultaneously best for each and every man.

Man Optimality

Claim. GS matching S^* is man-optimal.

Pf. (by contradiction)

- Suppose some man is paired with someone other than best partner. Men propose in decreasing order of preference \Rightarrow some man is rejected by valid partner.
- Let Y be **first** such man, and let A be **first** valid woman that rejects him.
- Let S be a stable matching where A and Y are matched.
- When Y is rejected, A forms (or reaffirms) engagement with a man, say Z , whom she prefers to Y .
- Let B be Z 's partner in S .
- Z not rejected by any valid partner at the point when Y is rejected by A . Thus, Z prefers A to B .
- But A prefers Z to Y .
- Thus A - Z is unstable in S . ▪

S	
	Amy-Yancey
	Bertha-Zeus
	...

↑
since this is first rejection
by a valid partner

Stable Matching Summary

Stable matching problem. Given preference profiles of n men and n women, find a **stable** matching.

↖
no man and woman prefer to be with each other than assigned partner

Gale-Shapley algorithm. Finds a stable matching in $O(n^2)$ time.

Man-optimality. In version of *GS* where men propose, each man receives best valid partner.

↖
 w is a valid partner of m if there exist some stable matching where m and w are paired

Q. Does man-optimality come at the expense of the women?

Woman Pessimality

Woman-pessimal assignment. Each woman receives worst valid partner.

Claim. GS finds **woman-pessimal** stable matching S^* .

Pf.

- Suppose A - Z matched in S^* , but Z is not worst valid partner for A .
- There exists stable matching S in which A is paired with a man, say Y , whom she likes less than Z .
- Let B be Z 's partner in S .
- Z prefers A to B . \leftarrow man-optimality
- Thus, A - Z is an unstable in S . ■

S	
Amy	Yancey
Bertha	Zeus
...	

Extensions: Matching Residents to Hospitals

Ex: Men \approx hospitals, Women \approx med school residents.

Variant 1. Some participants declare others as unacceptable.

Variant 2. Unequal number of men and women.

↖
resident A unwilling to
work in Cleveland

Variant 3. Limited polygamy.

↖
hospital X wants to hire 3 residents

Def. Matching S **unstable** if there is a hospital h and resident r such that:

- h and r are acceptable to each other; and
- either r is unmatched, or r prefers h to her assigned hospital; and
- either h does not have all its places filled, or h prefers r to at least one of its assigned residents.

Application: Matching Residents to Hospitals

NRMP. (National Resident Matching Program)

- Original use just after WWII. ← predates computer usage
- Ends of March, 23,000+ residents.

Rural hospital dilemma.

- Certain hospitals (mainly in rural areas) were unpopular and declared unacceptable by many residents.
- Rural hospitals were under-subscribed in NRMP matching.
- How can we find stable matching that benefits "rural hospitals"?







Rural Hospital Theorem. Rural hospitals get exactly same residents in every stable matching!

Lessons Learned

Powerful ideas learned in course.

- Isolate underlying structure of problem.
- Create useful and efficient algorithms.

Potentially deep social ramifications. [legal disclaimer]

-  Historically, men propose to women. Why not vice versa?
-  Men: propose early and often.
-  Men: be more honest.
-  Women: ask out the guys.
-  Theory can be socially enriching and fun!
-  CS majors get the best partners!

