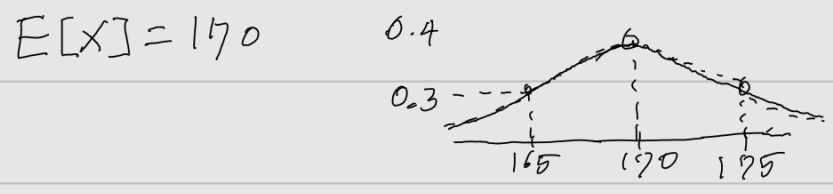


• 행렬에서 열(column)은 x , 행(row)은 y

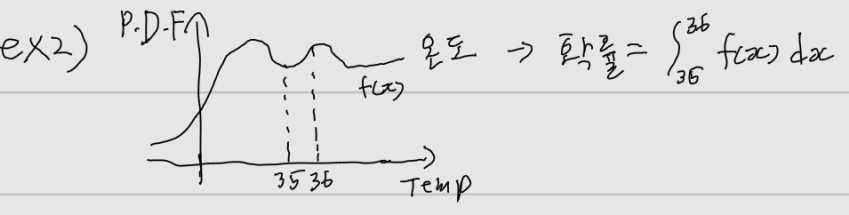
• 확률 분포

ex) $X = \{x_1, \dots, x_{100}\}$
 $= \{170, 160, 159, \dots\}$

$\Rightarrow E[X] = \sum_{i=1}^{100} x_i \cdot P_X(x_i)$ $P_X(x_i)$: 확률
 $V[X] = E[(X - \bar{x})^2] = E[X^2] - E[X]^2$



키: 시간이나 온도 같은 개체가 아니라, 개체의 특성
 \rightarrow 이산 확률 분포



• 공분산

$X = \mathbf{X} = \{x_1, \dots, x_n\} \Rightarrow E[X], V[X]$

$Y = \mathbf{Y} = \{y_1, \dots, y_n\} \Rightarrow E[Y], V[Y]$

$Z = \{z_1, \dots, z_n\} \in \mathbb{R}^2$ $z_i = (x_i, y_i)$

$\Rightarrow E[Z] = \begin{bmatrix} \bar{x} \\ \bar{y} \end{bmatrix}$ $V[Z] \leftrightarrow \text{covariance (공분산)}$

etc) $X, Y, K \rightarrow \begin{bmatrix} \text{cov}_{11} & \text{cov}_{12} & \text{cov}_{13} \\ \vdots & \ddots & \vdots \\ \vdots & \ddots & \vdots \end{bmatrix} \Rightarrow$ 공분산 행렬

• E 와 V 의 특징

$E[X]$

$\rightarrow E[\alpha X] = \alpha E[X]$ ex) $X = \{3, 4, 5\}$ $E[X] = 4$ $E[2X] = 8$
 $2X = \{6, 8, 10\}$

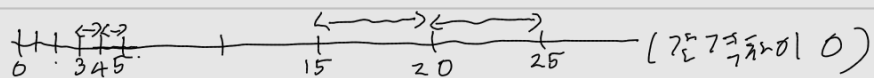
$\rightarrow E[X + Y] = E[X] + E[Y]$

$\rightarrow E[XY] = E[X] \cdot E[Y] + \text{cov}(X, Y)$ • X 와 Y 가 독립일 경우 $\text{cov}(X, Y) = 0$

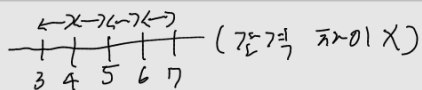
$\text{cov}(X, Y) = E[XY] - E[X]E[Y]$

$$V[X]$$

$$\rightarrow V[\alpha X] = \alpha^2 V[X] \quad \text{ex) } X = \{3, 4, 5\} \quad \alpha = 5 \quad \alpha X = \{15, 20, 25\}$$



$$\rightarrow V[X + \beta] = V[X] \quad \text{ex) } X = \{3, 4, 5\} \quad \beta = 2 \quad X + \beta = \{5, 6, 7\}$$



$$\rightarrow V[X + Y] = V[X] + V[Y] + 2\text{cov}(X, Y)$$

• 공분산 2

X : 과일 (190) Y : 수확량 (200) Z : 토양 수분 (10) H : 식물 높이 (5)

$$\text{cov}(X, Y) = E[XY] - E[X] \cdot E[Y] \quad \text{cov}(X, X) = E[X^2] - E[X]^2 = V[X]$$

$$\text{cov}(Z, H) = \quad //$$

$$\text{상관 계수 } \rho \quad -1 \leq \rho_{XY} = \frac{\text{cov}(X, Y)}{\sqrt{V(X)V(Y)}} \leq 1 \quad \rho_{XX} = \frac{V[X]}{V[X]} = 1 \quad \rho_{X-X} = \frac{\text{cov}(X, -X)}{\sqrt{V(X)V(-X)}} = \frac{-V[X]}{V[X]} = -1$$

• $X \quad Y \quad Z$

$E \quad \mu_1 \quad \mu_2 \quad \mu_3$

$V \quad \sigma_1 \quad \sigma_2 \quad \sigma_3$

공분산 행렬: $\Sigma = \begin{bmatrix} \Sigma_{11} & \Sigma_{12} & \Sigma_{13} \\ \Sigma_{21} & \Sigma_{22} & \Sigma_{23} \\ \Sigma_{31} & \Sigma_{32} & \Sigma_{33} \end{bmatrix} = \begin{bmatrix} \sigma_1^2 & \Sigma_{12} & \Sigma_{13} \\ \Sigma_{12} & \sigma_2^2 & \Sigma_{23} \\ \Sigma_{13} & \Sigma_{23} & \sigma_3^2 \end{bmatrix} \quad \rho_{12} = \frac{\text{cov}(1, 2)}{\sqrt{V(1)V(2)}} = \frac{\Sigma_{12}}{\sigma_1 \sigma_2}$

$\text{cov} = \Sigma \quad \hookrightarrow \Sigma_{12} = \sigma_1 \sigma_2 \cdot \rho_{12}$