

# “On the Density of Neutral Hydrogen in Intergalactic Space”

**James Gunn** (Caltech) and **Bruce Peterson** (Caltech)  
**1965**

(J. Gunn: aged 27; B. Peterson: aged 32)

$$\int_{-\infty}^{\infty} g(x) dx = 1.$$

...shift of the object observed be  $z_0$ , and suppose the redshift of the layer as seen from here is  $z$ ;  $z < z_0$ , and if the observed

$$\nu_o = \nu(1 + z)$$

...is the frequency seen by an observer stationary with respect to t  
Thus the total optical depth at  $\nu$  is

$$\tau = \int_0^{z_0} d\tau = \int_0^{z_0} n[l(z)] \sigma[\nu(1 + z)] \frac{dl}{dz} dz.$$

Presenter

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$$\int_{-\infty}^{\infty} g(x) dx = 1.$$

Preview:

- 1. G-P Optical Depth: A uniform neutral hydrogen assumption
- 2. Interpretations on low-z (z=2.01) hydrogen composition (H I or H II)

$$\nu_r = \nu(1 + z)$$

$$\tau = \int_0^{z_0} d\tau = \int_0^{z_0} n[l(z)] \sigma[\nu(1 + z)] \frac{dl}{dz} dz.$$

# Introduction - Quasars

- Active Galactic Nucleus (AGN)
- Super Massive BlackHole
- The gas falling towards the quasar releases electromagnetic radiation.
- In 1965, the most distant quasar 3C 9 was only at redshift  $z=2.01$ .