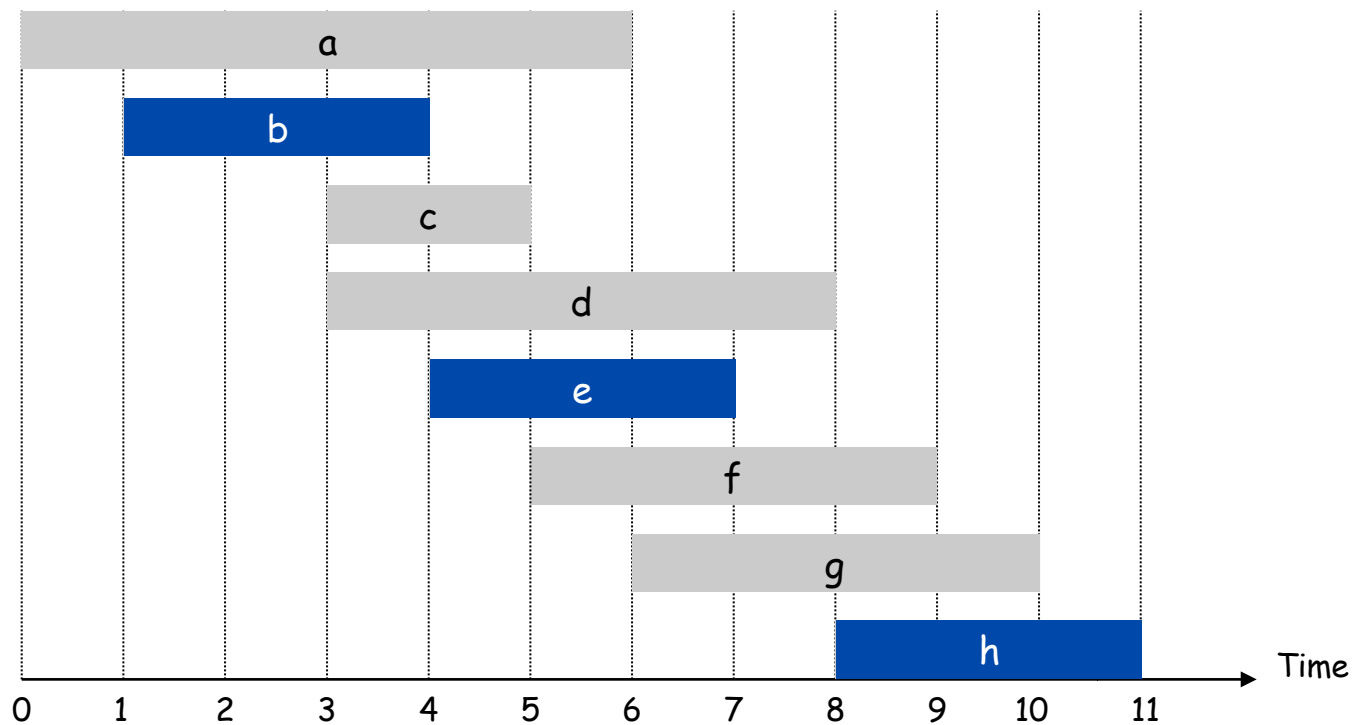
1.2 Five Representative Problems

Interval Scheduling

Input. Set of jobs with start times and finish times.

Goal. Find **maximum cardinality** subset of mutually compatible jobs.

