eEOM DEMO

This is a demostration for running the genetic algorithm for structural refinement against the small- and wideangle x-ray scattering data.

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Background

The refinement is implemented as the genetic algorithm and based on the customized χ^2 :

$$\chi^2 = rac{1}{n-1} \sum_{i=1}^n igg\{ rac{\log_{10} \left[I_{ens}(q_i)
ight] - \log_{10} \left[I_{exp}(q_i)
ight]}{\sigma'(q_i)} igg\}^2,$$

where $I_{ens}(q_i)$ is the computed scattering profile from the ensemble and $I_{exp}(q_i)$ is the experimental measurement at q_i . $\sigma'(q_i)$ is the propagated error.

$$\sigma'(q_i) = rac{\sigma(q_i)}{I_{exp}(q_i)\log 10} = rac{1}{\left[rac{S}{N}
ight]_i\log 10}$$

The refinement function was developed and run in Julia version 1.6.0-DEV.

Required Packages

- 1. JLD.jl
- 2. StatsBase.jl
- 3. DelimitedFiles.jl
- 4. Plots.jl
- 5. Dierckx.jl

```
In [1]: # Load the dependencies

using Plots, DelimitedFiles, StatsBase, JLD
include("ga.jl"); # The algorithm
```

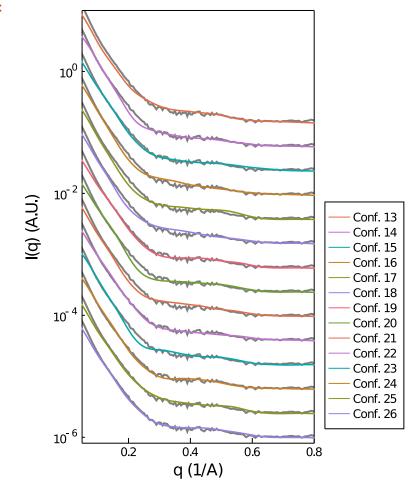
```
In [2]: # Load data to play with
# I will talk about the data later
pool1, pool2 = load("pool.jld", "pool1", "pool2");
data1, data2 = readdlm("data1.dat"), readdlm("data2.dat");
q = collect(0.0:0.005:1.25); # The q grid
```

Example 1:

The data1 and pool1 pair.

```
In [11]: # Plot the data and see what's going on
    p = plot(size=(400, 500), grid=false, legend=:outerbottomright, framestyle=:bo
    x);
    s = 0.4;
    for i = 1:14
        plot!(data1[:,1], s^(i-1) * data1[:,2], yscale=:log10, lw=2.0, c=:black, linealpha=0.5, lab="");
        plot!(q, s^(i-1)*pool1[:,7i-6], lw=1.5, yscale=:log10, lab="Conf. $(12+i)"
    );
    end
    xlims!(0.05, 0.8)
    ylims!(0.8e-6, 10)
    ylabel!("I(q) (A.U.)")
    xlabel!("q (1/A)")
```

Out[11]:



This is just plotting some of the conformations in pool1 against data1 with offsets for better visualization. It is suggested to see this plot first since the Refine function is not scaling for you.

