



11.3 Regional descriptors

- Common practice to combine boundary and regional descriptors

11.3.1 Some simple descriptors

- Area: Number of pixels in region
- Perimeter: Length of boundary
- Compactness: $\text{Perimeter}^2 / \text{Area}$
- Mean and median gray levels
- Min and max gray level values
- Number of pixels with values above or below mean

11.3.2 Topological Descriptors

- Topology: Study of properties of a figure that are unaffected by any deformation
- Euler number: $E = C - H$
 - Number of connected components: C
 - Number of holes: H



FIGURE 11.22 Infrared images of the Americas at night. (Courtesy of NOAA.)



Region no. (from top)	Ratio of lights per region to total lights
1	0.204
2	0.640
3	0.049
4	0.107



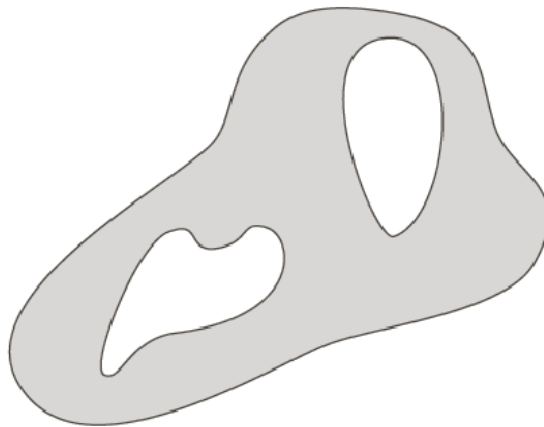


FIGURE 11.23
A region with
two holes.

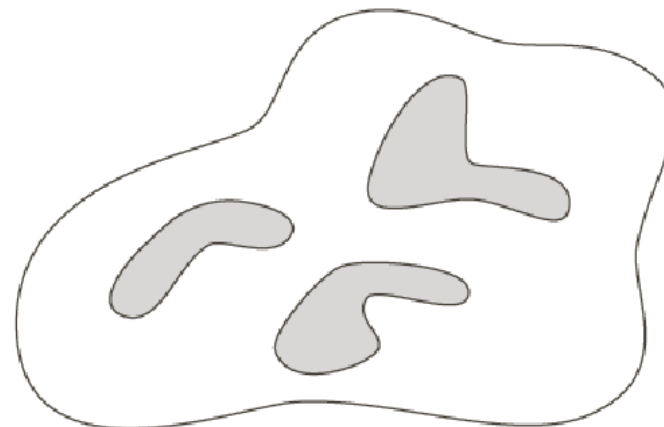
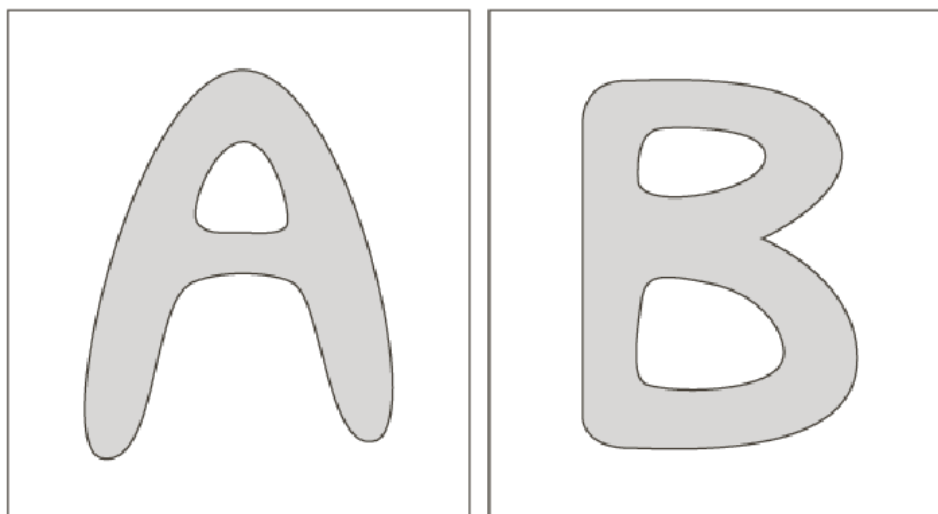


FIGURE 11.24
A region with
three connected
components.



a b

FIGURE 11.25
Regions with
Euler numbers
equal to 0 and -1 ,
respectively.



