

Time Series Analysis on Tata motors sales

```
library(ggplot2)
library(tseries)
```

```
## Registered S3 method overwritten by 'quantmod':
##   method           from
##   as.zoo.data.frame zoo
```

```
library(imputeTS)
```

```
##
## Attaching package: 'imputeTS'
```

```
## The following object is masked from 'package:tseries':
##   na.remove
```

```
library(forecast)
# library(greybox)
# library(smooth)
library(graphics)
library(datasets)
library(fpp2)
```

```
## — Attaching packages ————— fpp2 2.4 —
```

```
## ✓ fma      2.4     ✓ expsmooth 2.3
```

```
##
```

```
library(TTR)
```

Importing data

```
data = read.csv("Data/tata_data.csv")
head(data)
```

```
##           Date Sales
## 1 01-04-2001  9683
## 2 01-05-2001 11831
## 3 01-06-2001 13823
## 4 01-07-2001 12249
## 5 01-08-2001 14423
## 6 01-09-2001 15358
```

Converting data into time-series object

```
df = ts(data$Sales, start = c(2001,4), frequency = 12)
df
```

```

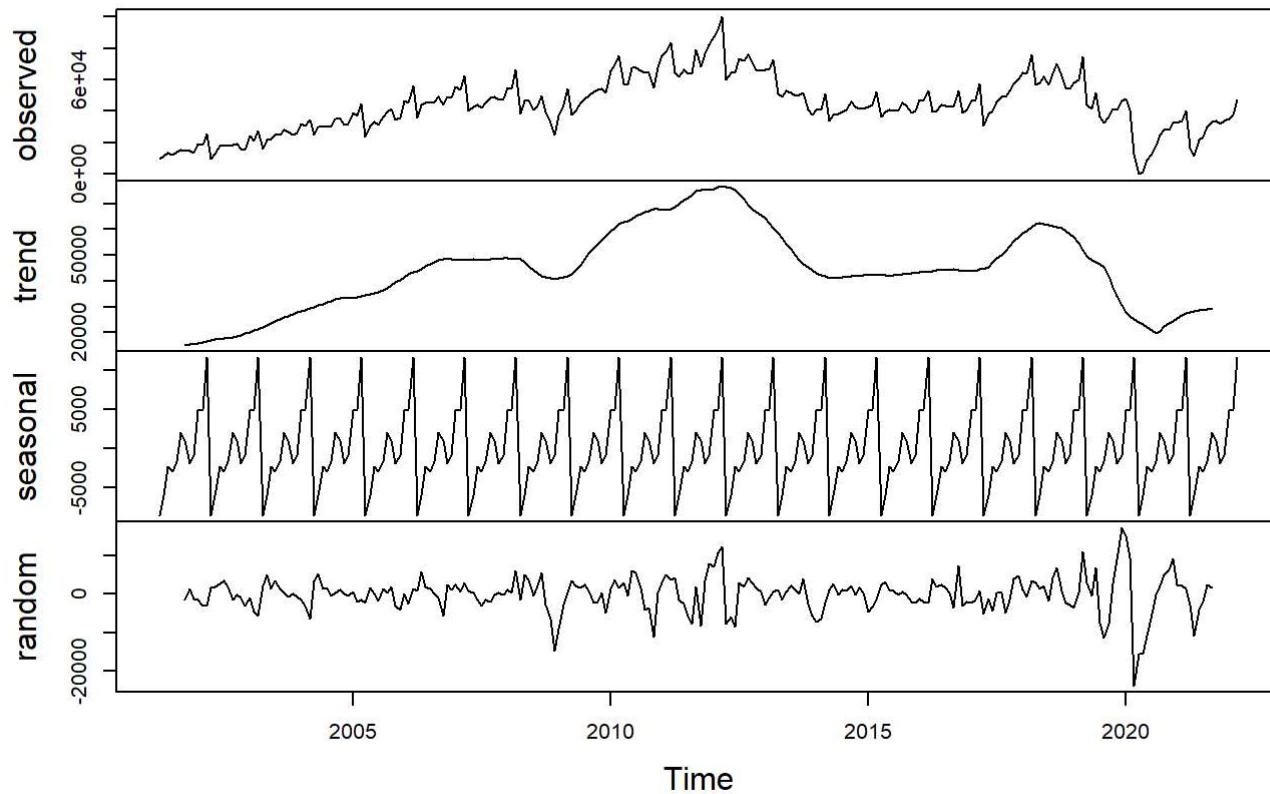
##          Jan   Feb   Mar   Apr   May   Jun   Jul   Aug   Sep   Oct
## 2001           9683 11831 13823 12249 14423 15358 14897
## 2002 19325 18342 25402 9970 13066 17733 18107 18113 18885 19294
## 2003 24116 21176 27558 15821 21928 22643 24993 24827 28304 26860
## 2004 31839 30800 34714 24961 29774 30183 30057 30113 35406 35283
## 2005 39000 36977 44432 23889 30593 33017 31173 36206 39707 41338
## 2006 46635 45113 56406 36082 44357 45223 45056 45681 49157 43770
## 2007 55440 53707 62779 40486 42558 44317 42098 45144 48347 49354
## 2008 54796 54181 66495 38149 46339 47245 40729 43576 49647 39729
## 2009 36931 43811 54076 37518 40196 45399 48054 49810 52513 53404
## 2010 65478 69427 75151 57202 56777 67730 67799 65938 64668 64757
## 2011 75423 77543 83363 64383 62105 66360 63761 64078 78783 68008
## 2012 87467 92119 100414 60086 64347 64341 73491 71826 75773 71770
## 2013 66500 66500 72712 51160 49304 52708 51468 49611 50387 51638
## 2014 40863 40863 51184 33892 37525 38557 39619 40883 46119 42819
## 2015 42582 44209 52479 36145 39496 40869 40154 40690 45215 43486
## 2016 47035 46674 53057 39382 40071 44276 43160 43061 43061 52813
## 2017 46349 47574 57145 30972 38361 40358 46216 48988 48988 53197
## 2018 64624 63761 76153 56521 57994 62019 56867 63757 69991 62264
## 2019 58185 60151 74679 43979 41792 51774 36312 32343 36376 41354
## 2020 47862 40634 12924    0 1488  8824 12688 17889 24876 28472
## 2021 32816 33859 40462 16644 11401 22100 23848 29781 33258 33674
## 2022 35268 37552 47050

##          Nov   Dec
## 2001 14726 13406
## 2002 16148 15695
## 2003 25265 26254
## 2004 31428 31951
## 2005 34282 35598
## 2006 49061 48792
## 2007 46947 47678
## 2008 32696 25219
## 2009 54108 51627
## 2010 54622 67494
## 2011 76823 82279
## 2012 66500 65582
## 2013 40863 37836
## 2014 41720 41734
## 2015 38918 39973
## 2016 38900 40944
## 2017 57391 60920
## 2018 55074 54439
## 2019 41124 46903
## 2020 27982 32869
## 2021 32245 34151
## 2022

```

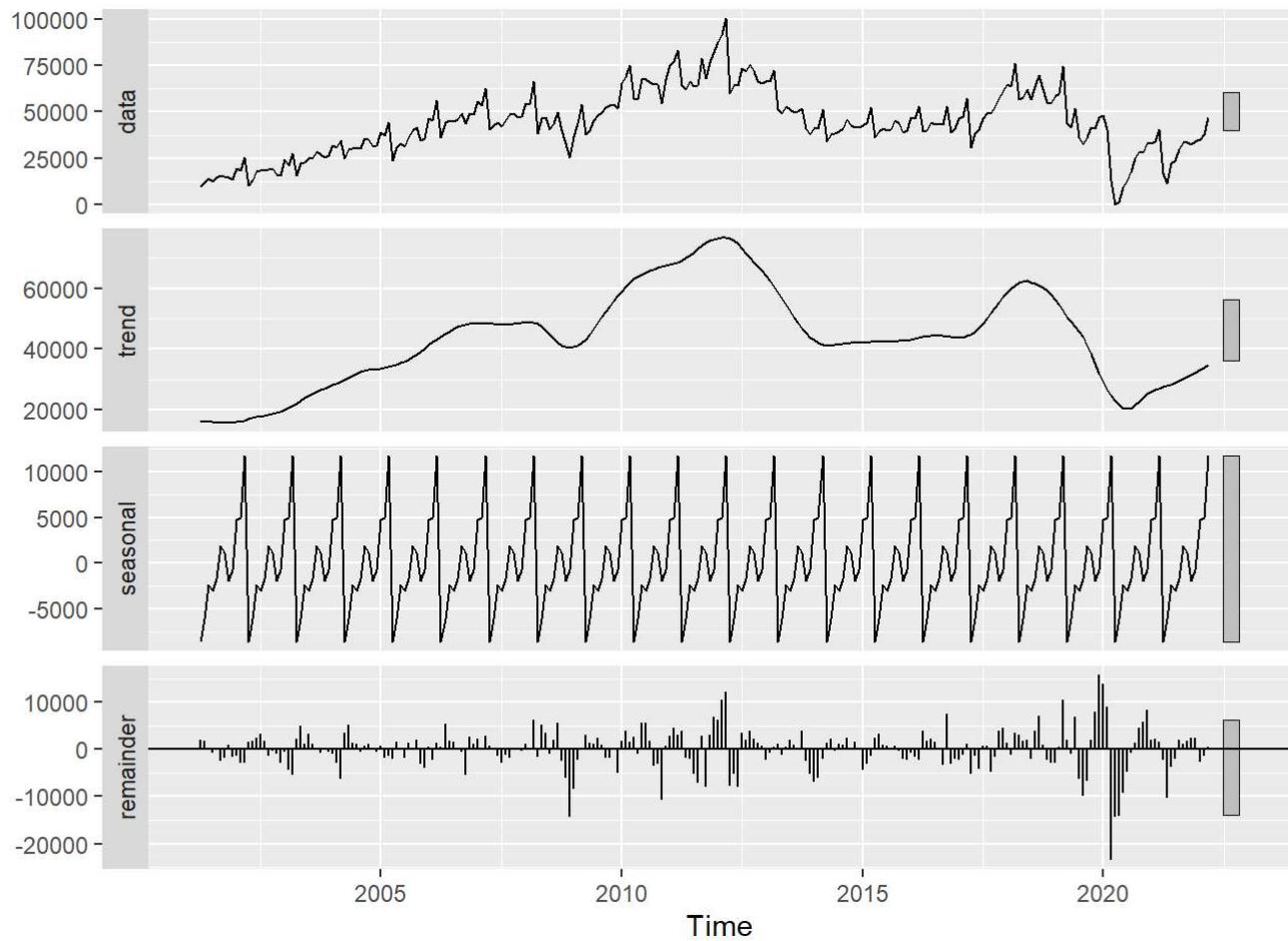
```
plot(decompose(df))
```

Decomposition of additive time series



Decomposition of time series

```
df_decom = stl(df, s.window = "p")
autoplot(df_decom)
```