Now let's run the eEOM refinement using the Refine function in ga.jl.

```
In [12]: # Run the eEOM structural refinement
         idx = findall(data1[:,1] .<= 0.8); # Cuts the experimental profile</pre>
         tmp = data1[idx, :];
         ensize = 10; # ensemble size
         cycles = 50; # number of cycles
         survivors1 = zeros(Int64, ensize, cycles); # container for selected conformati
         ons
         fitness1 = zeros(cycles); # container for fitness scores
         t = @elapsed for i = 1:cycles
             @info("===== Cycle number $i ====");
             # The core of eEOM: getting the best ensemble from all the 100000 generati
         ons
             fitness1[i], survivor = Refine(tmp, [q pool1], ensize, 0.15; population=10
         , maxiter=100000, reports=10);
             survivors1[:,i] = survivor[:,1];
         end
         println("- eEOM for $cycles cycles and $(size(pool1, 2)) conformaitons took $(
         round(t, digits=2)) seconds.");
```

```
Info: ===== Cycle number 1 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.51587, best fit so far = 0.4474.
Generation #20000: fitness = 0.49856, best fit so far = 0.44413.
Generation #30000: fitness = 0.61213, best fit so far = 0.44413.
Generation #40000: fitness = 0.65826, best fit so far = 0.44413.
Generation #50000: fitness = 0.49971, best fit so far = 0.44396.
Generation #60000: fitness = 0.69345, best fit so far = 0.44396.
Generation #70000: fitness = 0.64867, best fit so far = 0.44396.
Generation #80000: fitness = 0.50304, best fit so far = 0.44396.
Generation #90000: fitness = 0.65665, best fit so far = 0.44396.
Generation #100000: fitness = 0.6715, best fit so far = 0.44396.
Finished Genetic Algorithm, with best fitness = 0.44396.
 Info: ===== Cycle number 2 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.58868, best fit so far = 0.45339.
Generation #20000: fitness = 0.60585, best fit so far = 0.45009.
Generation #30000: fitness = 0.51705, best fit so far = 0.44857.
Generation #40000: fitness = 0.56632, best fit so far = 0.44585.
Generation #50000: fitness = 0.51985, best fit so far = 0.44585.
Generation #60000: fitness = 0.48491, best fit so far = 0.44585.
Generation #70000: fitness = 0.67473, best fit so far = 0.44585.
Generation #80000: fitness = 0.56989, best fit so far = 0.44585.
Generation #90000: fitness = 0.63684, best fit so far = 0.44413.
Generation #100000: fitness = 0.7374, best fit so far = 0.44413.
Finished Genetic Algorithm, with best fitness = 0.44413.
 Info: ===== Cycle number 3 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.73462, best fit so far = 0.45936.
Generation #20000: fitness = 0.59965, best fit so far = 0.44731.
Generation #30000: fitness = 0.52111, best fit so far = 0.44731.
Generation #40000: fitness = 0.69165, best fit so far = 0.44413.
Generation #50000: fitness = 0.56107, best fit so far = 0.44413.
Generation #60000: fitness = 0.51179, best fit so far = 0.44413.
Generation #70000: fitness = 0.6355, best fit so far = 0.44413.
Generation #80000: fitness = 0.49479, best fit so far = 0.44413.
Generation #90000: fitness = 0.50911, best fit so far = 0.44413.
Generation #100000: fitness = 0.72958, best fit so far = 0.44413.
Finished Genetic Algorithm, with best fitness = 0.44413.
 Info: ===== Cycle number 4 ====
 @ Main In[12]:10
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Generation #10000: fitness = 0.63439, best fit so far = 0.46462.
Generation #20000: fitness = 0.57941, best fit so far = 0.45339.
Generation #30000: fitness = 0.61102, best fit so far = 0.45339.
Generation #40000: fitness = 0.56932, best fit so far = 0.45339.
Generation #50000: fitness = 0.57131, best fit so far = 0.45339.
Generation #60000: fitness = 0.56413, best fit so far = 0.45339.
Generation #70000: fitness = 0.74909, best fit so far = 0.45058.
Generation #80000: fitness = 0.55105, best fit so far = 0.44413.
Generation #90000: fitness = 0.75398, best fit so far = 0.44413.
Generation #100000: fitness = 0.49111, best fit so far = 0.44413.
Finished Genetic Algorithm, with best fitness = 0.44413.
 Info: ===== Cycle number 5 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.58605, best fit so far = 0.45652.
Generation #20000: fitness = 0.51094, best fit so far = 0.44413.
Generation #30000: fitness = 0.61036, best fit so far = 0.44413.
Generation #40000: fitness = 0.57759, best fit so far = 0.44413.
Generation #50000: fitness = 0.62629, best fit so far = 0.44413.
Generation #60000: fitness = 0.65373, best fit so far = 0.44413.
Generation #70000: fitness = 0.65727, best fit so far = 0.44413.
Generation #80000: fitness = 0.61126, best fit so far = 0.44413.
Generation #90000: fitness = 0.59854, best fit so far = 0.44413.
Generation #100000: fitness = 0.4999, best fit so far = 0.44413.
Finished Genetic Algorithm, with best fitness = 0.44413.
Info: ===== Cycle number 6 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.59741, best fit so far = 0.46029.
Generation #20000: fitness = 0.55663, best fit so far = 0.46029.
Generation #30000: fitness = 0.59588, best fit so far = 0.45716.
Generation #40000: fitness = 0.51491, best fit so far = 0.45094.
Generation #50000: fitness = 0.70756, best fit so far = 0.45094.
Generation #60000: fitness = 0.53027, best fit so far = 0.45094.
Generation #70000: fitness = 0.68429, best fit so far = 0.45094.
Generation #80000: fitness = 0.60972, best fit so far = 0.44811.
Generation #90000: fitness = 0.6192, best fit so far = 0.44811.
Generation #100000: fitness = 0.53807, best fit so far = 0.44413.
Finished Genetic Algorithm, with best fitness = 0.44413.
 Info: ===== Cycle number 7 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.61237, best fit so far = 0.46208.
Generation #20000: fitness = 0.58337, best fit so far = 0.44946.
Generation #30000: fitness = 0.53608, best fit so far = 0.44946.
Generation #40000: fitness = 0.72519, best fit so far = 0.44946.
Generation #50000: fitness = 0.65708, best fit so far = 0.44946.
Generation #60000: fitness = 0.50634, best fit so far = 0.44396.
Generation #70000: fitness = 0.55391, best fit so far = 0.44396.
Generation #80000: fitness = 0.61304, best fit so far = 0.44396.
Generation #90000: fitness = 0.59761, best fit so far = 0.44396.
Generation #100000: fitness = 0.58402, best fit so far = 0.44396.
Finished Genetic Algorithm, with best fitness = 0.44396.
Generation #10000: fitness = 0.5999, best fit so far = 0.44731.
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Info: ===== Cycle number 8 ====
 @ Main In[12]:10
Generation #20000: fitness = 0.58014, best fit so far = 0.44542.
Generation #30000: fitness = 0.65388, best fit so far = 0.44542.
Generation #40000: fitness = 0.53931, best fit so far = 0.44542.
Generation \#50000: fitness = 0.58541, best fit so far = 0.44413.
Generation #60000: fitness = 0.50273, best fit so far = 0.44413.
Generation #70000: fitness = 0.62441, best fit so far = 0.44413.
Generation #80000: fitness = 0.63337, best fit so far = 0.44413.
Generation #90000: fitness = 0.62327, best fit so far = 0.44413.
Generation #100000: fitness = 0.56274, best fit so far = 0.44413.
Finished Genetic Algorithm, with best fitness = 0.44413.
 Info: ===== Cycle number 9 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.90303, best fit so far = 0.45569.
Generation \#20000: fitness = 0.70905, best fit so far = 0.45569.
Generation #30000: fitness = 0.55902, best fit so far = 0.45569.
Generation #40000: fitness = 0.51867, best fit so far = 0.44463.
Generation #50000: fitness = 0.73996, best fit so far = 0.44463.
Generation #60000: fitness = 0.59503, best fit so far = 0.44463.
Generation #70000: fitness = 0.6651, best fit so far = 0.44463.
Generation #80000: fitness = 0.53207, best fit so far = 0.44463.
Generation #90000: fitness = 0.63716, best fit so far = 0.44463.
Generation #100000: fitness = 0.54961, best fit so far = 0.44463.
Finished Genetic Algorithm, with best fitness = 0.44463.
「Info: ===== Cycle number 10 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.59168, best fit so far = 0.45813.
Generation #20000: fitness = 0.48072, best fit so far = 0.44413.
Generation #30000: fitness = 0.51676, best fit so far = 0.44413.
Generation #40000: fitness = 0.56805, best fit so far = 0.44413.
Generation #50000: fitness = 0.53093, best fit so far = 0.44413.
Generation #60000: fitness = 0.65684, best fit so far = 0.44413.
Generation #70000: fitness = 0.55724, best fit so far = 0.44413.
Generation #80000: fitness = 0.48266, best fit so far = 0.44413.
Generation \#90000: fitness = 0.58195, best fit so far = 0.44413.
Generation #100000: fitness = 0.58202, best fit so far = 0.44413.
Finished Genetic Algorithm, with best fitness = 0.44413.
r Info: ===== Cycle number 11 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.62772, best fit so far = 0.46296.
Generation #20000: fitness = 0.78115, best fit so far = 0.45479.
Generation #30000: fitness = 0.60881, best fit so far = 0.45339.
Generation #40000: fitness = 0.61477, best fit so far = 0.45339.
Generation #50000: fitness = 0.67066, best fit so far = 0.45339.
Generation #60000: fitness = 0.60045, best fit so far = 0.44413.
Generation #70000: fitness = 0.5626, best fit so far = 0.44413.
Generation #80000: fitness = 0.79951, best fit so far = 0.44413.
Generation #90000: fitness = 0.80744, best fit so far = 0.44413.
Generation #100000: fitness = 0.57401, best fit so far = 0.44413.
Finished Genetic Algorithm, with best fitness = 0.44413.
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Info: ===== Cycle number 12 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.73959, best fit so far = 0.44811.
Generation #20000: fitness = 0.66835, best fit so far = 0.44811.
Generation #30000: fitness = 0.51915, best fit so far = 0.44811.
Generation #40000: fitness = 0.54927, best fit so far = 0.44811.
Generation #50000: fitness = 0.56547, best fit so far = 0.44811.
Generation #60000: fitness = 0.57236, best fit so far = 0.44811.
Generation #70000: fitness = 0.63213, best fit so far = 0.44413.
Generation #80000: fitness = 0.79692, best fit so far = 0.44413.
Generation #90000: fitness = 0.57278, best fit so far = 0.44413.
Generation #100000: fitness = 0.51582, best fit so far = 0.44413.
Finished Genetic Algorithm, with best fitness = 0.44413.
 Info: ===== Cycle number 13 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.56893, best fit so far = 0.46145.
Generation #20000: fitness = 0.48645, best fit so far = 0.44413.
Generation #30000: fitness = 0.60972, best fit so far = 0.44413.
Generation #40000: fitness = 0.51477, best fit so far = 0.44413.
Generation #50000: fitness = 0.79414, best fit so far = 0.44413.
Generation #60000: fitness = 0.5455, best fit so far = 0.44413.
Generation #70000: fitness = 1.05194, best fit so far = 0.44413.
Generation #80000: fitness = 0.55216, best fit so far = 0.44413.
Generation #90000: fitness = 0.50588, best fit so far = 0.44413.
Generation #100000: fitness = 0.50042, best fit so far = 0.44413.
Finished Genetic Algorithm, with best fitness = 0.44413.
 Info: ===== Cycle number 14 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.52386, best fit so far = 0.44956.
Generation #20000: fitness = 0.61468, best fit so far = 0.44413.
Generation #30000: fitness = 0.58638, best fit so far = 0.44413.
Generation #40000: fitness = 0.50439, best fit so far = 0.44413.
Generation #50000: fitness = 0.52269, best fit so far = 0.44413.
Generation #60000: fitness = 0.60066, best fit so far = 0.44413.
Generation #70000: fitness = 0.72366, best fit so far = 0.44413.
Generation #80000: fitness = 0.61019, best fit so far = 0.44413.
Generation #90000: fitness = 0.67222, best fit so far = 0.44413.
Generation #100000: fitness = 0.74036, best fit so far = 0.44413.
Finished Genetic Algorithm, with best fitness = 0.44413.
 Info: ===== Cycle number 15 ====
 @ Main In[12]:10
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> Generation #10000: fitness = 0.58121, best fit so far = 0.453. Generation #20000: fitness = 0.48977, best fit so far = 0.45094. Generation #30000: fitness = 0.60009, best fit so far = 0.45094. Generation #40000: fitness = 0.50439, best fit so far = 0.45094. Generation #50000: fitness = 0.67325, best fit so far = 0.44811. Generation #60000: fitness = 0.56732, best fit so far = 0.44811. Generation #70000: fitness = 0.52788, best fit so far = 0.44811. Generation #80000: fitness = 0.6877, best fit so far = 0.44811. Generation #90000: fitness = 0.82239, best fit so far = 0.44811. Generation #100000: fitness = 0.61284, best fit so far = 0.44799. Finished Genetic Algorithm, with best fitness = 0.44799. Info: ===== Cycle number 16 ====

@ Main In[12]:10

Generation #10000: fitness = 0.64562, best fit so far = 0.45818. Generation #20000: fitness = 0.61301, best fit so far = 0.44396. Generation #30000: fitness = 0.60391, best fit so far = 0.44396. Generation #40000: fitness = 0.48936, best fit so far = 0.44396. Generation #50000: fitness = 0.62909, best fit so far = 0.44396. Generation #60000: fitness = 0.55533, best fit so far = 0.44396. Generation #70000: fitness = 0.69786, best fit so far = 0.44396. Generation #80000: fitness = 0.52896, best fit so far = 0.44396. Generation #90000: fitness = 0.63996, best fit so far = 0.44396. Generation #100000: fitness = 0.66031, best fit so far = 0.44396. Finished Genetic Algorithm, with best fitness = 0.44396.

Info: ===== Cycle number 17 ==== @ Main In[12]:10

Generation #10000: fitness = 0.56521, best fit so far = 0.45936. Generation #20000: fitness = 0.71741, best fit so far = 0.45318. Generation #30000: fitness = 0.49446, best fit so far = 0.44413. Generation #40000: fitness = 0.53705, best fit so far = 0.44413. Generation #50000: fitness = 0.55753, best fit so far = 0.44413. Generation #60000: fitness = 0.68539, best fit so far = 0.44413. Generation #70000: fitness = 0.59641, best fit so far = 0.44413. Generation #80000: fitness = 0.5976, best fit so far = 0.44413. Generation #90000: fitness = 0.5546, best fit so far = 0.44413. Generation #100000: fitness = 0.67831, best fit so far = 0.44413. Finished Genetic Algorithm, with best fitness = 0.44413.

Info: ===== Cycle number 18 ==== @ Main In[12]:10

Generation #10000: fitness = 0.48379, best fit so far = 0.44413. Generation #20000: fitness = 0.62374, best fit so far = 0.44413. Generation #30000: fitness = 0.55682, best fit so far = 0.44413. Generation #40000: fitness = 0.89252, best fit so far = 0.44413. Generation #50000: fitness = 0.7669, best fit so far = 0.44413. Generation #60000: fitness = 0.58124, best fit so far = 0.44413. Generation #70000: fitness = 0.712, best fit so far = 0.44413. Generation #80000: fitness = 0.61505, best fit so far = 0.44413. Generation #90000: fitness = 0.54907, best fit so far = 0.44413. Generation #100000: fitness = 0.68735, best fit so far = 0.44413. Finished Genetic Algorithm, with best fitness = 0.44413.

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Info: ===== Cycle number 19 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.66755, best fit so far = 0.44778.
Generation #20000: fitness = 0.491, best fit so far = 0.44778.
Generation #30000: fitness = 0.57344, best fit so far = 0.44778.
Generation #40000: fitness = 0.67085, best fit so far = 0.44778.
Generation #50000: fitness = 0.63547, best fit so far = 0.44778.
Generation #60000: fitness = 0.75432, best fit so far = 0.44778.
Generation #70000: fitness = 0.53989, best fit so far = 0.44778.
Generation #80000: fitness = 0.55185, best fit so far = 0.44778.
Generation #90000: fitness = 0.6361, best fit so far = 0.44413.
Generation #100000: fitness = 0.66906, best fit so far = 0.44413.
Finished Genetic Algorithm, with best fitness = 0.44413.
 Info: ===== Cycle number 20 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.73196, best fit so far = 0.45339.
Generation #20000: fitness = 0.53513, best fit so far = 0.44602.
Generation #30000: fitness = 0.69145, best fit so far = 0.44602.
Generation #40000: fitness = 0.68195, best fit so far = 0.44541.
Generation #50000: fitness = 0.72149, best fit so far = 0.44541.
Generation #60000: fitness = 0.74628, best fit so far = 0.44541.
Generation #70000: fitness = 0.68965, best fit so far = 0.44541.
Generation #80000: fitness = 0.77751, best fit so far = 0.44413.
Generation #90000: fitness = 0.5461, best fit so far = 0.44383.
Generation #100000: fitness = 0.53981, best fit so far = 0.44383.
Finished Genetic Algorithm, with best fitness = 0.44383.
 Info: ===== Cycle number 21 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.9737, best fit so far = 0.44731.
Generation #20000: fitness = 0.6132, best fit so far = 0.44413.
Generation #30000: fitness = 0.53945, best fit so far = 0.44413.
Generation #40000: fitness = 0.53113, best fit so far = 0.44413.
Generation #50000: fitness = 0.63571, best fit so far = 0.44413.
Generation #60000: fitness = 0.54486, best fit so far = 0.44413.
Generation #70000: fitness = 0.66348, best fit so far = 0.44413.
Generation #80000: fitness = 0.74024, best fit so far = 0.44413.
Generation #90000: fitness = 0.66513, best fit so far = 0.44413.
Generation #100000: fitness = 0.50793, best fit so far = 0.44413.
Finished Genetic Algorithm, with best fitness = 0.44413.
 Info: ===== Cycle number 22 ====
 @ Main In[12]:10
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Generation #10000: fitness = 0.58623, best fit so far = 0.44828. Generation #20000: fitness = 0.64759, best fit so far = 0.44828. Generation #30000: fitness = 0.62431, best fit so far = 0.44413. Generation #40000: fitness = 0.57482, best fit so far = 0.44413. Generation #50000: fitness = 0.63286, best fit so far = 0.44413. Generation #60000: fitness = 0.55002, best fit so far = 0.44413. Generation #70000: fitness = 0.62973, best fit so far = 0.44413. Generation #80000: fitness = 0.55905, best fit so far = 0.44413. Generation #90000: fitness = 0.50147, best fit so far = 0.44413. Generation #100000: fitness = 0.75743, best fit so far = 0.44413. Finished Genetic Algorithm, with best fitness = 0.44413. Info: ===== Cycle number 23 ==== @ Main In[12]:10 Generation #10000: fitness = 0.61111, best fit so far = 0.44713. Generation #20000: fitness = 0.5875, best fit so far = 0.44602. Generation #30000: fitness = 0.58512, best fit so far = 0.44602. Generation #40000: fitness = 0.76667, best fit so far = 0.44602. Generation #50000: fitness = 0.52758, best fit so far = 0.44602. Generation #60000: fitness = 0.484, best fit so far = 0.44413. Generation #70000: fitness = 0.64222, best fit so far = 0.44413. Generation #80000: fitness = 0.55492, best fit so far = 0.44413. Generation #90000: fitness = 0.55892, best fit so far = 0.44413. Generation #100000: fitness = 0.54161, best fit so far = 0.44413. Finished Genetic Algorithm, with best fitness = 0.44413. Info: ===== Cycle number 24 ==== @ Main In[12]:10 Generation #10000: fitness = 0.99254, best fit so far = 0.45401. Generation #20000: fitness = 0.5496, best fit so far = 0.44713. Generation #30000: fitness = 0.58632, best fit so far = 0.44713. Generation #40000: fitness = 0.49616, best fit so far = 0.44713. Generation #50000: fitness = 0.71096, best fit so far = 0.44463. Generation #60000: fitness = 0.63444, best fit so far = 0.44463. Generation #70000: fitness = 0.59022, best fit so far = 0.44463. Generation #80000: fitness = 0.6251, best fit so far = 0.44463. Generation #90000: fitness = 0.56588, best fit so far = 0.44463. Generation #100000: fitness = 0.57644, best fit so far = 0.44463. Finished Genetic Algorithm, with best fitness = 0.44463. Generation #10000: fitness = 0.59921, best fit so far = 0.44413. Info: ===== Cycle number 25 ==== @ Main In[12]:10 Generation #20000: fitness = 0.52022, best fit so far = 0.44413. Generation #30000: fitness = 0.81134, best fit so far = 0.44413. Generation #40000: fitness = 0.65937, best fit so far = 0.44413. Generation #50000: fitness = 0.59447, best fit so far = 0.44413. Generation #60000: fitness = 0.98634, best fit so far = 0.44413. Generation #70000: fitness = 0.75493, best fit so far = 0.44413. Generation #80000: fitness = 0.56461, best fit so far = 0.44413. Generation #90000: fitness = 0.48881, best fit so far = 0.44413. Generation #100000: fitness = 0.72551, best fit so far = 0.44413. Finished Genetic Algorithm, with best fitness = 0.44413.

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Info: ===== Cycle number 26 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.70168, best fit so far = 0.45561.
Generation #20000: fitness = 0.62773, best fit so far = 0.45342.
Generation #30000: fitness = 0.60328, best fit so far = 0.45256.
Generation #40000: fitness = 0.4648, best fit so far = 0.45103.
Generation #50000: fitness = 0.63167, best fit so far = 0.45047.
Generation #60000: fitness = 0.51522, best fit so far = 0.44413.
Generation #70000: fitness = 0.60769, best fit so far = 0.44413.
Generation #80000: fitness = 0.52073, best fit so far = 0.44413.
Generation #90000: fitness = 0.55575, best fit so far = 0.44413.
Generation #100000: fitness = 0.51331, best fit so far = 0.44413.
Finished Genetic Algorithm, with best fitness = 0.44413.
 Info: ===== Cycle number 27 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.52076, best fit so far = 0.45688.
Generation #20000: fitness = 0.66816, best fit so far = 0.4474.
Generation #30000: fitness = 0.55875, best fit so far = 0.4474.
Generation #40000: fitness = 0.67406, best fit so far = 0.4474.
Generation \#50000: fitness = 0.4546, best fit so far = 0.4474.
Generation #60000: fitness = 0.73788, best fit so far = 0.44621.
Generation #70000: fitness = 0.56547, best fit so far = 0.44541.
Generation #80000: fitness = 0.64378, best fit so far = 0.44541.
Generation #90000: fitness = 0.51076, best fit so far = 0.44541.
Generation #100000: fitness = 0.56266, best fit so far = 0.44541.
Finished Genetic Algorithm, with best fitness = 0.44541.
 Info: ===== Cycle number 28 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.60691, best fit so far = 0.45339.
Generation #20000: fitness = 0.8205, best fit so far = 0.45339.
Generation #30000: fitness = 0.6305, best fit so far = 0.44598.
Generation #40000: fitness = 0.52204, best fit so far = 0.44463.
Generation #50000: fitness = 0.57224, best fit so far = 0.44463.
Generation #60000: fitness = 0.53762, best fit so far = 0.44463.
Generation #70000: fitness = 0.5934, best fit so far = 0.44463.
Generation #80000: fitness = 0.48753, best fit so far = 0.44463.
Generation #90000: fitness = 0.96486, best fit so far = 0.44463.
Generation #100000: fitness = 0.68987, best fit so far = 0.44463.
Finished Genetic Algorithm, with best fitness = 0.44463.
 Info: ===== Cycle number 29 ====
```