- Polygonal networks: Euler formula...

$$\begin{aligned} V - Q + F &= C - H \\ &= E \end{aligned}$$

V : Number of vertices

Q : Number of edges

F : Number of faces

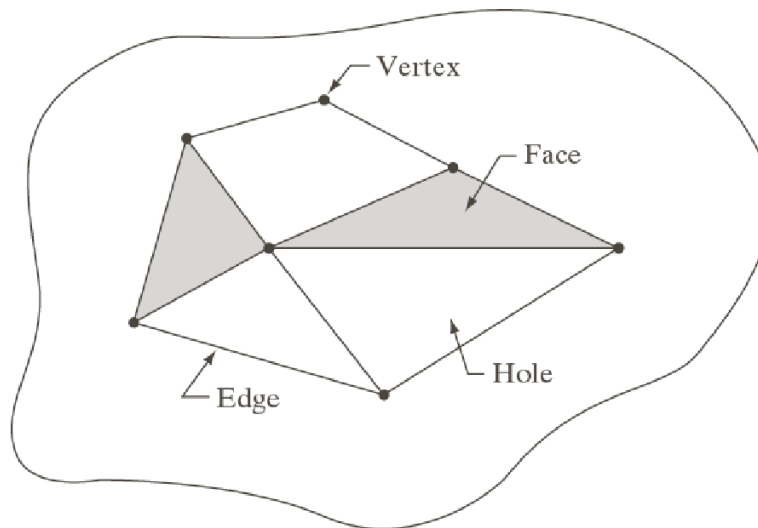
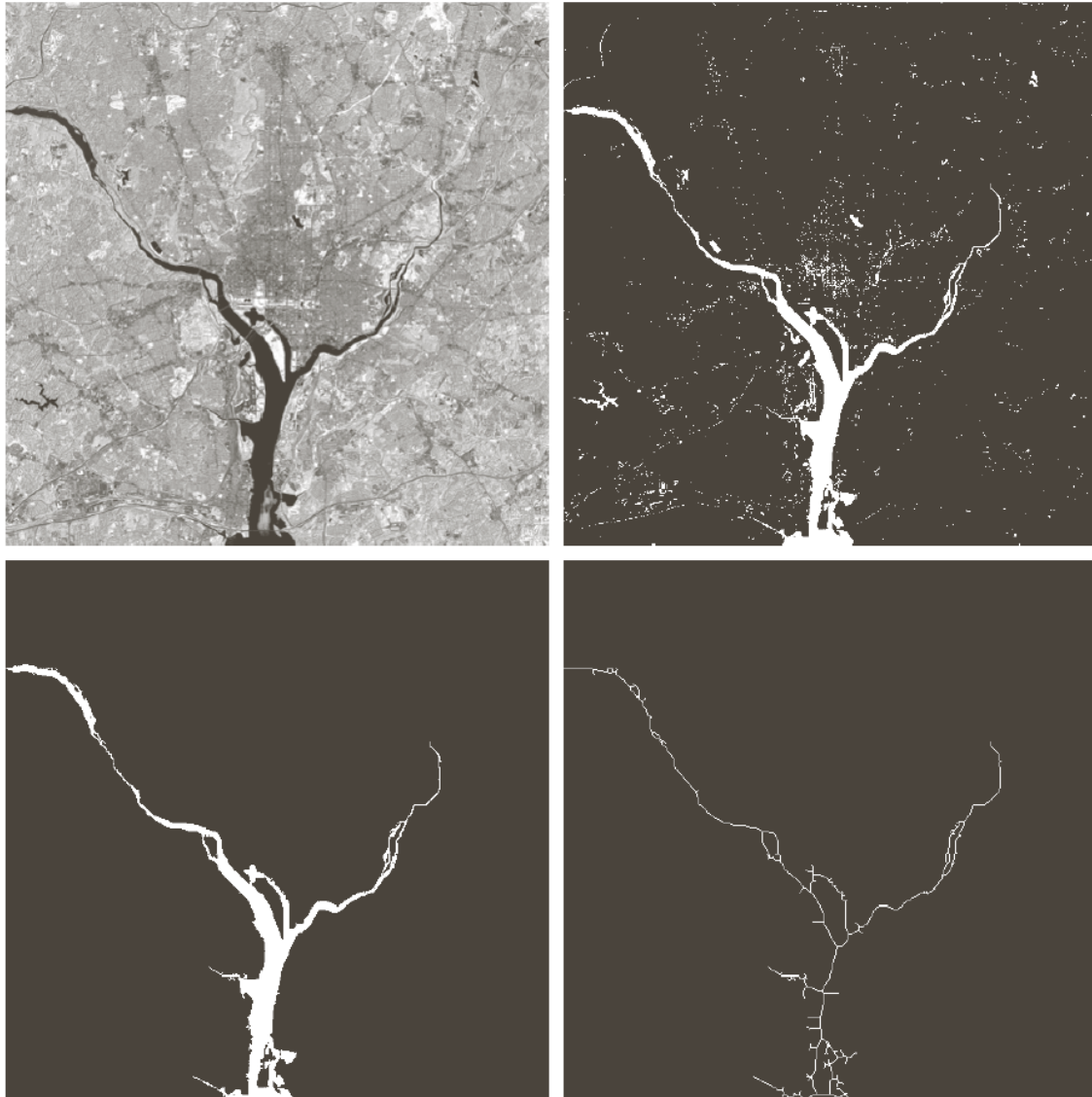


