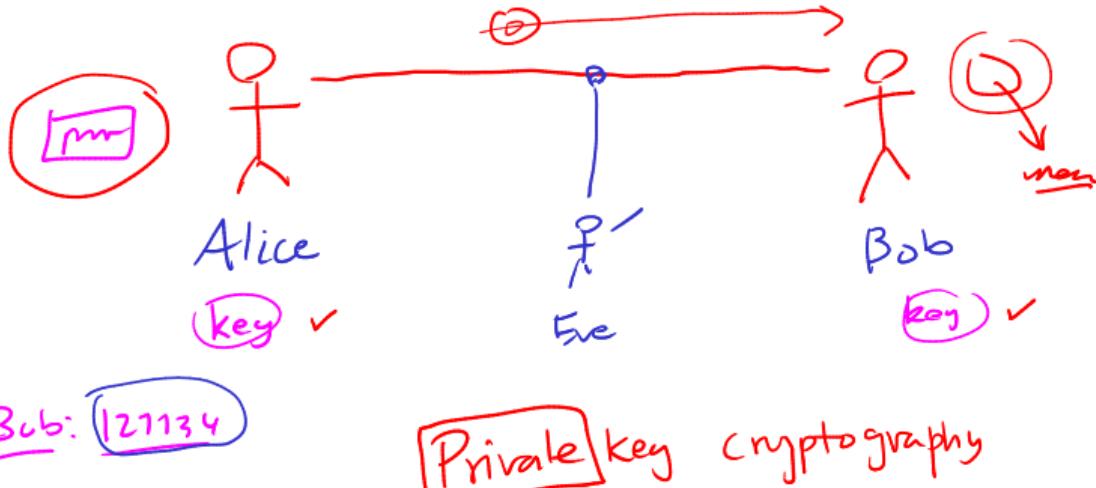


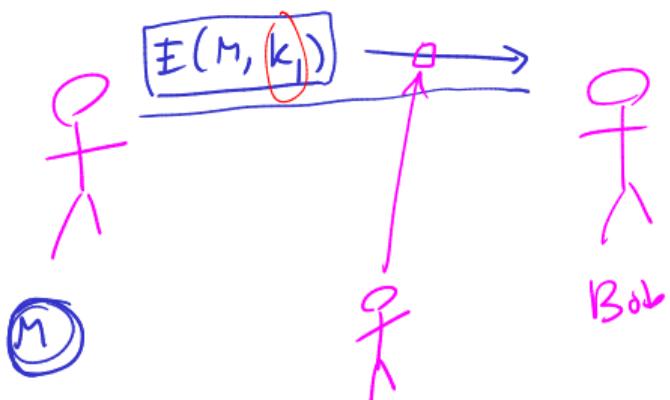
## Public-key cryptography

public key  $k_1$   
private key  $k_2$



Bob: 121134

**Private** key cryptography



$$D(E(M, k_1), k_2) \Rightarrow M$$

$k_1 = 121134$   
 $(k_2)$

RSA

|| Adelmae  
Shamir  
Rivest

Public key  $(e, n)$  big number  
Private key  $(d, n)$

Message:  $m$

- encrypt( $m$ ) =  $(m^e) \bmod n$
- decrypt( $r$ ) =  $(r^d) \bmod n$

Pick two prime numbers:  $p, q$

$$\boxed{n = pq}$$

pick  $\boxed{e}$

$$65535$$

Calculate  $d$ :

$$\boxed{e^{-1} \pmod{(p-1)(q-1)}}$$

RSA

$$(m^e) \bmod n$$

$$\begin{matrix} (a+b) \bmod n \\ || \end{matrix}$$

$$((a \bmod n) + (b \bmod n)) \bmod n$$

$$(a \cdot b) \bmod n$$

$$\begin{matrix} ((a \bmod n) (b \bmod n)) \bmod n \\ || \end{matrix}$$

## RSA: steps

- ▶ Private key:  $(d, n)$ , Public key:  $(e, n)$
- ▶ Encryption  $E(m) = m^e \text{ mod } n$ , Decryption:  $D(w) = w^d \text{ mod } n$ .
- ▶ Goal: Select  $e, d, n$  such that  $D(E(m)) = m^{ed} \text{ mod } n = m$ .