

# Backpropagation

In this assignment, you will implement Backpropagation from scratch. You will then verify the correctness of the your implementation using a "grader" function/cell (provided by us) which will match your implementation.

The grader fucntion would help you validate the correctness of your code.

Please submit the final Colab notebook in the classroom ONLY after you have verified your code using the grader function/cell.

## Loading data

```
In [1]: import pickle
import numpy as np
from math import exp
from tqdm import tqdm
from statistics import mean
import matplotlib.pyplot as plt

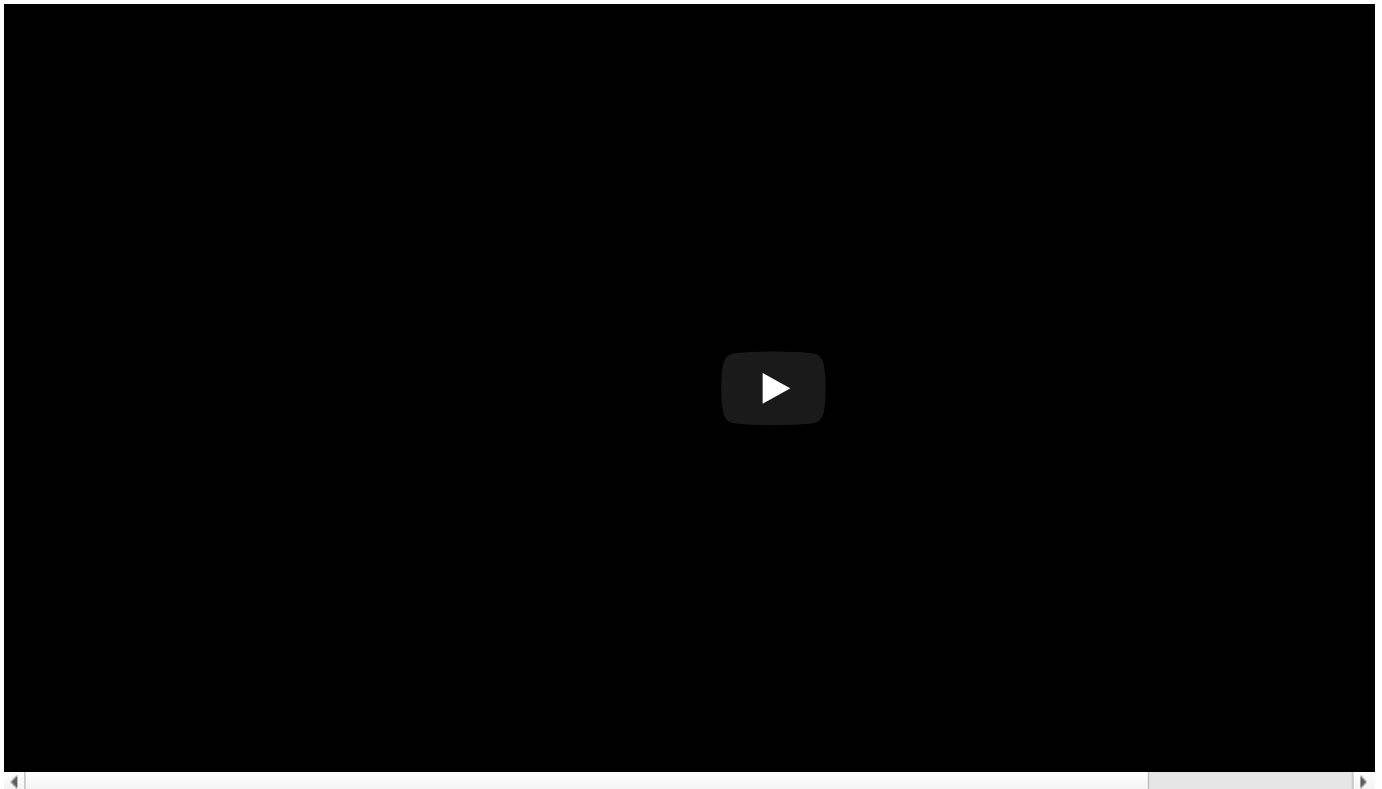
with open('data.pkl', 'rb') as f:
    data = pickle.load(f)
print(data.shape)
X = data[:, :5]
y = data[:, -1]
print(X.shape, y.shape)

(506, 6)
(506, 5) (506,)
```

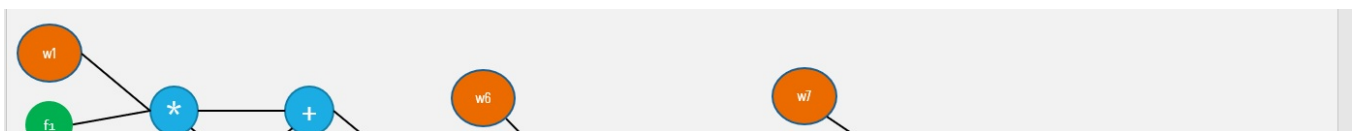
[Check this video for better understanding of the computational graphs and back propagation](#)