FIGURE 11.26 A region containing a polygonal network.

$$\begin{aligned} 7 - 11 + 2 &= 1 - 3 \\ &= -2 \end{aligned}$$



Example 11.9



a	b
c	d

FIGURE 11.27
(a) Infrared image of the Washington, D.C. area. (b) Thresholded image. (c) The largest connected component of (b). (d) Skeleton of (c).

$$E = C - H$$

$$1552 = 1591 - 39$$



11.3.3 Texture

(1) Statistical approaches (2) Structural approaches (3) Spectral approaches

Statistical approaches

When $p(z_i)$, $i = 0, \dots, L - 1$ represents a histogram of gray-levels, the n th moment of z about the mean is

$$\mu_n(z) = \sum_{i=0}^{L-1} (z_i - m)^n p(z_i)$$

where m is the mean value of z ...

$$m = \sum_{i=0}^{L-1} z_i p(z_i)$$

- Relative smoothness...

$$R(z) = 1 - \frac{1}{1 + \sigma^2(z)}$$

- The third moment...

$$\mu_3(z) = \sum_{i=0}^{L-1} (z_i - m)^3 p(z_i)$$



- **The fourth moment...**

$$\mu_4(z) = \sum_{i=0}^{L-1} (z_i - m)^4 p(z_i)$$

... measure of histogram's flatness

- **Measure of uniformity...**

$$U(z) = \sum_{i=0}^{L-1} p^2(z_i)$$

... is maximum for an image in which all grey levels are equal

