

e. 75th PERCENTILE:

From the above graph, it can be observed that the 75th percentile is shown on y-axis at 75 and the values corresponding to x-axis value is 504. Therefore, the values at 75th percentile is 504

Q6.

a. Since, the standard deviation of statistics which is 8 is greater than the standard deviation of algebra which is 7.6. So statistics has a higher absolute dispersion than algebra.

Coefficient of variation for statistics:

$$CVar = \frac{S}{\bar{x}} = \frac{8}{78} = 0.1026$$

Coefficient of variation for algebra:

$$CVar = \frac{S}{\bar{x}} = \frac{7.6}{73} = 0.1041$$

Since, the coefficient of variation for algebra is $\frac{0.1041}{0.1026}$ which is greater than coefficient of variation for statistics which is 0.1026. So Algebra has a higher relative dispersion than Statistics.

b. Student's Final Average = $\frac{20 \times 83 + 30 \times 72 + 50 \times 90}{100}$

$$= \frac{1660 + 2160 + 4500}{100} = \frac{8320}{100}$$

$$= 83.2$$

Q7. MEAN DEVIATION ABOUT MEDIAN:

CLASS INTERVAL	FREQUENCY f_i	CUMULATIVE FREQUENCY	CLASS MIDPOINTS x_i	DEVIATION $d_i = x_i - M $	$f_i \cdot d_i$
10-20	15	15	15	17	255
20-30	25	40	25	7	175
30-40	20	60	35	3	60
40-50	12	72	45	13	156
50-60	8	80	55	23	184
60-70	5	85	65	33	165
70-80	3	88	75	43	123
	$\sum f_i = 88$				$\sum f_i d_i = 124$

Now we calculate median,

$$\text{Here } N = 88, \frac{N}{2} = 44$$

CUMULATIVE FREQUENCY is 60

& CORRESPONDING CLASS IS 30-40

$\therefore L = 30, f = 20, \text{ CUMULATIVE FREQUENCY BEFORE MEDIAN CLASS } F = 40,$
 $h = 10, \frac{N}{2} = 44$

$$M_{\text{MEDIAN}} = L + \left[\frac{\frac{N}{2} - F}{f} \right] \times h = 30 + \left[\frac{44 - 40}{20} \right] \times 10$$

$$= 32$$

Let calculate $x_i - M$ & $f_i d_i$ for first class interval 10-20

$$\therefore (x_i - \bar{M}) = 25 - 32 = -7$$

$$\therefore |x_i - \bar{M}| = 7$$

$$\& f_i \cdot d_i = 15 \times 7 = 225$$

Similarly we will calculate all values for all class interval in table
Now we calculate Mean deviation about Median,

$$\text{Mean Deviation About median} = \frac{\sum f_i d_i}{N} = \frac{1124}{88}$$

$$= 12.77$$

Q8. Mean Deviation About Mean:

Class Interval	FREQUENCY f_i	Class Midpoint x_i	$f_i \cdot x_i$	Deviation $d_i = x_i - \bar{M} $	$f_i \cdot d_i$
10 - 20	15	15	225	20	300
20 - 30	25	25	625	10	250
30 - 40	20	35	700	0	0
40 - 50	12	45	540	10	120
50 - 60	8	55	440	20	160
60 - 70	5	65	325	30	150
70 - 80	3	75	225	40	120
$\sum f_i = 88$			$\sum f_i x_i = 3080$		$\sum f_i \cdot d_i = 1300$

$$\therefore \bar{M}_{\text{MEAN}} = \frac{\sum f_i x_i}{\sum f_i} = \frac{3080}{88} = 35$$

\therefore Deviation $|x_i - \bar{M}|$ & $f_i |x_i - \bar{M}|$ for first class interval

10 - 20 is

$$|x_i - M| = |15 - 35| = 20$$

$$f_i |x_i - M| = 5 \times 20 = 300$$

$$\therefore \text{MEAN Deviation} = \frac{\sum f_i |x_i - M|}{N} = \frac{300}{88} = 12.5$$