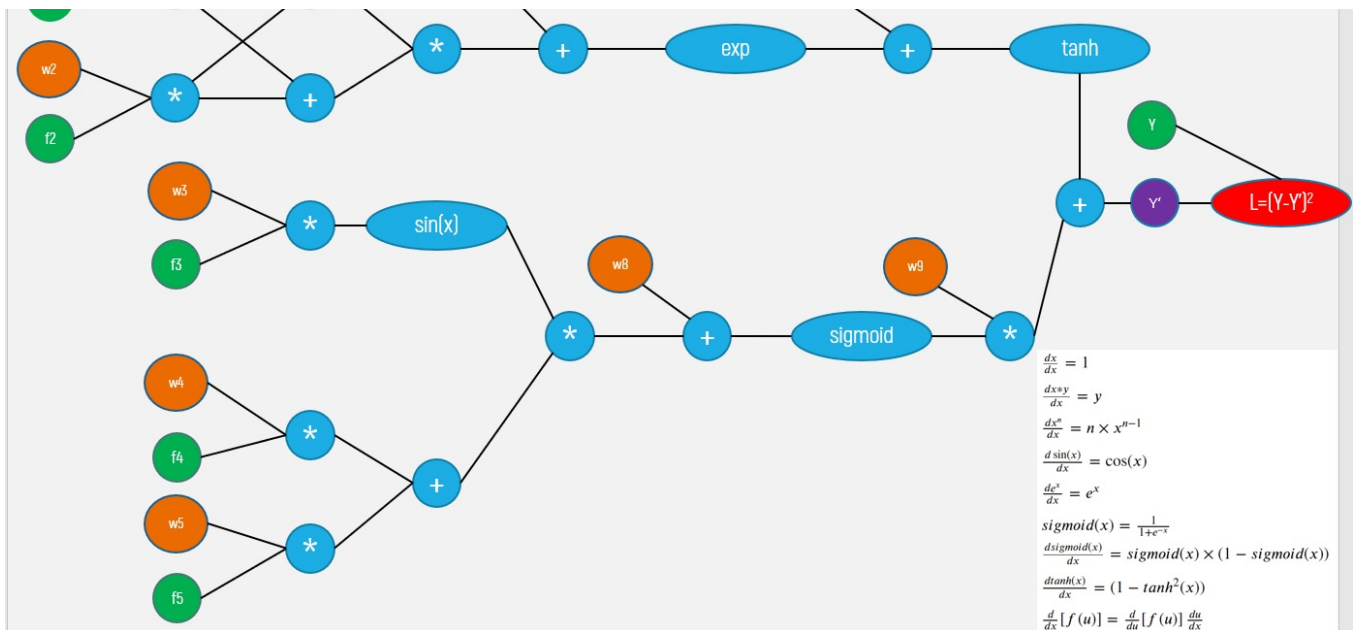
```
In [2]: from IPython.display import YouTubeVideo
YouTubeVideo('i940vYb6noo',width="1000",height="500")
```

Out[2]:



## Computational graph





- If you observe the graph, we are having input features [f1, f2, f3, f4, f5] and 9 weights [w1, w2, w3, w4, w5, w6, w7, w8, w9].
- The final output of this graph is a value L which is computed as  $(Y - Y')^2$

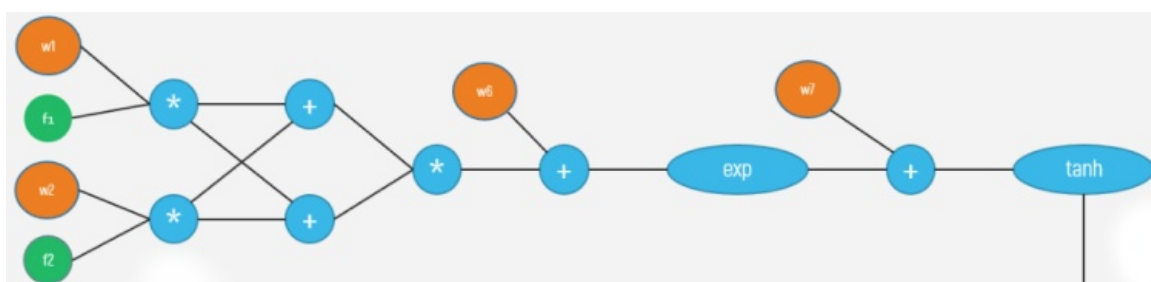
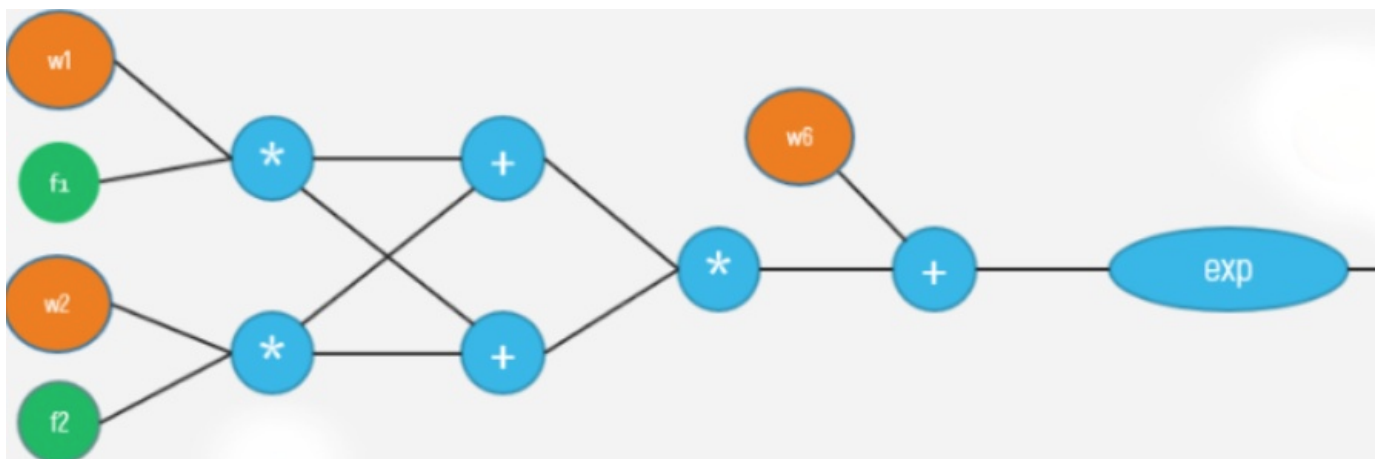
## Task 1: Implementing Forward propagation, Backpropagation and Gradient checking