- **Average entropy measure...**

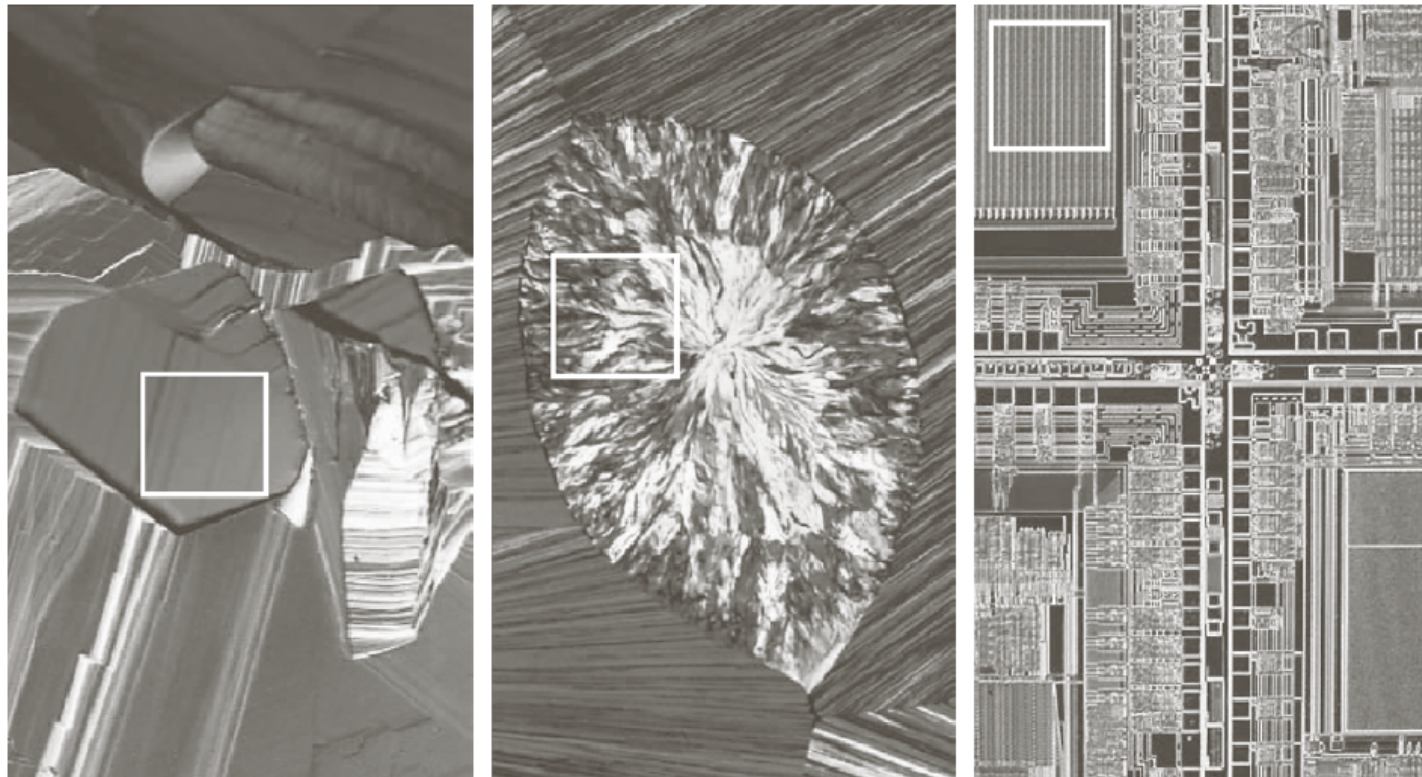
$$e(z) = - \sum_{i=0}^{L-1} p(z_i) \log_2 p(z_i)$$

... measure of variability and is 0 for a constant image

Measures of texture computed using only histograms suffer from the limitation that they carry no information regarding the relative position of pixels with respect to each other

- **Gray-level co-occurrence matrices: READ**

Example 11.10: Texture measures based on histograms



a b c

FIGURE 11.28

The white squares mark, from left to right, smooth, coarse, and regular textures. These are optical microscope images of a superconductor, human cholesterol, and a microprocessor. (Courtesy of Dr. Michael W. Davidson, Florida State University.)

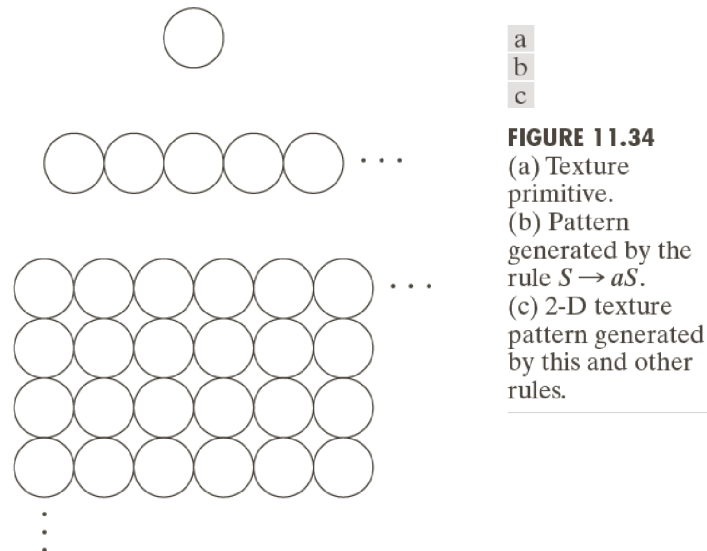
Texture	Mean	Standard deviation	R (normalized)	Third moment	Uniformity	Entropy
Smooth	82.64	11.79	0.002	−0.105	0.026	5.434
Coarse	143.56	74.63	0.079	−0.151	0.005	7.783
Regular	99.72	33.73	0.017	0.750	0.013	6.674

TABLE 11.2

Texture measures for the subimages shown in Fig. 11.28.