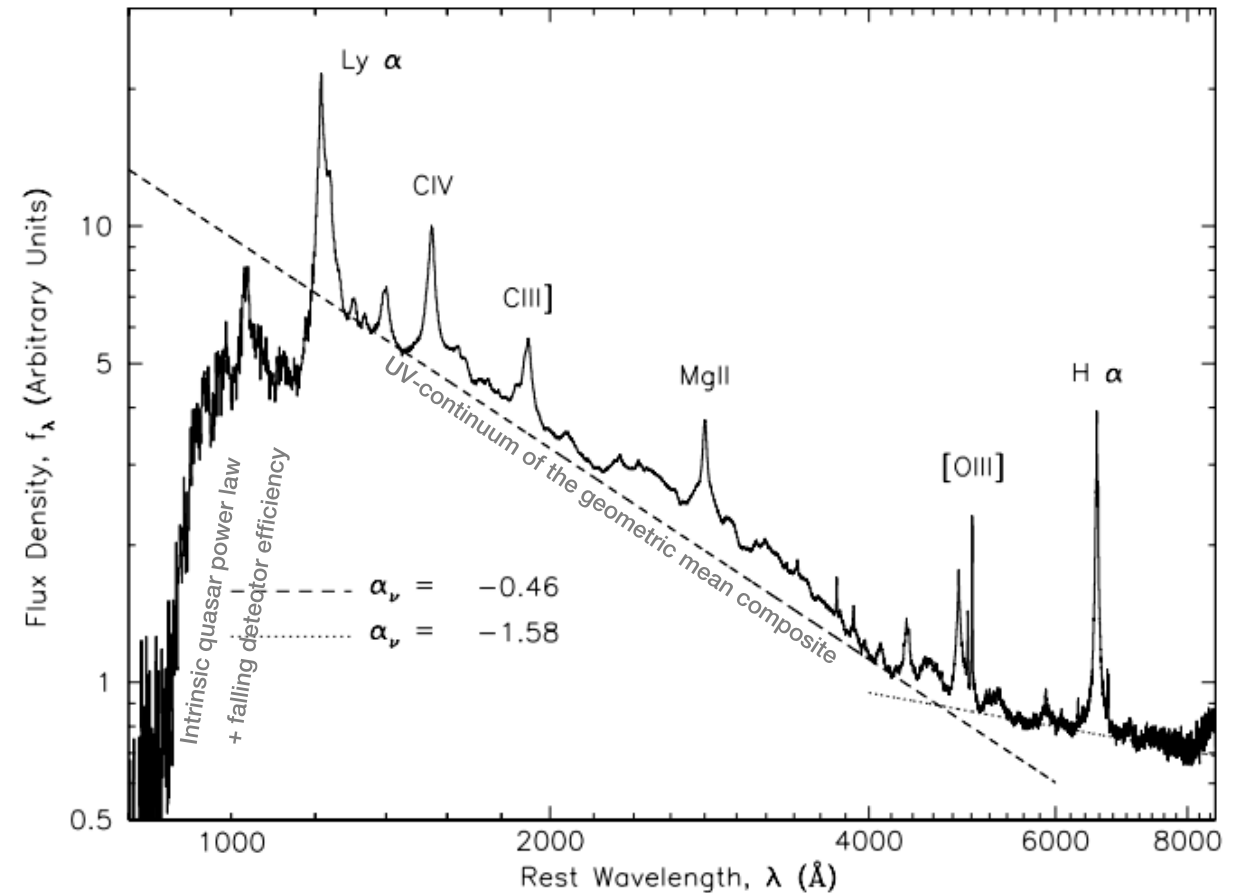
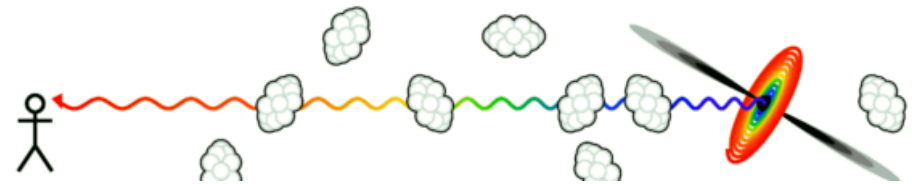
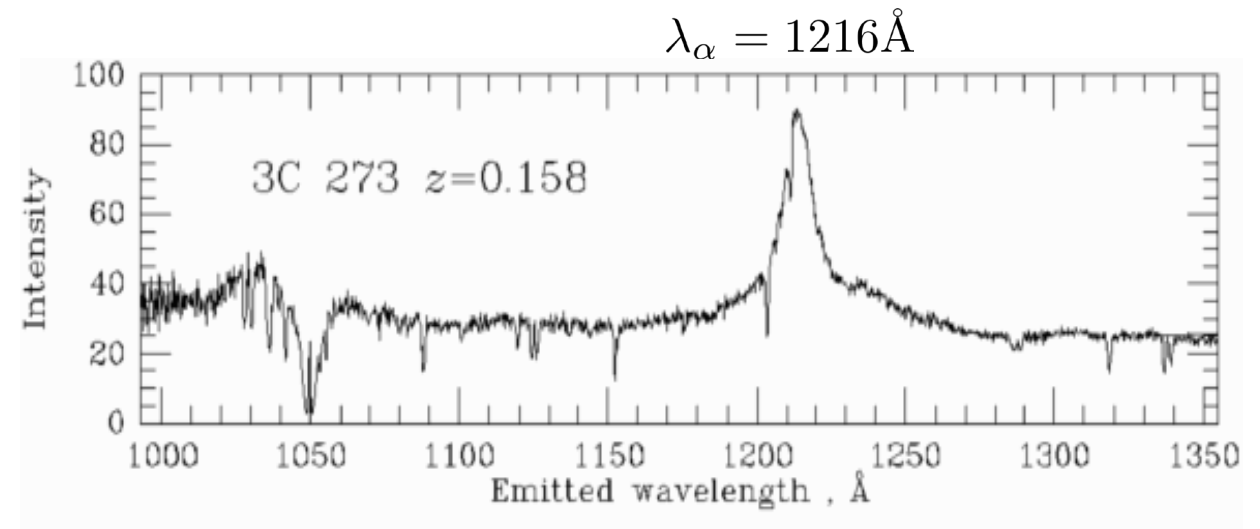


Fig. 3.— Composite quasar spectrum using median combining. Power-law fits to the estimated continuum flux are shown. The resolution of the input spectra is  $\approx 1800$ , which gives a wavelength resolution of about  $1\text{\AA}$  in the rest frame.