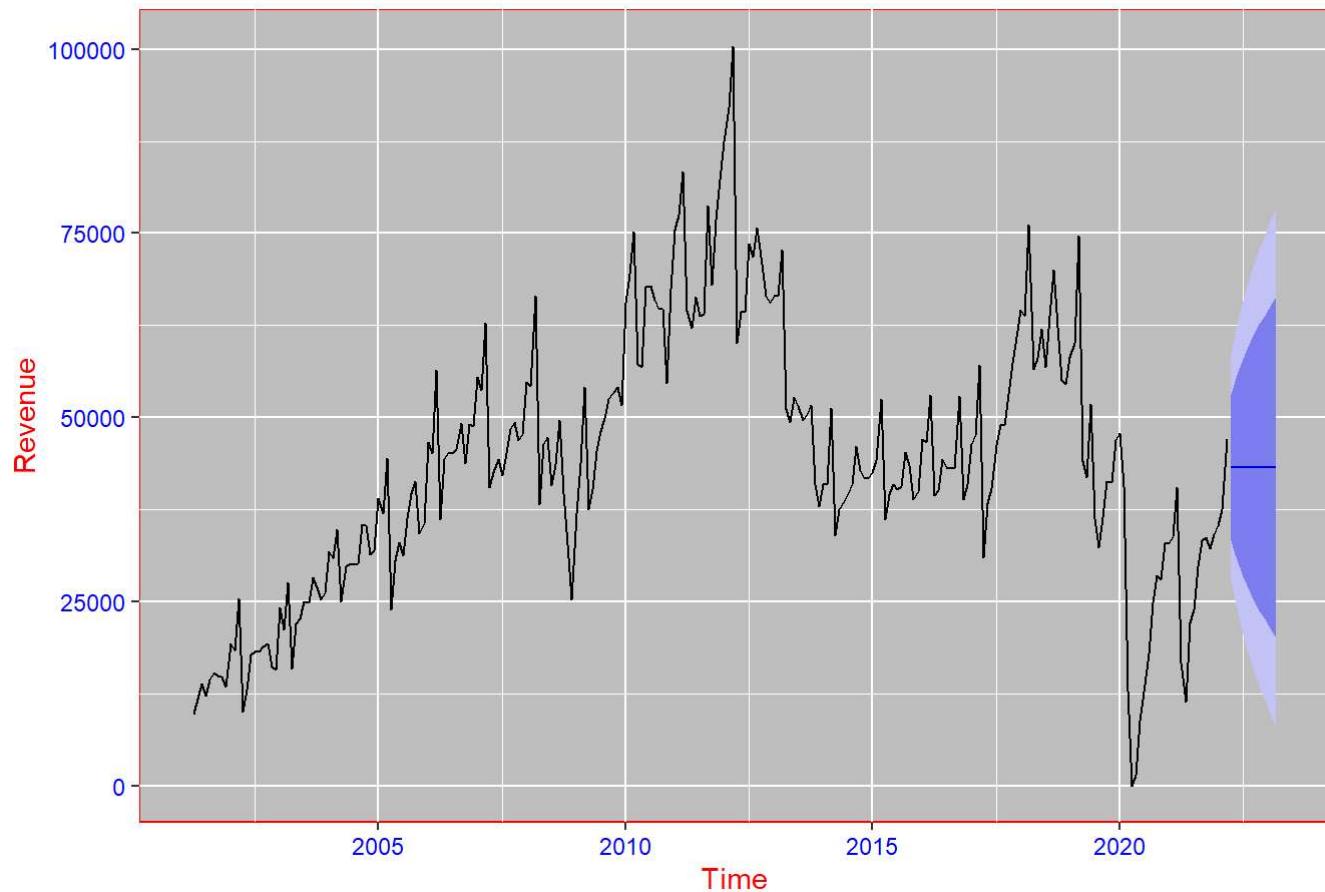


Simple exponential smoothing method

```
df_ses = ses(df, h=12)

autoplot(df_ses)+ xlab("Time") + ylab("Revenue") + theme(panel.background = element_rect(fill = "gray", colour = "red"), axis.text.x = element_text(colour = "blue"), axis.text.y = element_text(colour = "blue"), axis.title.x.bottom = element_text(colour = "red"), axis.title.y.left = element_text(color = "red"))
```

Forecasts from Simple exponential smoothing



```
summary(df_ses)
```

```

## Forecast method: Simple exponential smoothing
##
## Model Information:
## Simple exponential smoothing
##
## Call:
##   ses(y = df, h = 12)
##
## Smoothing parameters:
##   alpha = 0.6354
##
## Initial states:
##   l = 10693.3147
##
## sigma: 7746.86
##
##      AIC     AICc      BIC
## 5910.750 5910.847 5921.338
##
## Error measures:
##             ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set 202.9963 7716.057 5399.643 -Inf  Inf 0.5463252 0.05347263
##
## Forecasts:
##           Point Forecast    Lo 80    Hi 80    Lo 95    Hi 95
## Apr 2022      43198.94 33270.94 53126.94 28015.373 58382.51
## May 2022      43198.94 31436.14 54961.74 25209.295 61188.58
## Jun 2022      43198.94 29851.22 56546.66 22785.367 63612.51
## Jul 2022      43198.94 28435.48 57962.40 20620.175 65777.70
## Aug 2022      43198.94 27144.10 59253.78 18645.177 67752.70
## Sep 2022      43198.94 25949.12 60448.76 16817.623 69580.26
## Oct 2022      43198.94 24831.73 61566.15 15108.718 71289.16
## Nov 2022      43198.94 23778.52 62619.36 13497.977 72899.90
## Dec 2022      43198.94 22779.57 63618.31 11970.206 74427.67
## Jan 2023      43198.94 21827.25 64570.63 10513.768 75884.11
## Feb 2023      43198.94 20915.60 65482.28 9119.516 77278.36
## Mar 2023      43198.94 20039.81 66358.07 7780.107 78617.77

```

Double exponential exponential smoothing

```

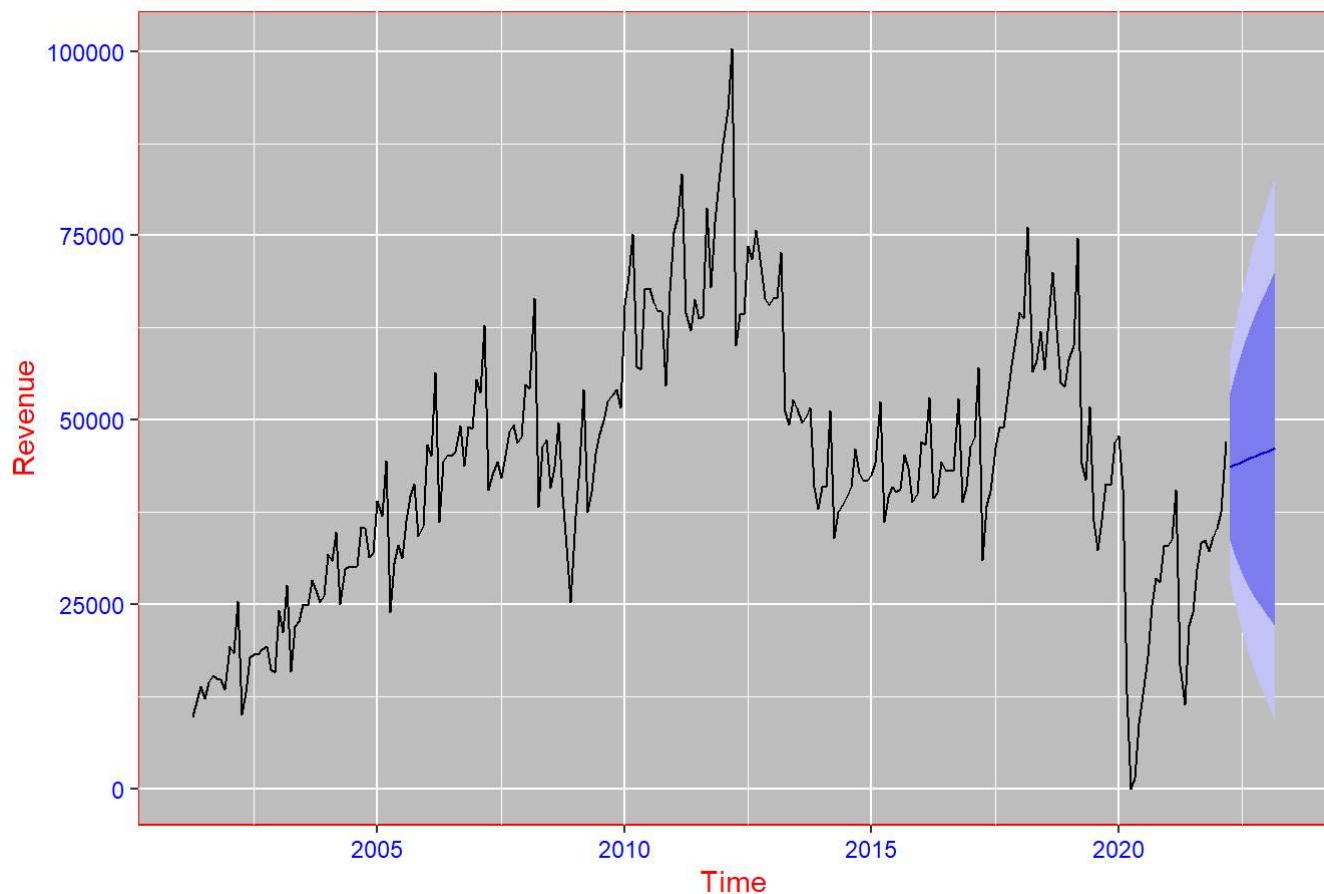
df_dex = holt(df, h = 12)
df_dex

