

Fermat's Little Thm

$$a^n + b^n = c^n$$

do not have solutions in integers when $n > 2$.

Fermat's Little Theorem

If p is a prime, given an integer a , s.t. $\gcd(a, p) = 1$,

$$a^{p-1} \equiv 1 \pmod{p}$$

Euler's Thm

If p & q are different primes, an integer a s.t. $\gcd(a, pq) = 1$

$$a^{(p-1)(q-1)} \equiv 1 \pmod{pq}$$

↓ RSA

$$d = e^{-1} \pmod{(p-1)(q-1)}$$

$$\begin{aligned} D(E(m)) &= (m^e)^d \equiv m^{e \cdot d} \\ &\equiv m^{1 + k(p-1)(q-1)} \pmod{n} \\ &\equiv m \cdot m^{k(p-1)(q-1)} \\ &\equiv m \cdot 1 \pmod{n} \\ &\equiv m \pmod{n} \end{aligned}$$