# Introduction – QSO's Spectrum

- Active Galactic Nucleus (AGN)
- Super Massive BlackHole
- The gas falling towards the quasar releases electromagnetic radiation.
- In 1965, the most distant quasar 3C 9 was only at redshift  $z=2.01$ .
- The **HI (neutral hydrogen)** regions along the light-of-sight can show absorption lines blueward  $\lambda_{\alpha} = 1216\text{\AA}$  in the spectrum.
- Notice the wings and depths of the absorption lines.



# Main Goals of Gunn&Peterson (1965)

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1. Study a fate of photons emitted to the blue of  $\text{Ly}\alpha$ .
2. Assume a uniform **HI gas** in IGM to calculate an optical depth as a function of redshift.
3. Compare the number density of **HI gas** derived from the observation of 3C 9 with other works.
4. Analyze an interpretation of **HII (ionized hydrogen)** at 3C 9 and support based on models and assumptions.

# GP Optical Depth

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Again, Gunn and Peterson (1965) assumed a uniformly distributed HI (neutral hydrogen) gas at the density of  $n_{\text{HI}}(z)$  in IGM at redshift  $z$ . Do not confuse this redshift of regions absorbing HI,  $z$ , with the quasar's redshift  $z_{\text{em}}$ , e.g.,  $z < z_{\text{em}} = 2.01$  for 3C 9. The optical depth is defined as

$$d\tau(z) = n_{\text{HI}}(z) \sigma(\nu_s(z)) dl(z), \quad (13)$$

where  $\nu_s(z)$  is the frequency of the absorption scattering, with respect to the scattering plane at redshift  $z$ . This can be implied from the observed frequency  $\nu$  by  $\nu_s(z) = \nu(1 + z)$ . The  $dl(z)$  and  $\sigma(\nu(z))$  terms are read as the tiny length along the line-of-sight and cross-section of radiative excitation for Ly $\alpha$  transition respectively.



Since we have integrated absorption coefficient (See Class Note 16), we can introduce an additional normalized and strongly peaked function  $g(\nu - \nu_\alpha)$  at  $\nu_\alpha = c/1216\text{\AA}$  and rewrite the cross-section

$$\sigma(\nu) = \frac{\pi e^2 f_\alpha}{m_e c} g(\nu - \nu_\alpha), \quad (14)$$

in terms of the electron charge  $e$ , the electron mass  $m_e$ , the speed of light  $c$ , and  $f_\alpha = 0.416$  is the oscillator strength of Ly $\alpha$  transition.

Using the scale relation and Hubble parameter at  $z$ ,  $H(z)$  simply rewrite  $dl(z)$  terms into

$$dl(z) = \left( \frac{dl}{dz} \right) dz = \frac{c H(z)^{-1}}{1 + z} dz. \quad (15)$$

# GP Optical Depth



Now, taking  $n_{\text{HI}}(z) = n_{\text{HI}}(1+z)^3$  and plugging above equations into the optical depth integrant, we get

$$\tau(z) = \int_0^z d\tau(z) = \int_0^z \left[ n_{\text{HI}}(1+z)^3 \frac{\pi e^2 f_\alpha}{m_e c} g(\nu - \nu_\alpha) \frac{c H(z)^{-1}}{1+z} \right] dz = n_{\text{HI}} \frac{\pi e^2 f_\alpha}{m_e c} \lambda_\alpha H(z)^{-1}. \quad (16)$$

From a more intuitive perspective,

$$\tau(z) = 1.8 \times 10^5 h^{-1} \Omega_{\text{m}}^{-1/2} \left( \frac{\Omega_{\text{b}} h^2}{0.02} \right) \left( \frac{1+z}{7} \right)^{3/2} \left\langle \frac{n_{\text{HI}}}{n_{\text{H}}} \right\rangle. \quad (17)$$