```

```
##          Point Forecast    Lo 80     Hi 80     Lo 95     Hi 95
## Apr 2022      43627.54 33622.43 53632.66 28326.038 58929.05
## May 2022      43857.20 31943.83 55770.57 25637.279 62077.12
## Jun 2022      44086.86 30515.73 57657.98 23331.612 64842.10
## Jul 2022      44316.52 29255.11 59377.92 21282.082 67350.95
## Aug 2022      44546.17 28116.26 60976.08 19418.796 69673.55
## Sep 2022      44775.83 27070.88 62480.78 17698.440 71853.22
## Oct 2022      45005.49 26099.97 63911.00 16091.995 73918.98
## Nov 2022      45235.14 25190.11 65280.18 14578.907 75891.38
## Dec 2022      45464.80 24331.36 66598.24 13143.994 77785.60
## Jan 2023      45694.46 23516.15 67872.76 11775.672 79613.24
## Feb 2023      45924.11 22738.56 69109.67 10464.867 81383.36
## Mar 2023      46153.77 21993.82 70313.72 9204.319 83103.22
```

```
autoplot(df_dex)+ xlab("Time") + ylab("Revenue") + theme(panel.background = element_rect(fill = "gray", colour = "red"), axis.text.x = element_text(colour = "blue"), axis.text.y = element_text(colour = "blue"), axis.title.x.bottom = element_text(colour = "red"), axis.title.y.left = element_text(color = "red"))
```

Forecasts from Holt's method



```
summary(df_dex)
```

```

## 
## Forecast method: Holt's method
## 
## Model Information:
## Holt's method
## 
## Call:
## holt(y = df, h = 12)
## 
## Smoothing parameters:
##   alpha = 0.6432
##   beta  = 0.0032
## 
## Initial states:
##   l = 11185.9782
##   b = 673.9394
## 
## sigma: 7807.035
## 
##      AIC     AICc      BIC
## 5916.625 5916.869 5934.273
## 
## Error measures:
##             ME      RMSE      MAE      MPE      MAPE      MASE      ACF1
## Training set -543.0159 7744.826 5304.082 -Inf  Inf 0.5366565 0.04637631
## 
## Forecasts:
##           Point Forecast    Lo 80     Hi 80     Lo 95     Hi 95
## Apr 2022      43627.54 33622.43 53632.66 28326.038 58929.05
## May 2022       43857.20 31943.83 55770.57 25637.279 62077.12
## Jun 2022       44086.86 30515.73 57657.98 23331.612 64842.10
## Jul 2022        44316.52 29255.11 59377.92 21282.082 67350.95
## Aug 2022        44546.17 28116.26 60976.08 19418.796 69673.55
## Sep 2022        44775.83 27070.88 62480.78 17698.440 71853.22
## Oct 2022        45005.49 26099.97 63911.00 16091.995 73918.98
## Nov 2022        45235.14 25190.11 65280.18 14578.907 75891.38
## Dec 2022        45464.80 24331.36 66598.24 13143.994 77785.60
## Jan 2023        45694.46 23516.15 67872.76 11775.672 79613.24
## Feb 2023        45924.11 22738.56 69109.67 10464.867 81383.36
## Mar 2023        46153.77 21993.82 70313.72 9204.319 83103.22

```

Triple(Holt Winter)exponential smoothing

```

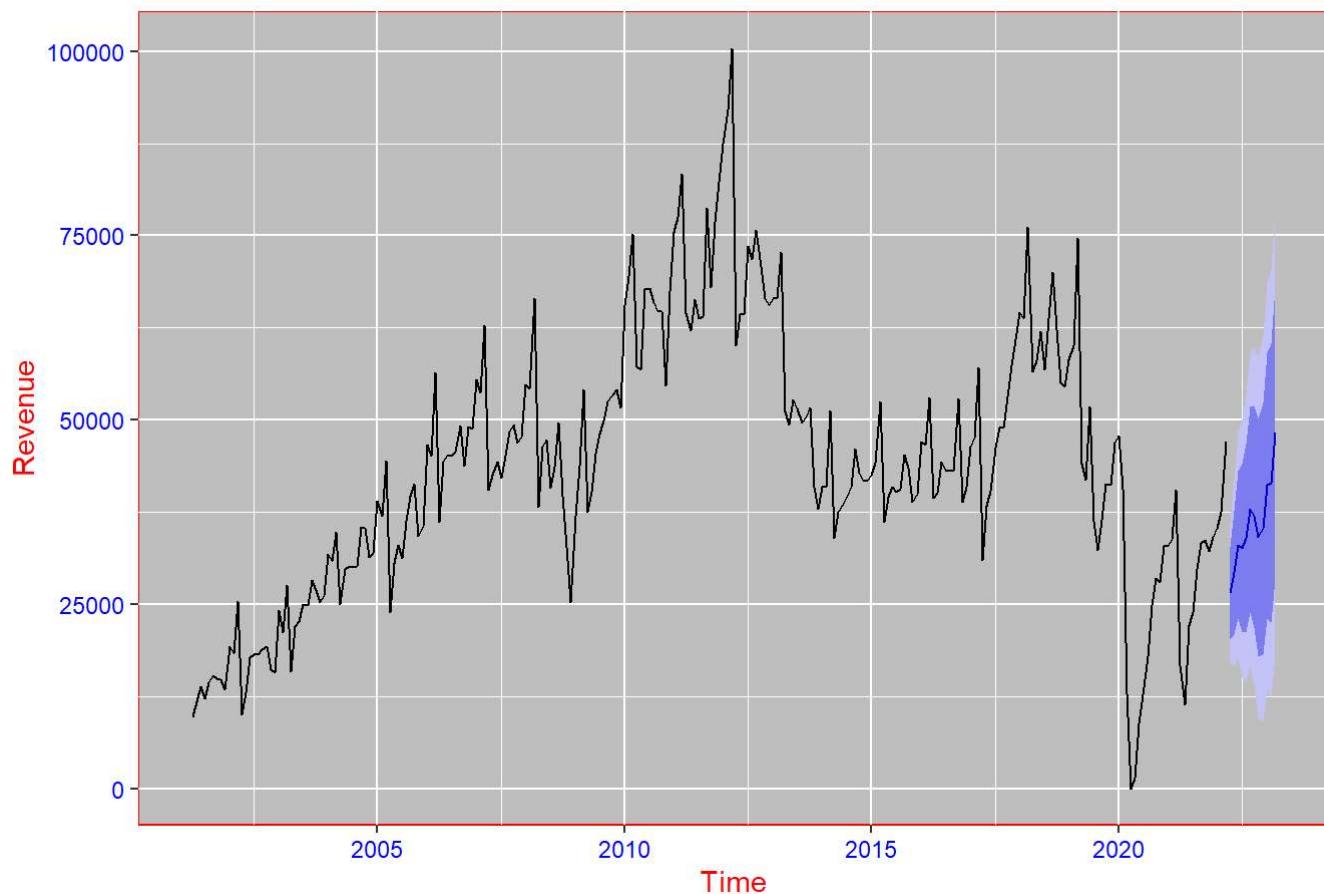
df_hw = hw(df, h=12)
df_hw

```

```
##          Point Forecast    Lo 80     Hi 80     Lo 95     Hi 95
## Apr 2022   26463.27 20243.70 32682.83 16951.258 35975.27
## May 2022   29270.55 20953.18 37587.93 16550.223 41990.88
## Jun 2022   33049.80 23049.79 43049.82 17756.103 48343.51
## Jul 2022   32594.58 21142.54 44046.63 15080.191 50108.98
## Aug 2022   33978.28 21225.72 46730.83 14474.924 53481.63
## Sep 2022   37872.95 23928.88 51817.01 16547.335 59198.56
## Oct 2022   36911.86 21859.32 51964.41 13890.983 59932.75
## Nov 2022   34024.71 17929.50 50119.92 9409.217 58640.20
## Dec 2022   35261.70 18177.55 52345.86 9133.741 61389.67
## Jan 2023   41146.16 23117.88 59174.45 13574.281 68718.05
## Feb 2023   41421.80 22487.46 60356.15 12464.221 70379.38
## Mar 2023   48183.61 28376.01 67991.22 17890.499 78476.73
```

```
autoplot(df_hw)+ xlab("Time") + ylab("Revenue") + theme(panel.background = element_rect(fill = "gray", colour = "red"), axis.text.x = element_text(colour = "blue"), axis.text.y = element_text(colour = "blue"), axis.title.x.bottom = element_text(colour = "red"), axis.title.y.left = element_text(color = "red"))
```

