01,3, 6,2, 5,3, 6,7

- 1a) [[log(-1)] = 2 log |-1| + iθ: θ ∈ [[arg (-1)]]]
 = 2 j = 7 k: R ∈ Z 3 log(-1) = j = 7
- b) [log(1-i)] = 2 |og |1-i| + i0: 0 E | Log(1-i)]}

 = 2 |og | \(\tau i \frac{7}{4} \cdot \cdo
- c) [log(e^{-2\frac{\pi_1}{3}}) = \glog(|e^{-2\frac{\pi_1}{3}}|) + i0: 0 \estarg(e^{-\frac{\pi_1}{3}})]
 = \left(-i\frac{\pi_2}{3}\right) : \right(\epsilon\frac{\pi_3}{3}\right) = -i\frac{\pi_1}{3}
- 3.1) f(z) = Re(z) $\gamma(t) = t - it^2 (t \in t_0, 0)$ $\int_{z} f(z) dz = \int_{z} Re(t - it^2) (1 - 2it) dt$ $= \int_{z}^{2} (t - 2it^2) dt$ $= \frac{1}{2} t^2 - \frac{1}{2}it^3 = \frac{1}{2}$ $= \frac{1}{2} - \frac{1}{2}i$
 - 2) f(z) = 1/2 8 = unit circle darkenise starting at 1 travership with circle 4+times

$$\mathcal{T} = e^{it} \quad (f \in [0, -8\pi])$$

$$\int_{\mathcal{T}} f(z) dz = \int_{0}^{-8\pi} \frac{1}{e^{it}} i e^{it} dt = \int_{0}^{8\pi} i dt = i \in [0, -8\pi]$$

3) f(2) = 1214 T = Stright line (rom-1+i to 1+i

5.7) I'r = hult cine in uppartuil of plane rodius R control at the ontin towersed CCW.

=Reit (telo, T)

Let f(2) = 2" eit. So |f(2)| = 121-4. On IR we If(Ir(+)) | = | Reie | -4 = R leit | -4 = R. So for $t \in [0, \pi]$ $|f(2)| \leq R$. Further we have that length $Re^{it} = \pi R S S$ Sf(ε) dε (€ R4 πR = πR3 by the estimation Comma. .3) T(toir) = circle radius r centred at to truesco CCW. rlo; R)=Ret (te[o, ea]) Let F(t) = 2-1 So. If(2) = (2-1). On & we have [f(v(o; R)) = | Reit = | Reit = 1] Clery the meximum will our when elt = -1 so are were $|f(z)| \leq \frac{|-1-R|}{|-R+1|} = \frac{|+R|}{|1-R|}$ providing R & I. Further length or (o, R) = 201 so by the astimution lemma [] f(b) 52 | < 1-n 2ar = 2ar (r+1) . σ₅ σ₆ σ₆ (1- ε);

t ε (ο, 1] f∈ [0, 1] Δ⁵(4) = (1-4) γ₃(t) = it + ∈ το, i) JE 12 = 0 by landy's theorem Since Vis dosed and I is holomorphic everywhere. b) \ \frac{7}{2} \rightarrow \frac{1}{2} \rightarrow \ =) (1-+)(1-i) + +; (1-i) - i ++; + :+ st =] [= 1 + i + i + 1 + 2i) + 1 - i - i dt 2] 4 it + 1-2; dt = 2: +2 + (1-2:)+