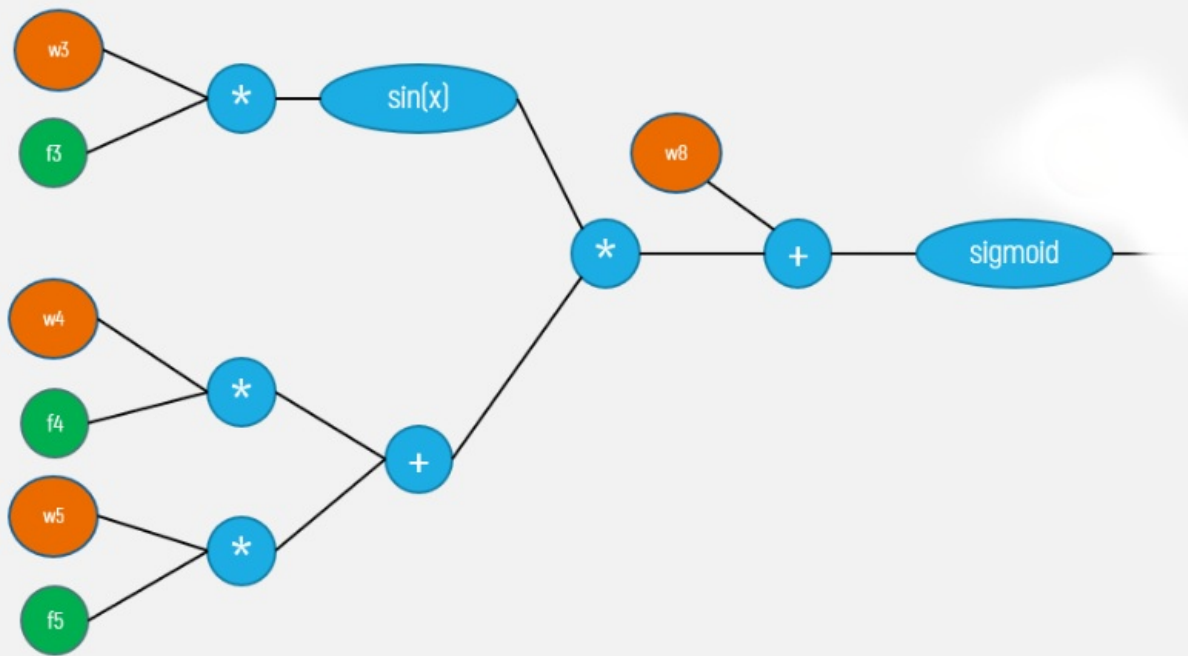
### Task 1.1

#### Forward propagation

- Forward propagation (Write your code in `def forward_propagation()`)

For easy debugging, we will break the computational graph into 3 parts.





```
In [3]: def sigmoid(z):
        '''In this function, we will compute the sigmoid(z)'''

        sigmoid_ = 1 / (1 + exp(-z))

        return sigmoid_
```

```
In [4]: def grader_sigmoid(z):
        #if you have written the code correctly then the grader function will output true

        val=sigmoid(z)
        assert(val==0.8807970779778823)
        return True

        grader_sigmoid(2)
```

Out[4]: True

```
In [5]: def forward_propagation(x, y, w):

        '''In this function, we will compute the forward propagation '''

        # X: input data point, note that in this assignment you are having 5-d data points
        # y: output variable
        # W: weight array, its of length 9, W[0] corresponds to w1 in graph, W[1] corresponds
        # to w2 in graph,..., W[8] corresponds to w9 in graph.

        # exp
        val_1 = (w[0] * x[0] + w[1] * x[1]) * (w[0] * x[0] + w[1] * x[1]) + w[5]
        part_1 = np.exp(val_1)

        # tanh
        val_2 = part_1 + w[6]
        part_2 = np.tanh(val_2)

        # sigmoid
        val_3 = w[2] * x[2]
        val_4 = (w[3] * x[3]) + (w[4] * x[4])
        part_3 = sigmoid((val_4 * np.sin(val_3)) + w[7])

        # dy_pred
        y_pred = part_2 + (part_3 * w[8])
        dy_pred = -2 * (y - y_pred)

        # loss
        loss = np.square(y - y_pred)

        forward_dict={}
        forward_dict['exp']= part_1
        forward_dict['tanh']= part_2
        forward_dict['sigmoid']= part_3
        forward_dict['loss']= loss
        forward_dict['dy_pred']= dy_pred
```

```
forward_dict['w2_f3']= val_3
```

```
return forward_dict
```

```
In [6]: def grader_forwardprop(data):

    dl = (data['dy_pred'] == -1.9285278284819143)
    loss = (data['loss'] == 0.9298048963072919)
    part1 = (data['exp'] == 1.1272967040973583)
    part2 = (data['tanh'] == 0.8417934192562146)
    part3 = (data['sigmoid'] == 0.5279179387419721)
    assert(dl and loss and part1 and part2 and part3)
    return True

w = np.ones(9) * 0.1

d1 = forward_propagation(X[0], y[0], w)

grader_forwardprop(d1)
```