Forecasts from Holt-Winters' additive method



```
summary(df_hw)
```

```

## 
## Forecast method: Holt-Winters' additive method
## 
## Model Information:
## Holt-Winters' additive method
## 
## Call:
##   hw(y = df, h = 12)
## 
## Smoothing parameters:
##   alpha = 0.8832
##   beta  = 0.0047
##   gamma = 1e-04
## 
## Initial states:
##   l = 15488.6332
##   b = 513.675
##   s = 11659.04 5020.318 4868.248 -893.8113 -2008.002 1001.713
##                  2086.399 -1685.689 -2946.29 -2368.218 -6024.297 -8709.416
## 
## sigma: 4853.155
## 
##      AIC     AICc      BIC
## 5688.527 5691.143 5748.528
## 
## Error measures:
##             ME     RMSE      MAE MPE MAPE      MASE      ACF1
## Training set -327.8063 4696.56 3181.131 Inf  Inf 0.3218605 -0.008629628
## 
## Forecasts:
##           Point Forecast    Lo 80     Hi 80     Lo 95     Hi 95
## Apr 2022      26463.27 20243.70 32682.83 16951.258 35975.27
## May 2022      29270.55 20953.18 37587.93 16550.223 41990.88
## Jun 2022      33049.80 23049.79 43049.82 17756.103 48343.51
## Jul 2022      32594.58 21142.54 44046.63 15080.191 50108.98
## Aug 2022      33978.28 21225.72 46730.83 14474.924 53481.63
## Sep 2022      37872.95 23928.88 51817.01 16547.335 59198.56
## Oct 2022      36911.86 21859.32 51964.41 13890.983 59932.75
## Nov 2022      34024.71 17929.50 50119.92 9409.217 58640.20
## Dec 2022      35261.70 18177.55 52345.86 9133.741 61389.67
## Jan 2023      41146.16 23117.88 59174.45 13574.281 68718.05
## Feb 2023      41421.80 22487.46 60356.15 12464.221 70379.38
## Mar 2023      48183.61 28376.01 67991.22 17890.499 78476.73

```

Training and testing of data for holt-Winter

```

df_train = window(df,start = c(2013,4), end = c(2021,2), frequency = 12)
df_train

```

```
##          Jan   Feb   Mar   Apr   May   Jun   Jul   Aug   Sep   Oct   Nov   Dec
## 2013           51160 49304 52708 51468 49611 50387 51638 40863 37836
## 2014 40863 40863 51184 33892 37525 38557 39619 40883 46119 42819 41720 41734
## 2015 42582 44209 52479 36145 39496 40869 40154 40690 45215 43486 38918 39973
## 2016 47035 46674 53057 39382 40071 44276 43160 43061 43061 52813 38900 40944
## 2017 46349 47574 57145 30972 38361 40358 46216 48988 48988 53197 57391 60920
## 2018 64624 63761 76153 56521 57994 62019 56867 63757 69991 62264 55074 54439
## 2019 58185 60151 74679 43979 41792 51774 36312 32343 36376 41354 41124 46903
## 2020 47862 40634 12924      0 1488 8824 12688 17889 24876 28472 27982 32869
## 2021 32816 33859
```

```
df_test = window(df, start = c(2021,3), frequency = 12)
df_test
```

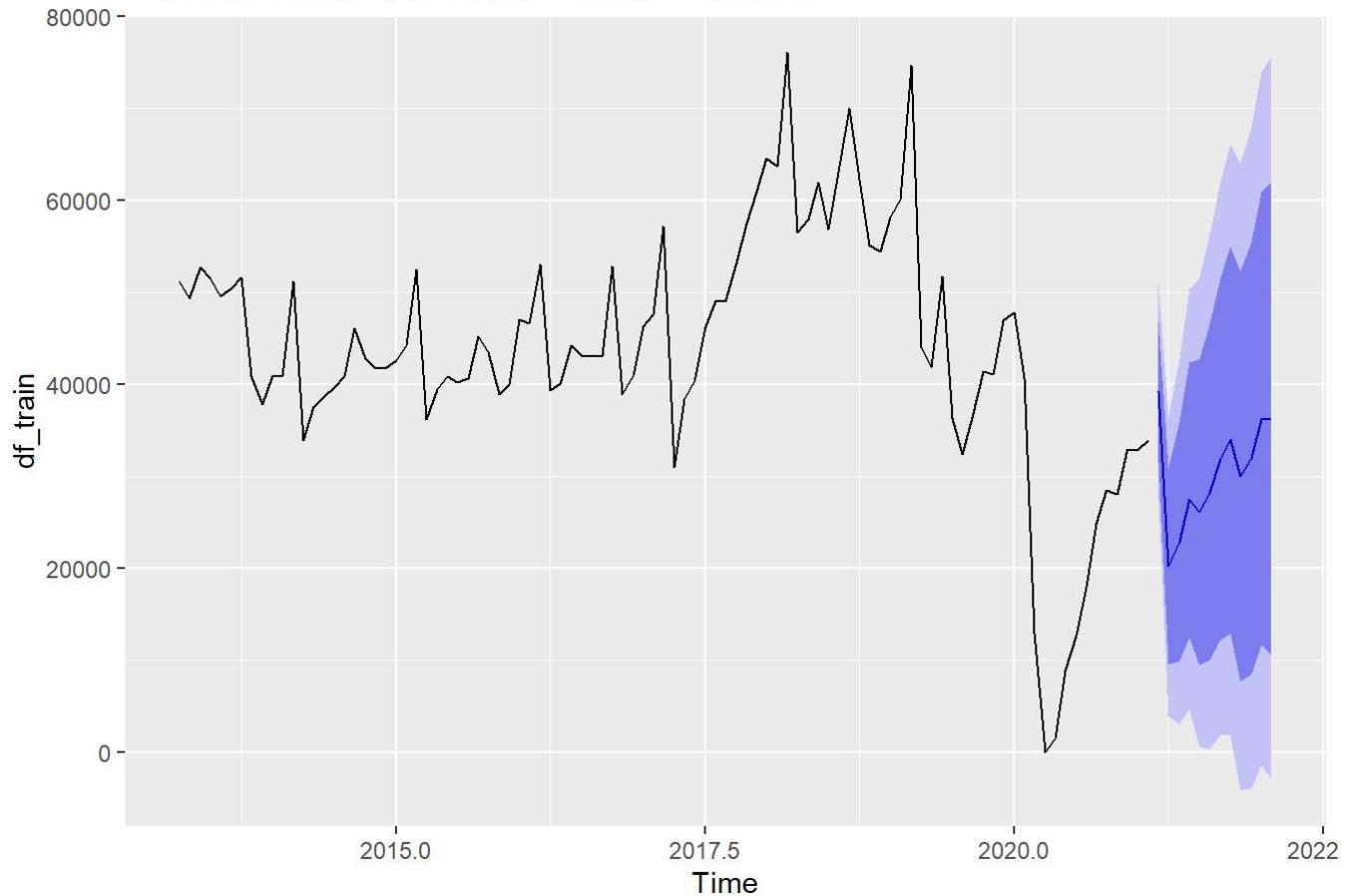
```
##          Jan   Feb   Mar   Apr   May   Jun   Jul   Aug   Sep   Oct   Nov   Dec
## 2021           40462 16644 11401 22100 23848 29781 33258 33674 32245 34151
## 2022 35268 37552 47050
```

```
df_hw_train = hw(df_train,h = 12)
df_hw_train
```

	Point Forecast	Lo 80	Hi 80	Lo 95	Hi 95
## Mar 2021	39201.42	31527.146	46875.69	27464.6302	50938.21
## Apr 2021	20166.14	9504.763	30827.53	3860.9685	36471.32
## May 2021	22849.17	9870.452	35827.88	2999.9360	42698.40
## Jun 2021	27442.78	12501.546	42384.00	4592.1367	50293.41
## Jul 2021	26061.85	9387.164	42736.53	560.1197	51563.57
## Aug 2021	28157.34	9912.861	46401.83	254.8154	56059.87
## Sep 2021	31877.22	12187.413	51567.03	1764.2570	61990.19
## Oct 2021	33973.39	12937.053	55009.73	1801.0895	66145.69
## Nov 2021	29973.36	7671.390	52275.32	-4134.5578	64081.27
## Dec 2021	31977.53	8477.755	55477.30	-3962.2737	67917.33
## Jan 2022	36212.51	11572.855	60852.16	-1470.5874	73895.60
## Feb 2022	36320.85	10591.555	62050.15	-3028.7124	75670.42

```
autoplot(df_hw_train)
```

