```
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
```

1 K-Means Clustering

Load Data

No missing Values

df.describe()

In [4]:

```
df = pd.read_csv('/Users/chenjiqing/Public/2022_Spring_term/QBS108 Applied ML/2022 file/Homework 2/tcga_pancancer/pancancer.csv')
          df = df.drop('Unnamed: 0',axis=1)
          df
                                               2
                                                                                                          7
Out[2]:
                       0
                                                           3
                                                                       4
                                                                                  5
                                                                                              6
                                                                                                                     8
                                                                                                                                 9
                                                                                                                                            10
                                                                                                                                                       11
                                                                                                                                                                   12
                                                                                                                                                                              13
                                                                                                                                                                                          14
              -25.875320
                           56.783945
                                      -58.522554
                                                  -23.657779
                                                               59.226184
                                                                          32.978484
                                                                                      -55.835789
                                                                                                   3.992981
                                                                                                             -16.705564
                                                                                                                         -14.854115
                                                                                                                                    -16.739289
                                                                                                                                                -12.236637
                                                                                                                                                             0.631551
                                                                                                                                                                        -0.895200
                                                                                                                                                                                    31.014503
            1 -78.976524
                           -62.312761
                                       33.852422
                                                   -2.165579
                                                               -5.288384
                                                                           0.446068
                                                                                      24.361695
                                                                                                 -44.745726
                                                                                                              17.395310
                                                                                                                         -22.758601
                                                                                                                                     13.726631
                                                                                                                                                 11.176496
                                                                                                                                                             -6.800069
                                                                                                                                                                         9.362851
                                                                                                                                                                                    -7.950115
                87.151357
                          -23.404469
                                       -10.054268
                                                   63.831495
                                                                -8.287112
                                                                          -42.402161
                                                                                      36.263516
                                                                                                 -54.548902
                                                                                                              33.558731
                                                                                                                          2.175367
                                                                                                                                    -26.291564
                                                                                                                                                -12.975848
                                                                                                                                                             24.410122
                                                                                                                                                                      -28.263414
                                                                                                                                                                                   -17.609067
               -43.224891
                           -24.016296
                                        -4.744443
                                                  -66.180500
                                                               75.203354
                                                                          -46.929467
                                                                                       37.587578
                                                                                                  -20.590401
                                                                                                               8.761443
                                                                                                                         -20.297368
                                                                                                                                      4.353383
                                                                                                                                                 -2.354844
                                                                                                                                                             5.791677
                                                                                                                                                                         1.503404
                                                                                                                                                                                    -1.664383
               -63.589175
                           -66.331180
                                        6.376695
                                                   25.804671
                                                              -35.920993
                                                                          -20.097241
                                                                                       4.684812
                                                                                                   -1.233395
                                                                                                             -26.762385
                                                                                                                         18.346569
                                                                                                                                     11.932363
                                                                                                                                                  0.081588
                                                                                                                                                            -3.752243
                                                                                                                                                                         4.445100
                                                                                                                                                                                    -0.940169
                -77.968110
                           -64.215899
                                       53.033778
                                                   16.772297
                                                                7.374632
                                                                           51.174647
                                                                                     -22.336068
                                                                                                   -17.173816
                                                                                                             -16.990365
                                                                                                                          9.496480
                                                                                                                                     19.249984
                                                                                                                                                -17.164237
                                                                                                                                                             9.619327
                                                                                                                                                                       -10.789798
                                                                                                                                                                                     8.587151
          660
          661
                 1.411024
                           33.721905
                                       -97.514669
                                                  -35.977829
                                                             -32.405695
                                                                          54.035778
                                                                                      27.624459
                                                                                                    1.633711
                                                                                                             -30.978002
                                                                                                                        -22.327608
                                                                                                                                     15.138285
                                                                                                                                               -20.205383
                                                                                                                                                             -6.395287
                                                                                                                                                                         5.546136
                                                                                                                                                                                    2.314934
                -69.761387
                           -80.963905
                                        40.077150
                                                    7.640976
                                                              -18.890106
                                                                           18.978991
                                                                                       -2.254887
                                                                                                  -34.397698
                                                                                                               2.597095
                                                                                                                          -6.976562
                                                                                                                                    -11.659815
                                                                                                                                                 -6.662376
                                                                                                                                                             9.278010
                                                                                                                                                                         -4.117283
                                                                                                                                                                                   -30.055490
          663
                -24.481133
                            61.988138
                                      -65.444488
                                                   34.473801
                                                                -6.558216
                                                                          54.685834
                                                                                      42.522086
                                                                                                   0.694724
                                                                                                              43.626111
                                                                                                                         22.321826
                                                                                                                                    -20.691297
                                                                                                                                                44.923379
                                                                                                                                                            -14.805007
                                                                                                                                                                       -20.591455
                                                                                                                                                                                   -25.827407
         664
                 5.547498
                            47.154601 -49.546932
                                                    1.701638
                                                             -56.533622
                                                                          -96.443116
                                                                                      34.725324
                                                                                                   69.097112 65.273405
                                                                                                                         45.460026 32.333668
                                                                                                                                                -22.421023
                                                                                                                                                             0.659979
                                                                                                                                                                        27.597299
                                                                                                                                                                                    13.250129
        665 rows x 15 columns
          df.info()
         <class 'pandas.core.frame.DataFrame'>
         RangeIndex: 665 entries, 0 to 664
         Data columns (total 15 columns):
              Column Non-Null Count Dtype
          0
              0
                        665 non-null
                                          float64
          1
              1
                        665 non-null
                                          float64
                        665 non-null
                                          float64
          3
              3
                        665 non-null
                                          float64
                        665 non-null
              4
                                          float64
          5
              5
                        665 non-null
                                          float.64
                        665 non-null
                                          float64
              7
                        665 non-null
                                          float64
          8
              8
                        665 non-null
                                          float64
          9
              9
                        665 non-null
                                          float.64
          10
              10
                        665 non-null
                                          float64
          11
              11
                        665 non-null
                                          float64
          12
              12
                        665 non-null
                                          float64
          13
              13
                        665 non-null
                                          float.64
                        665 non-null
          14
              14
                                          float64
         dtypes: float64(15)
         memory usage: 78.1 KB
```

file:///Users/chenjiqing/Public/2022_Spring_term/QBS108 Applied ML/2022 file/Homework 2/F0034WQ_code.html

Out[4]:		0	1	2	3	4	5	6	7	8	9	10	11	12
	count	6.650000e+02												
	mean	5.128730e-16	2.564365e-16	6.838306e-16	-7.265700e-16	-8.547883e-17	-5.128730e-16	2.564365e-16	-1.709577e-16	2.136971e-16	2.564365e-16	8.547883e-16	-8.547883e-17	3.846547e-16
	std	8.126705e+01	6.536298e+01	5.221270e+01	3.631874e+01	3.486074e+01	3.342800e+01	2.608269e+01	2.340081e+01	2.243101e+01	1.965236e+01	1.914324e+01	1.779294e+01	1.708988e+01
	min	-1.018639e+02	-9.465788e+01	-1.238769e+02	-1.209602e+02	-7.862494e+01	-9.644312e+01	-8.113492e+01	-7.474574e+01	-5.490130e+01	-5.870098e+01	-7.391167e+01	-5.091354e+01	-5.368153e+01
	25%	-5.585776e+01	-5.007898e+01	-2.176080e+01	-2.296131e+01	-2.246344e+01	-2.361122e+01	-1.600493e+01	-1.637985e+01	-1.411962e+01	-1.336469e+01	-1.203067e+01	-1.022459e+01	-1.027628e+01
	50%	-3.121861e+01	-1.626691e+01	9.400684e+00	-6.231582e+00	-3.753839e+00	1.149227e+00	-1.129484e+00	4.821054e-01	-6.971027e-01	-3.945739e-01	-1.057407e+00	-1.360354e-01	-1.799235e+00
	75%	1.828140e+00	3.597135e+01	3.356166e+01	1.716525e+01	1.390316e+01	2.234912e+01	1.621502e+01	1.574662e+01	1.330756e+01	1.237379e+01	1.109708e+01	8.011535e+00	8.542092e+00
	max	1.799845e+02	1.977116e+02	1.300737e+02	1.657368e+02	1.253445e+02	9.710720e+01	1.063313e+02	8.092908e+01	9.623726e+01	8.809292e+01	8.502497e+01	5.819931e+01	8.065588e+01

1-1 a. Choose a suitable type of plot and visualize the first two features of the data.

```
In [5]: # load module import seaborn as sns
```

First feature

```
In [6]: sns.distplot(df['0'], hist = True, hist_kws = {"edgecolor":"black"})
    plt.title("Histogram of First feature")
    plt.xlabel("First Feature")
```

/Users/chenjiqing/anaconda3/envs/Class/lib/python3.7/site-packages/seaborn/distributions.py:2557: FutureWarning: `distplot` is a deprecated function and will be removed in a future version. Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histogram s).

warnings.warn(msg, FutureWarning)
Out[6]: Text(0.5, 0, 'First Feature')

Histogram of First feature

0.012

0.010

0.008

0.004

0.002

0.000

First Feature

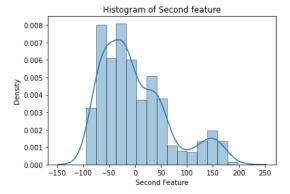
Second feature

```
In [7]: sns.distplot(df['1'], hist = True, hist_kws = {"edgecolor":"black"})
plt.title("Histogram of Second feature")
plt.xlabel("Second Feature")
```

/Users/chenjiqing/anaconda3/envs/Class/lib/python3.7/site-packages/seaborn/distributions.py:2557: FutureWarning: `distplot` is a deprecated function and will be removed in a future version. Please adapt your code to use either `displot` (a figure-level function with similar flexibility) or `histplot` (an axes-level function for histogram s).

warnings.warn(msg, FutureWarning)

Out[7]: Text(0.5, 0, 'Second Feature')



1-1 b. From your plot, how many clusters, k, do you recognize in the dataset?