^L @ Main In[12]:10

Generation #10000: fitness = 0.52598, best fit so far = 0.45252. Generation #20000: fitness = 0.69916, best fit so far = 0.44837. Generation #30000: fitness = 0.63596, best fit so far = 0.44837. Generation #40000: fitness = 0.55325, best fit so far = 0.44837. Generation #50000: fitness = 0.52297, best fit so far = 0.44413. Generation #60000: fitness = 0.53153, best fit so far = 0.44413. Generation #70000: fitness = 0.60199, best fit so far = 0.44413. Generation #80000: fitness = 0.70472, best fit so far = 0.44413. Generation #90000: fitness = 0.73006, best fit so far = 0.44413. Generation #100000: fitness = 0.58586, best fit so far = 0.44413. Finished Genetic Algorithm, with best fitness = 0.44413. Info: ===== Cycle number 30 ==== @ Main In[12]:10 Generation #10000: fitness = 0.53818, best fit so far = 0.45832. Generation #20000: fitness = 0.80784, best fit so far = 0.4546. Generation #30000: fitness = 0.55863, best fit so far = 0.45339. Generation #40000: fitness = 0.55197, best fit so far = 0.45339. Generation #50000: fitness = 0.68128, best fit so far = 0.44857. Generation #60000: fitness = 0.53259, best fit so far = 0.44857. Generation #70000: fitness = 0.57207, best fit so far = 0.44857. Generation #80000: fitness = 0.79971, best fit so far = 0.44778. Generation #90000: fitness = 0.58393, best fit so far = 0.44778. Generation #100000: fitness = 0.55861, best fit so far = 0.4448. Finished Genetic Algorithm, with best fitness = 0.4448. ┌ Info: ===== Cycle number 31 ==== @ Main In[12]:10 Generation #10000: fitness = 0.63403, best fit so far = 0.46916. Generation #20000: fitness = 0.51004, best fit so far = 0.44413. Generation #30000: fitness = 0.50964, best fit so far = 0.44413. Generation #40000: fitness = 0.56123, best fit so far = 0.44413. Generation #50000: fitness = 0.52806, best fit so far = 0.44413. Generation #60000: fitness = 0.66156, best fit so far = 0.44413. Generation #70000: fitness = 0.71815, best fit so far = 0.44413. Generation #80000: fitness = 0.85675, best fit so far = 0.44413. Generation #90000: fitness = 0.60943, best fit so far = 0.44413. Generation #100000: fitness = 0.56624, best fit so far = 0.44413. Finished Genetic Algorithm, with best fitness = 0.44413. Info: ===== Cycle number 32 ==== @ Main In[12]:10 Generation #10000: fitness = 0.56079, best fit so far = 0.45103. Generation #20000: fitness = 0.59548, best fit so far = 0.45103. Generation #30000: fitness = 0.51049, best fit so far = 0.45103. Generation #40000: fitness = 0.72269, best fit so far = 0.45103. Generation #50000: fitness = 0.61502, best fit so far = 0.4448. Generation #60000: fitness = 0.57255, best fit so far = 0.4448. Generation #70000: fitness = 0.7154, best fit so far = 0.4448. Generation #80000: fitness = 0.60506, best fit so far = 0.4448. Generation #90000: fitness = 0.79084, best fit so far = 0.4448. Generation #100000: fitness = 0.52174, best fit so far = 0.4448.

Finished Genetic Algorithm, with best fitness = 0.4448.

```
Info: ===== Cycle number 33 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.59021, best fit so far = 0.44828.
Generation #20000: fitness = 0.71045, best fit so far = 0.44396.
Generation #30000: fitness = 0.70113, best fit so far = 0.44396.
Generation #40000: fitness = 0.61561, best fit so far = 0.44396.
Generation #50000: fitness = 0.77068, best fit so far = 0.44396.
Generation #60000: fitness = 0.56232, best fit so far = 0.44396.
Generation #70000: fitness = 0.56584, best fit so far = 0.44396.
Generation #80000: fitness = 0.59506, best fit so far = 0.44396.
Generation #90000: fitness = 1.04289, best fit so far = 0.44396.
Generation #100000: fitness = 0.51169, best fit so far = 0.44396.
Finished Genetic Algorithm, with best fitness = 0.44396.
Generation #10000: fitness = 0.51908, best fit so far = 0.454.
 Info: ===== Cycle number 34 ====
 @ Main In[12]:10
Generation #20000: fitness = 0.68456, best fit so far = 0.44886.
Generation #30000: fitness = 0.54942, best fit so far = 0.44886.
Generation #40000: fitness = 0.58323, best fit so far = 0.44621.
Generation #50000: fitness = 0.6636, best fit so far = 0.44413.
Generation #60000: fitness = 0.55507, best fit so far = 0.44413.
Generation #70000: fitness = 0.59041, best fit so far = 0.44413.
Generation #80000: fitness = 0.61204, best fit so far = 0.44413.
Generation #90000: fitness = 0.58971, best fit so far = 0.44413.
Generation #100000: fitness = 0.54017, best fit so far = 0.44413.
Finished Genetic Algorithm, with best fitness = 0.44413.
 Info: ===== Cycle number 35 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.5468, best fit so far = 0.45103.
Generation #20000: fitness = 0.59911, best fit so far = 0.44585.
Generation #30000: fitness = 0.5609, best fit so far = 0.44585.
Generation #40000: fitness = 0.54154, best fit so far = 0.44585.
Generation \#50000: fitness = 0.542, best fit so far = 0.44537.
Generation #60000: fitness = 0.62209, best fit so far = 0.44537.
Generation #70000: fitness = 0.68889, best fit so far = 0.44537.
Generation #80000: fitness = 0.71664, best fit so far = 0.44413.
Generation #90000: fitness = 0.53042, best fit so far = 0.44413.
Generation #100000: fitness = 0.57913, best fit so far = 0.44413.
Finished Genetic Algorithm, with best fitness = 0.44413.
 Info: ===== Cycle number 36 ====
```

@ Main In[12]:10

Generation #10000: fitness = 0.56104, best fit so far = 0.45342. Generation #20000: fitness = 0.5636, best fit so far = 0.44396. Generation #30000: fitness = 0.65115, best fit so far = 0.44396. Generation #40000: fitness = 0.68145, best fit so far = 0.44396. Generation #50000: fitness = 0.57561, best fit so far = 0.44396. Generation #60000: fitness = 0.59455, best fit so far = 0.44396. Generation #70000: fitness = 0.57282, best fit so far = 0.44396. Generation #80000: fitness = 0.57743, best fit so far = 0.44396. Generation #90000: fitness = 0.62214, best fit so far = 0.44396. Generation #100000: fitness = 0.51717, best fit so far = 0.44396. Finished Genetic Algorithm, with best fitness = 0.44396. Info: ===== Cycle number 37 ==== @ Main In[12]:10 Generation #10000: fitness = 0.59503, best fit so far = 0.44963. Generation #20000: fitness = 0.95568, best fit so far = 0.44963. Generation #30000: fitness = 0.64377, best fit so far = 0.44731. Generation #40000: fitness = 0.84197, best fit so far = 0.44413. Generation #50000: fitness = 0.55659, best fit so far = 0.44413. Generation #60000: fitness = 0.60482, best fit so far = 0.44413. Generation #70000: fitness = 0.68731, best fit so far = 0.44413. Generation #80000: fitness = 0.5816, best fit so far = 0.44413. Generation #90000: fitness = 0.4794, best fit so far = 0.44413. Generation #100000: fitness = 0.52553, best fit so far = 0.44413. Finished Genetic Algorithm, with best fitness = 0.44413. Info: ==== Cycle number 38 ==== @ Main In[12]:10 Generation #10000: fitness = 0.53648, best fit so far = 0.46225. Generation #20000: fitness = 0.59955, best fit so far = 0.45015. Generation #30000: fitness = 0.65017, best fit so far = 0.44665. Generation #40000: fitness = 0.59287, best fit so far = 0.44665. Generation #50000: fitness = 0.91473, best fit so far = 0.44496. Generation #60000: fitness = 0.61471, best fit so far = 0.44496. Generation #70000: fitness = 0.52256, best fit so far = 0.44496. Generation #80000: fitness = 0.65989, best fit so far = 0.44413. Generation #90000: fitness = 0.52132, best fit so far = 0.44413. Generation #100000: fitness = 0.52554, best fit so far = 0.44413. Finished Genetic Algorithm, with best fitness = 0.44413. Info: ===== Cycle number 39 ==== @ Main In[12]:10 Generation #10000: fitness = 0.58629, best fit so far = 0.44413. Generation #20000: fitness = 0.55925, best fit so far = 0.44413. Generation #30000: fitness = 0.58626, best fit so far = 0.44413. Generation #40000: fitness = 0.65541, best fit so far = 0.44413. Generation #50000: fitness = 0.56973, best fit so far = 0.44413. Generation #60000: fitness = 0.69262, best fit so far = 0.44413. Generation #70000: fitness = 0.75389, best fit so far = 0.44413. Generation #80000: fitness = 0.53818, best fit so far = 0.44413. Generation #90000: fitness = 0.59632, best fit so far = 0.44413. Generation #100000: fitness = 0.60869, best fit so far = 0.44413.