Forecasts from Holt-Winters' additive method

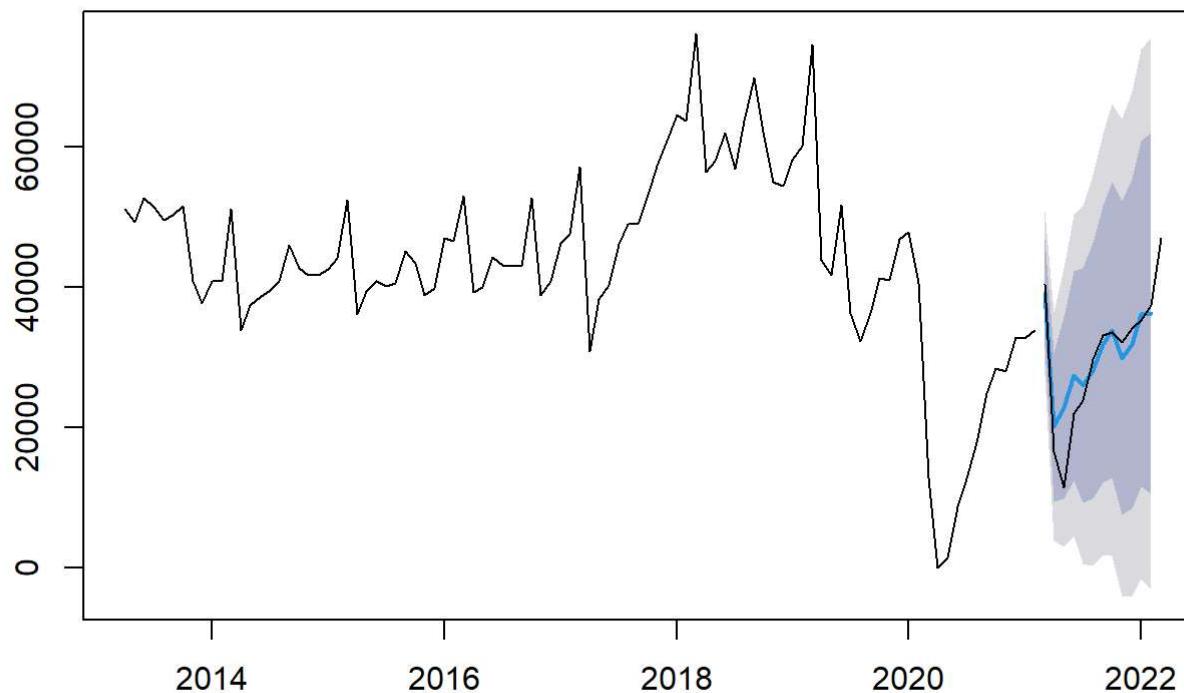


```
accuracy(df_hw_train, df_test)
```

```
##               ME      RMSE      MAE      MPE      MAPE      MASE
## Training set -478.9344 5460.759 3615.728      Inf      Inf 0.3331588
## Test set     -1152.4626 4035.530 2809.342 -10.76618 15.66734 0.2588571
##                   ACF1 Theil's U
## Training set -0.009780104       NA
## Test set      0.490355570 0.7164281
```

```
plot(df_hw_train)
lines(df_test)
```

Forecasts from Holt-Winters' additive method



```
summary(df_hw_train)
```

```

##  

## Forecast method: Holt-Winters' additive method  

##  

## Model Information:  

## Holt-Winters' additive method  

##  

## Call:  

##   hw(y = df_train, h = 12)  

##  

## Smoothing parameters:  

##   alpha = 0.9643  

##   beta  = 1e-04  

##   gamma = 1e-04  

##  

## Initial states:  

##   l = 52913.2716  

##   b = 212.0459  

##   s = 9991.502 4828.538 4928.23 900.0585 -896.6439 3311.234  

##                 1422.19 -2089.809 -3978.229 -2389.644 -6775.394 -9252.032  

##  

## sigma: 5988.268  

##  

##      AIC     AICc     BIC  

## 2101.633 2109.582 2145.049  

##  

## Error measures:  

##      ME     RMSE     MAE MPE MAPE     MASE     ACF1  

## Training set -478.9344 5460.759 3615.728 Inf  Inf 0.3331588 -0.009780104  

##  

## Forecasts:  

##      Point Forecast    Lo 80    Hi 80    Lo 95    Hi 95  

## Mar 2021      39201.42 31527.146 46875.69 27464.6302 50938.21  

## Apr 2021      20166.14  9504.763 30827.53 3860.9685 36471.32  

## May 2021      22849.17  9870.452 35827.88 2999.9360 42698.40  

## Jun 2021      27442.78 12501.546 42384.00 4592.1367 50293.41  

## Jul 2021      26061.85  9387.164 42736.53 560.1197 51563.57  

## Aug 2021      28157.34  9912.861 46401.83 254.8154 56059.87  

## Sep 2021      31877.22 12187.413 51567.03 1764.2570 61990.19  

## Oct 2021      33973.39 12937.053 55009.73 1801.0895 66145.69  

## Nov 2021      29973.36  7671.390 52275.32 -4134.5578 64081.27  

## Dec 2021      31977.53  8477.755 55477.30 -3962.2737 67917.33  

## Jan 2022      36212.51 11572.855 60852.16 -1470.5874 73895.60  

## Feb 2022      36320.85 10591.555 62050.15 -3028.7124 75670.42

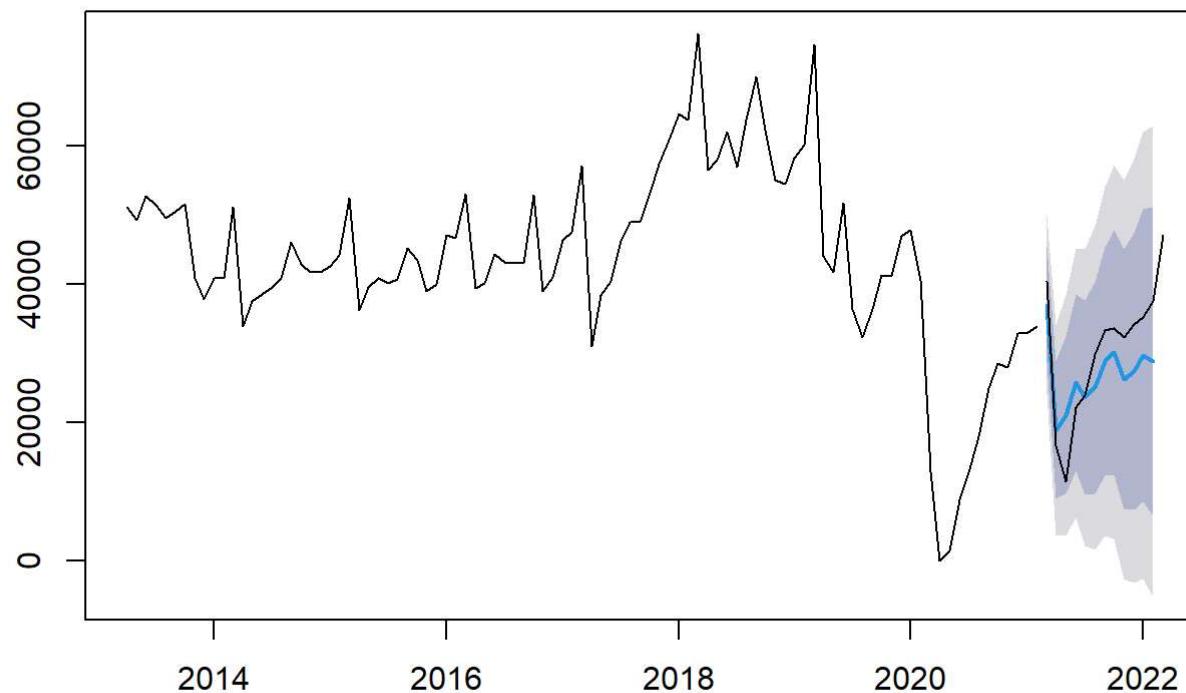
```

```

df_hw_train2 = hw(df_train, alpha = 0.62, beta = .02, gamma = .1, h=12)
plot(df_hw_train2)
lines(df_test)