Out[6]: True

## Task 1.2

### Backward propagation

```
In [7]: def backward_propagation(x, y, w, forward_dict):

    '''In this function, we will compute the backward propagation '''

    dw1 = forward_dict['dy_pred'] * (1 - np.square(forward_dict['tanh'])) * forward_dict['exp'] \
        * 2 * ((w[0] * x[0] + w[1] * x[1]) * x[0])

    dw2 = forward_dict['dy_pred'] * (1 - np.square(forward_dict['tanh'])) * forward_dict['exp'] \
        * 2 * ((w[1] * x[1] + w[0] * x[0]) * x[1])

    dw3 = forward_dict['dy_pred'] * w[8] * forward_dict['sigmoid'] * (1 - forward_dict['sigmoid']) \
        * ((x[3] * w[3] + x[4] * w[4]) * x[2]) * np.cos(forward_dict['w2_f3'])

    dw4 = forward_dict['dy_pred'] * w[8] * forward_dict['sigmoid'] * (1 - forward_dict['sigmoid']) \
        * x[3] * np.sin(forward_dict['w2_f3'])

    dw5 = forward_dict['dy_pred'] * w[8] * forward_dict['sigmoid'] * (1 - forward_dict['sigmoid']) \
        * x[4] * np.sin(forward_dict['w2_f3'])

    dw6 = forward_dict['dy_pred'] * (1 - np.square(forward_dict['tanh'])) * forward_dict['exp']

    dw7 = forward_dict['dy_pred'] * (1 - np.square(forward_dict['tanh']))

    dw8 = forward_dict['dy_pred'] * w[8] * forward_dict['sigmoid'] * (1 - forward_dict['sigmoid'])

    dw9 = forward_dict['sigmoid'] * forward_dict['dy_pred']

    backward_dict = {}

    backward_dict['dw1'] = dw1
    backward_dict['dw2'] = dw2
    backward_dict['dw3'] = dw3
    backward_dict['dw4'] = dw4
    backward_dict['dw5'] = dw5
    backward_dict['dw6'] = dw6
    backward_dict['dw7'] = dw7
    backward_dict['dw8'] = dw8
    backward_dict['dw9'] = dw9

    return backward_dict
```

```
In [8]: def grader_backprop(data):

    dw1=(np.round(data['dw1'],6))==-0.229733)
    dw2=(np.round(data['dw2'],6))==-0.021408)
    dw3=(np.round(data['dw3'],6))==-0.005625)
    dw4=(np.round(data['dw4'],6))==-0.004658)
    dw5=(np.round(data['dw5'],6))==-0.001008)
    dw6=(np.round(data['dw6'],6))==-0.633475)
    dw7=(np.round(data['dw7'],6))==-0.561942)
    dw8=(np.round(data['dw8'],6))==-0.048063)
    dw9=(np.round(data['dw9'],6))==-1.018104)
```

```

    assert(dw1 and dw2 and dw3 and dw4 and dw5 and dw6 and dw7 and dw8 and dw9)
    return True

w = np.ones(9)*0.1

forward_dict = forward_propagation(X[0],y[0],w)

backward_dict = backward_propagation(X[0],y[0],w,forward_dict)

grader_backprop(backward_dict)

```

Out[8]: True

## Task 1.3

### Gradient clipping

Check this [blog link](#) for more details on Gradient clipping

we know that the derivative of any function is

$$\lim_{\epsilon \rightarrow 0} \frac{f(x + \epsilon) - f(x - \epsilon)}{2\epsilon}$$

- The definition above can be used as a numerical approximation of the derivative. Taking an epsilon small enough, the calculated approximation will have an error in the range of epsilon squared.
- In other words, if epsilon is 0.001, the approximation will be off by 0.00001.

Therefore, we can use this to approximate the gradient, and in turn make sure that backpropagation is implemented properly. This forms the basis of gradient checking!

### Gradient checking example

lets understand the concept with a simple example:

$$f(w_1, w_2, x_1, x_2) = w_1^2 \cdot x_1 + w_2 \cdot x_2$$

from the above function , lets assume

$$w_1 = 1$$

,

$$w_2 = 2$$

,

$$x_1 = 3$$

,

$$x_2 = 4$$

the gradient of

$f$

w.r.t

$w_1$

is

$$\begin{aligned}
 \frac{df}{dw_1} = dw_1 &= 2 \cdot w_1 \cdot x_1 \\
 &= 2 \cdot 1 \cdot 3 \\
 &= 6
 \end{aligned}$$

let calculate the aproximate gradient of

$w_1$

as mentinoned in the above formula and considering

$$\epsilon = 0.0001$$

$$\begin{aligned}
 dw_1^{approx} &= \frac{f(w_1+\epsilon, w_2, x_1, x_2) - f(w_1-\epsilon, w_2, x_1, x_2)}{2\epsilon} \\
 &= \frac{((1+0.0001)^2 \cdot 3 + 2.4) - ((1-0.0001)^2 \cdot 3 + 2.4)}{2\epsilon} \\
 &= \frac{(1.00020001 \cdot 3 + 2.4) - (0.99980001 \cdot 3 + 2.4)}{2 \cdot 0.0001} \\
 &= \frac{(11.00060003) - (10.99940003)}{0.0002} \\
 &= 5.999999999999
 \end{aligned}$$

Then, we apply the following formula for gradient check: **gradient\_check** =

$$\frac{\|(dW - dW^{approx})\|_2}{\|(dW)\|_2 + \|(dW^{approx})\|_2}$$

The equation above is basically the Euclidean distance normalized by the sum of the norm of the vectors. We use normalization in case that one of the vectors is very small. As a value for epsilon, we usually opt for 1e-7. Therefore, if gradient check return a value less than 1e-7, then it means that backpropagation was implemented correctly. Otherwise, there is potentially a mistake in your implementation. If the value exceeds 1e-3, then you are sure that the code is not correct.