# GP Optical Depth

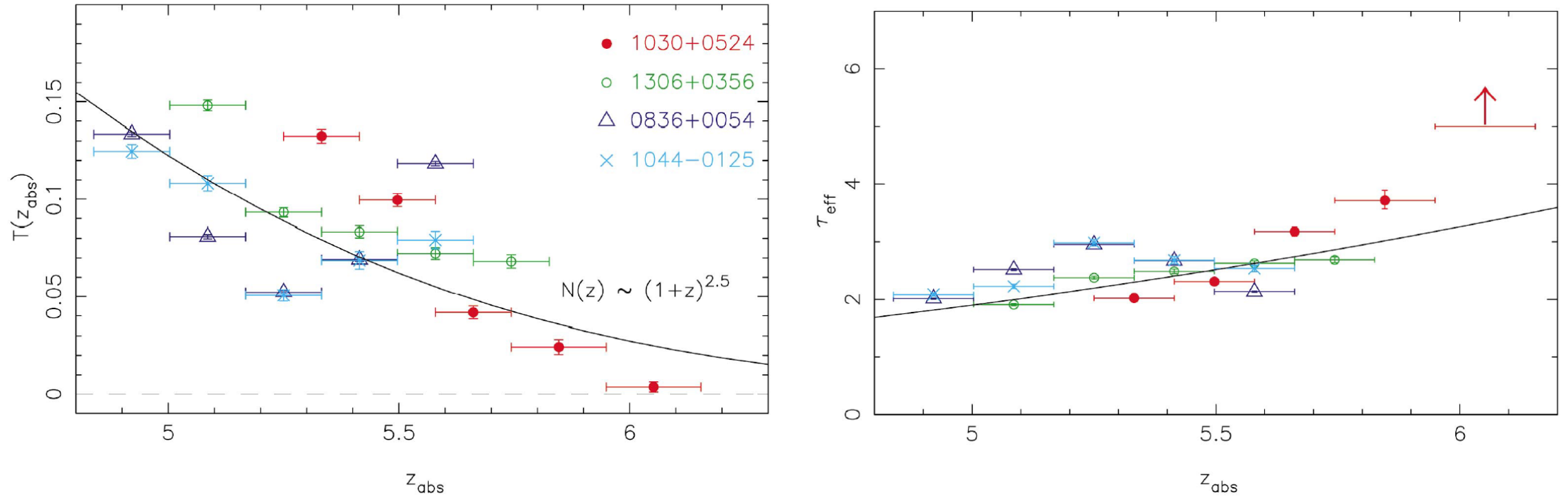


FIG. 2.—Evolution of transmitted flux ratio and effective Gunn-Peterson optical depth as functions of redshift. The solid line is the expected evolution if the number density of Ly $\alpha$  clouds increases as  $N(z) \propto (1+z)^{2.5}$ . No flux is detected in the spectrum of SDSS 1030+0524 at  $z_{\text{abs}} \sim 6$ , indicating  $\tau_{\text{eff}} > 5.0$ . The nondetection of flux in the Ly $\beta$  trough gives a substantially stronger  $1\sigma$  upper limit of  $\tau_{\text{eff}} > 20$ .

# HI Density from Quasar 3C 9



- The blueward flux of 3C 9 ( $z=2.01$ ) component and the wing of the line are noticeably depressed about 40%.
- It corresponds to an optical depth of about  $\tau(z = 2.01) = \frac{1}{2}$ .
- Field (1962) derived a  $\rho_{\text{HI}} \sim 10^{-29} \text{ g cm}^{-3}$  from the 21cm hydrogen observation.
- For the  $q_0 = 0.5$ ,  $\Omega_m = 1$  model,
  - The mass density of **neutral hydrogen** is  $\rho_{\text{HI}} = 1 \times 10^{-34} \text{ g cm}^{-3}$ . Much smaller than Field (1962).
  - The total density is  $\rho_{\text{total}} = 5 \times 10^{-28} \text{ g cm}^{-3}$ .
  - Thus, only about  $\Omega_{\text{HI}}(z = 2.01) := \rho_{\text{HI}}/\rho_{\text{total}} = 2 \times 10^{-7}$  of the total mass at that time could have been in the form of intergalactic **neutral hydrogen**.
- For the steady-state model ( $\Omega_m = 1$ , creation of matter),
  - $\rho_{\text{HI}} = 2 \times 10^{-35} \text{ g cm}^{-3}$ .
  - Constant total density is  $4 \times 10^{-29} \text{ g cm}^{-3}$ .
  - the factor here is somewhat less about  $\Omega_{\text{HI}}(z = 2.01) = 5 \times 10^{-7}$ .