```

Forecasts from Holt-Winters' additive method



ARIMA Model

```
lags = window(df, start = c(2006,4))  
lags
```

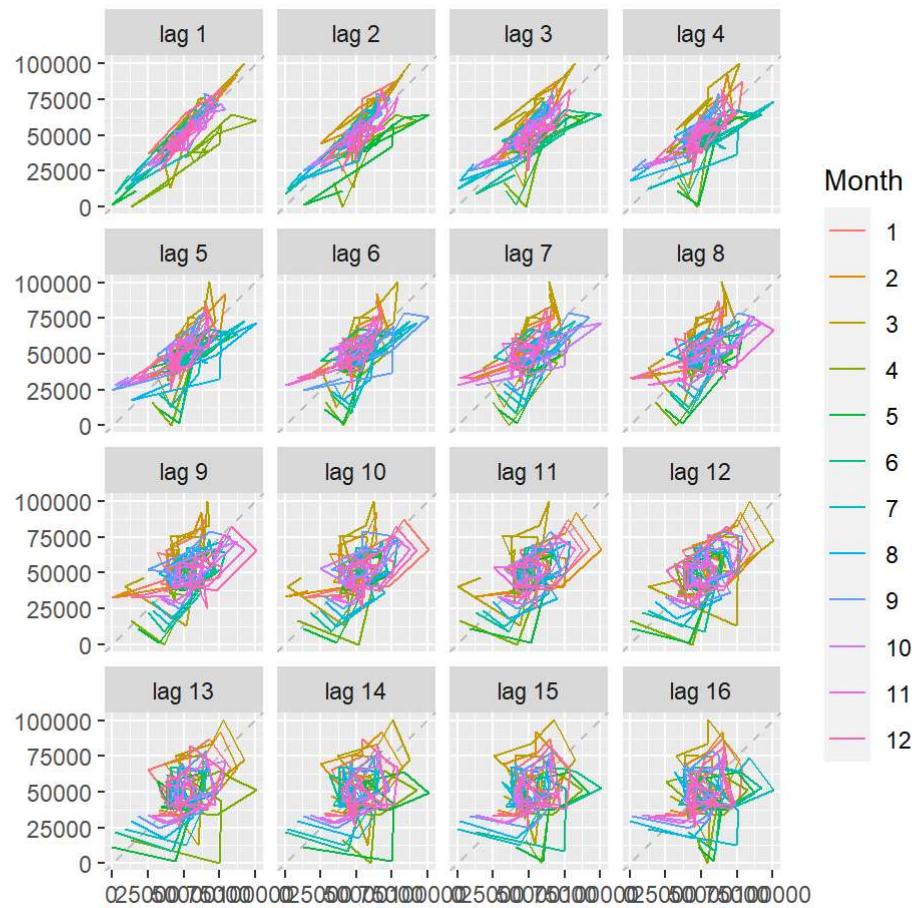
```

##          Jan   Feb   Mar   Apr   May   Jun   Jul   Aug   Sep   Oct
## 2006           36082 44357 45223 45056 45681 49157 43770
## 2007 55440 53707 62779 40486 42558 44317 42098 45144 48347 49354
## 2008 54796 54181 66495 38149 46339 47245 40729 43576 49647 39729
## 2009 36931 43811 54076 37518 40196 45399 48054 49810 52513 53404
## 2010 65478 69427 75151 57202 56777 67730 67799 65938 64668 64757
## 2011 75423 77543 83363 64383 62105 66360 63761 64078 78783 68008
## 2012 87467 92119 100414 60086 64347 64341 73491 71826 75773 71770
## 2013 66500 66500 72712 51160 49304 52708 51468 49611 50387 51638
## 2014 40863 40863 51184 33892 37525 38557 39619 40883 46119 42819
## 2015 42582 44209 52479 36145 39496 40869 40154 40690 45215 43486
## 2016 47035 46674 53057 39382 40071 44276 43160 43061 43061 52813
## 2017 46349 47574 57145 30972 38361 40358 46216 48988 48988 53197
## 2018 64624 63761 76153 56521 57994 62019 56867 63757 69991 62264
## 2019 58185 60151 74679 43979 41792 51774 36312 32343 36376 41354
## 2020 47862 40634 12924      0 1488 8824 12688 17889 24876 28472
## 2021 32816 33859 40462 16644 11401 22100 23848 29781 33258 33674
## 2022 35268 37552 47050

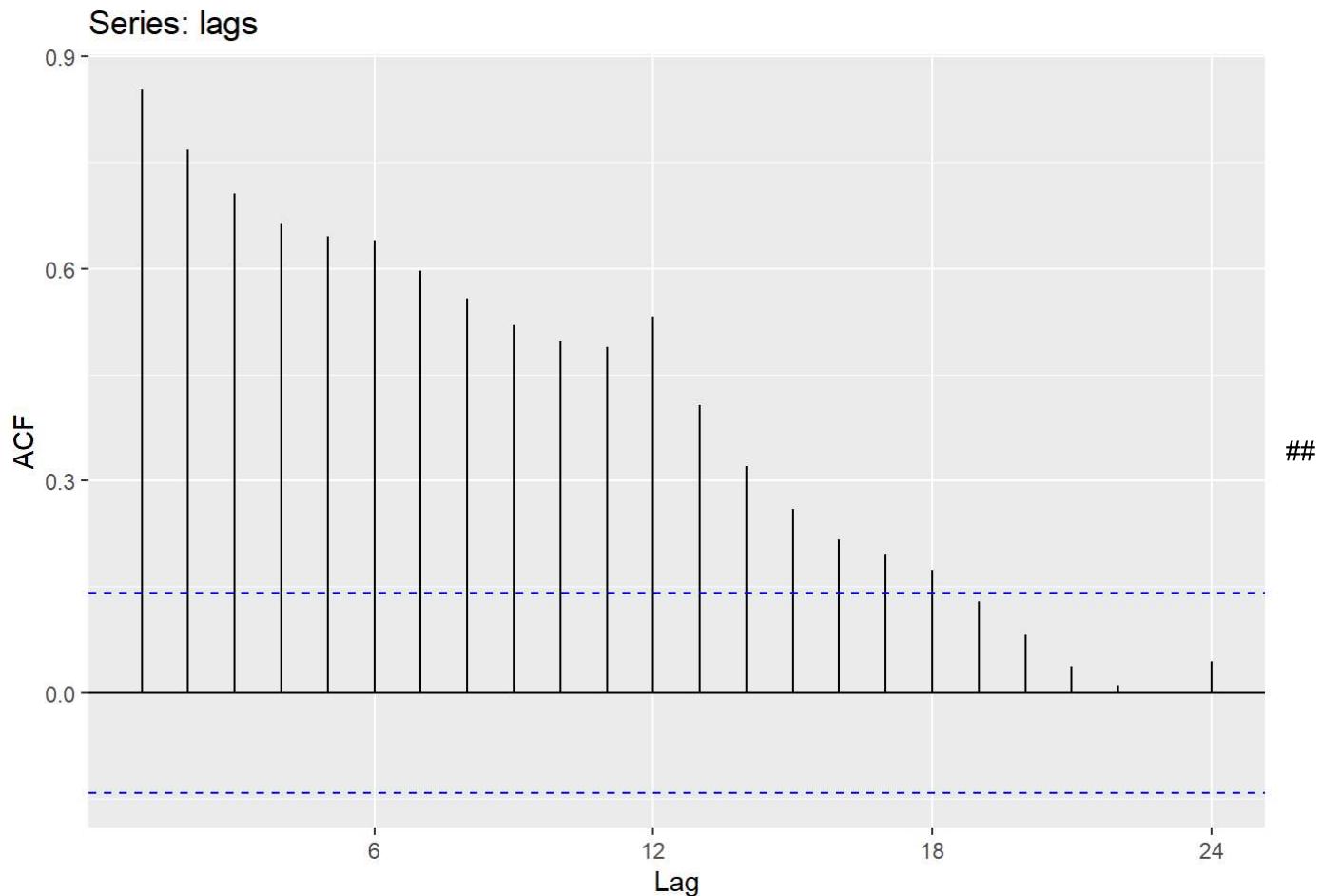
##          Nov   Dec
## 2006 49061 48792
## 2007 46947 47678
## 2008 32696 25219
## 2009 54108 51627
## 2010 54622 67494
## 2011 76823 82279
## 2012 66500 65582
## 2013 40863 37836
## 2014 41720 41734
## 2015 38918 39973
## 2016 38900 40944
## 2017 57391 60920
## 2018 55074 54439
## 2019 41124 46903
## 2020 27982 32869
## 2021 32245 34151
## 2022

```

```
gglagplot(lags)
```



```
ggAcf(lags)
```



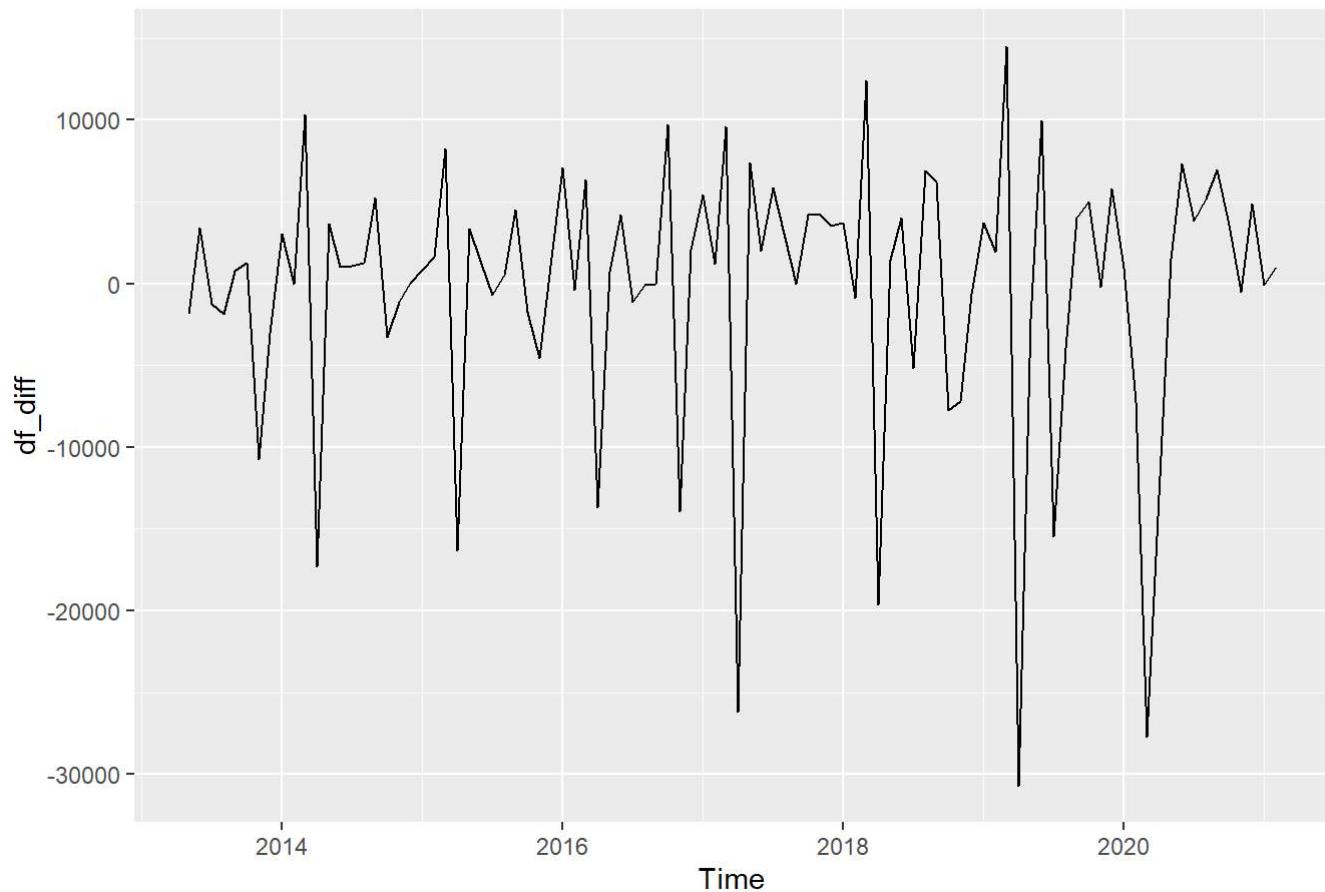
Checking stationarity of the data #### H0 : Data is not stationary #### H1 : Data is stationary

```
adf.test(df)
```

```
##  
##  Augmented Dickey-Fuller Test  
##  
## data: df  
## Dickey-Fuller = -2.1134, Lag order = 6, p-value = 0.5281  
## alternative hypothesis: stationary
```

