Merge Sort

→ First we need to know merging.

Combining 2 list in 1

e.g

List A	List B
2	5
8	9
15	12
18	17

The list can be of same & different sizes. But, they are sorted.

For merging, we ~~have~~ need another list C

These list can be array / linked list

	A	B	C
i →	2	5 ← j	k
	8	9	
	15	12	
	18	17	

Compare i with j if i is smaller then copy in k

A	B	C
2	5 j	2
→ i 8	9	k
15	12	
18	17	

A	B	C
2	5	2
i → 8	9 ← j	5
15	12	← k
18	17	

Continue until ~~not~~ all sorted.

in the end.

A	B	C
2	5	2
8	9	5
15	12	8
i → 18	17	9
	← j	12
		15
		17
		← k

if one list is finished, copy remaining items of the list

So C list is with sorted elements

This was merging

Assume

A has m elements

B has n elements

So Total elements sorted are

$O(m+n)$

Now Algorithm of merge.

```
                                    List      size
Algorithm merge ( A, B, m, n )
{
  i=1, j=1, k=1   :: Assuming index 1
  while ( i<=m && j<=n)   so for pesudocode.
                          Until one list finishes.
                          this will happen
  { if ( A[i] < B[j] )
      C[k] = A[i]
      k++ ; i++      ]-> C[k++] + A[i++]
```

else

```
    C[k++] = B[j++]
}
```

Once while is done., there might be a possiblity that list have remoing item. We dont know which one so we need to copy all remaing elements (Assume List A have 5 more elements)

```
for( ; i<=m ; i++)
    C[k++] = A[i];
for( ; j<=n ; j++)
    C[k++] = B[j];
}.
```

⇒ What if we more then 2 list ?

A	B	C	D.
4	3	8	2
6	5	10	4 → After comparison,
12	9	16	18

Sorted List.

2
3
4

So this one is 4 way merging

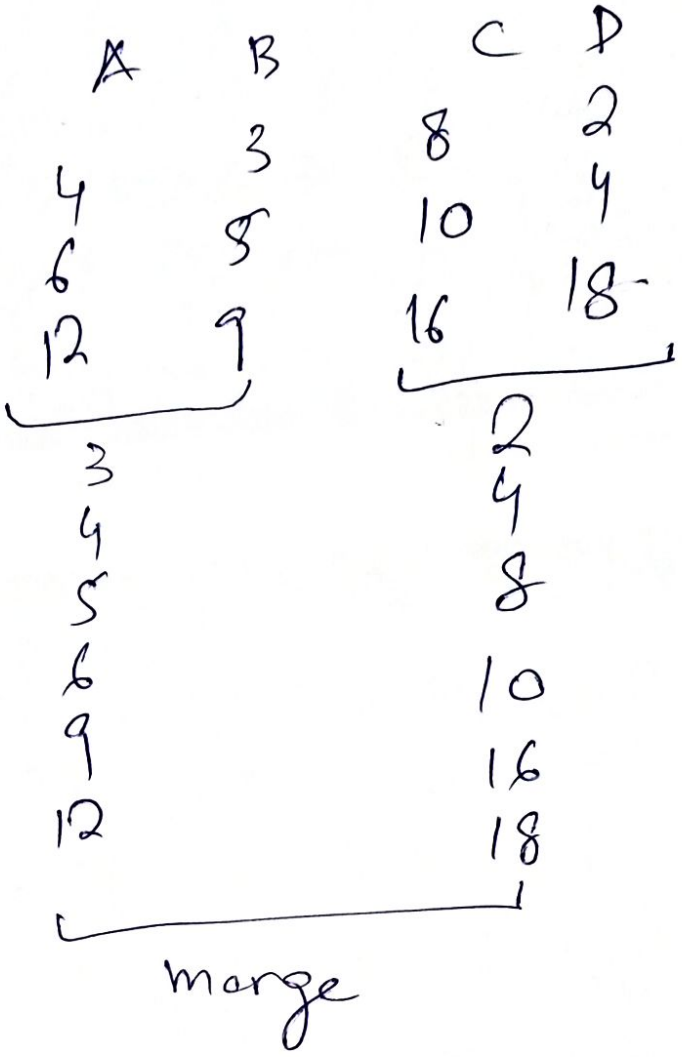
or generalize as

m - way merging

= mostly 2 way merging.

Now we will sort above one. with 2 way merging.

merge.



So take pair & do it again

Can we do it another way?

