

P₂

$$h_1 = \frac{1}{1 + e^{-Z_{11}}}$$

$$h_2 = \frac{1}{1 + e^{-Z_{22}}}$$

$$Z_1 = 0,35 + \underbrace{0,05}_{e} \cdot 0,15 + \underbrace{0,025}_{0,1 \cdot 0,120} = 0,3775$$

$$Z_2 = 0,35 + \underbrace{0,25 \cdot 0,05}_{0,0125} + \underbrace{0,3 \cdot 0,1}_{0,103} = 0,3925$$

$$h_1 = \frac{1}{1 + e^{-0,3775}} = 0,59328$$

$$h_2 = \frac{1}{1 + e^{-0,3925}} = 0,59688$$

$$O_1 = \frac{1}{1 + e^{Z_{11}}} ,$$

$$Z_{11} = 0,6 + \underbrace{0,4 \cdot 0,5932}_{0,23728} + \underbrace{0,45 \cdot 0,59688}_{0,268556} = 1,105$$

$$O_2 = \frac{1}{1 + e^{Z_{22}}} ,$$

$$Z_{22} = 0,6 + \underbrace{0,5 \cdot 0,5932}_{0,2966} + \underbrace{0,55 \cdot 0,59688}_{0,328284} = 1,105$$

$$\delta_1 = 0,751359$$

$$\delta_2 = 0,772521$$

P₃

$$\frac{(0,751359 - 0,91)^2 + (0,772521 - 0,93)^2}{2} =$$

$$\frac{0,5496131^2 + 0,0471232}{2} = 0,258368$$

P_y

$$f = \frac{1}{2} \left(\frac{\text{DiF}_1}{\text{C}_{\text{avg}} \cdot \text{D}_{\text{out},1}} - \text{out}_{01} \right)^2 + \frac{1}{2} \left(\frac{\text{DiF}_2}{\text{C}_{\text{avg}} \cdot \text{D}_{\text{out},2}} - \text{out}_{02} \right)^2$$

w₅

$$\frac{\partial f}{\partial w_5} = \frac{\partial f}{\partial \text{out}_{01}} \cdot \frac{\partial \text{out}_{01}}{\partial w_5} =$$

$$\frac{\partial f}{\partial w_5} = \frac{\partial f}{\partial \text{out}_{01}} \cdot \frac{\partial \text{out}_{01}}{\partial w_5} = 0,741355$$

$$\frac{\partial f}{\partial \text{out}_{01}} = \frac{2}{\text{out}_{01}^2} \cdot \text{DiF}_1 \cdot -1 = -0,01 - 0,741355 =$$

$$\text{out}_{01} = \frac{1}{1 - e^{-z_{21}}} \Rightarrow \frac{\partial \text{out}_{01}}{\partial z_{21}} = \frac{(1 - \text{out}_{01}) \cdot \text{out}_{01}}{(1 - \text{out}_{01})^2} = \frac{0,18681}{0,8131855}$$

$$\frac{\partial \text{out}_{01}}{\partial w_5} = (0,1 \cdot (1 - 0,1)) = 0,18681$$

$$\frac{\partial \text{out}_{01}}{\partial w_5} = \frac{\partial \text{out}_{01}}{\partial z_{21}} = h_1 = 0,5532$$

$$0,741355 \cdot 0,18681 \cdot 0,5532 = 0,082184$$

$$\frac{\partial f}{\partial w_5} = 0,741355 \cdot 0,18681 \cdot 0,5532 = 0,08266372$$

For w₆, the result is:

$$\frac{\partial f}{\partial \text{out}_{01}} \cdot \frac{\partial \text{out}_{01}}{\partial z_{22}} \cdot \frac{\partial z_{22}}{\partial w_6} = h_2$$

$$0,741355 \cdot 0,18681 \cdot 0,55688$$

For w₇ & w₈:

$$\frac{\partial f}{\partial w_7} = \frac{\partial f}{\partial \text{out}_{02}} \cdot \frac{\partial \text{out}_{02}}{\partial z} \cdot \frac{\partial z}{\partial w_7} = -0,03659$$

$$- \text{DiF}_2 \cdot (1 - \text{out}_{02}) \cdot (\text{out}_{02}) \cdot h_1 = -0,21075 \cdot 0,17551 \cdot 0,5532 = -0,02199$$