in our example: **gradient\_check**

$$= \frac{(6 - 5.999999999994898)}{(6 + 5.999999999994898)} = 4.2514140356330737e^{-13}$$

you can mathamatically derive the same thing like this

$$\begin{aligned}
 dw_1^{approx} &= \frac{f(w_1+\epsilon, w_2, x_1, x_2) - f(w_1-\epsilon, w_2, x_1, x_2)}{2\epsilon} \\
 &= \frac{((w_1+\epsilon)^2 \cdot x_1 + w_2 \cdot x_2) - ((w_1-\epsilon)^2 \cdot x_1 + w_2 \cdot x_2)}{2\epsilon} \\
 &= \frac{4\epsilon \cdot w_1 \cdot x_1}{2\epsilon} \\
 &= 2 \cdot w_1 \cdot x_1
 \end{aligned}$$

## Implement Gradient checking

(Write your code in `def gradient_checking()`)

Algorithm

```

W = initilize_randomly
def gradient_checking(data_point, W):

    # compute the L value using forward_propagation()
    # compute the gradients of W using backward_propagation()
    approx_gradients = []
    for each wi weight value in W:
        # add a small value to weight wi, and then find the values of L with the updated weights
        # subtract a small value to weight wi, and then find the values of L with the updated weights
        # compute the approximation gradients of weight wi
        approx_gradients.append(approximation gradients of weight wi)
    # compare the gradient of weights W from backward_propagation() with the aproximation gradients
    # of weights with <br> gradient_check formula
    return gradient_check

```

NOTE: you can do sanity check by checking all the return values of gradient\_checking(), they have to be zero. if not you have bug in your code

In [9]:

```

def gradient_checking(x, y, w, eps):

    # compute the dict value using forward_propagation()
    # compute the actual gradients of W using backward_propagation()
    forward_dict = forward_propagation(x, y, w)
    backward_dict = backward_propagation(x, y, w, forward_dict)

    #we are storing the original gradients for the given datapoints in a list
    original_gradients_list = list(backward_dict.values())

    approx_gradients_list=[]

    ...

```

```

now we have to write code for approx gradients, here you have to make sure that you
update only one weight at a time
write your code here and append the approximate gradient value for each weight in approx_gradients_list
'''

for i in range(len(w)):

    w_original = w[i]
    w[i] = w_original + eps
    for_pos_updated = forward_propagation(x, y, w)
    updated_loss_pos = for_pos_updated['loss']

    w[i] = w_original - eps
    for_neg_updated = forward_propagation(x, y, w)
    updated_loss_neg = for_neg_updated['loss']

    dw_approx = (updated_loss_pos - updated_loss_neg) / ( 2 * eps)
    approx_gradients_list.append(dw_approx)

#performing gradient check operation
original_gradients_list = np.array(original_gradients_list)
approx_gradients_list = np.array(approx_gradients_list)
gradient_check_value = (original_gradients_list - approx_gradients_list) / \
                        (original_gradients_list + approx_gradients_list)

return gradient_check_value

```

```

In [10]: def grader_grad_check(value):
          print(value)
          assert(np.all(value <= 10**-3))
          return True

w = [ 0.00271756,  0.01260512,  0.00167639, -0.00207756,  0.00720768,
      0.00114524,  0.00684168,  0.02242521,  0.01296444]

eps = 10**-7
value = gradient_checking(X[0], y[0], w, eps)
grader_grad_check(value)

```

```

[-1.73921918e-08  1.28741906e-05 -2.55164399e-04 -1.05871856e-05
 -1.95446016e-04 -1.16536595e-10 -9.63625495e-08 -1.06774472e-07
 -1.43339489e-08]

```

Out[10]: True

## Task 2 : Optimizers

- As a part of this task, you will be implementing 2 optimizers(methods to update weight)
- Use the same computational graph that was mentioned above to do this task
- The weights have been initialized from normal distribution with mean=0 and std=0.01. The initialization of weights is very important otherwise you can face vanishing gradient and exploding gradients problem.

Check below video for reference purpose

```

In [11]: from IPython.display import YouTubeVideo
          YouTubeVideo('gYpoJMLgyXA',width="1000",height="500")

```

Out[11]:



## Algorithm

```
for each epoch(1-20):
    for each data point in your data:
        using the functions forward_propagation() and backward_propagation() compute the
        gradients of weights
        update the weights with help of gradients
```

## Implement below tasks

- Task 2.1: you will be implementing the above algorithm with Vanilla update of weights
- Task 2.2: you will be implementing the above algorithm with Momentum update of weights
- Task 2.3: you will be implementing the above algorithm with Adam update of weights

Note : If you get any assertion error while running grader functions, please print the variables in grader functions and check which variable is returning False .Recheck your logic for that variable .

### 2.1 Algorithm with Vanilla update of weights

- <https://stats.stackexchange.com/a/295181>  
" Vanilla means standard, usual, or unmodified version of something. Vanilla gradient descent means the basic gradient descent algorithm without any bells or whistles."
- <https://ruder.io/optimizing-gradient-descent/>  
Vanilla gradient descent, aka batch gradient descent, computes the gradient of the cost function w.r.t. to the parameters  $\theta$  for the entire training dataset:

$$\theta = \theta - \eta * \nabla_{\theta} J(\theta)$$

- <https://www.analyticsvidhya.com/blog/2017/03/introduction-to-gradient-descent-algorithm-along-its-variants/>