• According to Histogram plot, I think 2 clusters in the dataset.

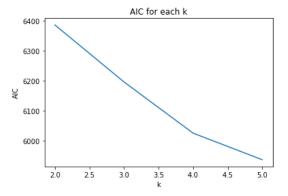
1-2 a. Using the k-Means algorithm, implement a clustering model. Train the clustering model using all 15 features from the data.

```
In [8]: from sklearn.cluster import KMeans

k_cluster = []
AICs = []
BICs = []
for k in range(2,6):
    kmeans = KMeans(n_clusters=k, random_state=3).fit(df)
    AIC = df.shape[0]*np.log(kmeans.inertia_/df.shape[0]) + 2*k
    BIC = df.shape[0]*np.log(kmeans.inertia_/df.shape[0]) + k*np.log(df.shape[0])
    k_cluster.append(k)
    AICs.append(AIC)
    BICs.append(BIC)
```

Plot AIC for each value of k.

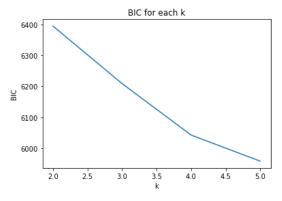
```
In [9]: plt.plot(k_cluster, AICs)
    plt.title("AIC for each k")
    plt.xlabel("k")
    plt.ylabel("AIC")
Out[9]: Text(0, 0.5, 'AIC')
```



Plot BIC for each value of k.

```
In [10]: plt.plot(k_cluster, BICs)
    plt.title("BIC for each k")
    plt.xlabel("k")
    plt.ylabel("BIC")
```

Out[10]: Text(0, 0.5, 'BIC')



1-2 b. Which value of k is optimal?

• According to AIC and BIC plots, the optimal k is 5 (with lowest AIC and BIC values). The result doesn't meet my expectation in 1.1b

2 K-Nearest Neighbor Classification

Load Data

Training Set

```
In [11]: df_train = pd.read_csv('/Users/chenjiqing/Public/2022_Spring_term/QBS108 Applied ML/2022 file/Homework 2/wine/train.csv')
df_train = df_train.assign(good_quality = np.where(df_train['good_quality']==False,0,1)) # Convert target into 1, 0
df_train
```

Out[11]:		fixed acidity	volatile acidity	citric acid	residual sugar	chlorides	free sulfur dioxide	total sulfur dioxide	density	рН	sulphates	alcohol	good_quality
	0	7.6	0.420	0.08	2.70	0.084	15.0	48.0	0.99680	3.21	0.59	10.0	0

	fixed acidity	volatile acidity	citric acid	residual sugar	chlorides	free sulfur dioxide	total sulfur dioxide	density	рН	sulphates	alcohol	good_quality
1	5.7	0.600	0.00	1.40	0.063	11.0	18.0	0.99191	3.45	0.56	12.2	1
2	7.5	0.610	0.26	1.90	0.073	24.0	88.0	0.99612	3.30	0.53	9.8	0
3	8.9	0.480	0.24	2.85	0.094	35.0	106.0	0.99820	3.10	0.53	9.2	0
4	7.0	0.620	0.18	1.50	0.062	7.0	50.0	0.99510	3.08	0.60	9.3	0
1018	7.4	0.635	0.10	2.40	0.080	16.0	33.0	0.99736	3.58	0.69	10.8	1
1019	10.3	0.440	0.50	4.50	0.107	5.0	13.0	0.99800	3.28	0.83	11.5	0
1020	6.6	0.520	0.08	2.40	0.070	13.0	26.0	0.99358	3.40	0.72	12.5	1
1021	5.1	0.510	0.18	2.10	0.042	16.0	101.0	0.99240	3.46	0.87	12.9	1
1022	11.6	0.410	0.54	1.50	0.095	22.0	41.0	0.99735	3.02	0.76	9.9	1

1023 rows × 12 columns

```
In [12]: df_train.info()
```

RangeIndex: 1023 entries, 0 to 1022 Data columns (total 12 columns): # Column Non-Null Count Dtype fixed acidity 1023 non-null float64 1023 non-null volatile acidity float64 citric acid 1023 non-null float64 3 residual sugar 1023 non-null float64 chlorides 1023 non-null float64 5 free sulfur dioxide 1023 non-null float64 total sulfur dioxide 1023 non-null float64 density 1023 non-null float64

1023 non-null

1023 non-null

float64

float64

10 alcohol 1023 non-null float64 11 good_quality 1023 non-null int64 dtypes: float64(11), int64(1)

<class 'pandas.core.frame.DataFrame'>

· No missing values in each feature

Validation Set

рΗ

sulphates

memory usage: 96.0 KB

In [13]: df_val = pd.read_csv('/Users/chenjiqing/Public/2022_Spring_term/QBS108 Applied ML/2022 file/Homework 2/wine/val.csv')
df_val = df_val.assign(good_quality = np.where(df_val['good_quality']==False,0,1)) # Convert target into 1, 0
df_val

Out[13]:		fixed acidity	volatile acidity	citric acid	residual sugar	chlorides	free sulfur dioxide	total sulfur dioxide	density	рН	sulphates	alcohol	good_quality
	0	7.0	0.655	0.16	2.1	0.074	8.0	25.0	0.99606	3.37	0.55	9.7	0
	1	10.4	0.440	0.42	1.5	0.145	34.0	48.0	0.99832	3.38	0.86	9.9	0
	2	5.2	0.480	0.04	1.6	0.054	19.0	106.0	0.99270	3.54	0.62	12.2	1
	3	9.7	0.320	0.54	2.5	0.094	28.0	83.0	0.99840	3.28	0.82	9.6	0
	4	8.1	0.870	0.00	2.2	0.084	10.0	31.0	0.99656	3.25	0.50	9.8	0
	251	8.7	0.690	0.31	3.0	0.086	23.0	81.0	1.00020	3.48	0.74	11.6	1
:	252	5.0	1.020	0.04	1.4	0.045	41.0	85.0	0.99380	3.75	0.48	10.5	0

	fixed acidity	volatile acidity	citric acid	residual sugar	chlorides	free sulfur dioxide	total sulfur dioxide	density	рН	sulphates	alcohol	good_quality
253	9.9	0.590	0.07	3.4	0.102	32.0	71.0	1.00015	3.31	0.71	9.8	0
254	9.1	0.500	0.30	1.9	0.065	8.0	17.0	0.99774	3.32	0.71	10.5	1
255	7.8	0.590	0.33	2.0	0.074	24.0	120.0	0.99680	3.25	0.54	9.4	0

256 rows × 12 columns

```
In [14]: | df_val.info()
```

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 256 entries, 0 to 255
Data columns (total 12 columns):

#	Column	Non-Null Count	Dtype
0	fixed acidity	256 non-null	float64
1	volatile acidity	256 non-null	float64
2	citric acid	256 non-null	float64
3	residual sugar	256 non-null	float64
4	chlorides	256 non-null	float64
5	free sulfur dioxide	256 non-null	float64
6	total sulfur dioxide	256 non-null	float64
7	density	256 non-null	float64
8	рН	256 non-null	float64
9	sulphates	256 non-null	float64
10	alcohol	256 non-null	float64
11	good quality	256 non-null	int64
dtyp	es: float64(11), int64	(1)	
memo	ry usage: 24.1 KB		

• No missing values in each feature

Testing Set

Out[15]:		fixed acidity	volatile acidity	citric acid	residual sugar	chlorides	free sulfur dioxide	total sulfur dioxide	density	рН	sulphates	alcohol	good_quality
	0	10.8	0.470	0.43	2.10	0.171	27.0	66.0	0.99820	3.17	0.76	10.8	1
	1	8.1	0.820	0.00	4.10	0.095	5.0	14.0	0.99854	3.36	0.53	9.6	0
	2	9.1	0.290	0.33	2.05	0.063	13.0	27.0	0.99516	3.26	0.84	11.7	1
	3	10.2	0.645	0.36	1.80	0.053	5.0	14.0	0.99820	3.17	0.42	10.0	1
	4	12.2	0.450	0.49	1.40	0.075	3.0	6.0	0.99690	3.13	0.63	10.4	0
3	15	10.1	0.270	0.54	2.30	0.065	7.0	26.0	0.99531	3.17	0.53	12.5	1
3	16	6.9	0.390	0.24	2.10	0.102	4.0	7.0	0.99462	3.44	0.58	11.4	0
3	17	9.1	0.340	0.42	1.80	0.058	9.0	18.0	0.99392	3.18	0.55	11.4	0
3	18	9.1	0.765	0.04	1.60	0.078	4.0	14.0	0.99800	3.29	0.54	9.7	0
3	19	8.2	0.320	0.42	2.30	0.098	3.0	9.0	0.99506	3.27	0.55	12.3	1

320 rows × 12 columns

In [16]: df_test.info()