Finished Genetic Algorithm, with best fitness = 0.44413.

```
Info: ==== Cycle number 40 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.61503, best fit so far = 0.45746.
Generation #20000: fitness = 0.46294, best fit so far = 0.44713.
Generation #30000: fitness = 0.53918, best fit so far = 0.44713.
Generation #40000: fitness = 0.64077, best fit so far = 0.44713.
Generation #50000: fitness = 0.57742, best fit so far = 0.44713.
Generation #60000: fitness = 0.55851, best fit so far = 0.44713.
Generation #70000: fitness = 0.91691, best fit so far = 0.44713.
Generation #80000: fitness = 0.62185, best fit so far = 0.44713.
Generation #90000: fitness = 0.65992, best fit so far = 0.44383.
Generation #100000: fitness = 0.61752, best fit so far = 0.44383.
Finished Genetic Algorithm, with best fitness = 0.44383.
 Info: ===== Cycle number 41 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.51061, best fit so far = 0.45035.
Generation #20000: fitness = 0.60628, best fit so far = 0.44413.
Generation #30000: fitness = 0.69183, best fit so far = 0.44413.
Generation #40000: fitness = 0.5218, best fit so far = 0.44413.
Generation #50000: fitness = 0.50619, best fit so far = 0.44413.
Generation #60000: fitness = 0.6654, best fit so far = 0.44413.
Generation #70000: fitness = 0.58083, best fit so far = 0.44413.
Generation \#80000: fitness = 0.5242, best fit so far = 0.44413.
Generation #90000: fitness = 0.5923, best fit so far = 0.44413.
Generation #100000: fitness = 0.56725, best fit so far = 0.44413.
Finished Genetic Algorithm, with best fitness = 0.44413.
 Info: ===== Cycle number 42 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.55384, best fit so far = 0.44811.
Generation #20000: fitness = 0.81149, best fit so far = 0.44811.
Generation #30000: fitness = 0.64398, best fit so far = 0.44811.
Generation #40000: fitness = 0.5408, best fit so far = 0.44811.
Generation #50000: fitness = 0.50506, best fit so far = 0.44811.
Generation #60000: fitness = 0.646, best fit so far = 0.44811.
Generation #70000: fitness = 0.53939, best fit so far = 0.44731.
Generation #80000: fitness = 0.51687, best fit so far = 0.44731.
Generation #90000: fitness = 0.56703, best fit so far = 0.44413.
Generation #100000: fitness = 0.63468, best fit so far = 0.44413.
Finished Genetic Algorithm, with best fitness = 0.44413.
 Info: ===== Cycle number 43 ====
 @ Main In[12]:10
```

Generation #10000: fitness = 0.74268, best fit so far = 0.45015. Generation #20000: fitness = 0.53139, best fit so far = 0.45015. Generation #30000: fitness = 0.80824, best fit so far = 0.45015. Generation #40000: fitness = 0.90688, best fit so far = 0.44532. Generation #50000: fitness = 0.63212, best fit so far = 0.44532. Generation #60000: fitness = 0.51174, best fit so far = 0.44532. Generation #70000: fitness = 0.70395, best fit so far = 0.44532. Generation #80000: fitness = 0.56088, best fit so far = 0.44391. Generation #90000: fitness = 0.5844, best fit so far = 0.44391. Generation #100000: fitness = 0.55424, best fit so far = 0.44391. Finished Genetic Algorithm, with best fitness = 0.44391. Info: ===== Cycle number 44 ==== @ Main In[12]:10 Generation #10000: fitness = 0.5458, best fit so far = 0.4471. Generation #20000: fitness = 0.64819, best fit so far = 0.44537. Generation #30000: fitness = 0.52979, best fit so far = 0.44537. Generation #40000: fitness = 0.80663, best fit so far = 0.44537. Generation #50000: fitness = 0.54639, best fit so far = 0.44537. Generation #60000: fitness = 0.6903, best fit so far = 0.44537. Generation #70000: fitness = 0.54497, best fit so far = 0.44537. Generation #80000: fitness = 0.60223, best fit so far = 0.44413. Generation #90000: fitness = 0.54817, best fit so far = 0.44413. Generation #100000: fitness = 0.64262, best fit so far = 0.44413. Finished Genetic Algorithm, with best fitness = 0.44413. Info: ==== Cycle number 45 ==== @ Main In[12]:10 Generation #10000: fitness = 0.5398, best fit so far = 0.4783. Generation #20000: fitness = 0.67104, best fit so far = 0.46321. Generation #30000: fitness = 0.62467, best fit so far = 0.44731. Generation #40000: fitness = 0.67164, best fit so far = 0.4445. Generation #50000: fitness = 0.70337, best fit so far = 0.4445. Generation #60000: fitness = 0.55841, best fit so far = 0.4445. Generation #70000: fitness = 0.56839, best fit so far = 0.4445. Generation #80000: fitness = 0.64996, best fit so far = 0.44413. Generation #90000: fitness = 0.54164, best fit so far = 0.44413. Generation #100000: fitness = 0.63672, best fit so far = 0.44413. Finished Genetic Algorithm, with best fitness = 0.44413. Info: ===== Cycle number 46 ==== @ Main In[12]:10 Generation #10000: fitness = 0.51245, best fit so far = 0.44713. Generation #20000: fitness = 0.50754, best fit so far = 0.44713. Generation #30000: fitness = 0.48008, best fit so far = 0.44413. Generation #40000: fitness = 0.65568, best fit so far = 0.44413. Generation #50000: fitness = 0.49246, best fit so far = 0.44413. Generation #60000: fitness = 0.54678, best fit so far = 0.44413. Generation #70000: fitness = 0.6665, best fit so far = 0.44396. Generation #80000: fitness = 0.53418, best fit so far = 0.44396. Generation #90000: fitness = 0.48068, best fit so far = 0.44396. Generation #100000: fitness = 0.75252, best fit so far = 0.44396.

Finished Genetic Algorithm, with best fitness = 0.44396.

```
Info: ===== Cycle number 47 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.60379, best fit so far = 0.45094.
Generation #20000: fitness = 0.55718, best fit so far = 0.44963.
Generation #30000: fitness = 0.6635, best fit so far = 0.44963.
Generation #40000: fitness = 0.53533, best fit so far = 0.44963.
Generation #50000: fitness = 0.55105, best fit so far = 0.44929.
Generation #60000: fitness = 0.60053, best fit so far = 0.44929.
Generation #70000: fitness = 0.64667, best fit so far = 0.44857.
Generation #80000: fitness = 0.66338, best fit so far = 0.44857.
Generation #90000: fitness = 0.58627, best fit so far = 0.44731.
Generation #100000: fitness = 0.5076, best fit so far = 0.44731.
Finished Genetic Algorithm, with best fitness = 0.44731.
 Info: ===== Cycle number 48 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.61738, best fit so far = 0.45107.
Generation #20000: fitness = 0.62386, best fit so far = 0.44874.
Generation #30000: fitness = 0.60359, best fit so far = 0.4448.
Generation #40000: fitness = 0.64306, best fit so far = 0.4448.
Generation #50000: fitness = 0.67387, best fit so far = 0.4448.
Generation #60000: fitness = 0.61001, best fit so far = 0.4448.
Generation #70000: fitness = 0.6234, best fit so far = 0.4448.
Generation #80000: fitness = 0.75032, best fit so far = 0.4448.
Generation #90000: fitness = 0.58647, best fit so far = 0.4448.
Generation #100000: fitness = 0.63653, best fit so far = 0.4448.
Finished Genetic Algorithm, with best fitness = 0.4448.
 Info: ===== Cycle number 49 ====
 @ Main In[12]:10
Generation #10000: fitness = 0.49372, best fit so far = 0.4546.
Generation #20000: fitness = 0.61403, best fit so far = 0.4546.
Generation #30000: fitness = 0.67771, best fit so far = 0.45094.
Generation #40000: fitness = 0.59411, best fit so far = 0.45094.
Generation #50000: fitness = 0.55605, best fit so far = 0.45094.
Generation #60000: fitness = 0.46881, best fit so far = 0.45094.
Generation #70000: fitness = 0.77179, best fit so far = 0.44542.
Generation #80000: fitness = 0.53536, best fit so far = 0.44542.
Generation #90000: fitness = 0.51772, best fit so far = 0.44542.
Generation #100000: fitness = 0.62005, best fit so far = 0.44542.
Finished Genetic Algorithm, with best fitness = 0.44542.
 Info: ===== Cycle number 50 ====
 @ Main In[12]:10
```

```
Generation #10000: fitness = 0.56158, best fit so far = 0.45339. Generation #20000: fitness = 0.56783, best fit so far = 0.44542. Generation #30000: fitness = 0.59628, best fit so far = 0.44542. Generation #40000: fitness = 0.50888, best fit so far = 0.44542. Generation #50000: fitness = 0.61279, best fit so far = 0.44542. Generation #60000: fitness = 0.48761, best fit so far = 0.44542. Generation #70000: fitness = 0.58016, best fit so far = 0.44542. Generation #80000: fitness = 0.55966, best fit so far = 0.44413. Generation #90000: fitness = 0.61469, best fit so far = 0.44413. Generation #100000: fitness = 0.73127, best fit so far = 0.44413. Finished Genetic Algorithm, with best fitness = 0.44413.
```

The Refine function is defined as

```
function Refine(data::Matrix{T}, tmatch::Matrix{T}, ensize::Int64, qstart::T; popul
ation::Int64=10, maxiter::Int64=100000, reports::Int64=100) where T<:Real</pre>
```

The required arguments:

- 1. data::Matrix{T} is the truncated experimental data.
- tmatch::Matrix{T} is the profile pool where tmatch[:, 1] is the scattering angle q and tmatch[:, 2:end] are all the size(tmatch, 2) 1 profiles.
- 3. ensize::Int64 is the ensemble size.
- 4. qstart::T is the minimum q that eEOM fits to.

The optional arguments:

population::Int64=10 is the number of population in one generation with default 10.

Note that the survivors are selected based on Possion-Boltzmann distribution of the fitness values.

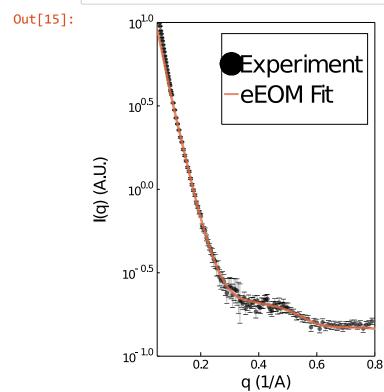
- 1. maxiter::Int64=100000 is the number of generations in one cycle.
- 2. report::Int64=100 is the number of times one wants to see the current progress in each cycle. Set to 1 if the outputs are too verbose.

The outputs:

```
return best fitness, best chromosome
```

- 1. best_fitness: The fitness score of the best ensemble
- 2. best chromosome: The survivors of the best ensemble

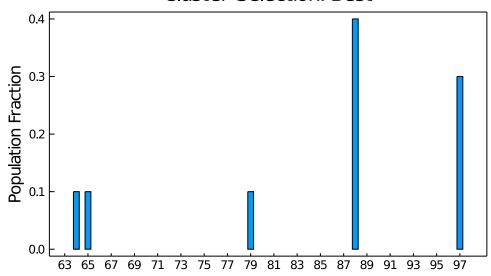
```
In [15]: # Plot the eEOM results
    p = scatter(data1[:,1], data1[:,2], yerror=data1[:,3], yscale=:log10, markersi
    ze=2.5, c=:black, markeralpha=0.6, linealpha=0.25, lab="Experiment", size=(300
    ,450), legendfont=font(16), titlefont=font(20));
    plot!(q, mean(pool1[:, survivors1[:, findall(fitness1 .== minimum(fitness1))[1
    ]]], dims=2), lw=2.5, linealpha=0.8, lab="eEOM Fit")
    plot!(size=(300,400), grid=false, legend=true, framestyle=:box);
    xlims!(0.05, 0.8);
    ylims!(0.1, 10)
    xlabel!("q (1/A)");
    ylabel!("I(q) (A.U.)")
```



```
In [16]: # Plot the best ensemble
    best = survivors1[:, findall(fitness1 .== minimum(fitness1))[1]];
    dic = countmap(reshape(best, (length(best), )));
    b = bar(collect(keys(dic)), collect(values(dic)) / length(best), title="Cluste r Selection: Best", xticks=collect(1:2:98), bar_width=0.5);
    plot!(size=(500, 300), grid=false, legend=false, framestyle=:box);
    ylabel!("Population Fraction")
```

Out[16]:

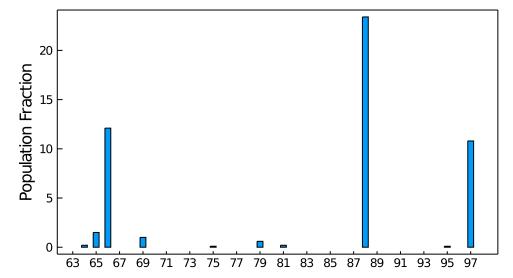
Cluster Selection: Best



```
In [17]: # Plot the all ensemble
    dic = countmap(reshape(survivors1, (length(survivors1), )));
    b = bar(collect(keys(dic)), collect(values(dic)) / length(best), title="Cluste
    r Selection: All", xticks=collect(1:2:98), bar_width=0.5);
    plot!(size=(500, 300), grid=false, legend=false, framestyle=:box);
    ylabel!("Population Fraction")
```

Out[17]:

Cluster Selection: All



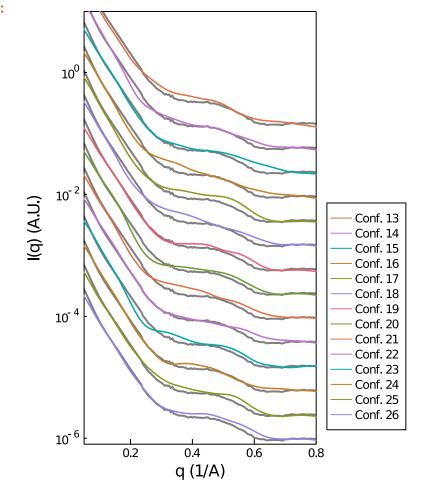
And then one can do more analyses in the structures based on the selection.

