

Algorithm: DFS BiPartite

Input: A simple connected undirected graph $G = (V, E)$

Output: A partition of $V(G)$.

Is (V_0, V_1) if G is bipartite and $(V(G), \phi)$ otherwise.

Initialize a stack S .

Initialize an array $Color[1..n]$ with value -1.

// -1 not colored. 0, 1 two different colors

Pick a starting vertex s and $Color(s) \leftarrow 0$.

$S.push(s)$

while $S \neq \emptyset$ **do**

$v \leftarrow S.peek()$

if there a vertex w vertex adjacent to v that is not colored **then**

$w \leftarrow$ next vertex adjacent to v to be colored.

if all colored vertices adjacent to w has the same color as v **then**

$Color[w] = (Color[v] + 1) \% 2$

 Push w onto S

else // color conflict. G is not bipartite

return $(V(G), \phi)$.

else

$S.pop()$

// coloring completed.

$V_0 \leftarrow$ all vertices of G colored 0

$V_1 \leftarrow$ all vertices of G colored 1

return (V_0, V_1)

Algorithm: BFS Bipartite

Input: A simple connected undirected graph $G = (V, E)$

Output: A partition of $V(G)$.

Is (V_0, V_1) if G is bipartite and $(V(G), \phi)$ otherwise.

Initialize a queue Q

Initialize an array $\text{Color}[1..n]$ with value -1.

Pick a starting vertex s and $\text{Color}(s) \leftarrow 0$.

$Q.\text{add}(s)$

while $Q \neq \emptyset$ **do**

$v \leftarrow Q.\text{dequeue}()$

for all vertex w adjacent to v that is not colored

if all colored vertices adjacent to w has the same color as v **then**

$\text{Color}[w] = (\text{Color}[v] + 1) \% 2$

$Q.\text{add}(w)$

else **// color conflict. G is not bipartite**

return $(V(G), \phi)$.

// coloring completed.

$V_0 \leftarrow$ all vertices of G colored 0

$V_1 \leftarrow$ all vertices of G colored 1

return (V_0, V_1)