Merg (AB) then (C) then (D)

or (CD) then B the A

Merge Sort

	1	2	3	4	5	6	7	8
A	9	3	7	5	6	4	8	2

Done by divide & conquer / recursive

if greter then 1 element, we merge sort.

start ↑ end ↑

Algorithm MergeSort (l, h)

{

if (l < h)

{

mid = (l+h)/2

mergeSort (l , mid)

mergeSort (mid +1, h):

merge (l, mid, h)

A B

}

}

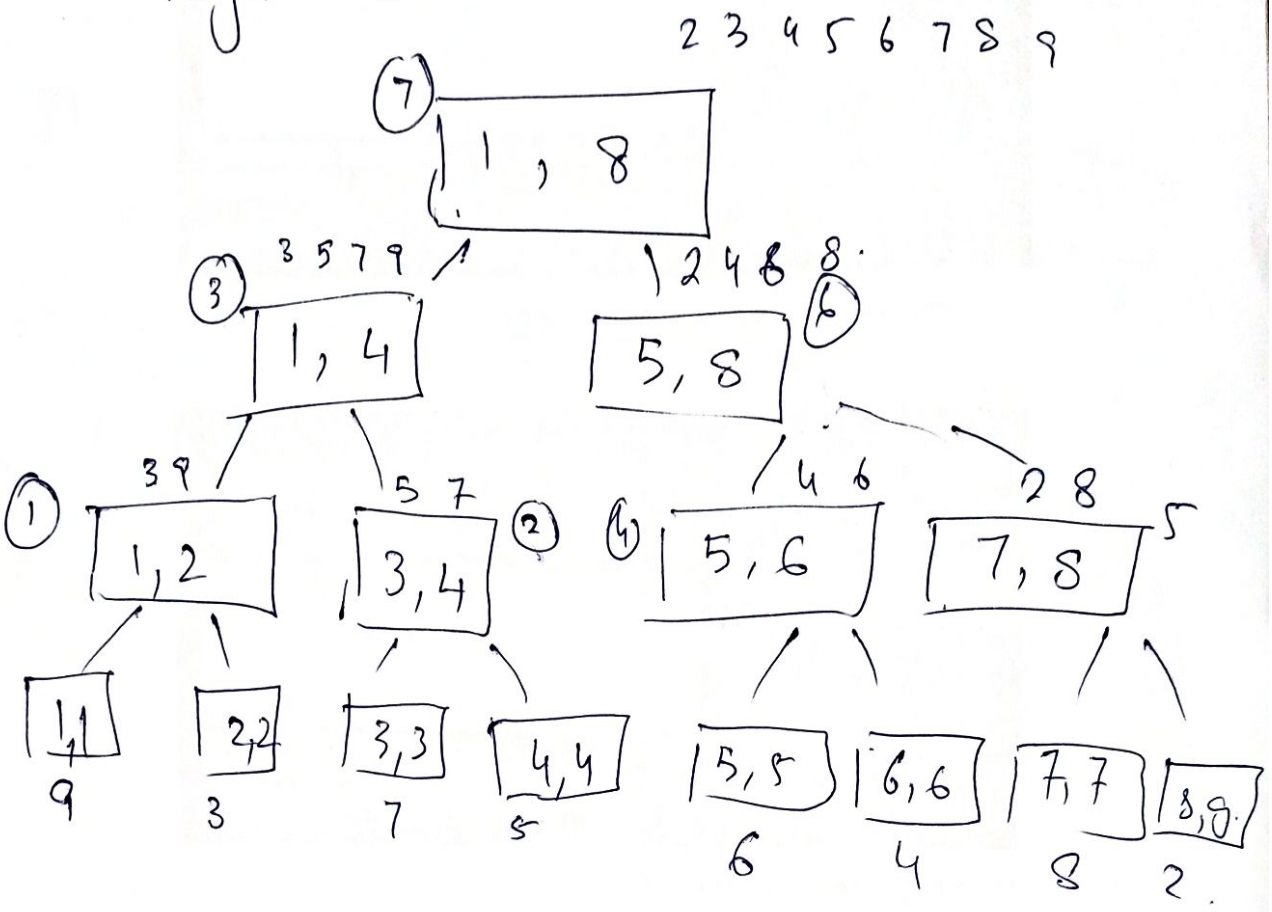
Go now

9	3	7	5	6	4	8	2

(7)

low = 1

high = 8.