Example 2

The data2 and pool2 pair.

```
In [20]: # Plot the data and see what's going on
    p = plot(size=(400, 500), grid=false, legend=:outerbottomright, framestyle=:bo
    x);
    s = 0.4;
    for i = 1:14
        plot!(data2[:,1], s^(i-1) * data2[:,2], yscale=:log10, lw=2.0, c=:black, linealpha=0.5, lab="");
        plot!(q, s^(i-1)*pool2[:,7i-6], lw=1.5, yscale=:log10, lab="Conf. $(12+i)"
    );
    end
    xlims!(0.05, 0.8)
    ylims!(0.8e-6, 10)
    ylabel!("I(q) (A.U.)")
    xlabel!("q (1/A)")
```

Out[20]:



```
In [19]: # Run the eEOM structural refinement
         # Try running from 0.1 to 1.0 due to better S/N
         idx = findall(data2[:,1] .<= 1.0);</pre>
         tmp = data2[idx, :];
         ensize = 10;
          cycles = 50;
          survivors2 = zeros(Int64, ensize, cycles);
         fitness2 = zeros(cycles);
          t = @elapsed for i = 1:cycles
             @info("===== Cycle number $i ====");
             fitness2[i], survivor = Refine(tmp, [q pool2], ensize, 0.10; population=10
          , maxiter=100000, reports=10);
              survivors2[:,i] = survivor[:,1];
         end
         println("- eEOM for $cycles cycles and $(size(pool2, 2)) conformaitons took $(
         round(t, digits=2)) seconds.");
```

```
Info: ===== Cycle number 1 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.14111, best fit so far = 5.09469.
Generation #20000: fitness = 5.14111, best fit so far = 5.09469.
Generation #30000: fitness = 5.14111, best fit so far = 5.09469.
Generation #40000: fitness = 5.14111, best fit so far = 5.09469.
Generation #50000: fitness = 5.11789, best fit so far = 4.95215.
Generation #60000: fitness = 5.14111, best fit so far = 4.90302.
Generation #70000: fitness = 5.32805, best fit so far = 4.90302.
Generation #80000: fitness = 5.15766, best fit so far = 4.90302.
Generation #90000: fitness = 5.28434, best fit so far = 4.90302.
Generation #100000: fitness = 5.2116, best fit so far = 4.90302.
Finished Genetic Algorithm, with best fitness = 4.90302.
 Info: ===== Cycle number 2 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.16178, best fit so far = 4.85306.
Generation #20000: fitness = 4.77376, best fit so far = 4.77376.
Generation #30000: fitness = 5.26739, best fit so far = 4.77376.
Generation #40000: fitness = 5.05083, best fit so far = 4.77376.
Generation #50000: fitness = 4.77376, best fit so far = 4.77376.
Generation #60000: fitness = 4.77376, best fit so far = 4.77376.
Generation #70000: fitness = 5.15766, best fit so far = 4.77376.
Generation #80000: fitness = 5.15766, best fit so far = 4.77376.
Generation #90000: fitness = 5.29207, best fit so far = 4.77376.
Generation #100000: fitness = 5.14111, best fit so far = 4.77376.
Finished Genetic Algorithm, with best fitness = 4.77376.
 Info: ===== Cycle number 3 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.09624, best fit so far = 5.09624.
Generation #20000: fitness = 5.09624, best fit so far = 4.92485.
Generation #30000: fitness = 5.41014, best fit so far = 4.92485.
Generation #40000: fitness = 5.42213, best fit so far = 4.92485.
Generation #50000: fitness = 5.41014, best fit so far = 4.92485.
Generation #60000: fitness = 5.14111, best fit so far = 4.90302.
Generation #70000: fitness = 5.42781, best fit so far = 4.90302.
Generation #80000: fitness = 5.14111, best fit so far = 4.90302.
Generation #90000: fitness = 5.14111, best fit so far = 4.90302.
Generation #100000: fitness = 5.17169, best fit so far = 4.85306.
Finished Genetic Algorithm, with best fitness = 4.85306.
 Info: ===== Cycle number 4 ====
 @ Main In[19]:11
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Generation #10000: fitness = 5.32412, best fit so far = 4.95084. Generation #20000: fitness = 5.08407, best fit so far = 4.8183. Generation #30000: fitness = 5.08407, best fit so far = 4.8183. Generation #40000: fitness = 5.38052, best fit so far = 4.8183. Generation #50000: fitness = 5.08407, best fit so far = 4.8183. Generation #60000: fitness = 5.08407, best fit so far = 4.8183. Generation #70000: fitness = 5.50941, best fit so far = 4.8183. Generation #80000: fitness = 5.41014, best fit so far = 4.8183. Generation #90000: fitness = 4.94775, best fit so far = 4.8183. Generation #100000: fitness = 5.08407, best fit so far = 4.8183. Finished Genetic Algorithm, with best fitness = 4.8183. Info: ===== Cycle number 5 ==== @ Main In[19]:11 Generation #10000: fitness = 5.14111, best fit so far = 5.09469. Generation #20000: fitness = 5.14111, best fit so far = 5.06565. Generation #30000: fitness = 5.14111, best fit so far = 5.06565. Generation #40000: fitness = 5.47021, best fit so far = 5.06565. Generation #50000: fitness = 5.14111, best fit so far = 5.06565. Generation #60000: fitness = 5.1127, best fit so far = 5.06565. Generation #70000: fitness = 5.16178, best fit so far = 4.85306. Generation #80000: fitness = 5.14111, best fit so far = 4.85306. Generation #90000: fitness = 5.14111, best fit so far = 4.85306. Generation #100000: fitness = 5.19785, best fit so far = 4.85306. Finished Genetic Algorithm, with best fitness = 4.85306. ┌ Info: ===== Cycle number 6 ==== @ Main In[19]:11 Generation #10000: fitness = 5.4871, best fit so far = 5.29901. Generation #20000: fitness = 5.55498, best fit so far = 5.24036. Generation #30000: fitness = 5.29207, best fit so far = 5.1014. Generation #40000: fitness = 5.15766, best fit so far = 5.09696. Generation #50000: fitness = 5.14111, best fit so far = 5.09696. Generation #60000: fitness = 5.15766, best fit so far = 5.09696. Generation #70000: fitness = 5.18258, best fit so far = 4.85306. Generation #80000: fitness = 5.14551, best fit so far = 4.85306. Generation #90000: fitness = 5.29207, best fit so far = 4.85306. Generation #100000: fitness = 5.15766, best fit so far = 4.85306. Finished Genetic Algorithm, with best fitness = 4.85306. Info: ===== Cycle number 7 ==== @ Main In[19]:11 Generation #10000: fitness = 5.44707, best fit so far = 5.04613. Generation #20000: fitness = 5.30751, best fit so far = 4.85306. Generation #30000: fitness = 5.41014, best fit so far = 4.85306. Generation #40000: fitness = 4.94775, best fit so far = 4.77376. Generation #50000: fitness = 5.08407, best fit so far = 4.77376. Generation #60000: fitness = 5.08407, best fit so far = 4.77376. Generation #70000: fitness = 5.08407, best fit so far = 4.77376. Generation #80000: fitness = 5.08407, best fit so far = 4.77376. Generation #90000: fitness = 5.23226, best fit so far = 4.77376. Generation #100000: fitness = 5.23226, best fit so far = 4.77376. Finished Genetic Algorithm, with best fitness = 4.77376.

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Info: ===== Cycle number 8 ====
 @ Main In[19]:11
Generation #10000: fitness = 4.90302, best fit so far = 4.77376.
Generation #20000: fitness = 4.77376, best fit so far = 4.77376.
Generation #30000: fitness = 5.08407, best fit so far = 4.77376.
Generation #40000: fitness = 5.32412, best fit so far = 4.77376.
Generation #50000: fitness = 5.45203, best fit so far = 4.77376.
Generation #60000: fitness = 5.41014, best fit so far = 4.77376.
Generation #70000: fitness = 5.44968, best fit so far = 4.77376.
Generation #80000: fitness = 5.08407, best fit so far = 4.77376.
Generation #90000: fitness = 4.98403, best fit so far = 4.77376.
Generation #100000: fitness = 4.94775, best fit so far = 4.77376.
Finished Genetic Algorithm, with best fitness = 4.77376.
 Info: ===== Cycle number 9 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.29207, best fit so far = 4.90302.
Generation #20000: fitness = 5.15766, best fit so far = 4.90302.
Generation #30000: fitness = 5.11789, best fit so far = 4.85306.
Generation #40000: fitness = 5.15766, best fit so far = 4.85306.
Generation #50000: fitness = 5.15766, best fit so far = 4.85306.
Generation #60000: fitness = 5.42697, best fit so far = 4.85306.
Generation #70000: fitness = 5.15766, best fit so far = 4.85306.
Generation #80000: fitness = 5.34383, best fit so far = 4.85306.
Generation #90000: fitness = 5.29207, best fit so far = 4.85306.
Generation #100000: fitness = 4.90302, best fit so far = 4.85306.
Finished Genetic Algorithm, with best fitness = 4.85306.
 Info: ===== Cycle number 10 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.75482, best fit so far = 4.77376.
Generation #20000: fitness = 5.08407, best fit so far = 4.77376.
Generation #30000: fitness = 5.08407, best fit so far = 4.77376.
Generation #40000: fitness = 5.08407, best fit so far = 4.77376.
Generation #50000: fitness = 5.08407, best fit so far = 4.77376.
Generation #60000: fitness = 5.08407, best fit so far = 4.77376.
Generation #70000: fitness = 5.3504, best fit so far = 4.77376.
Generation #80000: fitness = 5.3504, best fit so far = 4.77376.
Generation #90000: fitness = 5.08407, best fit so far = 4.77376.
Generation #100000: fitness = 5.08407, best fit so far = 4.77376.
Finished Genetic Algorithm, with best fitness = 4.77376.
 Info: ===== Cycle number 11 ====
 @ Main In[19]:11
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Generation #10000: fitness = 5.47021, best fit so far = 4.85306. Generation #20000: fitness = 5.39049, best fit so far = 4.85306. Generation #30000: fitness = 5.11789, best fit so far = 4.85306. Generation #40000: fitness = 5.29207, best fit so far = 4.85306. Generation #50000: fitness = 5.15766, best fit so far = 4.85306. Generation #60000: fitness = 5.15766, best fit so far = 4.85306. Generation #70000: fitness = 4.77376, best fit so far = 4.77376. Generation #80000: fitness = 4.77376, best fit so far = 4.77376. Generation #90000: fitness = 4.77376, best fit so far = 4.77376. Generation #100000: fitness = 5.25402, best fit so far = 4.77376. Finished Genetic Algorithm, with best fitness = 4.77376. Info: ===== Cycle number 12 ==== @ Main In[19]:11 Generation #10000: fitness = 4.92485, best fit so far = 4.86981. Generation #20000: fitness = 5.08407, best fit so far = 4.86981. Generation #30000: fitness = 4.98403, best fit so far = 4.86981. Generation #40000: fitness = 5.07127, best fit so far = 4.86981. Generation #50000: fitness = 5.23226, best fit so far = 4.86981. Generation #60000: fitness = 5.24634, best fit so far = 4.86981. Generation #70000: fitness = 5.09296, best fit so far = 4.86981. Generation #80000: fitness = 5.08407, best fit so far = 4.86981. Generation #90000: fitness = 5.08407, best fit so far = 4.86981. Generation #100000: fitness = 5.08407, best fit so far = 4.86981. Finished Genetic Algorithm, with best fitness = 4.86981. ┌ Info: ===== Cycle number 13 ==== @ Main In[19]:11 Generation #10000: fitness = 5.08407, best fit so far = 4.77376. Generation #20000: fitness = 5.08407, best fit so far = 4.77376. Generation #30000: fitness = 5.08407, best fit so far = 4.77376. Generation #40000: fitness = 5.08407, best fit so far = 4.77376. Generation #50000: fitness = 5.08407, best fit so far = 4.77376. Generation #60000: fitness = 5.08407, best fit so far = 4.77376. Generation #70000: fitness = 5.08407, best fit so far = 4.77376. Generation #80000: fitness = 4.98403, best fit so far = 4.77376. Generation #90000: fitness = 5.30499, best fit so far = 4.77376. Generation #100000: fitness = 5.08407, best fit so far = 4.77376. Finished Genetic Algorithm, with best fitness = 4.77376. Info: ===== Cycle number 14 ==== @ Main In[19]:11 Generation #10000: fitness = 5.08407, best fit so far = 4.89904. Generation #20000: fitness = 4.89904, best fit so far = 4.89904. Generation #30000: fitness = 5.29405, best fit so far = 4.89904. Generation #40000: fitness = 5.08407, best fit so far = 4.86981. Generation #50000: fitness = 5.23226, best fit so far = 4.86981. Generation #60000: fitness = 5.08407, best fit so far = 4.86981. Generation #70000: fitness = 4.86981, best fit so far = 4.86981. Generation #80000: fitness = 5.08407, best fit so far = 4.86981. Generation #90000: fitness = 4.98403, best fit so far = 4.86981. Generation #100000: fitness = 5.08407, best fit so far = 4.86981. Finished Genetic Algorithm, with best fitness = 4.86981.

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Info: ===== Cycle number 15 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.25473, best fit so far = 4.85306.
Generation #20000: fitness = 5.38299, best fit so far = 4.85306.
Generation #30000: fitness = 5.15766, best fit so far = 4.85306.
Generation #40000: fitness = 5.14111, best fit so far = 4.85306.
Generation #50000: fitness = 5.14111, best fit so far = 4.85306.
Generation #60000: fitness = 5.14551, best fit so far = 4.85306.
Generation #70000: fitness = 5.15766, best fit so far = 4.85306.
Generation #80000: fitness = 5.15766, best fit so far = 4.85306.
Generation #90000: fitness = 5.14111, best fit so far = 4.85306.
Generation #100000: fitness = 5.14111, best fit so far = 4.85306.
Finished Genetic Algorithm, with best fitness = 4.85306.
 Info: ===== Cycle number 16 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.15766, best fit so far = 5.1014.
Generation #20000: fitness = 5.15766, best fit so far = 4.85306.
Generation #30000: fitness = 5.14111, best fit so far = 4.85306.
Generation #40000: fitness = 5.14111, best fit so far = 4.85306.
Generation #50000: fitness = 5.14111, best fit so far = 4.85306.
Generation #60000: fitness = 5.26924, best fit so far = 4.85306.
Generation #70000: fitness = 5.11745, best fit so far = 4.85306.
Generation #80000: fitness = 4.90302, best fit so far = 4.85306.
Generation #90000: fitness = 4.90302, best fit so far = 4.85306.
Generation #100000: fitness = 4.90302, best fit so far = 4.77376.
Finished Genetic Algorithm, with best fitness = 4.77376.
 Info: ===== Cycle number 17 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.14111, best fit so far = 5.1127.
Generation #20000: fitness = 5.14111, best fit so far = 5.1127.
Generation #30000: fitness = 5.15766, best fit so far = 5.1127.
Generation #40000: fitness = 5.65622, best fit so far = 4.92485.
Generation #50000: fitness = 5.08407, best fit so far = 4.89904.
Generation #60000: fitness = 5.08407, best fit so far = 4.86981.
Generation #70000: fitness = 5.08407, best fit so far = 4.86981.
Generation #80000: fitness = 5.08407, best fit so far = 4.86981.