Structural approaches

A simple “texture primitive” can be used to form more complex texture patterns by means of some rules that limit the number of possible arrangements of the primitive(s)



a
b
c

FIGURE 11.34

(a) Texture primitive.
(b) Pattern generated by the rule $S \rightarrow aS$.
(c) 2-D texture pattern generated by this and other rules.

Spectral approaches

• Three features of Fourier spectrum that is useful for texture description...

- (1) Prominent peaks \rightarrow principal direction of texture patterns
- (2) Location of peaks \rightarrow fundamental spatial period
- (3) Elimination of periodic components \rightarrow non-periodic image elements \rightarrow statistical descriptors



- Spectrum is symmetric about origin \Rightarrow only half of frequency plane needs to be considered \Rightarrow every periodic pattern associated with only one peak
- Consider spectrum in polar coordinates $S(r, \theta)$
 - For each direction θ , consider 1-dimensional $S_\theta(r)$
 - For each frequency r , consider 1-dimensional $S_r(\theta)$
- More global description obtained by summation...

$$S(r) = \sum_{\theta=0}^{\pi} S_\theta(r)$$

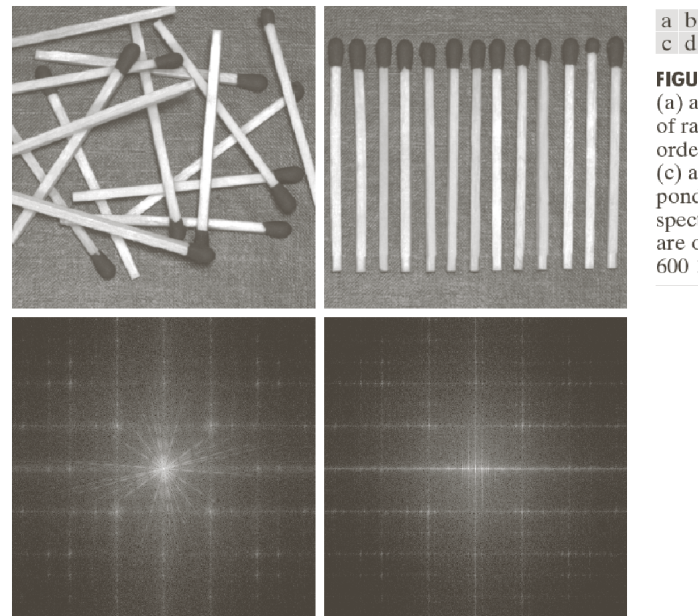
$$S(\theta) = \sum_{r=1}^{R_0} S_r(\theta)$$

... where R_0 is the radius of a circle centered at the origin

Descriptors of these functions themselves can be computed in order to characterize their behavior quantitatively, for example...

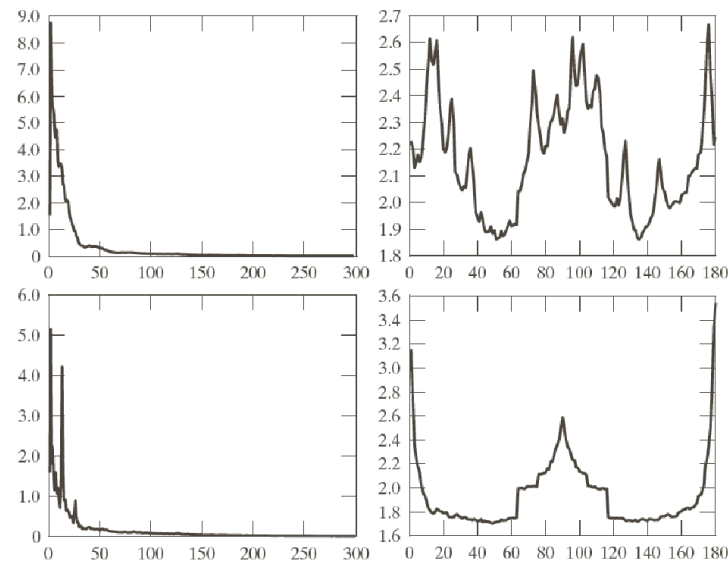
- (1) location of the highest value
- (2) mean and variance
- (3) distance between mean and highest value