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 320 entries, 0 to 319

```
Data columns (total 12 columns):
# Column
               Non-Null Count Dtype
                      _____
--- -----
                   320 non-null float64
0 fixed acidity
1 volatile acidity 320 non-null float64
2 citric acid
                      320 non-null
                                   float64
3 residual sugar
                      320 non-null
                                    float64
   chlorides
                      320 non-null
                                    float64
   free sulfur dioxide 320 non-null float64
   total sulfur dioxide 320 non-null float64
   density
                      320 non-null float64
                      320 non-null float64
   sulphates
                      320 non-null float64
                      320 non-null
                                    float64
10 alcohol
11 good quality
                      320 non-null
                                   int64
dtypes: float64(11), int64(1)
memory usage: 30.1 KB
```

· No missing values in each feature

```
In [17]: # Set Features and Target for each set.
          df train y = df train['good quality'].copy()
          df val y = df val['good quality'].copy()
          df_test_y = df_test['good_quality'].copy()
          df_train = df_train.drop(['good_quality'], axis=1).copy()
          df val = df val.drop(['good quality'], axis=1).copy()
          df test = df test.drop(['good quality'], axis=1).copy()
          print(df train.shape)
          print(df train y.shape)
          print(df val.shape)
          print(df val y.shape)
          print(df test.shape)
          print(df_test_y.shape)
         (1023, 11)
         (1023,)
         (256, 11)
         (256,)
         (320, 11)
         (320,)
In [18]: # Pre-processed data
          from sklearn.preprocessing import StandardScaler
          SS = StandardScaler()
          df train SS = SS.fit transform(df train)
          df val SS = SS.transform(df val)
          df test SS = SS.transform(df test)
```

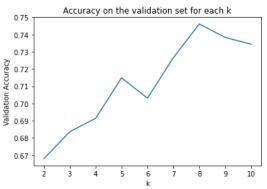
2-1. Train an k-Nearest Neighbors algorithm on the training dataset of your choice of k's

```
In [19]: from sklearn.neighbors import KNeighborsClassifier
k_cluster =[]
accuracy = []
for k in range(2,11):
    knn = KNeighborsClassifier(n_neighbors=k)
    knn = knn.fit(df_train_SS, df_train_y)
    print("k: ", k)
    print("Train Accuracy: ", knn.score(df_train_SS, df_train_y))
    print("Validation Accuracy: ", knn.score(df_val_SS, df_val_y))
    print('-'*20)
    k_cluster.append(k)
    accuracy.append(knn.score(df_val_SS, df_val_y))
k: 2
Train Accuracy: 0.878787878787888
```

```
Validation Accuracy: 0.66796875
-----
k: 3
Train Accuracy: 0.8699902248289345
Validation Accuracy: 0.68359375
_____
k: 4
Train Accuracy: 0.8250244379276638
Validation Accuracy: 0.69140625
_____
k: 5
Train Accuracy: 0.820136852394917
Validation Accuracy: 0.71484375
_____
k: 6
Train Accuracy: 0.8005865102639296
Validation Accuracy: 0.703125
_____
k: 7
Train Accuracy: 0.7947214076246334
Validation Accuracy: 0.7265625
k: 8
Train Accuracy: 0.7839687194525904
Validation Accuracy: 0.74609375
k: 9
Train Accuracy: 0.7859237536656891
Validation Accuracy: 0.73828125
k: 10
Train Accuracy: 0.7771260997067448
Validation Accuracy: 0.734375
```

2-2. Report the classification accuracy of this model on the validation set for different values for k. Plot these accuracies against k and report the optimal value for k.

```
In [20]: plt.plot(k_cluster, accuracy)
    plt.title("Accuracy on the validation set for each k")
    plt.xlabel("k")
    plt.ylabel("Validation Accuracy")
Out[20]: Text(0, 0.5, 'Validation Accuracy')
```



• According to the plot, the optimal value for k is 8.

2-3. Report the classification accuracy of this model on the data in test.csv using the optimal value of k that you found in 2.2.

```
In [21]: knn = KNeighborsClassifier(n_neighbors=8)
knn = knn.fit(df_train_SS, df_train_y)
print("k: ", 8)
print("Train Accuracy: ", knn.score(df_train_SS, df_train_y))
print("Testing Accuracy: ", knn.score(df_test_SS, df_test_y))

k: 8
Train Accuracy: 0.7839687194525904
Testing Accuracy: 0.71875
```

3 Decision Tree Classification

Load Data

Training Set

t[22]:		Survived	Pclass	Sex	Age	SibSp	Parch	Fare	Cabin	Embarked	Title
	0	1	1	female	24	0	0	69.3000	B35	С	Mrs
	1	0	3	female	3	3	1	21.0750	NaN	S	Miss
	2	1	3	female	16	0	0	7.7333	NaN	Q	Miss
	3	1	3	male	32	0	0	56.4958	NaN	S	Mr
	4	0	3	male	22	0	0	7.1250	NaN	S	Mr
	493	0	2	male	52	0	0	13.5000	NaN	S	Mr
	494	0	3	male	33	1	1	20.5250	NaN	S	Mr
	495	1	2	male	38	0	0	13.0000	NaN	S	Mr
	496	0	3	male	38	8	2	69.5500	NaN	S	Mr
	497	1	1	female	56	0	1	83.1583	C50	С	Mrs

498 rows \times 10 columns

```
In [23]: df_train.info()

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 498 entries, 0 to 497
Data columns (total 10 columns):
```

```
# Column Non-Null Count Dtype
           _____
0 Survived 498 non-null int64
1 Pclass 498 non-null int64
2 Sex
            498 non-null
3 Age
            498 non-null int64
4
   SibSp
            498 non-null
                         int64
   Parch
            498 non-null
                         int64
   Fare
            498 non-null
                         float64
   Cabin
            113 non-null
                         object
8 Embarked 497 non-null
                         object
            498 non-null
9 Title
                         object
dtypes: float64(1), int64(5), object(4)
memory usage: 39.0+ KB
```

Cabin and Embarked contain missing values

```
In [24]: print("Sex:")
```

```
print(df_train.Sex.value_counts(),"\n")
print("Cabin:")
print(df_train.Cabin.value_counts(),"\n")
print("Embarked:")
print(df train.Embarked.value counts(),"\n")
print("Title:")
print(df_train.Title.value_counts(),"\n")
male
          333
         165
female
Name: Sex, dtype: int64
Cabin:
C23 C25 C27
E101
              3
D35
C22 C26
В4
C78
D30
C87
Name: Cabin, Length: 91, dtype: int64
Embarked:
S
    373
      85
С
      39
Name: Embarked, dtype: int64
Title:
          295
Mr
Miss
          102
          61
          27
Master
Rare
          13
Name: Title, dtype: int64
```

Validation Set

In [25]: df_val = pd.read_csv('/Users/chenjiqing/Public/2022_Spring_term/QBS108 Applied ML/2022 file/Homework 2/titanic/val.csv')
df_val

Out[25]:		Survived	Pclass	Sex	Age	SibSp	Parch	Fare	Cabin	Embarked	Title
	0	1	3	female	24	1	0	15.8500	NaN	S	Mrs
	1	1	2	female	24	0	0	13.0000	F33	S	Miss
	2	0	3	male	40	1	1	15.5000	NaN	Q	Mr
	3	1	3	male	22	2	0	23.2500	NaN	Q	Mr
	4	1	2	female	3	1	2	41.5792	NaN	С	Miss
		•••									
1	20	1	2	female	31	1	1	26.2500	NaN	S	Mrs
,	121	1	3	male	19	0	0	7.7500	NaN	Q	Mr
1	122	1	1	female	43	0	1	211.3375	В3	S	Mrs
1	123	0	2	male	52	0	0	13.0000	NaN	S	Mr
1	24	1	1	female	35	1	0	53.1000	C123	S	Mrs

125 rows × 10 columns

```
In [26]: df_val.info()
        <class 'pandas.core.frame.DataFrame'>
        RangeIndex: 125 entries, 0 to 124
        Data columns (total 10 columns):
         # Column Non-Null Count Dtype
                      -----
         0
            Survived 125 non-null
            Pclass 125 non-null
                                     int64
                      125 non-null
                                     object
         2
            Sex
                      125 non-null int64
         3
            Age
            SibSp 125 non-null int64
            Parch
                    125 non-null
                      125 non-null float64
         6
           Fare
                      26 non-null
            Cabin
                                     object
         8 Embarked 125 non-null
                                     object
            Title
                      125 non-null
                                     object
        dtypes: float64(1), int64(5), object(4)
        memory usage: 9.9+ KB
         • Cabin contains missing values
In [27]: print("Sex:")
         print(df_val.Sex.value_counts(),"\n")
         print("Cabin:")
         print(df_val.Cabin.value_counts(),"\n")
         print("Embarked:")
         print(df_val.Embarked.value_counts(),"\n")
         print("Title:")
         print(df_val.Title.value_counts(),"\n")
        Sex:
        male
                 77
        female
        Name: Sex, dtype: int64
        Cabin:
        C65
        C83
        D46
        D37
        B101
        B71
        B51 B53 B55
        E121
        F33
        C2
        F38
        E33
        B18
        C124
        D9
        D26
        C125
        C123
        C68
        A19
        E58
        D49
        A24
        Name: Cabin, dtype: int64
        Embarked:
        S
            84
            25
            16
        Name: Embarked, dtype: int64
        Title:
```

```
Mr 73
Miss 26
Mrs 22
Master 4
Name: Title, dtype: int64
```