Generation #90000: fitness = 5.08407, best fit so far = 4.86981.
Generation #100000: fitness = 5.08407, best fit so far = 4.86981.
Finished Genetic Algorithm, with best fitness = 4.86981.
 Info: ===== Cycle number 18 ====
 @ Main In[19]:11
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Generation #10000: fitness = 5.41984, best fit so far = 4.95084. Generation #20000: fitness = 4.90302, best fit so far = 4.77376. Generation #30000: fitness = 4.90302, best fit so far = 4.77376. Generation #40000: fitness = 4.94775, best fit so far = 4.77376. Generation #50000: fitness = 5.2827, best fit so far = 4.77376. Generation #60000: fitness = 5.10429, best fit so far = 4.77376. Generation #70000: fitness = 4.98403, best fit so far = 4.77376. Generation #80000: fitness = 4.94775, best fit so far = 4.77376. Generation #90000: fitness = 5.38052, best fit so far = 4.77376. Generation #100000: fitness = 5.2744, best fit so far = 4.77376. Finished Genetic Algorithm, with best fitness = 4.77376. Info: ===== Cycle number 19 ==== @ Main In[19]:11 Generation #10000: fitness = 5.11789, best fit so far = 4.85306. Generation #20000: fitness = 5.29207, best fit so far = 4.85306. Generation #30000: fitness = 5.15766, best fit so far = 4.85306. Generation #40000: fitness = 5.29207, best fit so far = 4.85306. Generation #50000: fitness = 5.29207, best fit so far = 4.85306. Generation #60000: fitness = 5.15766, best fit so far = 4.85306. Generation #70000: fitness = 5.39695, best fit so far = 4.85306. Generation #80000: fitness = 5.42781, best fit so far = 4.85306. Generation #90000: fitness = 5.14111, best fit so far = 4.85306. Generation #100000: fitness = 5.14111, best fit so far = 4.85306. Finished Genetic Algorithm, with best fitness = 4.85306. 「Info: ===== Cycle number 20 ==== @ Main In[19]:11 Generation #10000: fitness = 4.89904, best fit so far = 4.89904. Generation #20000: fitness = 5.08407, best fit so far = 4.89904. Generation #30000: fitness = 5.08407, best fit so far = 4.89904. Generation #40000: fitness = 5.08407, best fit so far = 4.86981. Generation #50000: fitness = 5.08407, best fit so far = 4.86981. Generation #60000: fitness = 5.26365, best fit so far = 4.86981. Generation #70000: fitness = 5.15766, best fit so far = 4.85306. Generation #80000: fitness = 5.15766, best fit so far = 4.85306. Generation #90000: fitness = 5.51203, best fit so far = 4.85306. Generation #100000: fitness = 5.14111, best fit so far = 4.85306. Finished Genetic Algorithm, with best fitness = 4.85306. Info: ===== Cycle number 21 ==== @ Main In[19]:11 Generation #10000: fitness = 5.08407, best fit so far = 4.89904. Generation #20000: fitness = 4.95084, best fit so far = 4.86981. Generation #30000: fitness = 4.90302, best fit so far = 4.77376. Generation #40000: fitness = 4.90302, best fit so far = 4.77376. Generation #50000: fitness = 5.11789, best fit so far = 4.77376. Generation #60000: fitness = 5.14111, best fit so far = 4.77376. Generation #70000: fitness = 5.15766, best fit so far = 4.77376. Generation #80000: fitness = 5.29207, best fit so far = 4.77376. Generation #90000: fitness = 5.47021, best fit so far = 4.77376. Generation #100000: fitness = 5.15766, best fit so far = 4.77376.

Finished Genetic Algorithm, with best fitness = 4.77376.

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Info: ===== Cycle number 22 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.96964, best fit so far = 5.1127.
Generation #20000: fitness = 5.15766, best fit so far = 5.1127.
Generation #30000: fitness = 5.15766, best fit so far = 5.1127.
Generation #40000: fitness = 5.14111, best fit so far = 5.1127.
Generation #50000: fitness = 5.14111, best fit so far = 5.1127.
Generation #60000: fitness = 5.15766, best fit so far = 5.1127.
Generation #70000: fitness = 5.15766, best fit so far = 5.1127.
Generation #80000: fitness = 5.15766, best fit so far = 5.1127.
Generation #90000: fitness = 5.15766, best fit so far = 5.1127.
Generation #100000: fitness = 5.29207, best fit so far = 5.1127.
Finished Genetic Algorithm, with best fitness = 5.1127.
 Info: ===== Cycle number 23 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.32412, best fit so far = 4.99634.
Generation #20000: fitness = 5.46391, best fit so far = 4.85306.
Generation #30000: fitness = 5.14111, best fit so far = 4.85306.
Generation #40000: fitness = 5.29207, best fit so far = 4.85306.
Generation #50000: fitness = 5.29207, best fit so far = 4.85306.
Generation #60000: fitness = 5.14111, best fit so far = 4.85306.
Generation #70000: fitness = 5.14111, best fit so far = 4.85306.
Generation #80000: fitness = 5.29207, best fit so far = 4.85306.
Generation #90000: fitness = 5.38603, best fit so far = 4.85306.
Generation #100000: fitness = 5.15766, best fit so far = 4.85306.
Finished Genetic Algorithm, with best fitness = 4.85306.
 Info: ===== Cycle number 24 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.14111, best fit so far = 5.1127.
Generation #20000: fitness = 5.14111, best fit so far = 5.1127.
Generation #30000: fitness = 5.14111, best fit so far = 5.1127.
Generation #40000: fitness = 5.14111, best fit so far = 5.1127.
Generation #50000: fitness = 5.14111, best fit so far = 5.1127.
Generation #60000: fitness = 5.14111, best fit so far = 5.1127.
Generation #70000: fitness = 5.15766, best fit so far = 5.1127.
Generation #80000: fitness = 5.15766, best fit so far = 5.1127.
Generation #90000: fitness = 5.15766, best fit so far = 5.1127.
Generation #100000: fitness = 5.29207, best fit so far = 5.1127.
Finished Genetic Algorithm, with best fitness = 5.1127.
 Info: ===== Cycle number 25 ====
 @ Main In[19]:11
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file:///C:/Users/yc225/Desktop/eEOM_demo.html

Generation #10000: fitness = 4.98403, best fit so far = 4.86981. Generation #20000: fitness = 5.08407, best fit so far = 4.86981. Generation #30000: fitness = 5.08407, best fit so far = 4.86981. Generation #40000: fitness = 5.08407, best fit so far = 4.86981. Generation #50000: fitness = 5.08407, best fit so far = 4.86981. Generation #60000: fitness = 5.08407, best fit so far = 4.86981. Generation #70000: fitness = 5.08407, best fit so far = 4.86981. Generation #80000: fitness = 5.08407, best fit so far = 4.86981. Generation #90000: fitness = 4.98403, best fit so far = 4.86981. Generation #100000: fitness = 4.98403, best fit so far = 4.86981. Finished Genetic Algorithm, with best fitness = 4.86981. Info: ===== Cycle number 26 ==== @ Main In[19]:11 Generation #10000: fitness = 5.41014, best fit so far = 5.00644. Generation #20000: fitness = 4.90302, best fit so far = 4.85306. Generation #30000: fitness = 4.90302, best fit so far = 4.85306. Generation #40000: fitness = 4.90302, best fit so far = 4.85306. Generation #50000: fitness = 5.28796, best fit so far = 4.85306. Generation #60000: fitness = 5.0632, best fit so far = 4.85306. Generation #70000: fitness = 5.24672, best fit so far = 4.85306. Generation #80000: fitness = 5.32412, best fit so far = 4.85306. Generation #90000: fitness = 5.41796, best fit so far = 4.85306. Generation #100000: fitness = 5.40717, best fit so far = 4.85306. Finished Genetic Algorithm, with best fitness = 4.85306. ┌ Info: ===== Cycle number 27 ==== @ Main In[19]:11 Generation #10000: fitness = 4.95084, best fit so far = 4.95084. Generation #20000: fitness = 5.28111, best fit so far = 4.92485. Generation #30000: fitness = 5.08407, best fit so far = 4.92485. Generation #40000: fitness = 5.08407, best fit so far = 4.86981. Generation #50000: fitness = 5.08407, best fit so far = 4.86981. Generation #60000: fitness = 5.20344, best fit so far = 4.86981. Generation #70000: fitness = 4.98403, best fit so far = 4.86981. Generation #80000: fitness = 5.08407, best fit so far = 4.86981. Generation #90000: fitness = 5.08407, best fit so far = 4.86981. Generation #100000: fitness = 5.08407, best fit so far = 4.86981. Finished Genetic Algorithm, with best fitness = 4.86981. Info: ===== Cycle number 28 ==== @ Main In[19]:11 Generation #10000: fitness = 5.15766, best fit so far = 5.1127. Generation #20000: fitness = 5.26344, best fit so far = 5.1127. Generation #30000: fitness = 5.15766, best fit so far = 5.1127. Generation #40000: fitness = 5.15766, best fit so far = 5.1127. Generation #50000: fitness = 5.15766, best fit so far = 5.1127. Generation #60000: fitness = 5.15766, best fit so far = 5.09696. Generation #70000: fitness = 5.37021, best fit so far = 4.90302. Generation #80000: fitness = 5.05083, best fit so far = 4.77376. Generation #90000: fitness = 4.99712, best fit so far = 4.77376. Generation #100000: fitness = 5.3504, best fit so far = 4.77376. Finished Genetic Algorithm, with best fitness = 4.77376.

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Info: ===== Cycle number 29 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.43026, best fit so far = 5.1686.
Generation #20000: fitness = 4.914, best fit so far = 4.77376.
Generation #30000: fitness = 5.09624, best fit so far = 4.77376.
Generation #40000: fitness = 5.09624, best fit so far = 4.77376.
Generation #50000: fitness = 5.07939, best fit so far = 4.77376.
Generation #60000: fitness = 5.08407, best fit so far = 4.77376.
Generation #70000: fitness = 4.98403, best fit so far = 4.77376.
Generation #80000: fitness = 5.08407, best fit so far = 4.77376.
Generation #90000: fitness = 4.98403, best fit so far = 4.77376.
Generation #100000: fitness = 5.08407, best fit so far = 4.77376.
Finished Genetic Algorithm, with best fitness = 4.77376.
 Info: ===== Cycle number 30 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.18515, best fit so far = 5.08407.
Generation #20000: fitness = 4.98403, best fit so far = 4.86981.
Generation #30000: fitness = 5.21312, best fit so far = 4.86981.
Generation #40000: fitness = 5.45329, best fit so far = 4.85306.
Generation #50000: fitness = 5.15766, best fit so far = 4.85306.
Generation #60000: fitness = 5.15766, best fit so far = 4.85306.
Generation #70000: fitness = 5.15766, best fit so far = 4.85306.
Generation #80000: fitness = 5.15766, best fit so far = 4.85306.
Generation #90000: fitness = 5.15766, best fit so far = 4.85306.
Generation #100000: fitness = 5.39364, best fit so far = 4.85306.
Finished Genetic Algorithm, with best fitness = 4.85306.
 Info: ===== Cycle number 31 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.36033, best fit so far = 5.05083.
Generation #20000: fitness = 5.41014, best fit so far = 5.05083.
Generation #30000: fitness = 5.29207, best fit so far = 4.85306.
Generation #40000: fitness = 5.14111, best fit so far = 4.85306.
Generation #50000: fitness = 5.64209, best fit so far = 4.85306.
Generation #60000: fitness = 4.98403, best fit so far = 4.85306.
Generation #70000: fitness = 5.08407, best fit so far = 4.77376.
Generation #80000: fitness = 4.98403, best fit so far = 4.77376.
Generation #90000: fitness = 5.08407, best fit so far = 4.77376.
Generation #100000: fitness = 5.08407, best fit so far = 4.77376.
Finished Genetic Algorithm, with best fitness = 4.77376.
Generation #10000: fitness = 5.87354, best fit so far = 4.85306.
 Info: ===== Cycle number 32 ====
 @ Main In[19]:11
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Generation #20000: fitness = 5.36033, best fit so far = 4.85306.
Generation #30000: fitness = 5.37617, best fit so far = 4.85306.
Generation #40000: fitness = 4.90302, best fit so far = 4.77376.
Generation #50000: fitness = 5.15766, best fit so far = 4.77376.
Generation #60000: fitness = 5.55146, best fit so far = 4.77376.
Generation #70000: fitness = 5.21707, best fit so far = 4.77376.
Generation #80000: fitness = 5.08884, best fit so far = 4.77376.
Generation #90000: fitness = 4.98403, best fit so far = 4.77376.
Generation #100000: fitness = 4.98403, best fit so far = 4.77376.
Finished Genetic Algorithm, with best fitness = 4.77376.
r Info: ===== Cycle number 33 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.08407, best fit so far = 4.89904.
Generation #20000: fitness = 5.18515, best fit so far = 4.89904.
Generation #30000: fitness = 5.08407, best fit so far = 4.89904.
Generation #40000: fitness = 5.08407, best fit so far = 4.86981.
Generation #50000: fitness = 5.08407, best fit so far = 4.86981.
Generation #60000: fitness = 5.08407, best fit so far = 4.86981.
Generation #70000: fitness = 4.98403, best fit so far = 4.86981.
Generation #80000: fitness = 5.08407, best fit so far = 4.86981.
Generation #90000: fitness = 5.08407, best fit so far = 4.86981.
Generation #100000: fitness = 5.09296, best fit so far = 4.86981.
Finished Genetic Algorithm, with best fitness = 4.86981.
 Info: ===== Cycle number 34 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.32412, best fit so far = 4.95084.
Generation #20000: fitness = 5.58939, best fit so far = 4.95084.
Generation #30000: fitness = 5.41014, best fit so far = 4.95084.
Generation #40000: fitness = 5.536, best fit so far = 4.95084.
Generation #50000: fitness = 4.90302, best fit so far = 4.77376.
Generation #60000: fitness = 4.90302, best fit so far = 4.77376.
Generation #70000: fitness = 5.15766, best fit so far = 4.77376.
Generation #80000: fitness = 5.60939, best fit so far = 4.77376.
Generation #90000: fitness = 5.44968, best fit so far = 4.77376.
Generation #100000: fitness = 5.40272, best fit so far = 4.77376.
Finished Genetic Algorithm, with best fitness = 4.77376.
 Info: ===== Cycle number 35 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.46237, best fit so far = 4.9075.
Generation \#20000: fitness = 5.536, best fit so far = 4.9075.
Generation #30000: fitness = 5.41014, best fit so far = 4.9075.
Generation #40000: fitness = 5.41014, best fit so far = 4.9075.
Generation #50000: fitness = 4.92485, best fit so far = 4.9075.
Generation #60000: fitness = 4.92485, best fit so far = 4.8183.
Generation #70000: fitness = 4.77376, best fit so far = 4.77376.
Generation #80000: fitness = 5.03772, best fit so far = 4.77376.
Generation #90000: fitness = 5.40717, best fit so far = 4.77376.
Generation #100000: fitness = 5.41014, best fit so far = 4.77376.
Finished Genetic Algorithm, with best fitness = 4.77376.
 Info: ===== Cycle number 36 ====
 @ Main In[19]:11
```