$$\frac{\partial f}{\partial w_8} = - \text{DiF}_2 \cdot (1 - \text{out}_{02}) \cdot (\text{out}_{02}) \cdot h_2 = -0,21075 \cdot 0,17551 \cdot 0,55688 = -0,022079$$

$$\frac{\partial f}{\partial w_8} = -0,03659$$

$$\frac{\partial F}{\partial w_1} = \left(\frac{\partial F}{\partial \epsilon_1} \cdot \frac{\partial \epsilon_1}{\partial \theta_1} \cdot \frac{\partial \theta_1}{\partial h_1} \cdot \frac{\partial h_1}{\partial z_{21}} + \frac{\partial F}{\partial \epsilon_2} \cdot \frac{\partial \epsilon_2}{\partial \theta_2} \cdot \frac{\partial \theta_2}{\partial h_1} \cdot \frac{\partial h_1}{\partial z_{21}} \right) \frac{\partial h_1}{\partial z_{21}} \cdot \frac{\partial z_{21}}{\partial I_1} - D_i F_1 \cdot \theta_1(1-\theta_1) \cdot w_5$$

$$= D_i F_2 \cdot \theta_2(1-\theta_2) \cdot w_7 \cdot h_1(1-h_1) \cdot \frac{1}{I_1}$$

$$\frac{\partial F}{\partial w_1} = (1 \cdot -D_i F_1 \cdot \theta_1(1-\theta_1) \cdot w_5 + D_i F_2 \cdot \theta_2(1-\theta_2) \cdot w_7) h_1(1-h_1) \cdot I_1$$

$$= (0,141353 \cdot 0,18681 \cdot w_5 + 0,21075 \cdot 0,17551 \cdot w_7) h_1(1-h_1) \cdot 0,05$$

$$= (0,0533 - 0,01664) \frac{0,01206}{0,02366}$$

$$= 0,000442022$$

w₂
the only change for w₂ is in the last part. of the chain rule, where instead of I₁, we have I₂.

$$\frac{\partial F}{\partial w_2} = (0,0353) \cdot h_1(1-h_1) \cdot 0,1 = 0,00085189.$$

w₃ & w₄ =
for w₃ & w₄, we have to change a few things in the derivative.

$$\frac{\partial F}{\partial w_3} = \left(\frac{\partial F}{\partial \epsilon_1} \cdot \frac{\partial \epsilon_1}{\partial z_{21}} \cdot \frac{\partial z_{21}}{\partial h_2} + \frac{\partial F}{\partial \epsilon_2} \cdot \frac{\partial \epsilon_2}{\partial z_{21}} \cdot \frac{\partial z_{21}}{\partial h_2} \right) \cdot \frac{\partial h_2}{\partial z_{12}} \cdot \frac{\partial z_{12}}{\partial w_3}$$

$$= (-D_i F_1 \cdot \theta_1(1-\theta_1) \cdot w_6 + -D_i F_2 \cdot \theta_2(1-\theta_2) \cdot w_8) \cdot h_2(1-h_2) \cdot I_2$$

$$= (0,241353 \cdot 0,18681 \cdot w_6 + (-0,21075) \cdot 0,17551 \cdot w_8) 0,155688(1-0,59698) \cdot 0,05$$

$$\frac{\partial F}{\partial w_3} = (0,06232 - 0,0234766) \cdot 0,0120307 = 0,00046731$$

$$\frac{\partial F}{\partial w_4} = (0,06232 - 0,0234766) \cdot 0,59688(1-0,59688) \cdot \frac{I_2}{0,1}$$

$$= (\quad \quad \quad) \cdot 0,02406143$$

$$0,0388534 \cdot 0,02406143$$

$$= 0,00093487 //$$

P5-

$$w_k^+ = w_k + C \frac{\partial F}{\partial w}$$

$$\begin{bmatrix} w_1^+ \\ w_2^+ \\ w_3^+ \\ w_4^+ \\ w_5^+ \\ w_6^+ \\ w_7^+ \\ w_8^+ \end{bmatrix} = \begin{bmatrix} 0,15 \\ 0,2 \\ 0,25 \\ 0,3 \\ 0,4 \\ 0,45 \\ 0,5 \\ 0,55 \end{bmatrix} - C \begin{bmatrix} 0,0004202 \\ 0,00085184 \\ 0,00046131 \\ 0,00053487 \\ 0,082154 \\ 0,08266387 \\ 0,02154 \\ -0,022078 \end{bmatrix}$$

P1 As there are two $I_i \Rightarrow$ there are two features