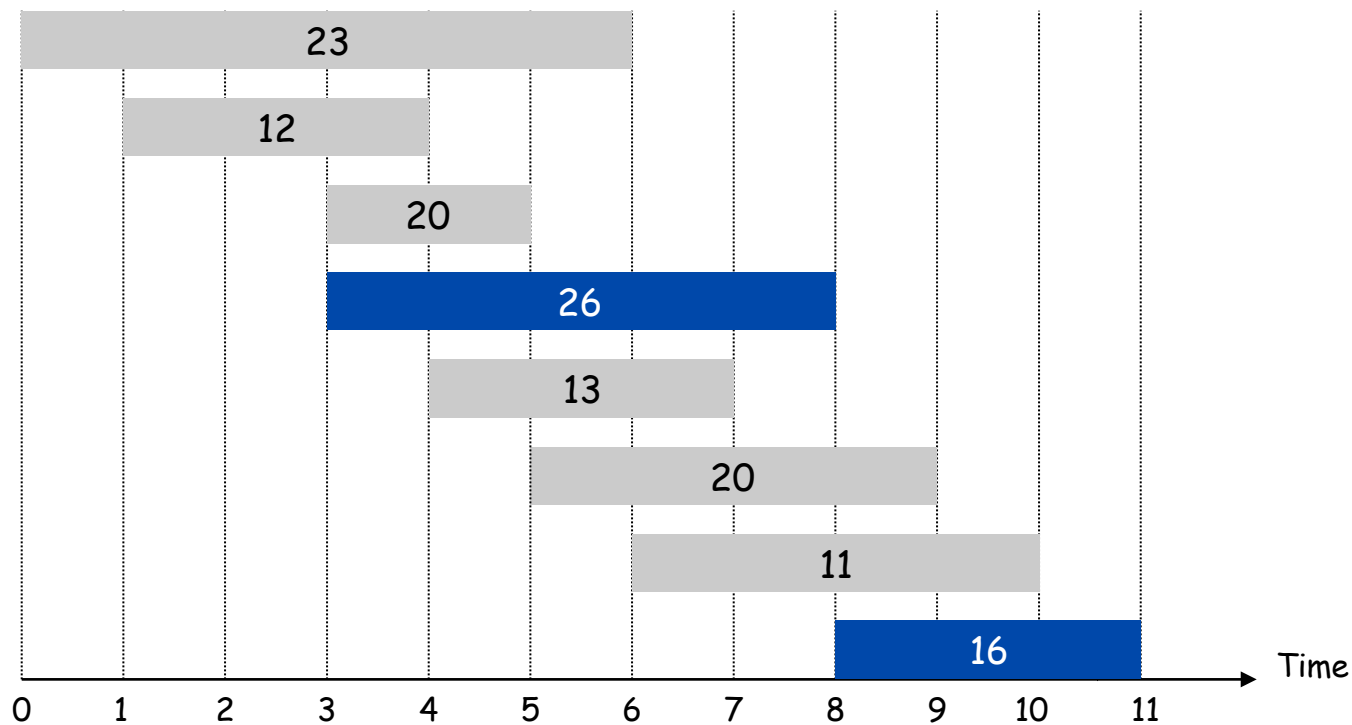
↑
jobs don't overlap



Weighted Interval Scheduling

Input. Set of jobs with start times, finish times, and weights.

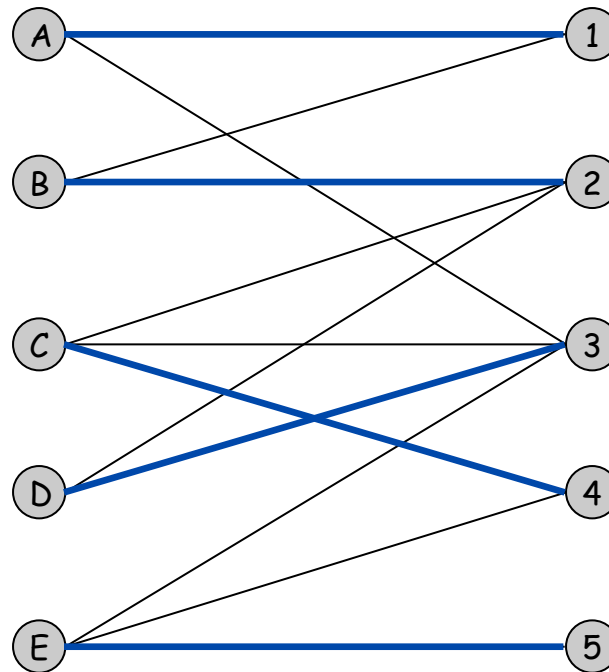
Goal. Find **maximum weight** subset of mutually compatible jobs.



Bipartite Matching

Input. Bipartite graph.

Goal. Find **maximum cardinality** matching.

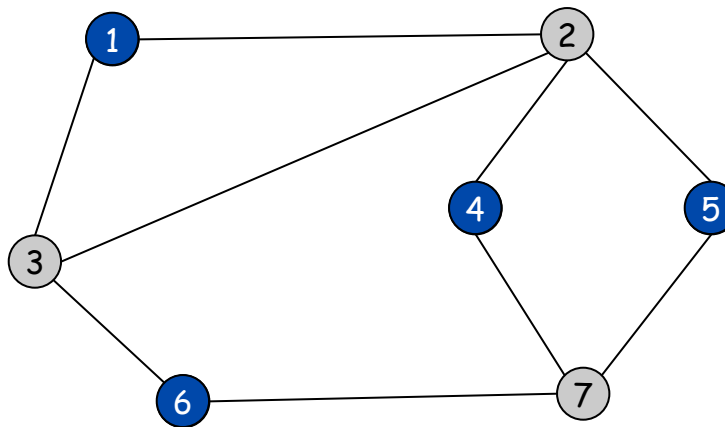


Independent Set

Input. Graph.

Goal. Find **maximum cardinality** independent set.

↑
subset of nodes such that no two
joined by an edge

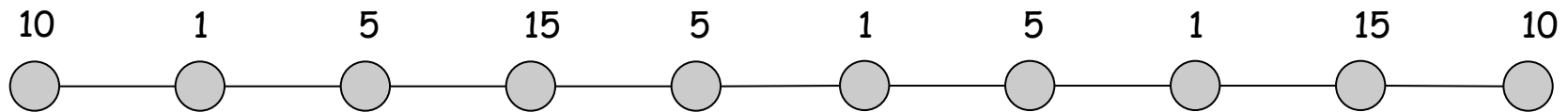


Competitive Facility Location

Input. Graph with weight on each node.

Game. Two competing players alternate in selecting nodes. Not allowed to select a node if any of its neighbors have been selected.

Goal. Select a **maximum weight** subset of nodes.



Second player can guarantee 20, but not 25.

Five Representative Problems

Variations on a theme: independent set.