Testing Set

```
In [28]: df_test = pd.read_csv('/Users/chenjiqing/Public/2022_Spring_term/QBS108 Applied ML/2022 file/Homework 2/titanic/test.csv')
    df_test
```

Out[28]:		Pclass	Sex	Age	SibSp	Parch	Fare	Cabin	Embarked	Title
	0	3	male	22	1	1	15.2458	NaN	С	Master
	1	2	male	31	0	0	10.5000	NaN	S	Mr
	2	3	male	20	0	0	7.9250	NaN	S	Mr
	3	2	female	6	0	1	33.0000	NaN	S	Miss
	4	3	female	14	1	0	11.2417	NaN	С	Miss
	263	3	male	27	0	0	8.6625	NaN	S	Mr
	264	1	male	27	0	0	0.0000	NaN	S	Mr
	265	1	male	65	0	0	26.5500	E38	S	Mr
	266	3	male	17	0	0	8.6625	NaN	S	Mr
	267	1	male	28	0	0	26.5500	C52	S	Mr

268 rows × 9 columns

```
In [29]: df_test.info()
```

female

101

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 268 entries, 0 to 267
Data columns (total 9 columns):
# Column Non-Null Count Dtype
0 Pclass 268 non-null int64
             268 non-null
1
    Sex
                           object
2
    Age
             268 non-null
                           int64
    SibSp
             268 non-null
                           int64
4
    Parch
             268 non-null
                           int64
5 Fare
             268 non-null float64
6 Cabin
             65 non-null
                           object
7 Embarked 267 non-null
                           object
8 Title
             268 non-null
                           object
dtypes: float64(1), int64(4), object(4)
memory usage: 19.0+ KB
```

• Cabin and Embarked contain missing values

```
In [30]: print("Sex:")
    print(df_test.Sex.value_counts(),"\n")
    print("Cabin:")
    print(df_test.Cabin.value_counts(),"\n")
    print("Embarked:")
    print(df_test.Embarked.value_counts(),"\n")
    print("Title:")
    print(df_test.Title.value_counts(),"\n")
Sex:
male 167
```

Name: Sex, dtype: int64 Cabin: E25 2 B58 B60 D B57 B59 B63 B66 C126 B96 B98 C52 C92 B49 E34 C82 1 C148 1 C110 D17 C104 C123 D11 C86 A31 Α7 E68 B69 D21 D19 D10 D12 B28 E77 Α6 E49 E36 D20 В39 C78 C45 B30 F33 E63 G6 B86 C22 C26 F2 E38 A20 B38 D7 D28 D47 D36 D15 C106 C95 C124 A5 D48 B20 D50 1 B78 C93 Name: Cabin, dtype: int64 Embarked: 187 58 С Name: Embarked, dtype: int64 Title: Mr 149 Miss 57

file:///Users/chenjiqing/Public/2022_Spring_term/QBS108 Applied ML/2022 file/Homework 2/F0034WQ_code.html

```
Mrs 43
Rare 10
Master 9
Name: Title, dtype: int64
```

3-1. Preprocess the data

• Set Features and Target for training and validation set.

• For each set, more than 75% values in Cabin are missing values so I will remove this feature for the following analysis.

```
In [32]: df_train2 = df_train.drop('Cabin',axis=1).copy()
    df_val2 = df_val.drop('Cabin',axis=1).copy()
    df_test2 = df_test.drop('Cabin',axis=1).copy()
```

• Because Decision Tree only can handle numbers so I need to convert the strings to numeric. However, in vlidation set, the 'Title' feature doesn't have 'Rare' label. As a result, I need to combine training, testing, and validation set together first, then, convert the strings to numeric.

Out[33]:	Pclass	Sex	Age	SibSp	Parch	Fare	Embarked	Title	set
0	1	female	24	0	0	69.3000	С	Mrs	Train
1	3	female	3	3	1	21.0750	S	Miss	Train
2	3	female	16	0	0	7.7333	Q	Miss	Train
3	3	male	32	0	0	56.4958	S	Mr	Train
4	3	male	22	0	0	7.1250	S	Mr	Train
•••									
263	3	male	27	0	0	8.6625	S	Mr	Test
264	1	male	27	0	0	0.0000	S	Mr	Test
265	1	male	65	0	0	26.5500	S	Mr	Test
266	3	male	17	0	0	8.6625	S	Mr	Test
267	1	male	28	0	0	26.5500	S	Mr	Test

891 rows × 9 columns

```
In [34]: print("Sex:")
         print(df.Sex.value_counts(),"\n")
         print("Embarked:")
         print(df.Embarked.value counts(),"\n")
         print("Title:")
         print(df.Title.value_counts(),"\n")
         Sex:
                   577
         male
                  314
         female
         Name: Sex, dtype: int64
         Embarked:
              644
         S
              168
              77
         Q
         Name: Embarked, dtype: int64
         Title:
                   517
         Mr
         Miss
                   185
                   126
         Mrs
         Master
                    40
         Rare
                    23
         Name: Title, dtype: int64
In [35]: # convert the strings to numeric
          \# Since Embarked has missing values, I will turn missing into new category.
         df = df.assign(Sex = np.where(df['Sex']=='male',0,1),
                        Embarked = np.where(df['Embarked']=='C',0,np.where(df['Embarked']=='S',1,
                                                                          np.where(df['Embarked']=='Q',2,3))),
                        Title = np.where(df['Title']=='Mr',0,np.where(df['Title']=='Miss',1,
                                                                     np.where(df['Title']=='Mrs',2,
                                                                             np.where(df['Title']=='Master',3,4)))).copy()
         df
              Pclass Sex Age SibSp Parch
                                            Fare Embarked Title set
                         24
                                       0 69.3000
                                                             2 Train
                      1
                           3
                                 3
                                       1 21.0750
                                                             1 Train
                          16
                                 0
                                       0 7.7333
                      1
                                                             1 Train
                                       0 56.4958
           3
                         32
                      0
                                 0
                                                             0 Train
           4
                      0
                         22
                                 0
                                       0 7.1250
                                                             0 Train
                                       0 8.6625
         263
                      0
                         27
                                 0
                                                             0 Test
         264
                      0
                         27
                                 0
                                       0.0000
                                                             0 Test
                      0
                         65
                                 0
                                       0 26.5500
                                                             0 Test
         266
                      0
                          17
                                 0
                                       0 8.6625
                                                             0 Test
         267
                  1 0 28
                                 0
                                                            0 Test
                                       0 26.5500
        891 rows × 9 columns
In [36]: # Check
         print("Sex:")
         print(df.Sex.value counts(),"\n")
         print("Embarked:")
         print(df.Embarked.value_counts(),"\n")
```

```
print("Title:")
        print(df.Title.value counts(),"\n")
        Sex:
        0 577
        1 314
        Name: Sex, dtype: int64
        Embarked:
            644
            168
        2
             77
              2
        3
        Name: Embarked, dtype: int64
        Title:
           517
        0
            185
            126
             40
             23
        Name: Title, dtype: int64
In [37]: # Split it back to 3 dataset
        df_train3 = df[df['set'] =='Train'].copy()
        df_train3 = df_train3.drop('set',axis=1)
        print(df train3)
        df val3 = df[df['set'] =='Val'].copy()
        df_val3 = df_val3.drop('set',axis=1)
        print(df_val3)
        df_test3 = df[df['set'] =='Test'].copy()
        df_test3 = df_test3.drop('set',axis=1)
        print(df_test3)
                                           Fare Embarked Title
            Pclass Sex Age SibSp Parch
                1 1 24
                             0
                                      0 69.3000
        1
                 3
                    1
                        3
                               3
                                      1 21.0750
        2
                 3
                    1 16
                               0
                                      0 7.7333
                                                      2
                                                             1
        3
                     0
                        32
                               0
                                      0 56.4958
                                                      1
                                                             0
                     0
                        22
                               0
                                        7.1250
        493
                2
                    0 52
                               0
                                      0 13.5000
                                                      1
        494
                                      1 20.5250
                3
                     0 33
                               1
                                                      1
        495
                2
                     0 38
                                      0 13.0000
        496
                3 0 38
                                      2 69.5500
                                                             0
                               8
                                                      1
        497
                1 1 56
                               0
                                      1 83.1583
        [498 rows x 8 columns]
            Pclass Sex Age SibSp Parch
                                            Fare Embarked Title
                3 1 24
                                      0 15.8500
        0
                             1
                                                       1
                                                              2
        1
                2
                    1 24
                               0
                                      0 13.0000
                                                       1
                                                              1
                                      1 15.5000
                     0 40
                                         23.2500
                3
                    0 22
        3
                             2
                                      0
                                                              0
                    1 3
                               1
                                      2 41.5792
                                                       0
                                                              1
                                             . . .
        120
                        31
                                         26.2500
                     1
                               1
        121
                3
                     0 19
                               0
                                      0
                                         7.7500
                                                              0
        122
                    1 43
                                      1 211.3375
                1
                               0
                                                       1
        123
                        52
                                      0 13.0000
                               0
        124
                                      0 53.1000
        [125 rows x 8 columns]
            Pclass Sex Age SibSp Parch
                                           Fare Embarked Title
                     0
                        22
                               1
                                      1 15.2458
                                                       0
                                      0 10.5000
        1
                 2
                     0
                        31
                               0
                                                             0
                     0
                        20
                                      0 7.9250
        2
                 3
                               0
                                                             0
                                                      1
                                      1 33.0000
        3
                 2
                    1
                        6
                               0
                                                      1
                                                             1
                                      0 11.2417
```

```
    263
    3
    0
    27
    0
    0
    8.6625
    1
    0

    264
    1
    0
    27
    0
    0
    0.0000
    1
    0

    265
    1
    0
    65
    0
    0
    26.5500
    1
    0

    266
    3
    0
    17
    0
    0
    8.6625
    1
    0

    267
    1
    0
    28
    0
    0
    26.5500
    1
    0
```

[268 rows x 8 columns]

3-2. Decision Trees Classification

3-2-a. Initialize a binary decision tree model for the training data.