Example 11.12: Spectral texture



a	b
c	d

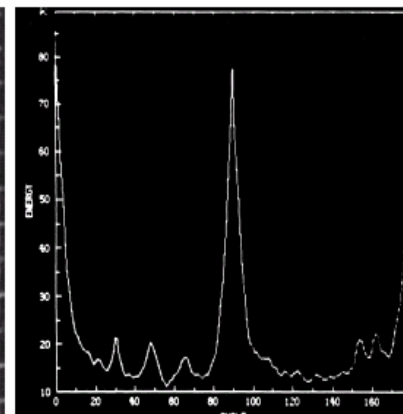
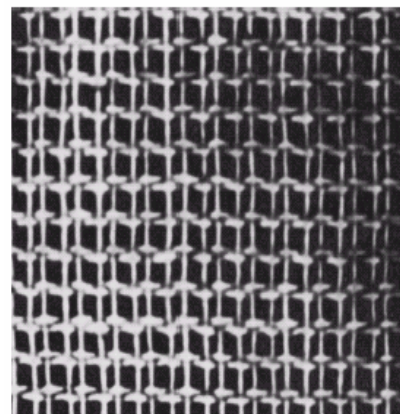
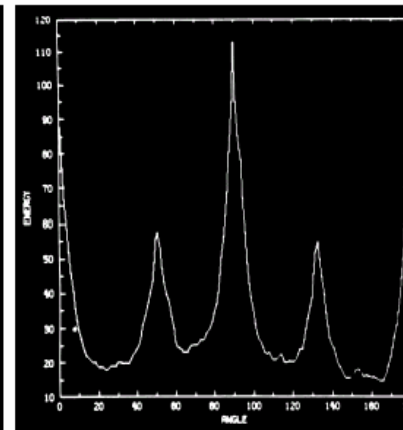
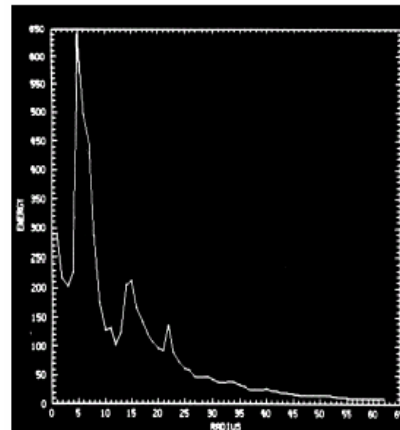
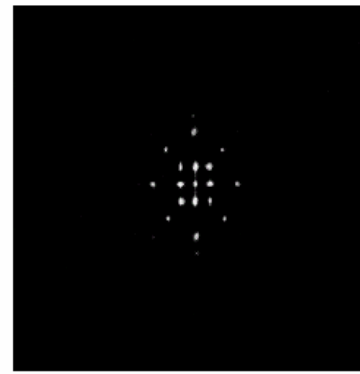
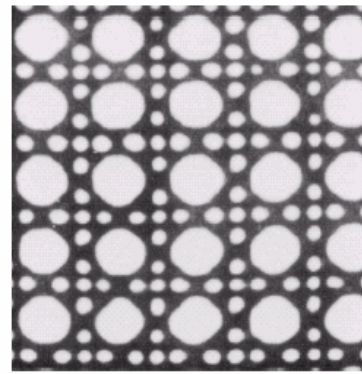
FIGURE 11.35
(a) and (b) Images of random and ordered objects. (c) and (d) Corresponding Fourier spectra. All images are of size 600×600 pixels.



a	b
c	d

FIGURE 11.36
Plots of (a) $S(r)$ and (b) $S(\theta)$ for Fig. 11.35(a). (c) and (d) are plots of $S(r)$ and $S(\theta)$ for Fig. 11.35(b). All vertical axes are $\times 10^5$.

Example in 2nd
edition:
Spectral texture



a	b
c	d
e	f

FIGURE 11.24 (a) Image showing periodic texture. (b) Spectrum. (c) Plot of $S(r)$. (d) Plot of $S(\theta)$. (e) Another image with a different type of periodic texture. (f) Plot of $S(\theta)$. (Courtesy of Dr. Dragana Brzakovic, University of Tennessee.)