Interval scheduling: $n \log n$ greedy algorithm.

Weighted interval scheduling: $n \log n$ dynamic programming algorithm.

Bipartite matching: n^k max-flow based algorithm.

Independent set: NP-complete.

Competitive facility location: PSPACE-complete.

Extra Slides

Stable Matching Problem

Goal: Given n men and n women, find a "suitable" matching.

- Participants rate members of opposite sex.
- Each man lists women in order of preference from best to worst.
- Each woman lists men in order of preference from best to worst.

	favorite ↓ 1 st	2 nd	3 rd	4 th	least favorite ↓ 5 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Men's Preference List

Stable Matching Problem

Goal: Given n men and n women, find a "suitable" matching.

- Participants rate members of opposite sex.
- Each man lists women in order of preference from best to worst.
- Each woman lists men in order of preference from best to worst.

	favorite ↓ 1 st	2 nd	3 rd	4 th	least favorite ↓ 5 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Women's Preference List

Understanding the Solution

Claim. The man-optimal stable matching is **weakly Pareto optimal**.

↑
No other perfect matching (stable or unstable)
where every man does strictly better

Pf.

- Let A be last woman in some execution of GS algorithm to receive a proposal.
- No man is rejected by A since algorithm terminates when last woman receives first proposal.
- No man matched to A will be strictly better off than in man-optimal stable matching. ▪

Deceit: Machiavelli Meets Gale-Shapley

Q. Can there be an incentive to misrepresent your preference profile?

- Assume you know men's propose-and-reject algorithm will be run.
- Assume that you know the preference profiles of all other participants.

Fact. No, for any man yes, for some women. No mechanism can guarantee a stable matching and be cheatproof.

	1 st	2 nd	3 rd
Xavier	A	B	C
Yancey	B	A	C
Zeus	A	B	C

Men's Preference List

	1 st	2 nd	3 rd
Amy	Y	X	Z
Bertha	X	Y	Z
Clare	X	Y	Z

Women's True Preference Profile

	1 st	2 nd	3 rd
Amy	Y	Z	X
Bertha	X	Y	Z
Clare	X	Y	Z

Amy Lies

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Victor proposes to Bertha.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Victor proposes to Bertha.

- Bertha accepts since previously unmatched.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Wyatt proposes to Diane.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Wyatt proposes to Diane.

- Diane accepts since previously unmatched.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Xavier proposes to Bertha.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Xavier proposes to Bertha.

- Bertha dumps Victor and accepts Xavier.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Victor proposes to Amy.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Victor proposes to Amy.

- Amy accepts since previously unmatched.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Yancey proposes to Amy.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Yancey proposes to Amy.

- Amy rejects since she prefers Victor.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Yancey proposes to Diane.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Yancey proposes to Diane.

- Diane dumps Wyatt and accepts Yancey.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Wyatt proposes to Bertha.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Wyatt proposes to Bertha.

- Bertha rejects since she prefers Xavier.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Wyatt proposes to Amy.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Wyatt proposes to Amy.

- Amy rejects since she prefers Victor.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Wyatt proposes to Clare.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Wyatt proposes to Clare.

- Clare accepts since previously unmatched.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Zeus proposes to Bertha.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Zeus proposes to Bertha.

- Bertha rejects since she prefers Xavier.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Zeus proposes to Diane.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Zeus proposes to Diane.

- Diane rejects Yancey and accepts Zeus.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Yancey proposes to Clare.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Yancey proposes to Clare.

- Clare rejects since she prefers Wyatt.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Yancey proposes to Bertha.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Yancey proposes to Bertha.

- Bertha rejects since she prefers Xavier.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Yancey proposes to Erika.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

Yancey proposes to Erika.

- Erika accepts since previously unmatched.

Men's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Victor	Bertha	Amy	Diane	Erika	Clare
Wyatt	Diane	Bertha	Amy	Clare	Erika
Xavier	Bertha	Erika	Clare	Diane	Amy
Yancey	Amy	Diane	Clare	Bertha	Erika
Zeus	Bertha	Diane	Amy	Erika	Clare

Women's Preference Profile

	0 th	1 st	2 nd	3 rd	4 th
Amy	Zeus	Victor	Wyatt	Yancey	Xavier
Bertha	Xavier	Wyatt	Yancey	Victor	Zeus
Clare	Wyatt	Xavier	Yancey	Zeus	Victor
Diane	Victor	Zeus	Yancey	Xavier	Wyatt
Erika	Yancey	Wyatt	Zeus	Xavier	Victor

STOP

- Everyone matched.
- Stable matching!