```
In [38]: from sklearn.tree import DecisionTreeClassifier
              from sklearn import tree
              dt = DecisionTreeClassifier(random state=0)
In [39]: dt2 = dt.fit(df train3, df train y)
              tree.plot tree(dt2)
Text(19.053658536585367, 185.4635294117647, 'K[5] <= 15.464\ngini = 0.46\nsamples = 53\nvalue = [34, 19]'),
Text(15.42439024390244, 172.6729411764706, 'gini = 0.0\nsamples = 4\nvalue = [4, 0]'),
              Text(22.682926829368293, 172.6729411764706, X[5] \le 27.135 = 0.475 = 49 = 49 = [30, 19]')
              Text(10.8878048780, 159.88235294117646, 'X[2] <= 53.5\ngini = 0.408\nsamples = 7\nvalue = [2, 5]'),
              Text(7.258536585365854, 147.09176470588235, 'gini = 0.0\nsamples = 5\nvalue = [0, 5]'),
              Text(14.517073170731708, 147.09176470588235, 'gini = 0.0\nsamples = 2\nvalue = [2, 0]'),
              \texttt{Text}(34.4780487804878, 159.88235294117646, \texttt{'X[3]} <= \texttt{0.5} \texttt{\sc ngini} = \texttt{0.444} \texttt{\sc nsamples} = \texttt{42} \texttt{\sc nsamples} = \texttt{128}, \texttt{14} \texttt{\sc 14})),
              Text(21.775609756097563, 147.09176470588235, 'X[4] \le 1.5 \cdot ngini = 0.34 \cdot nsamples = 23 \cdot nvalue = [18, 5]'),
              Text(18.146341463414636, 134.30117647058825, 'X[5] <= 32.0\ngini = 0.298\nsamples = 22\nvalue = [18, 4]'),
              Text(14.517073170731708, 121.51058823529411, 'X[5] <= 29.85\ngini = 0.48\nsamples = 10\nvalue = [6, 4]'),
              Text(7.258536585365854, 108.72, 'X[5] <= 28.725\ngini = 0.32\nsamples = 5\nvalue = [4, 1]'),
              Text(3.629268292682927, 95.92941176470588, 'gini = 0.0\nsamples = 2\nvalue = [2, 0]'),
              Text(10.887804878048781, 95.92941176470588, 'X[4] <= 0.5 \\ \ngini = 0.444 \\ \nsamples = 3 \\ \nsamples = [2, 1]'), \nsamples = 3 \\ \nsamples = [2, 1]'), \nsamples = [2, 1]'), \nsamples = [3, 1]', \nsamples =
              Text(10.887804878048781, 70.34823529411764, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
              Text(14.517073170731708, 83.13882352941175, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
              Text(21.775609756097563, 108.72, 'X[2] <= 28.0\ngini = 0.48\nsamples = 5\nvalue = [2, 3]'),
              Text(18.146341463414636, 95.92941176470588, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
              Text(25.40487804878049, 95.92941176470588, 'X[5] <= 30.25\ngini = 0.5\nsamples = 4\nvalue = [2, 2]'),
              Text(21.775609756097563, 83.13882352941175, 'X[2] <= 33.0\ngini = 0.444\nsamples = 3\nvalue = [1, 2]'),
              Text(18.146341463414636, 70.34823529411764, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
              Text(25.40487804878049, 70.34823529411764, 'gini = 0.0\nsamples = 2\nvalue = [0, 2]'),
              Text(29.034146341463416, 83.13882352941175, 'gini = 0.0 \nsamples = 1 \nvalue = [1, 0]'),
              Text(21.775609756097563, 121.51058823529411, 'gini = 0.0\nsamples = 12\nvalue = [12, 0]'),
              Text(25.40487804878049, 134.30117647058825, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
              Text(47.18048780487805, 147.09176470588235, 'X[5] <= 100.981\ngini = 0.499\nsamples = 19\nvalue = [10, 9]'),
              Text(43.551219512195125, 134.30117647058825, 'X[5] \le 85.638 \cdot gini = 0.492 \cdot gini = 16 \cdot gini = 17, 9]'
              Text(39.921951219512195, 121.51058823529411, 'X[5] <= 79.425\ngini = 0.497\nsamples = 13\nvalue = [7, 6]'),
              Text(36.29268292682927, 108.72, 'X[6] <= 0.5\ngini = 0.496\nsamples = 11\nvalue = [5, 6]'),
              Text(32.66341463414634, 95.92941176470588, 'gini = 0.0\nsamples = 3\nvalue = [0, 3]'),
              Text(32.66341463414634, 70.34823529411764, 'X[2] <= 23.0\ngini = 0.375\nsamples = 4\nvalue = [1, 3]'),
              Text(29.034146341463416, 57.557647058823534, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
              Text(36.29268292682927, 57.557647058823534, 'gini = 0.0 \nsamples = 3 \nvalue = [0, 3]'),
              Text(39.9219512195, 70.34823529411764, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
              Text(43.551219512195125, 83.13882352941175, 'gini = 0.0\nsamples = 3\nvalue = [3, 0]'),
              Text(43.551219512195125, 108.72, 'gini = 0.0\nsamples = 2\nvalue = [2, 0]'),
              Text(47.18048780487805, 121.51058823529411, 'gini = 0.0 \nsamples = 3 \nvalue = [0, 3]'),
              Text(50.809756097,56098, 134.30117647058825, 'gini = 0.0\nsamples = 3\nvalue = [3, 0]'),
              Text(148.8283536585366, 185.4635294117647, 'X[5] <= 51.698\ngini = 0.217\nsamples = 242\nvalue = [212, 30]'),
              Text(106.21280487804879, 172.6729411764706, 'X[6] <= 0.5\ngini = 0.205\nsamples = 233\nvalue = [206, 27]'),
              Text(68.9560975609756, 159.88235294117646, 'X[2] <= 29.5\ngini = 0.337\nsamples = 28\nvalue = [22, 6]'),
              Text(65.32682926829268, 147.09176470588235, 'X[2] <= 28.5\ngini = 0.469\nsamples = 16\nvalue = [10, 6]'),
              Text(61.69756097560976, 134.30117647058825, 'X[5] <= 10.546\ngini = 0.408\nsamples = 14\nvalue = [10, 4]'),
              Text(54.4390243902439, 121.51058823529411, 'X[2] <= 22.5\ngini = 0.198\nsamples = 9\nvalue = [8, 1]'),
              Text(50.809756097, 108.72, 'X[2] <= 21.0\ngini = 0.375\nsamples = 4\nvalue = [3, 1]'),
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Text(47.18048780487805, 95.92941176470588, 'gini = 0.0\nsamples = 3\nvalue = [3, 0]'),
Text(54.4390243902439, 95.92941176470588, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(58.06829268292683, 108.72, 'gini = 0.0\nsamples = 5\nvalue = [5, 0]'),
Text(68.9560975609756, 121.51058823529411, 'X[2] <= 23.5\ngini = 0.48\nsamples = 5\nvalue = [2, 3]'),
Text(65.32682926829268, 108.72, 'X[4] <= 0.5\ngini = 0.444\nsamples = 3\nvalue = [2, 1]'),
Text(61.69756097560976, 95.92941176470588, 'gini = 0.0\nsamples = 2\nvalue = [2, 0]'),
Text(68.9560975609756, 95.92941176470588, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(72.58536585365854, 108.72, 'gini = 0.0\nsamples = 2\nvalue = [0, 2]'),
Text(68.9560975609756, 134.30117647058825, 'gini = 0.0\nsamples = 2\nvalue = [0, 2]'),
Text(72.58536585365854, 147.09176470588235, 'gini = 0.0\nsamples = 12\nvalue = [12, 0]'),
Text(143.46951219512195, 159.88235294117646, 'X[5] <= 13.25\ngini = 0.184\nsamples = 205\nvalue = [184, 21]'),
Text(117.27073170731708, 147.09176470588235, 'X[2] <= 30.5\ngini = 0.22\nsamples = 159\nvalue = [139, 20]'),
Text(96.62926829268292, 134.30117647058825, 'X[5] <= 8.206\ngini = 0.173\nsamples = 94\nvalue = [85, 9]'),
Text(93.0, 121.51058823529411, 'X[5] <= 8.081\ngini = 0.242\nsamples = 64\nvalue = [55, 9]'),
Text(89.37073170731708, 108.72, 'X[3] <= 0.5\nqini = 0.222\nsamples = 63\nvalue = [55, 8]'),
Text(76.21463414634147, 95.92941176470588, 'X[5] <= 7.825\ngini = 0.206\nsamples = 60\nvalue = [53, 7]'),
Text(60.79024390243902, 83.13882352941175, 'X[2] <= 23.0\ngini = 0.278\nsamples = 30\nvalue = [25, 5]'),
Text(51.71707317073171, 70.34823529411764, 'X[5] <= 7.785\ngini = 0.105\nsamples = 18\nvalue = [17, 1]'),
Text(48.08780487804878, 57.557647058823534, 'gini = 0.0\nsamples = 16\nvalue = [16, 0]'),
Text(55.34634146341464, 57.557647058823534, 'X[2] <= 21.5\ngini = 0.5\nsamples = 2\nvalue = [1, 1]'),
Text(51.71707317073171, 44.767058823529396, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(58.975609756, 44.767058823529396, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
Text(69.86341463414634, 70.34823529411764, 'X[5] <= 3.525\ngini = 0.444\nsamples = 12\nvalue = [8, 4]'),
Text(66.23414634146341, 57.557647058823534, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(73.49268292682927, 57.557647058823534, 'X[2] <= 26.5\ngini = 0.397\nsamples = 11\nvalue = [8, 3]'),
Text(66.23414634146341, 44.767058823529396, 'X[5] <= 7.396\ngini = 0.278\nsamples = 6\nvalue = [5, 1]'),
Text(62.60487804878049, 31.976470588235287, 'X[2] <= 24.5\ngini = 0.5\nsamples = 2\nvalue = [1, 1]'),
Text(58.97560975609756, 19.185882352941178, 'gini = 0.0 \times 10^{-1} (58.97560975609756), 19.185882352941178, 'gini = 0.0 \times 10^{-1}
Text(66.23414634146341, 19.185882352941178, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
Text(69.86341463414634, 31.976470588235287, 'gini = 0.\nsamples = 4\nvalue = [4, 0]'),
Text(80.75121951219512, 44.767058823529396, 'X[2] <= 27.5\ngini = 0.48\nsamples = 5\nvalue = [3, 2]'),
Text(77.1219512195122, 31.976470588235287, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(84.38048780487806, 31.976470588235287, 'X[6] <= 1.5\ngini = 0.375\nsamples = 4\nvalue = [3, 1]'),
Text(80.75121951219512, 19.185882352941178, 'gini = 0.0\nsamples = 2\nvalue = [2, 0]'),
Text(88.00975609756098, 19.185882352941178, 'X[2] \le 29.5 / gini = 0.5 / nsamples = 2 / nvalue = [1, 1]'),
Text(84.38048780487806, 6.39529411764704, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(91.6390243902439, 6.39529411764704, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
Text(91.6390243902439, 83.13882352941175, 'X[2] <= 19.5\ngini = 0.124\nsamples = 30\nvalue = [28, 2]'),
Text(88.00975609756098, 70.34823529411764, 'X[5] <= 7.973 | ngini = 0.444 | nsamples = 6 | nvalue = [4, 2]')
Text(84.38048780487806, 57.557647058823534, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
Text(91.6390243902439, 57.557647058823534, 'X[2] <= 16.5\ngini = 0.48\nsamples = 5\nvalue = [3, 2]'),
Text(88.00975609756098, 44.767058823529396, 'gini = 0.5\nsamples = 2\nvalue = [1, 1]'),
Text(95.26829268292683, 44.767058823529396, 'X[2] \le 18.0 = 0.444 = 3.11')
Text(91.6390243902439, 31.976470588235287, 'gini = 0.0 \nsamples = 1 \nvalue = [1, 0]'),
