

## Data Types and Precision vs. Significance:

Mathematical models can help quantify the precision and significance of data. For instance, regression models can be used to understand how precise certain variables (like historical demand data) are in predicting future demand.

## 2. Demand Data

### Forecasting Models:

- **Time Series Analysis:**
  - Model:  $y_t = \alpha + \beta t + \gamma y_{t-1} + \epsilon_t$   $y_t = \alpha + \beta t + \gamma y_{t-1} + \epsilon_t$
  - Description: Predicts future demand  $y_{t+1}$  based on past demand data, time trend, and error term.
- **Exponential Smoothing:**
  - Model:  $S_t = \alpha y_t + (1-\alpha)S_{t-1}$   $S_t = \alpha y_t + (1-\alpha)S_{t-1}$
  - Description: Averages past data with more weight on recent observations.

## 3. Transportation Costs

### Cost Calculation:

- **Total Transportation Cost (TTC):**
  - Model:  $TTC = \sum_{i=1}^n (F_i + V_i Q_i)$   $TTC = \sum_{i=1}^n (F_i + V_i Q_i)$
  - Description: Sum of fixed costs  $F_i$  and variable costs  $V_i$  multiplied by the quantity transported  $Q_i$ .

## 4. Data Aggregation

### Aggregation Levels:

- **Weighted Sum:**
  - Model:  $A = \sum_{i=1}^n w_i x_i$   $A = \sum_{i=1}^n w_i x_i$
  - Description: Aggregating data  $x_i$  with weights  $w_i$ .

## 5. Data Analysis

### Advanced Analytics:

- **Regression Analysis:**
  - Model:  $y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n + \epsilon$   $y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_n x_n + \epsilon$
  - Description: Predicts dependent variable  $y$  based on independent variables  $x_1, x_2, \dots, x_n$  and error term  $\epsilon$ .

## 6. Date of Optimization Fixing

## Rolling Horizon:

- **Dynamic Programming:**

- Model:  $V_t(x) = \max_u \{ R_t(x, u) + \beta V_{t+1}(f(x, u)) \}$   $V_t(x) = \max_u \{ R_t(x, u) + \beta V_{t+1}(f(x, u)) \}$
- Description: Optimizes decisions over a rolling horizon.

## 7. Decision Making in Supply Chain Management

### Scenario Analysis:

- **Monte Carlo Simulation:**

- Model: Uses random sampling to simulate various scenarios and their outcomes.

## 8. Dedicated Fleet

### Fleet Optimization:

- **Vehicle Routing Problem (VRP):**

- Model:  $\min \sum_{k=1}^m \sum_{i=1}^n \sum_{j=1}^n c_{ij} x_{ijk}$   $\min \sum_{k=1}^m \sum_{i=1}^n \sum_{j=1}^n c_{ij} x_{ijk}$
- Constraints:  $\sum_{k=1}^m x_{ijk} = 1$   $\sum_{k=1}^m x_{ijk} = 1$  for all  $i, j$ , ensuring each customer is visited exactly once.
- Description: Minimizes total routing cost  $\sum_{i,j} c_{ij} x_{ijk}$  while ensuring all customers are served.

## 9. Differing Service Level Requirements

### Service Level Agreements (SLAs):

- **Service Level Calculation:**

- Model:  $SL = \frac{\text{Orders Delivered On Time}}{\text{Total Orders}} \times 100\%$   $SL = \frac{\text{Orders Delivered On Time}}{\text{Total Orders}} \times 100\%$
- Description: Measures the percentage of orders delivered on time.

## 10. Product Modelling

### Bill of Materials (BOM):

- **Product Structure Tree:** Represents the hierarchy of components in a product.

## 11. Disruption Costs

### Risk Management:

- **Expected Loss:**

- Model:  $EL = \sum_{i=1}^n p_i L_i$   $EL = \sum_{i=1}^n p_i L_i$
- Description: Sum of probabilities  $p_i$  of disruptions and their respective losses  $L_i$ .

## 12. Capacity Modelling

### Dynamic Capacity Planning:

- **Queuing Theory:**
  - Model:  $L = \lambda W$   $L = \lambda W$
  - Description: Relates average number of items in the system  $L$  to the arrival rate  $\lambda$  and average waiting time  $W$ .

## 13. Constraints in Optimization

### Soft Constraints:

- **Penalty Function:**
  - Model:  $\min_{f(x)} f(x) + \sum_{i=1}^n \lambda_i g_i(x)$   $\min f(x) + \sum_{i=1}^n \lambda_i g_i(x)$
  - Description: Objective function  $f(x)$  plus penalty for constraint violations  $g_i(x)$ .

## 14. Distribution Network Analysis

### Network Simulation:

- **Discrete Event Simulation (DES):**
  - Model: Simulates the operation of a system as a discrete sequence of events over time.

## 15. Evaluating Supply Chain Network Design

### Multi-Criteria Decision Analysis (MCDA):

- **Weighted Sum Model:**
  - Model:  $\text{Score} = \sum_{i=1}^n w_i c_i$   $\text{Score} = \sum_{i=1}^n w_i c_i$
  - Description: Aggregates criteria  $c_i$  with weights  $w_i$ .

## 16. Geocoding

### Spatial Analysis:

- **Distance Calculation:**
  - Model:  $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$   $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$
  - Description: Euclidean distance between two geographic points.

## 17. Geography in Supply Chain

### Geopolitical Factors:

- **Trade Model:**
  - Model:  $C = \sum_{i=1}^n t_i Q_i$
  - Description: Cost CCC based on tariffs  $t_i$  and quantities  $Q_i$ .

## 18. Baseline in Supply Chain Modelling

### Benchmarking:

- **Performance Benchmark:**
  - Model:  $P = \frac{\text{Current Performance}}{\text{Benchmark Performance}} \times 100\%$
  - Description: Compares current performance to a benchmark.

## 19. Labor and Sensitivity Analysis

### Labor Productivity:

- **Productivity Calculation:**
  - Model:  $P = \frac{\text{Output}}{\text{Labor Input}}$
  - Description: Measures output per labor unit.

## 20. Infeasible Solutions

### Feasibility Checks:

- **Constraint Satisfaction:**
  - Model: If  $g_i(x) \leq 0$ , solution is feasible.
  - Description: Checks if constraints  $g_i(x)$  are satisfied.

## 21. Per Unit Cost

### Activity-Based Costing (ABC):

- **Cost Allocation:**
  - Model:  $C = \sum_{i=1}^n A_i C_i$
  - Description: Allocates costs CCC based on activities  $A_i$ .

## 22. Weighted Average Location and Position

### Centroid Method:

- **Optimal Location:**

- Model:  

$$\text{Latitude}_{\text{optimal}} = \frac{\sum_{i=1}^n \text{Latitude}_i \times \text{Demand}_i}{\sum_{i=1}^n \text{Demand}_i}$$
- Description: Finds the optimal latitude considering demand weights.

## 23. What-If Scenarios

### Scenario Planning:

- **Linear Programming:**
  - Model:  $\max_{x_i} \sum_{i=1}^n c_i x_i$
  - Constraints:  $\sum_{j=1}^m a_{ij} x_j \leq b_i$
  - Description: Maximizes objective  $\sum_{i=1}^n c_i x_i$  subject to constraints  $\sum_{j=1}^m a_{ij} x_j \leq b_i$ .