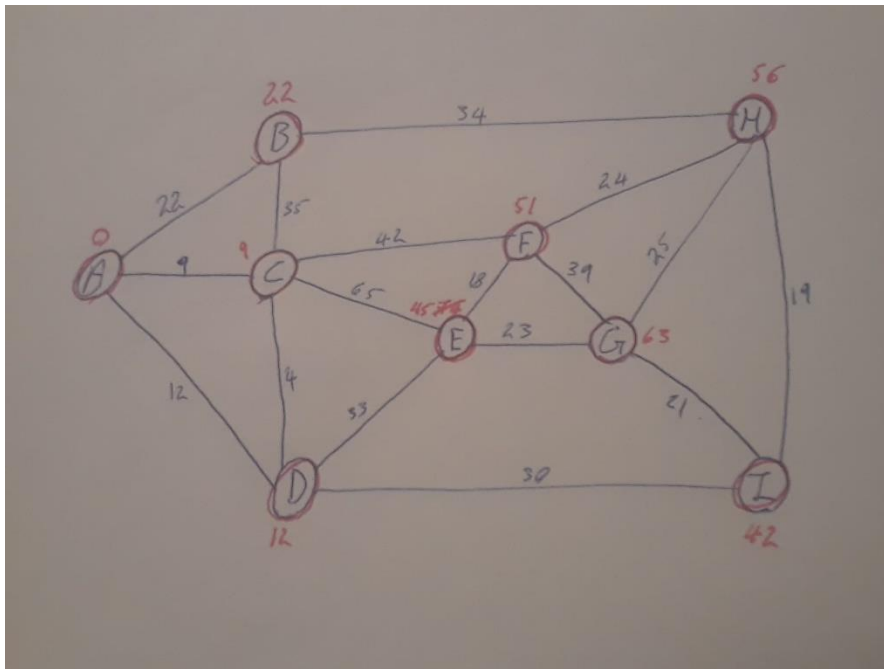


# W3D6

1,

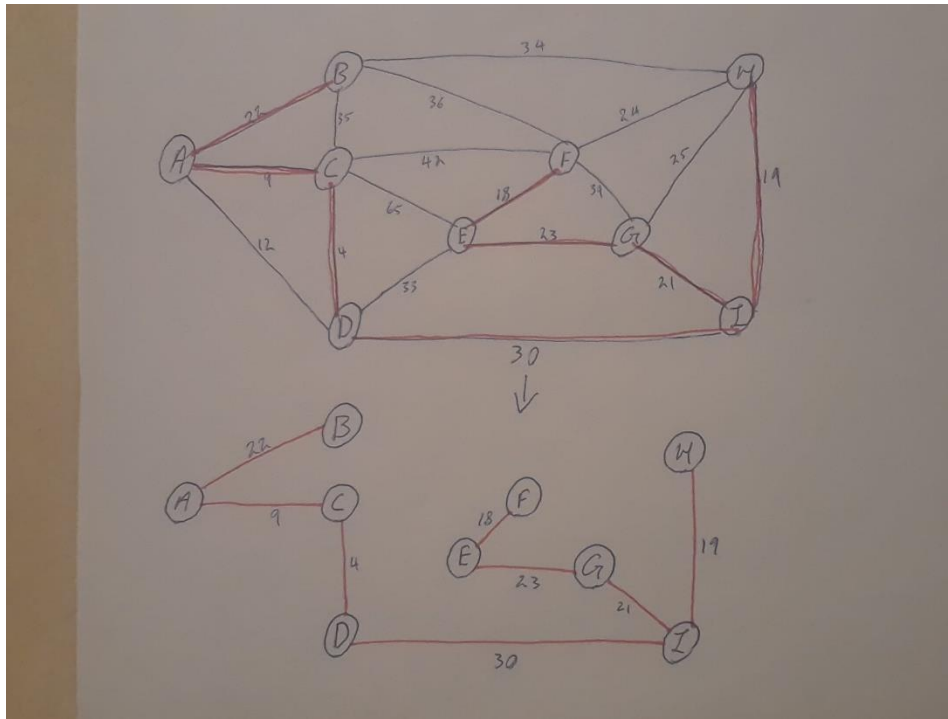
	A	B	C	D	E	F	G	H	I
A	0	22	9	12	0	0	0	0	0
B	22	0	35	0	0	36	0	34	0
C	9	35	0	4	65	42	0	0	0
D	12	0	4	0	33	0	0	0	30
E	0	0	65	33	0	18	23	0	0
F	0	36	42	0	18	0	39	24	0
G	0	0	0	0	23	39	0	25	21
H	0	34	0	0	0	24	25	0	19
I	0	0	0	30	0	0	21	19	0