First order differencing

```
df_diff = diff(df_train,1)  
  
autoplot(df_diff)
```



```
adf.test(df_diff, alternative = "stationary" ,k=0)
```

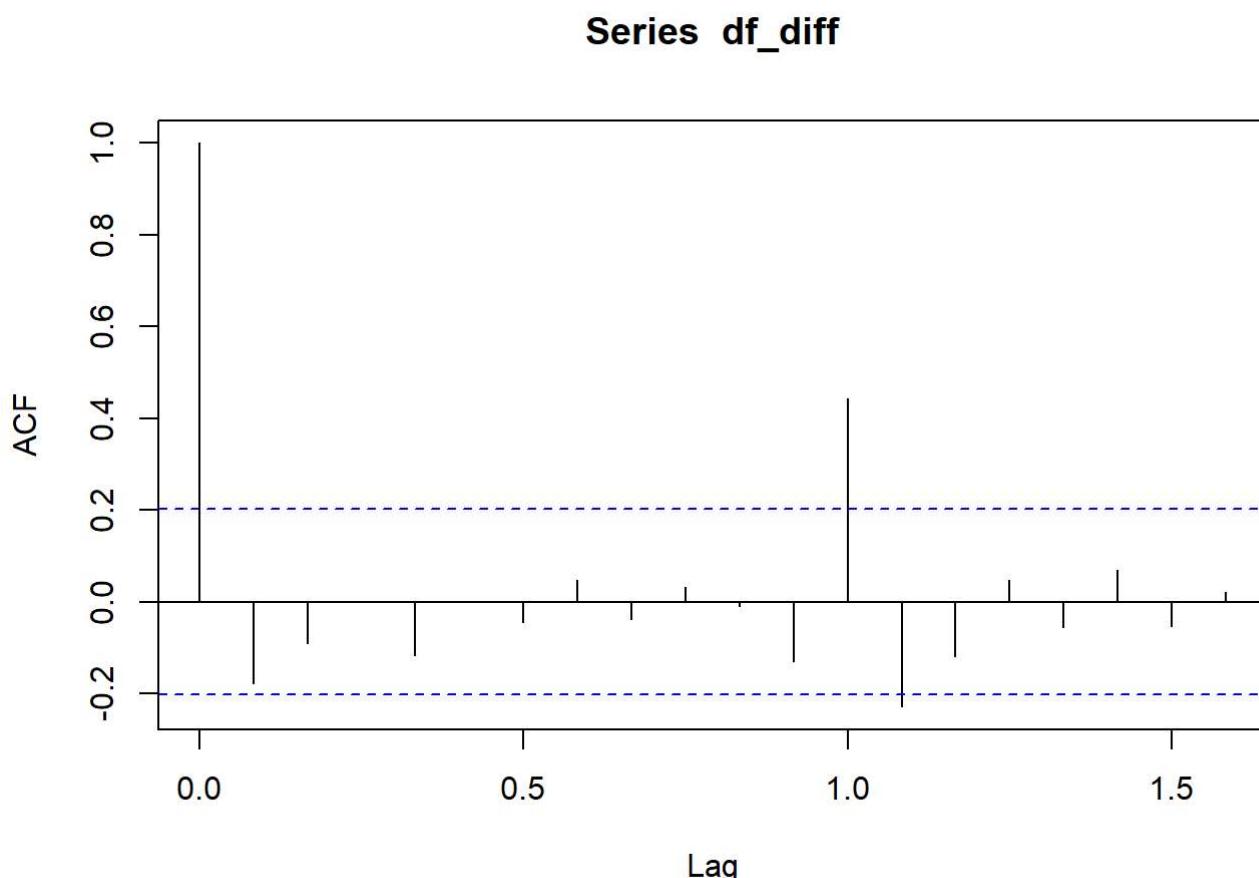
```
## Warning in adf.test(df_diff, alternative = "stationary", k = 0): p-value smaller  
## than printed p-value
```

```
##  
## Augmented Dickey-Fuller Test  
##  
## data: df_diff  
## Dickey-Fuller = -11.357, Lag order = 0, p-value = 0.01  
## alternative hypothesis: stationary
```

```
autoarima.fit.train = auto.arima(df_diff, trace = FALSE, stationary = TRUE, ic="bic")  
autoarima.fit.train
```

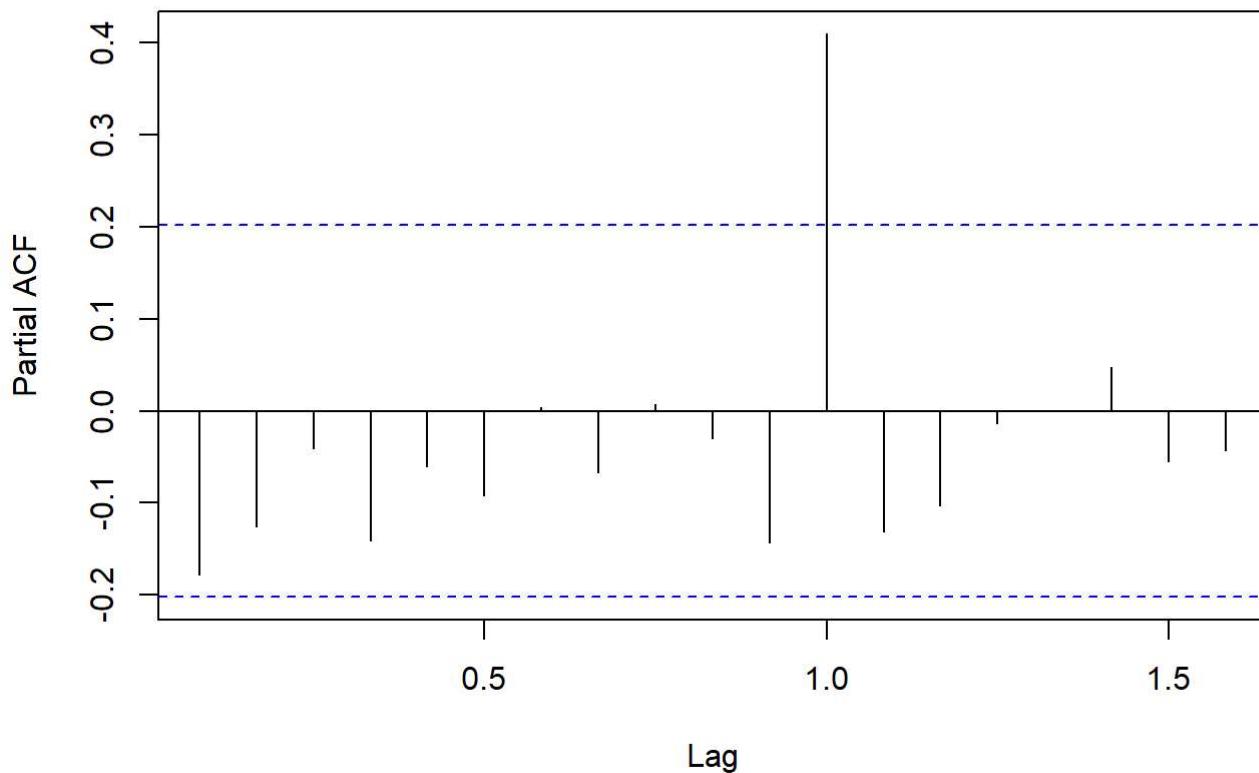
```
## Series: df_diff
## ARIMA(0,0,0)(2,0,0)[12] with zero mean
##
## Coefficients:
##      sar1    sar2
##      0.3267  0.3301
## s.e.  0.1126  0.1313
##
## sigma^2 = 45107720: log likelihood = -963.74
## AIC=1933.48   AICc=1933.74   BIC=1941.11
```

```
acf(df_diff)
```



```
pacf(df_diff)
```

Series df_diff



```
auto_arima_train= auto.arima(df_train, ic="bic", trace = TRUE)
```