ABOUT MEAN

$$\text{MEAN Deviation ABOUT MEAN} = 12.5$$

Q9. For National League:

x_m	f	$f \cdot x_m$	$f \cdot x_m^2$
0.244	3	0.732	0.178
0.249	6	1.494	0.372
0.254	1	0.254	0.064
0.259	11	2.849	0.731
0.264	11	2.904	0.766
0.269	1	0.269	0.072
$\sum f = 33$		$\sum f \cdot x_m = 8.502$	$\sum f \cdot x_m^2 = 2.192$

$$S^2 = \frac{n (\sum f \cdot x_m^2) - [\sum f \cdot x_m]^2}{n(n-1)} = \frac{33(2.192) - (8.502)^2}{33(33-1)}$$

$$= \frac{72.337 - 72.284}{1056} = \frac{0.053}{1056} = 0.0005042$$

$$S = \sqrt{0.00050} = 0.0071$$

For American LANGUAGE:

X_m	f	$f \cdot X_m$	$f \cdot X_m^2$
0.2465	3	0.7395	0.3622
0.2525	6	1.515	0.3825
0.2585	2	0.517	0.1336
0.2645	1	0.2645	0.0699
0.2705	3	0.815	0.21951
0.2765	0	0	0
	$\sum f = 15$	$\sum f \cdot X_m = 3.8475$	$\sum f \cdot X_m^2 = 0.9877$

$$S^2 = \frac{\sum [f \cdot X_m] - [\sum f \cdot X_m]^2}{n(n-1)} = \frac{14.819 - 14.803}{210} = \frac{0.01584}{210}$$

$$S^2 = 0.000075$$

$$S = \sqrt{0.000075} = 0.0086$$

So, we see that variability of NL is less which mean that NL batting averages are more consistent.

Q10.

For Observers:

$$\bar{X} = \frac{\sum x}{n} = \frac{3804}{10} = 380.4$$

$$M_{\text{MEDIAN}} = \frac{352 + 378}{2} = 365$$

Mode : No mode

$$M_{\text{MEDIAN}} \text{ RANGE} : \frac{484 + 302}{2} = 393$$

For Visits:

$$\bar{X} : \frac{\sum x}{n} = \frac{2769}{20} = 276.9$$

$$M_{EDIAN}: \frac{194 + 219}{2} = 206.5$$

M_{MODE} : No Mode

$$M_{MEDIAN\ RANGE}: \frac{114 + 632}{2} = 374$$

The values are higher for observers

Q11. For Temperatures:

$$RANGE: 61 - 29 = 32$$

$$MEAN: \bar{x} = \frac{50 + 37 + 29 + 54 + 30 + 61 + 47 + 38 + 34 + 61}{10} = \frac{441}{10} = 44.1$$

$$VARIANCE: S^2 = \frac{n(\sum x^2) - (\sum x)^2}{n(n-1)} = \frac{10(20777) - (441)^2}{10(10-1)} = 147.7$$

$$STANDARD\ DEVIATION: s = \sqrt{147.7} = 12.1514$$

$$COEFFICIENT\ OF\ VARIATION: CVAR = \frac{s}{\bar{x}} = \frac{12.1514}{44.1} = 0.2755$$

For Precipitation:

$$RANGE: 5.1 - 1.1 = 4.0$$

$$MEAN: \bar{x} = \frac{4.8 + 2.6 + 1.5 + 1.8 + 1.8 + 3.3 + 5.1 + 1.1 + 1.8 + 2.5}{10} = \frac{26.3}{10}$$

$$\bar{x} = 2.63$$

$$VARIANCE: \frac{n(\sum x^2) - (\sum x)^2}{n(n-1)} = \frac{10(86.35) - (26.3)^2}{10(10-1)} = 1.88$$

STANDARD DEVIATION: $SD = S = \sqrt{1.9} = 1.3728$

COEFFICIENT OF VARIATION: $CV_{ar} = \frac{S}{\bar{x}} = \frac{1.372}{2.63} = 0.52$

COMPARE:

Daily High Temperature are more Variable, because all measure of variation are higher for daily high temperature

Q12. WEIGHTED MEAN

$$\bar{x} = \frac{\sum f \cdot x}{\sum f} = \frac{9(427000) + 6(365000) + 12(725000)}{9 + 6 + 12}$$

$$\bar{x} = \frac{14783000}{27}$$

$$\boxed{\bar{x} = \$ 545,666.67}$$