

What

kernel function

$$k(x, x') = \phi^T(x) \cdot \phi(x') = \langle \phi(x), \phi(x') \rangle.$$

$$\forall (x, x') \exists \phi: x \rightarrow z$$

$$s.t. \quad k(x, x') = \phi^T(x) \phi(x').$$

则称  $k(x, x')$  是一个核函数

$$k(x, x') = \exp\left\{-\frac{(x-x')^2}{2\sigma^2}\right\} \quad x, x' \text{ 为标量.}$$

代入可得  $k(x, x')$ , 即  $\phi^T(x) \phi(x')$  可得.

工作方式

- Embedding data in a vector space (with more high dim)
- ② look for (linear) relations in such space.

## 一些概念

Q.  $\phi$  necessary A. Not Necessary

Q. can we only employ  $K$ ? A. Yes.

Q. what kind of  $K$  can be used?

A. Finitely positive semi-definite

Q. 给定  $\phi$ , 可以找到  $K$ , 并在特征空间计算点积吗? A. Yes.

Q. 给定  $K$ , 我们能否构造特征空间  $\mathcal{H}$  吗? A. Yes