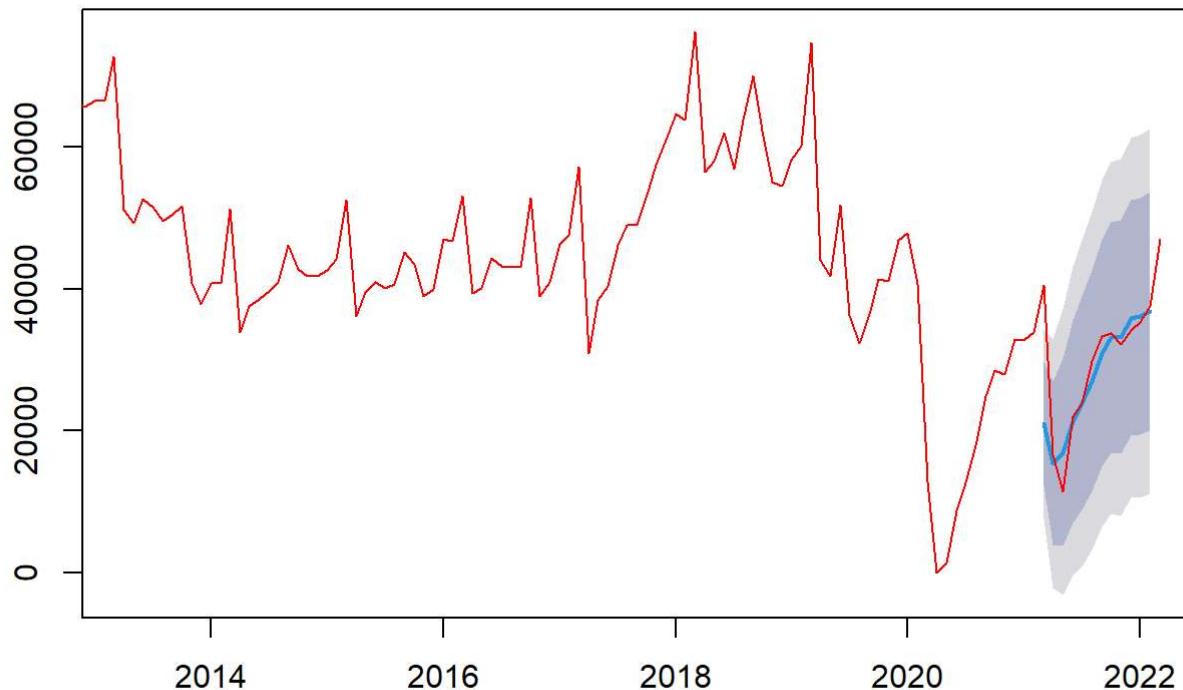
```
##  
## ARIMA(2,0,2)(1,0,1)[12] with non-zero mean : Inf  
## ARIMA(0,0,0) with non-zero mean : 2084.483  
## ARIMA(1,0,0)(1,0,0)[12] with non-zero mean : 1966.424  
## ARIMA(0,0,1)(0,0,1)[12] with non-zero mean : 2016.458  
## ARIMA(0,0,0) with zero mean : 2313.877  
## ARIMA(1,0,0) with non-zero mean : 1984.273  
## ARIMA(1,0,0)(2,0,0)[12] with non-zero mean : 1967.283  
## ARIMA(1,0,0)(1,0,1)[12] with non-zero mean : Inf  
## ARIMA(1,0,0)(0,0,1)[12] with non-zero mean : 1971.859  
## ARIMA(1,0,0)(2,0,1)[12] with non-zero mean : Inf  
## ARIMA(0,0,0)(1,0,0)[12] with non-zero mean : 2086.317  
## ARIMA(2,0,0)(1,0,0)[12] with non-zero mean : 1970.968  
## ARIMA(1,0,1)(1,0,0)[12] with non-zero mean : 1970.968  
## ARIMA(0,0,1)(1,0,0)[12] with non-zero mean : 2024.681  
## ARIMA(2,0,1)(1,0,0)[12] with non-zero mean : 1975.424  
## ARIMA(1,0,0)(1,0,0)[12] with zero mean : 1968.993  
##  
## Best model: ARIMA(1,0,0)(1,0,0)[12] with non-zero mean
```

```
arima_forecast = forecast(auto_arima_train,h=12)
arima_forecast
```

	Point Forecast	Lo 80	Hi 80	Lo 95	Hi 95
## Mar 2021	21028.35	12314.492	29742.21	7701.6524	34355.05
## Apr 2021	15466.82	3983.963	26949.68	-2094.6953	33028.34
## May 2021	17008.36	3853.686	30163.03	-3109.9772	37126.70
## Jun 2021	21372.73	7111.525	35633.94	-437.9030	43183.37
## Jul 2021	23897.58	8873.416	38921.74	920.1048	46875.06
## Aug 2021	27010.57	11448.382	42572.76	3210.2565	50810.89
## Sep 2021	30948.86	15002.010	46895.71	6560.2570	55337.47
## Oct 2021	33123.86	16899.529	49348.19	8310.8881	57936.83
## Nov 2021	33195.36	16769.664	49621.06	8074.4239	58316.30
## Dec 2021	35920.93	19348.486	52493.38	10575.5623	61266.30
## Jan 2022	36128.15	19448.446	52807.85	10618.7444	61637.55
## Feb 2022	36852.37	20094.107	53610.63	11222.8202	62481.91

```
plot(arima_forecast)
lines(df, col="red")
```

Forecasts from ARIMA(1,0,0)(1,0,0)[12] with non-zero mean



Using Moving average method

```
moving_avg = SMA(df_train,n = 3)
moving_avg
```

```
##          Jan       Feb       Mar       Apr       May       Jun       Jul
## 2013           NA           NA 51057.333 51160.000
## 2014 39854.000 39854.000 44303.333 41979.667 40867.000 36658.000 38567.000
## 2015 42012.000 42841.667 46423.333 44277.667 42706.667 38836.667 40173.000
## 2016 41975.333 44560.667 48922.000 46371.000 44170.000 41243.000 42502.333
## 2017 42064.333 44955.667 50356.000 45230.333 42159.333 36563.667 41645.000
## 2018 60978.333 63101.667 68179.333 65478.333 63556.000 58844.667 58960.000
## 2019 55899.333 57591.667 64338.333 59603.000 53483.333 45848.333 43292.667
## 2020 45296.333 45133.000 33806.667 17852.667 4804.000 3437.333 7666.667
## 2021 31222.333 33181.333
##          Aug       Sep       Oct       Nov       Dec
## 2013 51262.333 50488.667 50545.333 47629.333 43445.667
## 2014 39686.333 42207.000 43273.667 43552.667 42091.000
## 2015 40571.000 42019.667 43130.333 42539.667 40792.333
## 2016 43499.000 43094.000 46311.667 44924.667 44219.000
## 2017 45187.333 48064.000 50391.000 53192.000 57169.333
## 2018 60881.000 63538.333 65337.333 62443.000 57259.000
## 2019 40143.000 35010.333 36691.000 39618.000 43127.000
## 2020 13133.667 18484.333 23745.667 27110.000 29774.333
## 2021
```

```
forecast_ma = forecast(moving_avg,h=12)
```

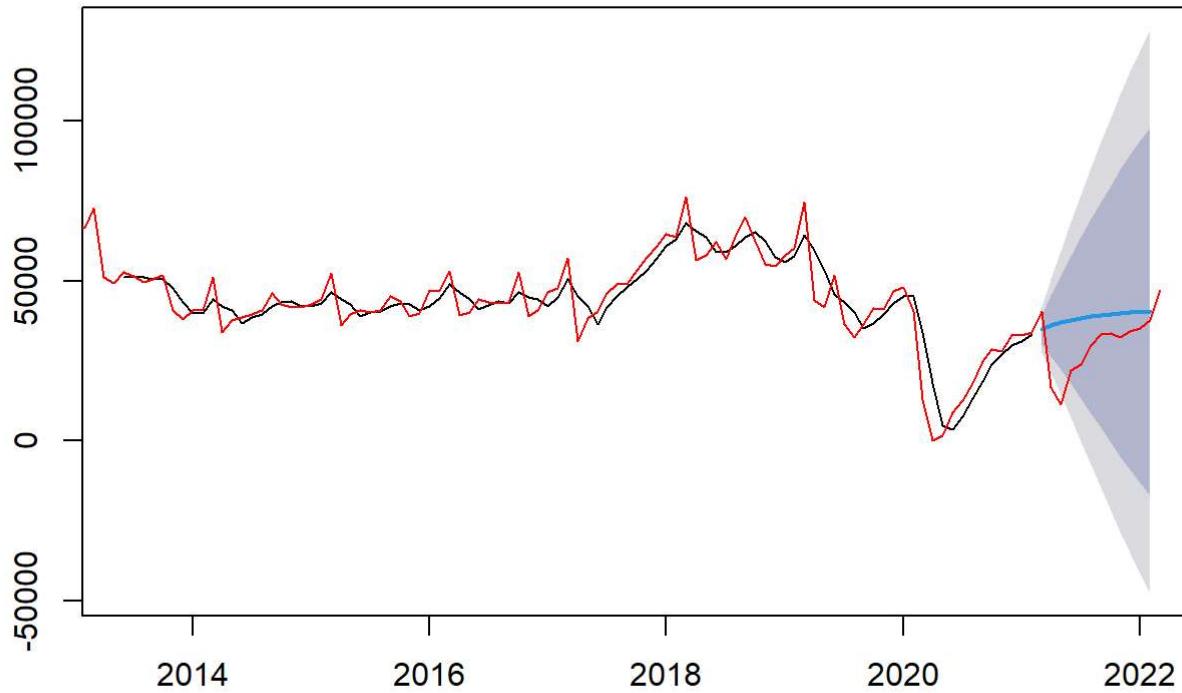
```
## Warning in ets(object, lambda = lambda, biasadj = biasadj,
## allow.multiplicative.trend = allow.multiplicative.trend, : Missing values
## encountered. Using longest contiguous portion of time series
```

```
forecast_ma
```

	Point	Forecast	Lo 80	Hi 80	Lo 95	Hi 95
## Mar 2021	34721.19	30076.881	39365.50	27618.3333	41824.04	
## Apr 2021	35961.68	26501.482	45421.87	21493.5578	50429.79	
## May 2021	36954.06	22315.864	51592.27	14566.8680	59341.26	
## Jun 2021	37747.98	17825.724	57670.23	7279.5215	68216.43	
## Jul 2021	38383.10	13209.885	63556.33	-116.0133	76882.22	
## Aug 2021	38891.21	8578.072	69204.34	-7468.7325	85251.15	
## Sep 2021	39297.69	3998.402	74596.98	-14687.9129	93283.29	
## Oct 2021	39622.88	-487.378	79733.13	-21720.4644	100966.22	
## Nov 2021	39883.03	-4854.688	84620.74	-28537.4026	108303.45	
## Dec 2021	40091.15	-9090.279	89272.57	-35125.3527	115307.64	
## Jan 2022	40257.64	-13188.412	93703.69	-41481.0427	121996.32	
## Feb 2022	40390.84	-17148.289	97929.96	-47607.6622	128389.34	

```
plot(forecast_ma)
lines(df, col = "red")
```

Forecasts from ETS(A,Ad,N)



```
accuracy(forecast_ma, df)
```

```
##               ME      RMSE     MAE      MPE     MAPE     MASE
## Training set -20.71935 3525.208 2537  3.04275 9.380983 0.2439746
## Test set     -9318.20279 12236.081 10275 -48.91381 51.278499 0.9881122
##                   ACF1 Theil's U
## Training set -0.0183776       NA
## Test set      0.2811546   1.92056
```