# HI Density from Quasar 3C 9 - Outcomes

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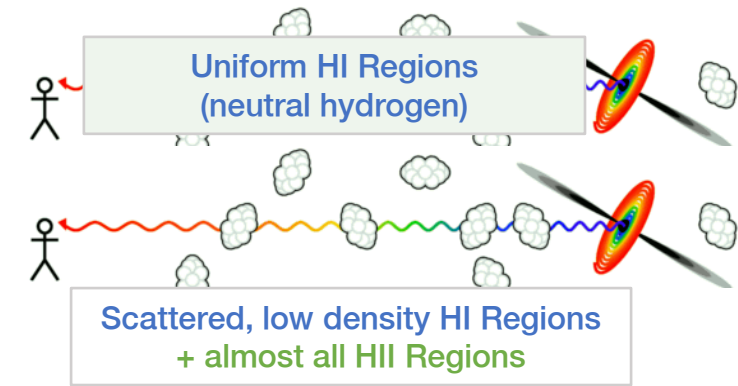
Interpretation:

Either

- the cosmological ideas (in 1960s) are grossly incorrect,
- that space is very nearly empty.

Or,

- the matter (all hydrogen contents) exists in some other form.



It is possible that this interpretation is still **valid** but requires essentially all hydrogen is ionized.

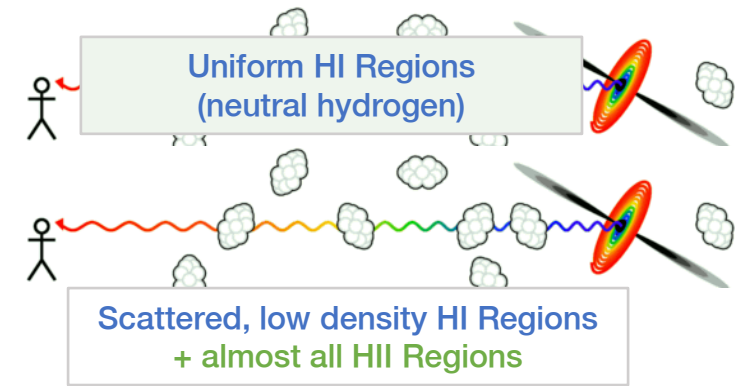
If the universe was **uniformly neutral** at  $z \sim 2$ , then **HI** should strongly absorb the flux.

Hence, the hydrogen gas must be **highly ionized** so that the flux at wavelengths can go through.

This can be defended if we are allowed to make the intergalactic electron temperature is high enough.