2,



3, Time complexity is  $O(m \log n)$ .

4,



5, Time complexity is  $O(E \log E)$  where  $E$  is number of edges .

6,

	P	Q	T	S	R	U
P	0	1	7	6	0	0
Q	0	0	0	4	1	0
T	0	0	0	3	0	2
S	0	0	3	0	2	2
R	0	0	0	2	0	1
U	0	0	0	0	0	0

7,

$$D[P] = 0$$

$$D[Q] = \min\{D[p] + \text{wt}(P, Q) \mid (P, Q) \text{ elemnt of } E\}$$

$$= \min\{0 + 1\} = 1$$

$$D[R] = \min\{D[Q] + \text{wt}(Q, R) \mid (Q, R) \text{ elemnt of } E\}$$

$$= \min\{1 + 1\} = 2$$

$$D[S] = \min\{D[p] + \text{wt}(P, S), D[Q] + \text{wt}(Q, S), D[R] + \text{wt}(R, S) \mid (P, S), (Q, S), (R, S) \text{ elemnt of } E\}$$

$$= \min\{0 + 6, 1 + 4, 2 + 2\} = 4$$

$$D[T] = \min\{D[p] + \text{wt}(P,T), D[S] + \text{wt}(S,T) \mid (S,T) \in E\}$$

$$= \min\{0+7, 4+3\} = 7$$

$$D[U] = \min\{D[R] + \text{wt}(R,U), D[S] + \text{wt}(S,U), D[T] + \text{wt}(T,U) \mid (R,U), (S,U), (T,U) \in E\}$$

$$= \min\{2+1, 4+2, 7+2\} = 3$$

8. Time complexity is  $O(m+n)$  where  $n$  is number of nodes and  $m$  is number of edges

9. yes by using Dijkstra's algorithm the shortest path is  $\{(P,Q), (Q,R), (R,U)\}$  which is 3

10,

step 1

$$A[P] = 0$$

$$B[P] = \{\}$$

Put P in X

Step 2

$$X = \{P\}$$

Find the minimum of the following

$$d[Q] = d[P] + \text{wt}(P,Q) = 0+1=1 \quad \leftarrow$$

$$d[S] = d[P] + \text{wt}(P,S) = 0+6=6$$

$$d[T] = d[P] + \text{wt}(P,T) = 0+7=7$$

Add Q to X

Step 3  $X = \{P, Q\}$

Find minimum of the following

$$d[S] = d[P] + \text{wt}(P,S) = 0+6=6$$

$$d[T] = d[P] + \text{wt}(P,T) = 0+7=7$$

$$d[S] = d[Q] + \text{wt}(Q,S) = 1+4=5$$

$$d[R] = d[Q] + \text{wt}(Q,R) = 1+1=2 \quad \leftarrow$$

Add R to X

Step 4

$$X = \{P, Q, R\}$$

Find the minimum of the following

$$d[S] = d[P] + \text{wt}(P,S) = 0+6=6$$

$$d[S]=d[Q]+wt(P,S)=1+4=5$$

$$d[T]=d[P]+wt(P,T)=0+7=7$$

$$d[S]=d[R]+wt(R,S)=2+2=4$$

$$d[U]=d[R]+wt(R,U)=2+1=3 \leftarrow$$

Add U to X

$$X=\{P,Q,R,U\}$$

The targeted vertex is U so shortest way is P,Q,R,U with length 3.