

Q13.

		high	Low	Total
Surface	high	12	16	28
Roughness	Low	88	34	122
Total		100	50	150

a. $P[\text{Roughness Surface High} \mid \text{Coating Weight High}] = \frac{12}{12+88} = \frac{12}{100}$

$$= 0.12$$

b. $P[\text{Coating Weight High} \mid \text{Surface Roughness High}] = \frac{12}{12+16} = \frac{12}{28}$

$$= 0.4285$$

c. $P[\text{Coating Weight Low} \mid \text{Surface Roughness Low}] = \frac{34}{88+34} = \frac{34}{122}$

$$= 0.2787$$

Q14. Given That:

Probability of customers use regular gas: $A_1 = 40\% = 0.4$

Probability of customer use plus gas: $A_2 = 35\% = 0.35$

Probability of customer use premium gas: $A_3 = 25\% = 0.25$

B is the event of customers fill their tanks and given conditional probabilities are:

$$P[B \mid A_1] = 30\% = 0.3$$

$$P[B \mid A_2] = 60\% = 0.6$$

$$P[B \mid A_3] = 50\% = 0.5$$

a. $P[A_2 \cap B] = P[A_2] P[B \mid A_2]$
 $= 0.35 \times 0.6$

$$= 0.21$$

b. Probability that next customer fills the tank is:

$$P(B) = P(A_1)P(B|A_1) + P(A_2)P(B|A_2) + P(A_3)P(B|A_3)$$

$$= 0.4 \times 0.3 + 0.35 \times 0.6 + 0.25 \times 0.5$$

$$= 0.455$$

c. If the next customer fill the tank, the probability that regular gas is requested is

$$P(A_1|B) = \frac{P(A_1) \cdot P(B|A_1)}{P(B)} = \frac{0.4 \times 0.3}{0.455}$$

$$= 0.264$$

If the next customer fill the tank, the probability that plus gas is requested is

$$P(A_2|B) = \frac{P(A_2) \cdot P(B|A_2)}{P(B)} = \frac{0.35 \times 0.6}{0.455}$$

$$= 0.462$$

If the next customer fill the tank, the probability that premium gas is requested is

$$P(A_3|B) = \frac{P(A_3) \cdot P(B|A_3)}{P(B)} = \frac{0.25 \times 0.5}{0.455}$$

$$= 0.274$$