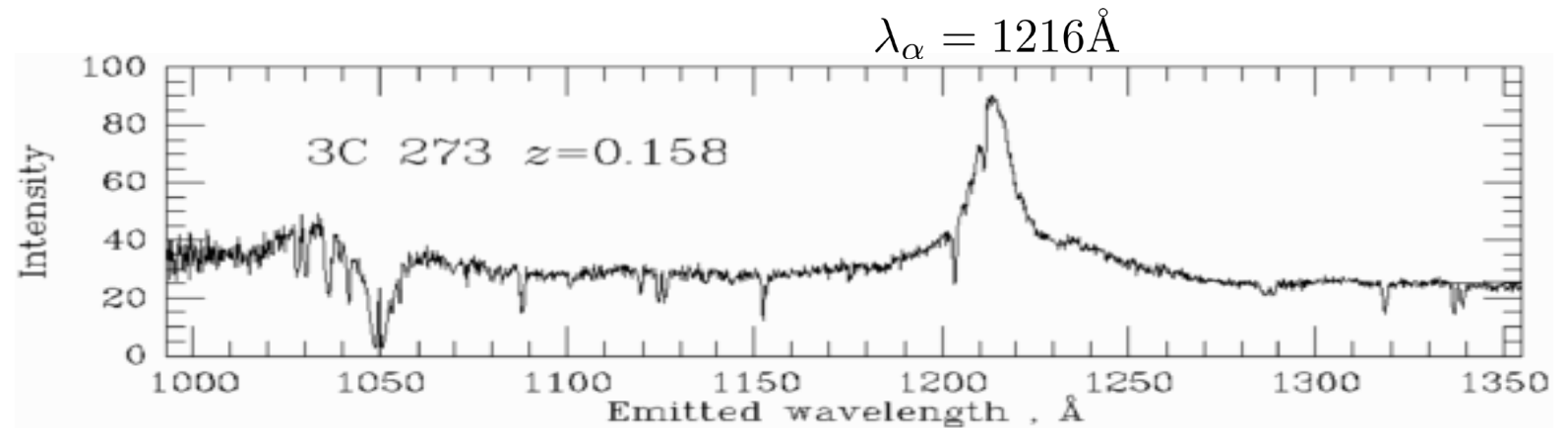
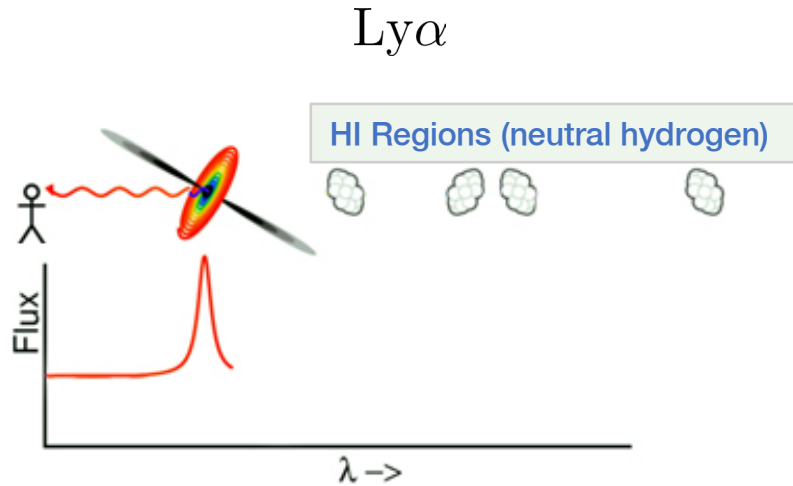
## More on Highly Ionized HII

- Mechanism of reionization:
  - Recombination requires a mean time of reionization:  
500 years per hydrogen atom.
  - Collisional reionization: Inadequate (mean lifetime  $\sim 10^4$  years)
  - Radiative reionization: need a mean intensity  $\sim 1.2 \times 10^{20} \text{ erg cm}^{-2} (\text{c/s})^{-1} \text{ sec}^{-1} \text{ ster}^{-1}$ .
    - Normal galaxies, Radiogalaxies: too low, ~10% from quasars
    - Quasars
    - IGM itself: more promising if  $T = 2 \times 10^5 \text{ K}$  at  $z = 2$ .
  - Ionization is more collisionally-dominant as  $T$  goes higher.



# A Sidenote - Ly $\alpha$ Forest

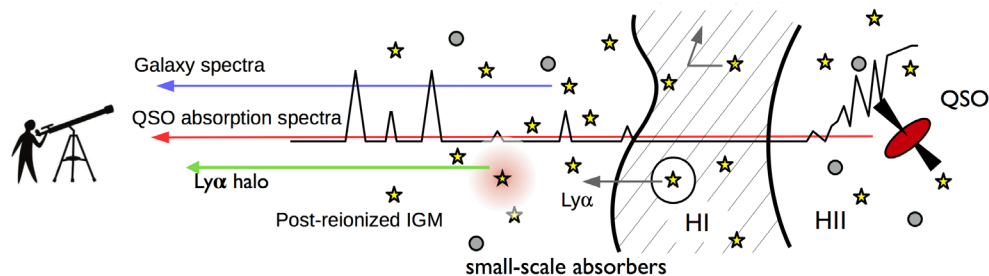
- At low  $z$ , **HI (neutral hydrogen)** is ionized into **HII (ionized hydrogen)**.
- At low  $z$ , only small portion of spectrum is absorbed by light-of-sight scattered **HI regions**.