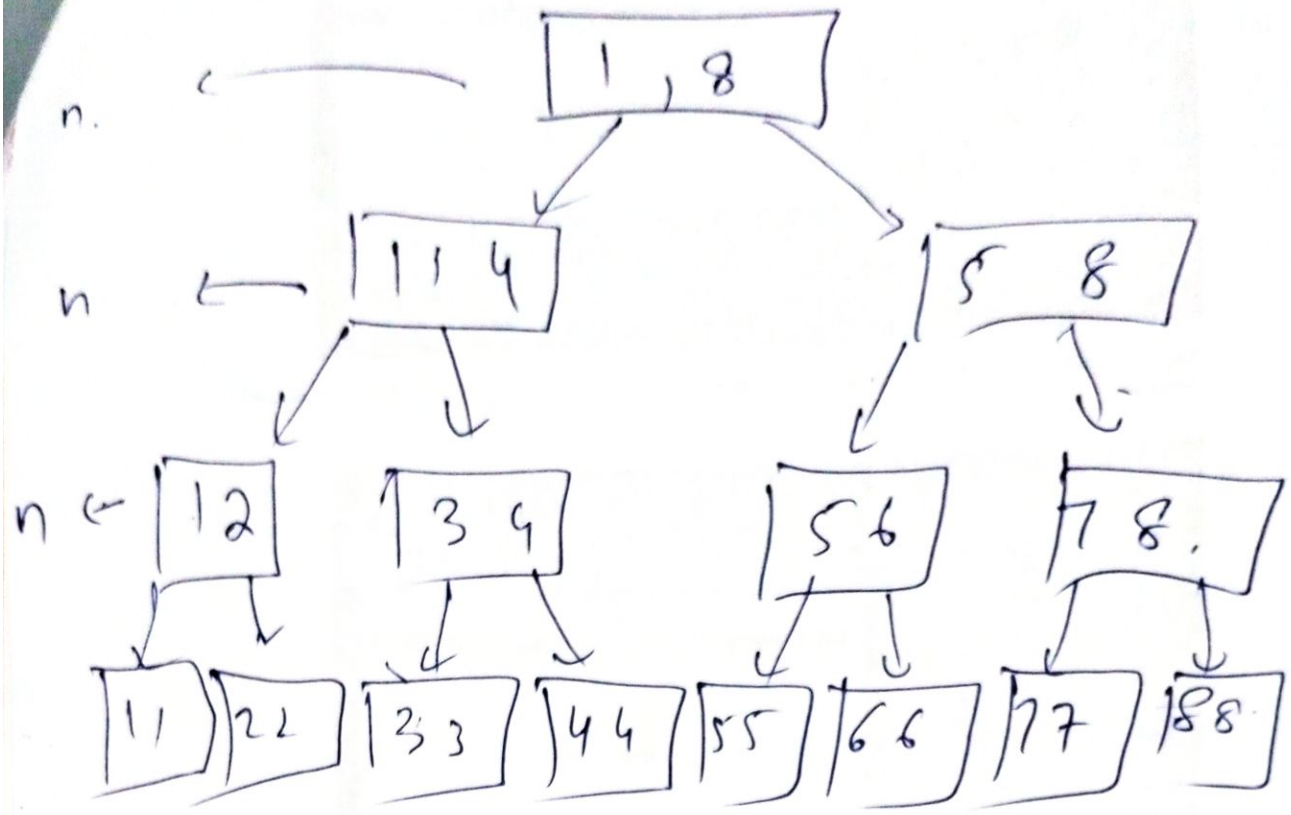
① → First merge

② merge.

⑥

So divide & conquer

Now Time Analysis



How many elements merged.

Last layer is only split element

How many levels ~~of~~ for 8 elements

= n so, ~~n log n~~ (n log n)

Algo Complexity

$T(n)$ — Algo merge Sort(l, h)

if (l < h)

mid (l < h)

mid = $\frac{(l+h)}{2}$.

1 —

$T(\frac{n}{2})$ / merge Sort (l, mid)

$T(\frac{n}{2})$ ^ (mid+1, h)

n merge (l mid h)

$$T(n) = \begin{cases} 2\left(\frac{T(n)}{2}\right) + n. & n > 1 \\ n = 1 \end{cases}$$

master theam.

$a = 2$
$b = 2$

$\log_b^a = \log_2^2 = 1$

$f(n) = 2$

$k = 1$

$p = 0$

$\log_2^2 = k$

So

$= O(n \log n)$