Text(98.89756097560976, 31.976470588235287, 'gini = 0.5\nsamples = 2\nvalue = [1, 1]'),
Text(95.26829268292683, 70.34823529411764, 'gini = 0.0\nsamples = 24\nvalue = [24, 0]'),
Text(102.52682926829269, 95.92941176470588, 'X[2] <= 21.0\ngini = 0.444\nsamples = 3\nvalue = [2, 1]'),
Text(98.89756097560976, 83.13882352941175, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(106.15609756097561, 83.13882352941175, 'gini = 0.0\nsamples = 2\nvalue = [2, 0]'),
Text(96.62926829268292, 108.72, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(100.258536586, 121.51058823529411, 'gini = 0.0\nsamples = 30\nvalue = [30, 0]'),
Text(137.9121951219512, 134.30117647058825, 'X[5] <= 7.763\ngini = 0.281\nsamples = 65\nvalue = [54, 11]'),
Text(134.2829268292683, 121.51058823529411, 'gini = 0.0\nsamples = 20\nvalue = [20, 0]'),
Text(141.54146341463414, 121.51058823529411, "X[2] <= 32.5\ngini = 0.369\nsamples = 45\nvalue = [34, 11]'),
Text(124.30243902439025, 108.72, 'X[5] <= 7.91\ngini = 0.5\nsamples = 8\nvalue = [4, 4]'),
Text(117.0439024390244, 95.92941176470588, 'X[5] <= 7.875 \\ ngini = 0.375 \\ nsamples = 4 \\ nvalue = [3, 1]'),
Text(113.41463414634147, 83.13882352941175, 'X[2] <= 31.5\ngini = 0.5\nsamples = 2\nvalue = [1, 1]'),
Text(109.78536585365855, 70.34823529411764, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
Text(117.0439024390244, 70.34823529411764, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(120.67317073170732, 83.13882352941175, 'gini = 0.0\nsamples = 2\nvalue = [2, 0]'),
Text(131.5609756097561, 95.92941176470588, 'X[5] <= 8.206\ngini = 0.375\nsamples = 4\nvalue = [1, 3]'),
Text(127.93170731707318, 83.13882352941175, 'gini = 0.0\nsamples = 3\nvalue = [0, 3]'),
Text(135.19024390243902, 83.13882352941175, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
Text(158.78048780487805, 108.72, 'X[5] \le 10.0 \cdot ngini = 0.307 \cdot nsamples = 37 \cdot nvalue = [30, 7]')
Text(146.07804878048782, 95.92941176470588, 'X[2] <= 38.5\ngini = 0.191\nsamples = 28\nvalue = [25, 3]'),
Text(142.4487804878049, 83.13882352941175, 'gini = 0.0\nsamples = 15\nvalue = [15, 0]'),
Text(149.70731707317074, 83.13882352941175, 'X[5] <= 7.988\ngini = 0.355\nsamples = 13\nvalue = [10, 3]'),
Text(146.07804878048782, 70.34823529411764, |X|_2| <= 46.0 | ngini = 0.49 | nsamples = 7 | nvalue = [4, 3]|,
Text(142.4487804878049, 57.557647058823534, 'X[5] \le 7.835 \cdot ngini = 0.48 \cdot nsamples = 5 \cdot nvalue = [2, 3]')
Text(138.81951219512194, 44.767058823529396, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(146.07804878048782, 44.767058823529396, 'X[5] <= 7.91\ngini = 0.5\nsamples = 4\nvalue = [2, 2]'),
Text(142.4487804878049, 31.976470588235287, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
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Text(149.70731707317074, 31.976470588235287, 'X[2] <= 41.5\nqini = 0.444\nsamples = 3\nvalue = [1, 2]'),
Text(146.07804878048782, 19.185882352941178, 'gini = 0.5\nsamples = 2\nvalue = [1, 1]'),
Text(153.33658536585367, 19.185882352941178, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(149.70731707317074, 57.557647058823534, 'gini = 0.0 \nsamples = 2 \nvalue = [2, 0]'),
Text(153.33658536585367, 70.34823529411764, 'gini = 0.0\nsamples = 6\nvalue = [6, 0]'),
 \texttt{Text}(164.22439024390243, 83.13882352941175, \texttt{'X[2]} <= 40.5 \texttt{\sc mgini} = 0.48 \texttt{\sc mples} = 5 \texttt{\sc mgini} = [2, 3] \texttt{')}, \\
Text(160.5951219512195, 70.34823529411764, 'X[2] <= 38.5\ngini = 0.5\nsamples = 4\nvalue = [2, 2]'),
Text(156.9658536585366, 57.557647058823534, X[2] \le 36.0 = 0.444 = 3.4 = 3.4 = 1.2 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 = 3.4 
Text(153.33658536585367, 44.767058823529396, 'gini = 0.5\nsamples = 2\nvalue = [1, 1]'),
Text(160.5951219512195, 44.767058823529396, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(164.22439024390243, 57.557647058823534, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
Text(167.85365853658539, 70.34823529411764, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(178.74146341463415, 83.13882352941175, 'X[5] <= 11.75\ngini = 0.375\nsamples = 4\nvalue = [3, 1]'),
Text(175.11219512195123, 70.34823529411764, 'X[2] <= 66.0\ngini = 0.5\nsamples = 2\nvalue = [1, 1]'),
Text(171.4829268292683, 57.557647058823534, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(178.74146341463415, 57.557647058823534, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
Text(182.37073170731708, 70.34823529411764, 'gini = 0.0\nsamples = 2\nvalue = [2, 0]'),
Text(169.66829268292685, 147.09176470588235, [X[5] <= 25.075\ngini = 0.043\nsamples = 46\nvalue = [45, 1]'),
Text(166.0390243902439, 134.30117647058825, 'gini = 0.0\nsamples = 29\nvalue = [29, 0]'),
Text(173.29756097560977, 134.30117647058825, 'X[2] <= 33.0\ngini = 0.111\nsamples = 17\nvalue = [16, 1]'),
Text(169.66829268292685, 121.51058823529411, 'X[2] \le 31.5 \cdot ingini = 0.245 \cdot insamples = 7 \cdot
 Text(166.0390243902439, 108.72, 'gini = 0.0\nsamples = 6\nvalue = [6, 0]'),
Text(176.9268292682927, 121.51058823529411, 'gini = 0.0\nsamples = 10\nvalue = [10, 0]'),
Text(187.81463414634146, 159.88235294117646, 'X[2] \le 30.0 = 0.375 = 4 = 4 = [1, 3]')
Text(184.18536585365854, 147.09176470588235, 'X[2] <= 27.0\ngini = 0.5\nsamples = 2\nvalue = [1, 1]'),
Text(180.55609756097562, 134.30117647058825, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(187.81463414634146, 134.30117647058825, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
Text(191.44390243902438, 147.09176470588235, 'gini = 0.0\nsamples = 2\nvalue = [0, 2]'),
Text(195.07317073170734, 159.88235294117646, 'gini = 0.0\nsamples = 5\nvalue = [5, 0]'),
Text(263.57560975609755, 198.25411764705882, 'X[0] <= 2.5\nqini = 0.428\nsamples = 203\nvalue = [63, 140]'),
Text(228.6439024390244, 185.4635294117647, 'X[7] <= 3.5\ngini = 0.215\nsamples = 106\nvalue = [13, 93]'),
Text(215.0341463414634, 172.6729411764706, 'X[5] <= 149.035\ngini = 0.082\nsamples = 93\nvalue = [4, 89]'),
Text(205.96097560, 159.88235294117646, 'X[2] <= 49.5\ngini = 0.048\nsamples = 82\nvalue = [2, 80]'),
Text(198.70243902439026, 147.09176470588235, 'X[5] <= 22.0\ngini = 0.026\nsamples = 75\nvalue = [1, 74]'),
 Text(195.07317073170734, 134.30117647058825, 'X[5] <= 20.25\ngini = 0.087\nsamples = 22\nvalue = [1, 21]'),
 Text(191.44390243902438, 121.51058823529411, 'gini = 0.0\nsamples = 20\nvalue = [0, 20]'),
 Text(198.70243902439026, 121.51058823529411, 'X[2] <= 28.5\ngini = 0.5\nsamples = 2\nvalue = [1, 1]'),
Text(195.07317073170734, 108.72, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
Text(202.33170731707318, 108.72, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(202.33170731707318, 134.30117647058825, 'gini = 0.0\nsamples = 53\nvalue = [0, 53]'),
Text(213.21951219512195, 147.09176470588235, 'X[2] \le 51.5 \cdot ngini = 0.245 \cdot nsamples = 7 \cdot nvalue = [1, 6]')
Text(209.59024390243903, 134.30117647058825, 'X[5] <= 19.606\ngini = 0.5\nsamples = 2\nvalue = [1, 1]'),
Text(205.9609756097561, 121.51058823529411, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(213.21951219512195, 121.51058823529411, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
Text(216.84878048780487, 134.30117647058825, 'gini = 0.0\nsamples = 5\nvalue = [0, 5]'),
Text(224.10731707317075, 159.88235294117646, 'X[5] <= 152.506\ngini = 0.298\nsamples = 11\nvalue = [2, 9]'),
Text(220.47804878048782, 147.09176470588235, 'gini = 0.0\nsamples = 2\nvalue = [2, 0]'),
Text(227.73658536585367, 147.09176470588235, 'gini = 0.0\nsamples = 9\nvalue = [0, 9]'),
Text(242.25365853658536, 172.6729411764706, 'X[1] <= 0.5\ngini = 0.426\nsamples = 13\nvalue = [9, 4]'),
Text(238.62439024390244, 159.88235294117646, 'X[6] <= 0.5\ngini = 0.298\nsamples = 11\nvalue = [9, 2]'),
Text(234.99512195121952, 147.09176470588235, 'X[5] \le 37.55  | x = 37.55  | 
 Text(231.3658536585366, 134.30117647058825, 'gini = 0.0\nsamples = 2\nvalue = [0, 2]'),
 Text(238.62439024390244, 134.30117647058825, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
Text(242.25365853658536, 147.09176470588235, 'gini = 0.0\nsamples = 8\nvalue = [8, 0]'),
Text(245.8829268292683, 159.88235294117646, 'gini = 0.0\nsamples = 2\nvalue = [0, 2]'),
Text(298.5073170731707, 185.4635294117647, 'x[5] \le 22.904 \text{ ngini} = 0.5 \text{ nsamples} = 97 \text{ nvalue} = [50, 47]'),
Text(269.47317073170734, 172.6729411764706, 'X[7] <= 2.5\ngini = 0.469\nsamples = 72\nvalue = [27, 45]'),
Text(265.8439024390244, 159.88235294117646, 'X[5] <= 7.744\ngini = 0.483\nsamples = 66\nvalue = [27, 39]'),
Text(249.51219512195124, 147.09176470588235, 'X[5] <= 6.987 \\ ngini = 0.18 \\ nsamples = 10 \\ nvalue = [1, 9]'), \\ number = 10 
Text(245.8829268292683, 134.30117647058825, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
 Text(253.14146341463416, 134.30117647058825, 'gini = 0.0\nsamples = 9\nvalue = [0, 9]'),
Text(282.1756097560976, 147.09176470588235, 'X[2] <= 26.5\ngini = 0.497\nsamples = 56\nvalue = [26, 30]'),
Text(260.40000000000003, 134.30117647058825, 'X[4] <= 0.5\ngini = 0.48\nsamples = 30\nvalue = [18, 12]'),
Text(247.69756097560978, 121.51058823529411, 'X[6] <= 1.5 \cdot ngini = 0.305 \cdot nsamples = 16 \cdot nvalue = [13, 3]')
Text(240.4390243902439, 108.72, 'X[2] \le 25.5 \cdot ngini = 0.142 \cdot nsamples = 13 \cdot nvalue = [12, 1]'),
Text(236.80975609756098, 95.92941176470588, 'gini = 0.0\nsamples = 11\nvalue = [11, 0]'),
 Text(240.4390243902439, 83.13882352941175, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
 Text(247.69756097560978, 83.13882352941175, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
```