file:///C:/Users/yc225/Desktop/eEOM_demo.html

Generation #10000: fitness = 5.40382, best fit so far = 4.86981. Generation #20000: fitness = 5.54676, best fit so far = 4.86981. Generation #30000: fitness = 4.77376, best fit so far = 4.77376. Generation #40000: fitness = 4.90302, best fit so far = 4.77376. Generation #50000: fitness = 5.29207, best fit so far = 4.77376. Generation #60000: fitness = 5.09696, best fit so far = 4.77376. Generation #70000: fitness = 5.29644, best fit so far = 4.77376. Generation #80000: fitness = 5.47021, best fit so far = 4.77376. Generation #90000: fitness = 5.14111, best fit so far = 4.77376. Generation #100000: fitness = 5.14111, best fit so far = 4.77376. Finished Genetic Algorithm, with best fitness = 4.77376. Info: ===== Cycle number 37 ==== @ Main In[19]:11 Generation #10000: fitness = 5.15766, best fit so far = 5.09469. Generation #20000: fitness = 5.15766, best fit so far = 5.09469. Generation #30000: fitness = 5.29207, best fit so far = 5.09469. Generation #40000: fitness = 5.29207, best fit so far = 5.09469. Generation #50000: fitness = 5.29207, best fit so far = 5.09469. Generation #60000: fitness = 5.15766, best fit so far = 5.09469. Generation #70000: fitness = 5.15766, best fit so far = 5.09469. Generation #80000: fitness = 5.15766, best fit so far = 5.09469. Generation #90000: fitness = 5.15766, best fit so far = 5.09469. Generation #100000: fitness = 5.15766, best fit so far = 5.09469. Finished Genetic Algorithm, with best fitness = 5.09469. ┌ Info: ===== Cycle number 38 ==== @ Main In[19]:11 Generation #10000: fitness = 5.08407, best fit so far = 5.07244. Generation #20000: fitness = 5.08407, best fit so far = 4.77376. Generation #30000: fitness = 5.18515, best fit so far = 4.77376. Generation #40000: fitness = 5.24358, best fit so far = 4.77376. Generation #50000: fitness = 5.37617, best fit so far = 4.77376. Generation #60000: fitness = 4.98403, best fit so far = 4.77376. Generation #70000: fitness = 5.01049, best fit so far = 4.77376. Generation #80000: fitness = 5.1575, best fit so far = 4.77376. Generation #90000: fitness = 5.38052, best fit so far = 4.77376. Generation #100000: fitness = 4.94775, best fit so far = 4.77376. Finished Genetic Algorithm, with best fitness = 4.77376. Generation #10000: fitness = 5.08407, best fit so far = 4.98403. Info: ===== Cycle number 39 ==== @ Main In[19]:11 Generation #20000: fitness = 5.08407, best fit so far = 4.89904. Generation #30000: fitness = 5.08407, best fit so far = 4.89904. Generation #40000: fitness = 5.08407, best fit so far = 4.89904. Generation #50000: fitness = 5.08407, best fit so far = 4.89904. Generation #60000: fitness = 5.3504, best fit so far = 4.89904. Generation #70000: fitness = 5.08407, best fit so far = 4.89904. Generation #80000: fitness = 5.08407, best fit so far = 4.86981. Generation #90000: fitness = 5.08407, best fit so far = 4.86981. Generation #100000: fitness = 5.08407, best fit so far = 4.86981. Finished Genetic Algorithm, with best fitness = 4.86981.

