

## DISTRIBUTIVE INVOLUTIVE RESIDUATED LATTICES UP TO CARDINALITY 8

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There are  $1+1+2+9+8+43+49+282 = 395$  distributive involutive residuated lattices with  $\leq 8$  elements. In the list below, each algebra is named  $D_{m,i}^n$  where  $n$  is the cardinality and  $m$  enumerates nonisomorphic involutive lattices of size  $n$ , in order of decreasing height. The index  $i$  enumerates nonisomorphic algebras with the same involutive lattice reduct. The linear negations  $\sim, -$  are determined by the element labeled 0 (bottom for integral algebras). Algebras with more central elements (round circles) are listed earlier, hence commutative algebras precede noncommutative ones. Finally, algebras are listed in decreasing order of number of idempotents (black nodes).

The monoid operation is indicated by labels. If a nonobvious product  $xy$  is not listed, then it can be deduced from the given information: either it follows from idempotence ( $x^2 = x$ ) indicated by a black node or from commutativity or there are products  $uv = wz$  such that  $u \leq x \leq w$  and  $v \leq y \leq z$  (possibly  $uv = \perp\perp$  or  $wz = \top\top$ ).

If you have comments or notice any issues in this list, please email [jipsen.AT.chapman.edu](mailto:jipsen.AT.chapman.edu).

- = central idempotent  
 ○ = central nonidempotent  
 ■ = noncentral idempotent  
 □ = noncentral nonidempotent







