```
Text(254.95609756097562, 108.72, 'X[5] <= 7.89\ngini = 0.444\nsamples = 3\nvalue = [1, 2]'),
Text(251.3268292682927, 95.92941176470588, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
Text(258.5853658536586, 95.92941176470588, 'gini = 0.0\nsamples = 2\nvalue = [0, 2]'),
Text(273.10243902439026, 121.51058823529411, 'X[7] <= 1.5\ngini = 0.459\nsamples = 14\nvalue = [5, 9]'),
Text(269.47317073170734, 108.72, 'X[2] <= 17.5\ngini = 0.496\nsamples = 11\nvalue = [5, 6]'),
Text(254.95609756097562, 70.34823529411764, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
Text(262.2146341463415, 70.34823529411764, 'gini = 0.0\nsamples = 5\nvalue = [0, 5]'),
Text(273.10243902439026, 83.13882352941175, 'X[5] \le 14.5 \cdot i = 0.444 \cdot i = 3 \cdot i = 2.1 \cdot i = 1.1 \cdot i = 1
Text(269.47317073170734, 70.34823529411764, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(276.7317073170732, 70.34823529411764, 'gini = 0.0\nsamples = 2\nvalue = [2, 0]'),
Text(273.10243902439026, 95.92941176470588, 'gini = 0.0\nsamples = 2\nvalue = [2, 0]'),
Text(276.7317073170732, 108.72, 'gini = 0.0 \nsamples = 3 \nvalue = [0, 3]'),
Text(287.61951219512196, 108.72, 'X[4] <= 3.0\ngini = 0.397\nsamples = 11\nvalue = [3, 8]'),
Text(283.99024390243903, 95.92941176470588, 'X[3] \le 0.5 \le 0.5 \le 0.32 \le
Text(280.3609756097561, 83.13882352941175, 'gini = 0.0\nsamples = 4\nvalue = [0, 4]'),
Text(287.61951219512196, 83.13882352941175, 'X[2] <= 32.0\ngini = 0.444\nsamples = 6\nvalue = [2, 4]'),
Text(283.99024390243903, 70.34823529411764, 'X[5] <= 19.262\ngini = 0.444\nsamples = 3\nvalue = [2, 1]'),
 Text(280.3609756097561, 57.557647058823534, 'gini = 0.0\nsamples = 2\nvalue = [2, 0]'),
 Text(287.61951219512196, 57.557647058823534, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(291.2487804878049, 70.34823529411764, 'gini = 0.0\nsamples = 3\nvalue = [0, 3]'),
 Text(291.2487804878049, 95.92941176470588, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
Text(302.13658536585365, 108.72, 'X[5] <= 15.673\ngini = 0.444\nsamples = 6\nvalue = [4, 2]'),
Text(298.5073170731707, 95.92941176470588, 'gini = 0.0\nsamples = 4\nvalue = [4, 0]'),
Text(305.76585365853657, 95.92941176470588, 'gini = 0.0\nsamples = 2\nvalue = [0, 2]'),
Text(313.0243902439025, 121.51058823529411, 'X[2] <= 41.0\nqini = 0.198\nsamples = 9\nvalue = [1, 8]'),
Text(309.3951219512195, 108.72, 'gini = 0.0 \nsamples = 7 \nvalue = [0, 7]'),
 Text(316.6536585365854, 108.72, 'X[3] <= 0.5 \neq 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0.5 = 0
 Text(313.0243902439025, 95.92941176470588, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
Text(320.2829268292683, 95.92941176470588, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(273.10243902439026, 159.88235294117646, 'gini = 0.0\nsamples = 6\nvalue = [0, 6]'),
Text(327.54146341463417, 172.6729411764706, 'X[2] <= 6.0\ngini = 0.147\nsamples = 25\nvalue = [23, 2]'),
Text(323.91219512195124, 159.88235294117646, 'X[2] <= 4.5\ngini = 0.346\nsamples = 9\nvalue = [7, 2]'),
Text(320.2829268292683, 147.09176470588235, 'X[2] \le 2.5 \text{ ngini} = 0.219 \text{ nsamples} = 8 \text{ nvalue} = [7, 1]'),
 Text(316.6536585365854, 134.30117647058825, 'gini = 0.0\nsamples = 5\nvalue = [5, 0]'),
 Text(323.91219512195124, 134.30117647058825, 'X[2] \le 3.5 \le 0.444 \le 3.5 \le 2.5 \le 3.5 \le 3.5
 Text(320.2829268292683, 121.51058823529411, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(327.54146341463417, 121.51058823529411, 'gini = 0.0\nsamples = 2\nvalue = [2, 0]'),
Text(327.54146341463417, 147.09176470588235, 'gini = 0.0\nsamples = 1\nvalue = [0, 1]'),
Text(331.1707317073171, 159.88235294117646, 'gini = 0.0\nsamples = 16\nvalue = [16, 0]')]
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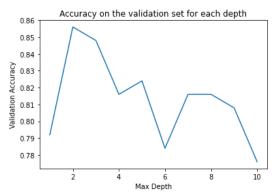
```
In [40]: dt2.score(df_train3, df_train_y)
Out[40]: 0.9919678714859438

In [41]: dt2.score(df_val3, df_val_y)
Out[41]: 0.768
```