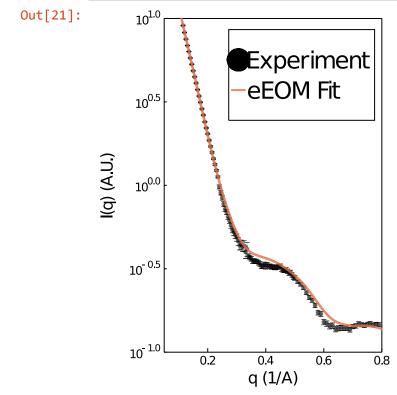
```
Info: ==== Cycle number 40 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.41014, best fit so far = 4.77376.
Generation #20000: fitness = 5.41014, best fit so far = 4.77376.
Generation #30000: fitness = 4.98403, best fit so far = 4.77376.
Generation \#40000: fitness = 5.3552, best fit so far = 4.77376.
Generation #50000: fitness = 5.08407, best fit so far = 4.77376.
Generation #60000: fitness = 5.08407, best fit so far = 4.77376.
Generation #70000: fitness = 5.08407, best fit so far = 4.77376.
Generation #80000: fitness = 5.08407, best fit so far = 4.77376.
Generation #90000: fitness = 5.05707, best fit so far = 4.77376.
Generation #100000: fitness = 5.08407, best fit so far = 4.77376.
Finished Genetic Algorithm, with best fitness = 4.77376.
 Info: ===== Cycle number 41 ====
 @ Main In[19]:11
Generation #10000: fitness = 4.94775, best fit so far = 4.92485.
Generation #20000: fitness = 5.08407, best fit so far = 4.86981.
Generation #30000: fitness = 5.08407, best fit so far = 4.86981.
Generation #40000: fitness = 5.08407, best fit so far = 4.86981.
Generation #50000: fitness = 5.08407, best fit so far = 4.86981.
Generation #60000: fitness = 5.09296, best fit so far = 4.86981.
Generation #70000: fitness = 5.08407, best fit so far = 4.86981.
Generation #80000: fitness = 5.44069, best fit so far = 4.86981.
Generation #90000: fitness = 4.98403, best fit so far = 4.77376.
Generation #100000: fitness = 5.08407, best fit so far = 4.77376.
Finished Genetic Algorithm, with best fitness = 4.77376.
 Info: ===== Cycle number 42 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.15766, best fit so far = 5.09696.
Generation #20000: fitness = 5.29207, best fit so far = 5.09696.
Generation #30000: fitness = 5.14111, best fit so far = 5.09696.
Generation #40000: fitness = 5.15766, best fit so far = 5.09696.
Generation #50000: fitness = 5.15766, best fit so far = 5.09696.
Generation #60000: fitness = 5.12645, best fit so far = 5.09696.
Generation #70000: fitness = 4.90302, best fit so far = 4.85306.
Generation #80000: fitness = 5.51895, best fit so far = 4.85306.
Generation #90000: fitness = 5.08407, best fit so far = 4.85306.
Generation #100000: fitness = 5.08407, best fit so far = 4.85306.
Finished Genetic Algorithm, with best fitness = 4.85306.
 Info: ===== Cycle number 43 ====
 @ Main In[19]:11
```

```
Generation #10000: fitness = 5.08407, best fit so far = 4.99634.
Generation #20000: fitness = 4.98403, best fit so far = 4.77376.
Generation #30000: fitness = 5.08407, best fit so far = 4.77376.
Generation #40000: fitness = 5.08407, best fit so far = 4.77376.
Generation #50000: fitness = 5.08407, best fit so far = 4.77376.
Generation #60000: fitness = 5.08407, best fit so far = 4.77376.
Generation #70000: fitness = 5.08407, best fit so far = 4.77376.
Generation #80000: fitness = 5.08407, best fit so far = 4.77376.
Generation #90000: fitness = 5.08407, best fit so far = 4.77376.
Generation #100000: fitness = 5.08407, best fit so far = 4.77376.
Finished Genetic Algorithm, with best fitness = 4.77376.
 Info: ===== Cycle number 44 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.14111, best fit so far = 5.1127.
Generation #20000: fitness = 5.14111, best fit so far = 5.09469.
Generation #30000: fitness = 4.90302, best fit so far = 4.85306.
Generation #40000: fitness = 4.85306, best fit so far = 4.85306.
Generation #50000: fitness = 5.45689, best fit so far = 4.85306.
Generation #60000: fitness = 5.15766, best fit so far = 4.85306.
Generation #70000: fitness = 5.15766, best fit so far = 4.85306.
Generation #80000: fitness = 5.15766, best fit so far = 4.85306.
Generation #90000: fitness = 5.14111, best fit so far = 4.85306.
Generation #100000: fitness = 5.15766, best fit so far = 4.85306.
Finished Genetic Algorithm, with best fitness = 4.85306.
Generation #10000: fitness = 5.19702, best fit so far = 4.89904.
r Info: ===== Cycle number 45 ====
 @ Main In[19]:11
Generation #20000: fitness = 5.08407, best fit so far = 4.89904.
Generation #30000: fitness = 5.08407, best fit so far = 4.89904.
Generation #40000: fitness = 5.08407, best fit so far = 4.86981.
Generation #50000: fitness = 5.08407, best fit so far = 4.86981.
Generation #60000: fitness = 5.08407, best fit so far = 4.86981.
Generation #70000: fitness = 4.94775, best fit so far = 4.86981.
Generation #80000: fitness = 5.08407, best fit so far = 4.86981.
Generation #90000: fitness = 5.08407, best fit so far = 4.86981.
Generation #100000: fitness = 4.94775, best fit so far = 4.77376.
Finished Genetic Algorithm, with best fitness = 4.77376.
 Info: ===== Cycle number 46 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.29207, best fit so far = 5.1127.
Generation #20000: fitness = 5.11789, best fit so far = 4.95215.
Generation #30000: fitness = 5.11789, best fit so far = 4.95215.
Generation #40000: fitness = 5.14111, best fit so far = 4.95215.
Generation #50000: fitness = 5.14111, best fit so far = 4.95215.
Generation #60000: fitness = 5.14111, best fit so far = 4.95215.
Generation #70000: fitness = 5.14111, best fit so far = 4.95215.
Generation #80000: fitness = 5.14111, best fit so far = 4.95215.
Generation #90000: fitness = 5.14111, best fit so far = 4.95215.
Generation #100000: fitness = 5.14111, best fit so far = 4.95215.
Finished Genetic Algorithm, with best fitness = 4.95215.
```

```
Info: ===== Cycle number 47 ====
 @ Main In[19]:11
Generation #10000: fitness = 5.09624, best fit so far = 5.09624.
Generation #20000: fitness = 5.74772, best fit so far = 5.00213.
Generation #30000: fitness = 5.14111, best fit so far = 5.00213.
Generation #40000: fitness = 5.29207, best fit so far = 5.00213.
Generation #50000: fitness = 5.15766, best fit so far = 5.00213.
Generation #60000: fitness = 5.34383, best fit so far = 5.00213.
Generation #70000: fitness = 5.14111, best fit so far = 5.00213.
Generation #80000: fitness = 5.30369, best fit so far = 5.00213.
Generation #90000: fitness = 5.15766, best fit so far = 5.00213.
Generation #100000: fitness = 5.38704, best fit so far = 5.00213.
Finished Genetic Algorithm, with best fitness = 5.00213.
 Info: ===== Cycle number 48 ====
 @ Main In[19]:11
Generation #10000: fitness = 4.98403, best fit so far = 4.92485.
Generation #20000: fitness = 5.08407, best fit so far = 4.89904.
Generation #30000: fitness = 5.08407, best fit so far = 4.89904.
Generation #40000: fitness = 5.08407, best fit so far = 4.89904.
Generation #50000: fitness = 5.08407, best fit so far = 4.89904.
Generation #60000: fitness = 5.08407, best fit so far = 4.89904.
Generation #70000: fitness = 5.08407, best fit so far = 4.86981.
Generation #80000: fitness = 5.3504, best fit so far = 4.86981.
Generation #90000: fitness = 4.98403, best fit so far = 4.86981.
Generation #100000: fitness = 5.08407, best fit so far = 4.77376.
Finished Genetic Algorithm, with best fitness = 4.77376.
 Info: ===== Cycle number 49 ====
 @ Main In[19]:11
Generation #10000: fitness = 4.90302, best fit so far = 4.77376.
Generation #20000: fitness = 4.90302, best fit so far = 4.77376.
Generation #30000: fitness = 5.11789, best fit so far = 4.77376.
Generation #40000: fitness = 5.45022, best fit so far = 4.77376.
Generation #50000: fitness = 5.37217, best fit so far = 4.77376.
Generation #60000: fitness = 5.32412, best fit so far = 4.77376.
Generation #70000: fitness = 5.28796, best fit so far = 4.77376.
Generation #80000: fitness = 5.21312, best fit so far = 4.77376.
Generation #90000: fitness = 4.90302, best fit so far = 4.77376.
Generation #100000: fitness = 4.90302, best fit so far = 4.77376.
Finished Genetic Algorithm, with best fitness = 4.77376.
 Info: ===== Cycle number 50 ====
 @ Main In[19]:11
```

```
Generation #10000: fitness = 5.3504, best fit so far = 4.9828. Generation #20000: fitness = 5.08407, best fit so far = 4.9828. Generation #30000: fitness = 5.08407, best fit so far = 4.89904. Generation #40000: fitness = 5.3504, best fit so far = 4.89904. Generation #50000: fitness = 5.3504, best fit so far = 4.89904. Generation #60000: fitness = 4.98403, best fit so far = 4.89904. Generation #70000: fitness = 5.09296, best fit so far = 4.86981. Generation #80000: fitness = 5.08407, best fit so far = 4.86981. Generation #90000: fitness = 4.98403, best fit so far = 4.77376. Generation #100000: fitness = 5.08407, best fit so far = 4.77376. Finished Genetic Algorithm, with best fitness = 4.77376.
```

In [21]: # Plot the eEOM results p = scatter(data2[:,1], data2[:,2], yerror=data2[:,3], yscale=:log10, markersi ze=2.5, c=:black, markeralpha=0.6, linealpha=0.25, lab="Experiment", size=(300 ,450), legendfont=font(16), titlefont=font(20)); plot!(q, mean(pool2[:, survivors2[:, findall(fitness2 .== minimum(fitness2))[1]]], dims=2), lw=2.5, linealpha=0.8, lab="eEOM Fit") plot!(size=(300, 400), grid=false, legend=true, framestyle=:box); xlims!(0.05, 0.8); ylims!(0.1, 10) xlabel!("q (1/A)"); ylabel!("I(q) (A.U.)")



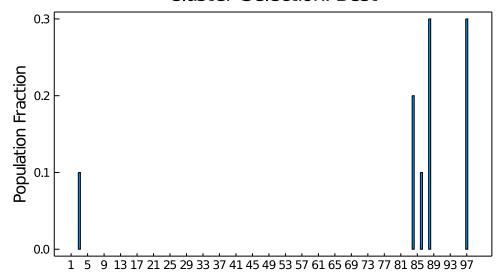
The mismatch might be due to the following

- 1. High S/N
- 2. Missing the correct structures in the pool
- 3. ensize too small given bimodal or multi-state molecules
- 4. pool size too small
- 5. Imbalance at low and high q

```
In [23]: # Plot the best ensemble
    best = survivors2[:, findall(fitness2 .== minimum(fitness2))[1]];
    dic = countmap(reshape(best, (length(best), )));
    b = bar(collect(keys(dic)), collect(values(dic)) / length(best), title="Cluste r Selection: Best", xticks=collect(1:4:98), bar_width=0.5);
    plot!(size=(500, 300), grid=false, legend=false, framestyle=:box);
    ylabel!("Population Fraction")
```

Out[23]:

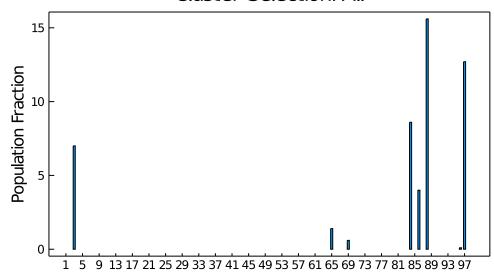
Cluster Selection: Best



```
In [24]: # Plot the all ensemble
    dic = countmap(reshape(survivors2, (length(survivors2), )));
    b = bar(collect(keys(dic)), collect(values(dic)) / length(best), title="Cluste
    r Selection: All", xticks=collect(1:4:98), bar_width=0.5);
    plot!(size=(500, 300), grid=false, legend=false, framestyle=:box);
    ylabel!("Population Fraction")
```

Out[24]:

Cluster Selection: All



The survivors from data1 and data2 are quite consistent, picking #88 and #97 very frequently. The mismatch between fit and exp suggests more care is need for building the structural pool for refinement.

Notes

- 1. The Refine function can be sped up quite a lot using parallelism in julia and should be ready for direct parallelization given its little memory consumption.
- 2. The customized χ^2 is S/N-dependent as well as pool -dependent, further study in preparation.
- 3. The eEOM has been cross-validated using 10-fold CV and different S/N in the same experimental data. Note that the data1 and data2 are the same molecule with different S/N and the pool1 and pool2 are the same with ddifferent scaling parameter. The results are consistent.
- 4. Note that the profile needs to be distinguished apart by a given set of experimental data and error.

References

1. **Chen, YL.** et al., Salt Dependence of A-Form RNA Duplexes: Structures and Implications. *J. Phys. Chem. B* 2019, 123, 46, 9773-9785

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