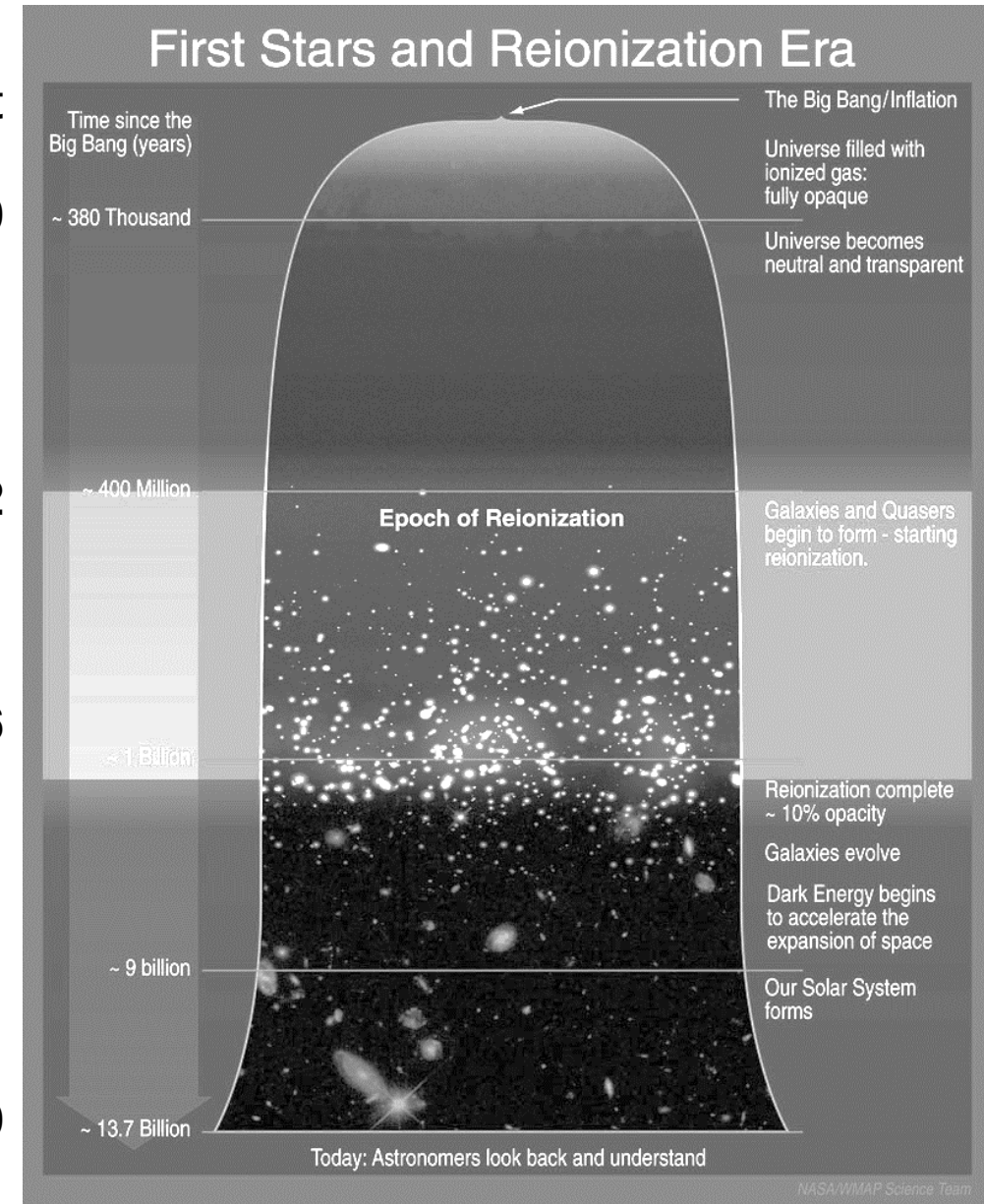
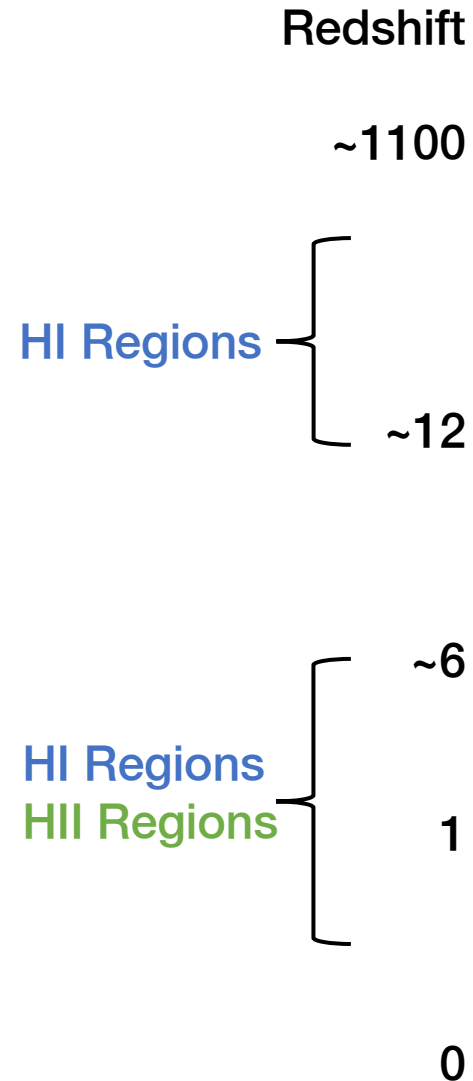
# A Sidenote - Gunn-Peterson Trough