Pseudocode :

```
update = learning_rate * gradient_of_parameters
parameters = parameters - update
```

```
In [12]: weight = np.random.normal(scale = 0.01, size =9)

learning_rate = 0.1

mean_v_loss = []

epochs = range(1, 21)

for epoch in epochs:

    v_loss = []
    for i in range(len(X)):

        forward_dict_ = forward_propagation(X[i], y[i], weight)
        backward_dict_ = backward_propagation(X[i], y[i], weight, forward_dict_)

        weight[0] = weight[0] - learning_rate * backward_dict_['dw1']
        weight[1] = weight[1] - learning_rate * backward_dict_['dw2']
        weight[2] = weight[2] - learning_rate * backward_dict_['dw3']
        weight[3] = weight[3] - learning_rate * backward_dict_['dw4']
```



```

weight[4] = weight[4] - learning_rate * backward_dict['dw5']
weight[5] = weight[5] - learning_rate * backward_dict['dw6']
weight[6] = weight[6] - learning_rate * backward_dict['dw7']
weight[7] = weight[7] - learning_rate * backward_dict['dw8']
weight[8] = weight[8] - learning_rate * backward_dict['dw9']

```

```

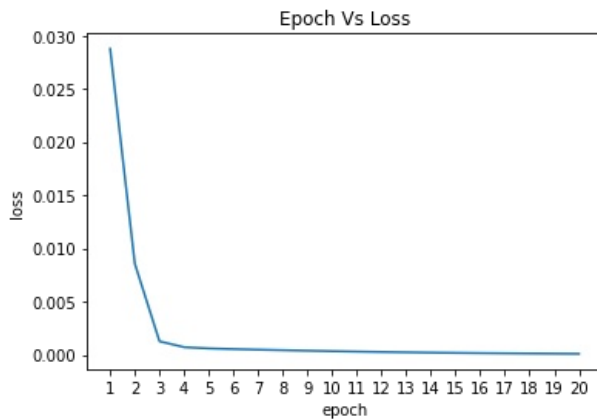
v_loss.append(forward_dict['loss'])
mean_v_loss.append(mean(v_loss))

```

```

plt.plot(epochs, mean_v_loss)
plt.xlabel("epoch")
plt.ylabel("Loss")
plt.xticks(range(1,21))
plt.title("Epoch Vs Loss")
plt.show()

```



## 2.2 Algorithm with Momentum update of weights

### Momentum based Gradient Descent Update Rule

$$v_t = \gamma * v_{t-1} + \eta \nabla w_t$$

$$w_{t+1} = w_t - v_t$$

Here Gamma refers to the momentum coefficient, eta is leaning rate and v\_t is moving average of our gradients at timestep t

```

In [13]: ...
Momentum update
v = mu * v - learning_rate * dx # integrate velocity
x += v # integrate position

learning_rate & mu from here : https://cs231n.github.io/neural-networks-3/
...

weight = np.random.normal(scale = 0.01, size = 9)

learning_rate = 0.1

mu = 0.9

mean_momentum_loss = []

v_1 = v_2 = v_3 = v_4 = v_5 = v_6 = v_7 = v_8 = v_9 = 0

epochs = range(1, 21)

for epoch in epochs:

    momentum_loss = []
    for i in range(len(X)):

        forward_dict_ = forward_propagation(X[i], y[i], weight)
        backward_dict_ = backward_propagation(X[i], y[i], weight, forward_dict_)

```

```

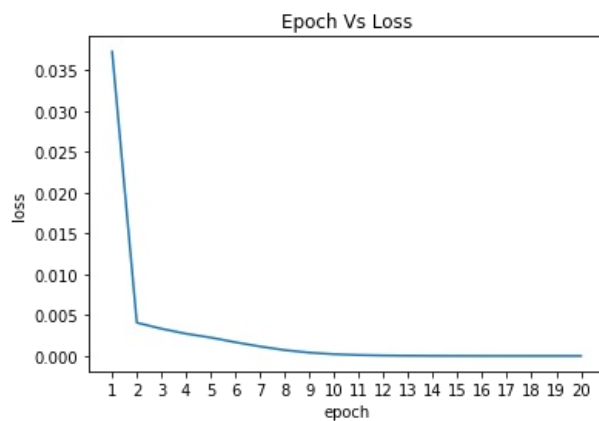
v_1 = (mu * v_1) + (learning_rate * backward_dict['dw1'])
v_2 = (mu * v_2) + (learning_rate * backward_dict['dw2'])
v_3 = (mu * v_3) + (learning_rate * backward_dict['dw3'])
v_4 = (mu * v_4) + (learning_rate * backward_dict['dw4'])
v_5 = (mu * v_5) + (learning_rate * backward_dict['dw5'])
v_6 = (mu * v_6) + (learning_rate * backward_dict['dw6'])
v_7 = (mu * v_7) + (learning_rate * backward_dict['dw7'])
v_8 = (mu * v_8) + (learning_rate * backward_dict['dw8'])
v_9 = (mu * v_9) + (learning_rate * backward_dict['dw9'])

weight[0] = weight[0] - v_1
weight[1] = weight[1] - v_2
weight[2] = weight[2] - v_3
weight[3] = weight[3] - v_4
weight[4] = weight[4] - v_5
weight[5] = weight[5] - v_6
weight[6] = weight[6] - v_7
weight[7] = weight[7] - v_8
weight[8] = weight[8] - v_9

momentum_loss.append(forward_dict['loss'])
mean_momentum_loss.append(mean(momentum_loss))

plt.plot(epochs, mean_momentum_loss)
plt.xlabel("epoch")
plt.ylabel("loss")
plt.xticks(range(1,21))
plt.title("Epoch Vs Loss")
plt.show()