The model is overfiting for default setting.

3-2-b. Improve a decision tree model by tuning some hyperparam- eters for terminating the splitting process. Tune the maximum depth of the tree

```
In [42]: depth =[]
         accuracy = []
         for max depth in range(1,11):
            dt = DecisionTreeClassifier(random state=0, max depth=max depth)
            dt = dt.fit(df_train3, df_train_y)
            print("Max Depth: ", max depth)
            print("Train Accuracy: ", dt.score(df train3, df train y))
            print("Validation Accuracy: ", dt.score(df_val3, df_val_y))
            print('-'*20)
            depth.append(max depth)
            accuracy.append(dt.score(df val3, df val y))
         plt.plot(depth, accuracy)
         plt.title("Accuracy on the validation set for each depth")
        plt.xlabel("Max Depth")
        plt.ylabel("Validation Accuracy")
        Max Depth: 1
        Train Accuracy: 0.7751004016064257
        Validation Accuracy: 0.792
        _____
        Max Depth: 2
        Train Accuracy: 0.7811244979919679
        Validation Accuracy: 0.856
        _____
        Max Depth: 3
        Train Accuracy: 0.8273092369477911
        Validation Accuracy: 0.848
        -----
        Max Depth: 4
        Train Accuracy: 0.8413654618473896
        Validation Accuracy: 0.816
        -----
        Max Depth: 5
        Train Accuracy: 0.8534136546184738
        Validation Accuracy: 0.824
        Max Depth: 6
        Train Accuracy: 0.8815261044176707
        Validation Accuracy: 0.784
        _____
        Max Depth: 7
        Train Accuracy: 0.8975903614457831
        Validation Accuracy: 0.816
        _____
        Max Depth: 8
        Train Accuracy: 0.9156626506024096
        Validation Accuracy: 0.816
        _____
        Max Depth: 9
        Train Accuracy: 0.9397590361445783
        Validation Accuracy: 0.808
        _____
        Max Depth: 10
        Train Accuracy: 0.9558232931726908
        Validation Accuracy: 0.776
        _____
Out[42]: Text(0, 0.5, 'Validation Accuracy')
```



- According to the plot, the optimum maximum depth is 2.
- 3-2-C. Train a decision tree classifier using the optimum setting of max- imum depth found in 3.2b on all data from the training and validation set.

```
In [43]: # Combine training and validation set
          df_train_val = pd.concat([df_train3, df_val3])
          df_train_val_y = pd.concat([df_train_y, df_val_y])
          # Set Decision tree classifier
          dt = DecisionTreeClassifier(random_state=1, max_depth = 2)
          # Train model
          dt.fit(df train val, df train val y)
Out[43]: DecisionTreeClassifier(max_depth=2, random_state=1)
In [44]:
          # Predict
          y_pred = dt.predict(df test3)
          # Create data frame for Prediction
          df pred = pd.DataFrame(y pred)
          df pred
          # save the predictions
          df pred.to csv('F0034WQ dt prediction.csv', index=False, header = False)
```

4 Random Forest Classification

4-1. Initialize a random forest classifier.

```
In [45]: from sklearn.ensemble import RandomForestClassifier

rf = RandomForestClassifier(max_depth=2, random_state=0)
    rf.fit(df_train3, df_train_y)

# Accuracy on Validation set in default set
    print("Validation Accuracy: ", rf.score(df_val3, df_val_y))
Validation Accuracy: 0.816
```

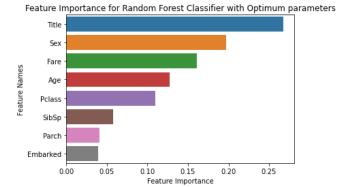
4-2. Optimize your classifier by tuning two hyperparameters to maximize the accuracy of your model:

```
In [46]: from sklearn.model_selection import GridSearchCV
```

4-3. Report and interpret the feature importance of each feature by your random forest model.

```
In [47]: # classifier with best hyperparameters
          rf = RandomForestClassifier(random state = 2, max depth = 7, n estimators = 150)
          rf.fit(df_train_val, df_train_val_y)
Out[47]: RandomForestClassifier(max_depth=7, n_estimators=150, random_state=2)
         # Generate feature importance and feature names
          feature_importance = np.array(rf.feature_importances_)
          feature_names = np.array(df_train_val.columns)
          # Generate a DataFrame for feature importance
          data={'feature names':feature names,'feature importance':feature importance}
          feature importance df = pd.DataFrame(data)
          # Sort the DataFrame according to feature importance
          feature importance df.sort values(by=['feature importance'], ascending=False, inplace=True)
          # Plot
          import seaborn as sns
          sns.barplot(x = feature importance df['feature importance'], y = feature importance df['feature names'])
          plt.title('Feature Importance for Random Forest Classifier with Optimum parameters')
          plt.xlabel('Feature Importance')
          plt.ylabel('Feature Names')
```

Out[48]: Text(0, 0.5, 'Feature Names')



• According to the above plot, we can see the most important feature in my model is "Title".

4-4. Predict the survivals on testing data using the classifier with the opti- mum parameters from 4.2.

```
In [49]: # Predict
y_pred = rf.predict(df_test3)
y_pred

# Create data frame for Prediction
df_pred = pd.DataFrame(y_pred)
df_pred

# save the predictions
df_pred.to_csv('F0034WQ_rf_prediction.csv', index=False, header = False)
```

5. SVM classification

```
In [50]: # Pre-processed data
    from sklearn.preprocessing import StandardScaler
    SS = StandardScaler()

    df_train3_SS = SS.fit_transform(df_train3)
    df_val3_SS = SS.transform(df_val3)
    df_test3_SS = SS.transform(df_test3)
```

5-1. Build SVM classifiers with the following three kernels: linear, polynomial with degree = 2, and radial basis function kernel. Train the classifiers and calculate the performance of each classifier on the validation set.

```
In [51]: from sklearn.metrics import accuracy_score, log_loss
          from sklearn.svm import SVC
          svm linear = SVC(kernel = 'linear')
          svm poly = SVC(kernel = 'poly', degree = 2, probability = True)
          svm_rbf = SVC(kernel = 'rbf', probability = True)
          # kernels: linear
          svm linear.fit(df train3 SS, df train y)
          print("kernels: linear")
          print("Validation Accuracy: ", svm linear.score(df val3 SS, df val y))
          print('-'*20)
          # kernels: polynomial with degree = 2
          svm poly.fit(df train3 SS, df train y)
          print("kernels: polynomial with degree = 2")
          print("Validation Accuracy: ", svm poly.score(df val3 SS, df val y))
          print('Loss of Validation Set:', log_loss(df_val_y, svm_poly.predict_proba(df_val3_SS)) )
          print('-'*20)
          # kernels: radial basis function
          svm rbf.fit(df train3 SS, df train y)
          print("kernels: radial basis function")
          print("Validation Accuracy: ", svm_rbf.score(df_val3_SS, df_val_y))
          print('Loss of Validation Set:', log_loss(df_val_y, svm_rbf.predict_proba(df_val3_SS)) )
          print('-'*20)
         kernels: linear
         Validation Accuracy: 0.84
         kernels: polynomial with degree = 2
         Validation Accuracy: 0.856
         Loss of Validation Set: 0.4049651318151844
```

kernels: radial basis function Validation Accuracy: 0.856

Loss of Validation Set: 0.3780804868895341

5-2. Which kernel gives the best result? Use your classifier with the this kernel to predict the survival outcomes in the testing set.

• Although classifier with kernel = polynomial and classifier with kernel = radial basis function return same accuracy, classifier with kernel = radial basis function returns smaller Loss. As a result, classifier with kernel = radial basis function gives the best result.