```



### 2.3 Algorithm with Adam update of weights

$$\begin{aligned}
m_t &= \beta_1 * m_{t-1} + (1 - \beta_1) * \nabla w_t \\
v_t &= \beta_2 * v_{t-1} + (1 - \beta_2) * (\nabla w_t)^2 \\
\hat{m}_t &= \frac{m_t}{1 - \beta_1^t} \quad \hat{v}_t = \frac{v_t}{1 - \beta_2^t} \\
w_{t+1} &= w_t - \frac{\eta}{\sqrt{\hat{v}_t} + \epsilon} * \hat{m}_t
\end{aligned}$$

```
m = beta1*m + (1-beta1)*dx mt = m / (1-beta1**t) v = beta2*v + (1-beta2)*(dx**2) vt = v / (1-beta2**t) x += - learning_rate * mt / (np.sqrt(vt) + eps)
```

In [14]:

```

eps = 1e-8
beta_1 = 0.9
beta_2 = 0.999
learning_rate = 0.1
weight = np.random.normal(scale = 0.1, size =9)

v_1 = v_2 = v_3 = v_4 = v_5 = v_6 = v_7 = v_8 = v_9 = 0
m_1 = m_2 = m_3 = m_4 = m_5 = m_6 = m_7 = m_8 = m_9 = 0
v_hat_1 = v_hat_2 = v_hat_3 = v_hat_4 = v_hat_5 = v_hat_6 = v_hat_7 = v_hat_8 = v_hat_9 = 0
m_hat_1 = m_hat_2 = m_hat_3 = m_hat_4 = m_hat_5 = m_hat_6 = m_hat_7 = m_hat_8 = m_hat_9 = 0

```

```

mean_adam_loss = []

epochs = range(1, 21)
for epoch in epochs:

    adam_loss = []
    for i in range(len(X)):

        forward_dict_ = forward_propagation(X[i], y[i], weight)
        backward_dict_ = backward_propagation(X[i], y[i], weight, forward_dict_)

        m_1 = (beta_1 * m_1) + ((1 - beta_1) * backward_dict_['dw1'])
        m_2 = (beta_1 * m_2) + ((1 - beta_1) * backward_dict_['dw2'])
        m_3 = (beta_1 * m_3) + ((1 - beta_1) * backward_dict_['dw3'])
        m_4 = (beta_1 * m_4) + ((1 - beta_1) * backward_dict_['dw4'])
        m_5 = (beta_1 * m_5) + ((1 - beta_1) * backward_dict_['dw5'])
        m_6 = (beta_1 * m_6) + ((1 - beta_1) * backward_dict_['dw6'])
        m_7 = (beta_1 * m_7) + ((1 - beta_1) * backward_dict_['dw7'])
        m_8 = (beta_1 * m_8) + ((1 - beta_1) * backward_dict_['dw8'])
        m_9 = (beta_1 * m_9) + ((1 - beta_1) * backward_dict_['dw9'])

        m_hat_1 = m_1 / (1 - (beta_1 ** epoch))
        m_hat_2 = m_2 / (1 - (beta_1 ** epoch))
        m_hat_3 = m_3 / (1 - (beta_1 ** epoch))
        m_hat_4 = m_4 / (1 - (beta_1 ** epoch))
        m_hat_5 = m_5 / (1 - (beta_1 ** epoch))
        m_hat_6 = m_6 / (1 - (beta_1 ** epoch))
        m_hat_7 = m_7 / (1 - (beta_1 ** epoch))
        m_hat_8 = m_8 / (1 - (beta_1 ** epoch))
        m_hat_9 = m_9 / (1 - (beta_1 ** epoch))

        v_1 = (beta_2 * v_1) + ((1 - beta_2) * (backward_dict_['dw1'] ** 2))
        v_2 = (beta_2 * v_2) + ((1 - beta_2) * (backward_dict_['dw2'] ** 2))
        v_3 = (beta_2 * v_3) + ((1 - beta_2) * (backward_dict_['dw3'] ** 2))
        v_4 = (beta_2 * v_4) + ((1 - beta_2) * (backward_dict_['dw4'] ** 2))
        v_5 = (beta_2 * v_5) + ((1 - beta_2) * (backward_dict_['dw5'] ** 2))
        v_6 = (beta_2 * v_6) + ((1 - beta_2) * (backward_dict_['dw6'] ** 2))
        v_7 = (beta_2 * v_7) + ((1 - beta_2) * (backward_dict_['dw7'] ** 2))
        v_8 = (beta_2 * v_8) + ((1 - beta_2) * (backward_dict_['dw8'] ** 2))
        v_9 = (beta_2 * v_9) + ((1 - beta_2) * (backward_dict_['dw9'] ** 2))

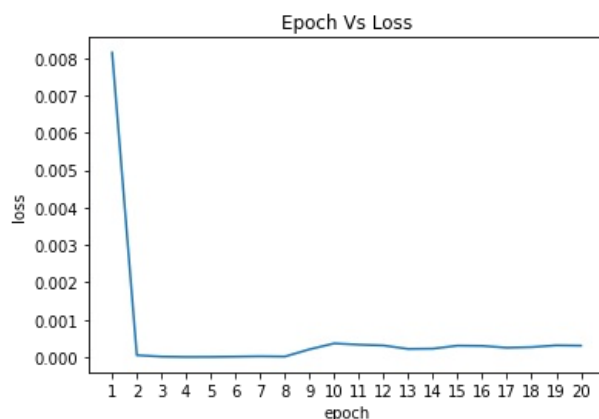
        v_hat_1 = v_1 / (1 - (beta_2 ** epoch))
        v_hat_2 = v_2 / (1 - (beta_2 ** epoch))
        v_hat_3 = v_3 / (1 - (beta_2 ** epoch))
        v_hat_4 = v_4 / (1 - (beta_2 ** epoch))
        v_hat_5 = v_5 / (1 - (beta_2 ** epoch))
        v_hat_6 = v_6 / (1 - (beta_2 ** epoch))
        v_hat_7 = v_7 / (1 - (beta_2 ** epoch))
        v_hat_8 = v_8 / (1 - (beta_2 ** epoch))
        v_hat_9 = v_9 / (1 - (beta_2 ** epoch))

        weight[0] = weight[0] - ((learning_rate * m_hat_1) / np.sqrt(v_hat_1 + eps))
        weight[1] = weight[1] - ((learning_rate * m_hat_2) / np.sqrt(v_hat_2 + eps))
        weight[2] = weight[2] - ((learning_rate * m_hat_3) / np.sqrt(v_hat_3 + eps))
        weight[3] = weight[3] - ((learning_rate * m_hat_4) / np.sqrt(v_hat_4 + eps))
        weight[4] = weight[4] - ((learning_rate * m_hat_5) / np.sqrt(v_hat_5 + eps))
        weight[5] = weight[5] - ((learning_rate * m_hat_6) / np.sqrt(v_hat_6 + eps))
        weight[6] = weight[6] - ((learning_rate * m_hat_7) / np.sqrt(v_hat_7 + eps))
        weight[7] = weight[7] - ((learning_rate * m_hat_8) / np.sqrt(v_hat_8 + eps))
        weight[8] = weight[8] - ((learning_rate * m_hat_9) / np.sqrt(v_hat_9 + eps))

    adam_loss.append(forward_dict_['loss'])
    mean_adam_loss.append(mean(adam_loss))

plt.plot(epochs, mean_adam_loss)
plt.xlabel("epoch")
plt.ylabel("loss")
plt.xticks(range(1, 21))
plt.title("Epoch Vs Loss")
plt.show()

```



You can go through the following blog to understand the implementation of other optimizers .

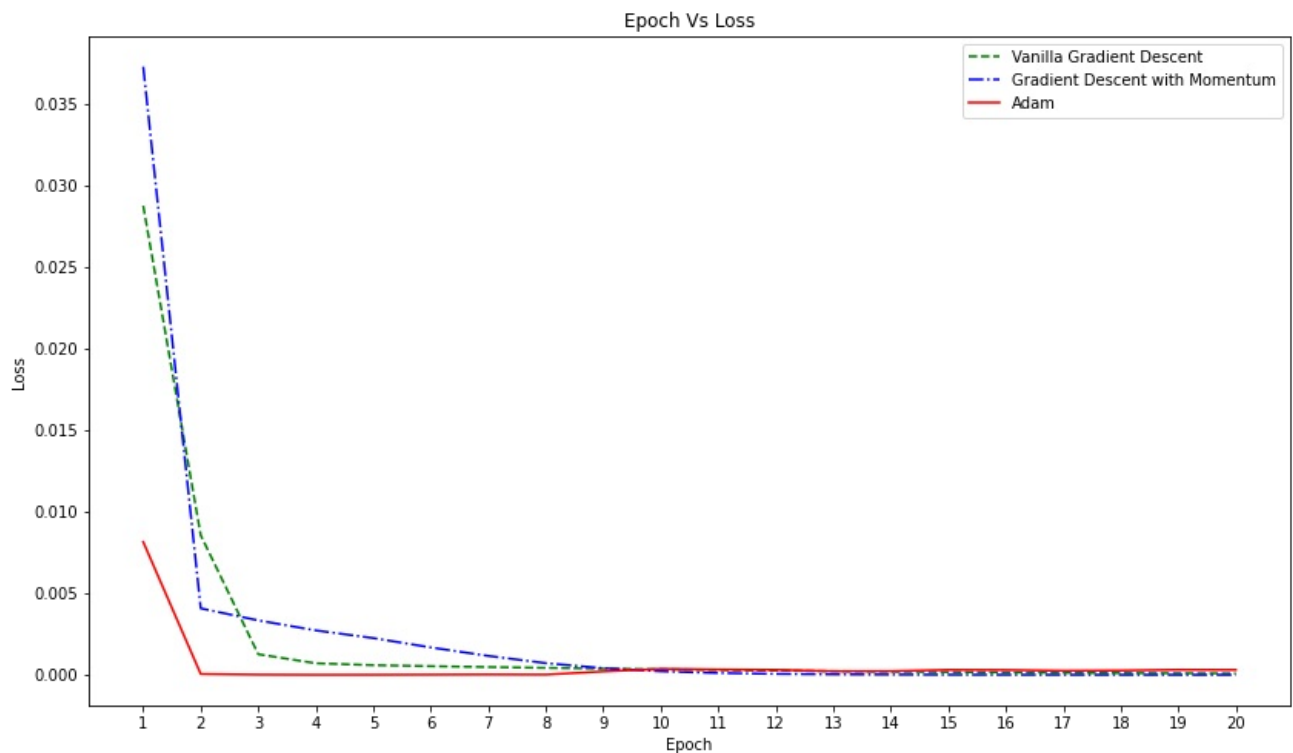
[Gradients update blog](<https://cs231n.github.io/neural-networks-3/>)

Comparison plot between epochs and loss with different optimizers. Make sure that loss is converging with increasing epochs

In [15]:

```
plt.figure(figsize = (14, 8))

plt.plot(epochs, mean_v_loss, c = 'g', linestyle = '--', label = 'Vanilla Gradient Descent')
plt.plot(epochs, mean_momentum_loss, c = 'b', linestyle = '-.', label = 'Gradient Descent with Momentum')
plt.plot(epochs, mean_adam_loss, c = 'r', linestyle = '-', label = 'Adam')
plt.xlabel("Epoch")
plt.ylabel("Loss")
plt.xticks(range(1, 21))
plt.title("Epoch Vs Loss")
plt.legend()
plt.show()
```



Its clear **Adam** converges fast