- Early Universe (high- $z$ , “dark”):
  - Dense **HI region**
  - High optical depth
- Late Universe (low- $z$ ):
  - Reionization
  - **HI region** is less dense
  - Higher transparency

Spectroscopic survey of Ly $\alpha$  emitting galaxies in QSO fields



Credits: Koki Kakiichi (UCL); NASA/WMAP



# GP Optical Depth vs. HI Density at High-z

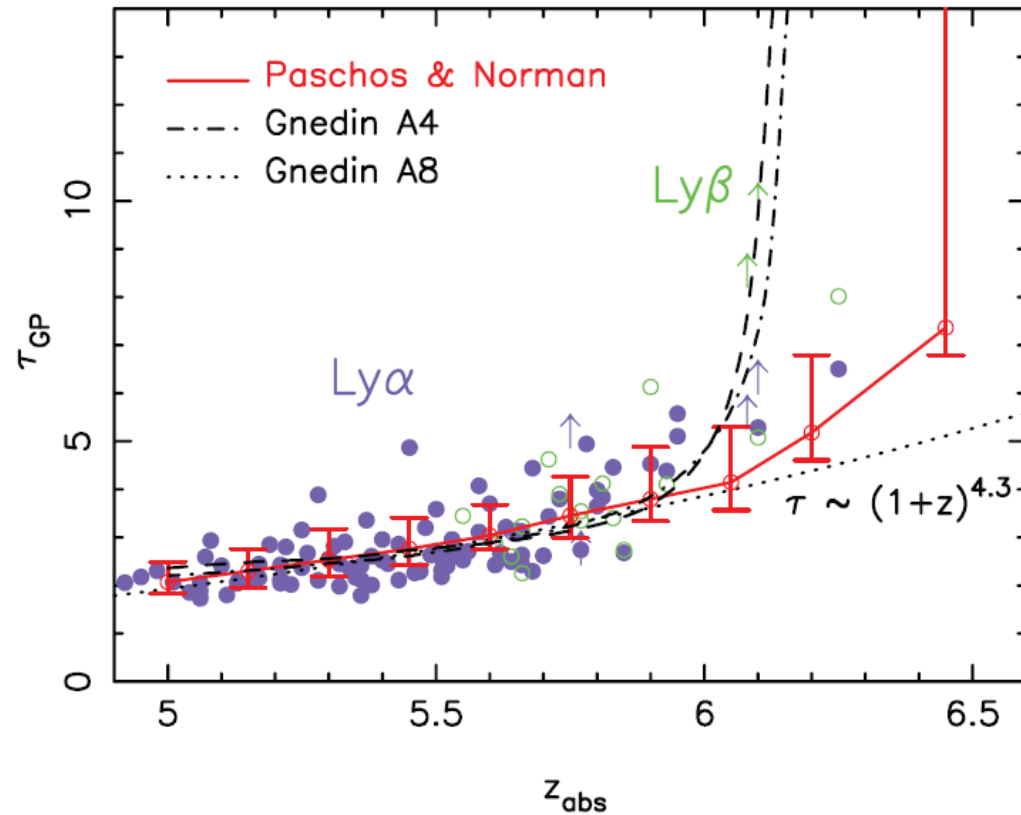
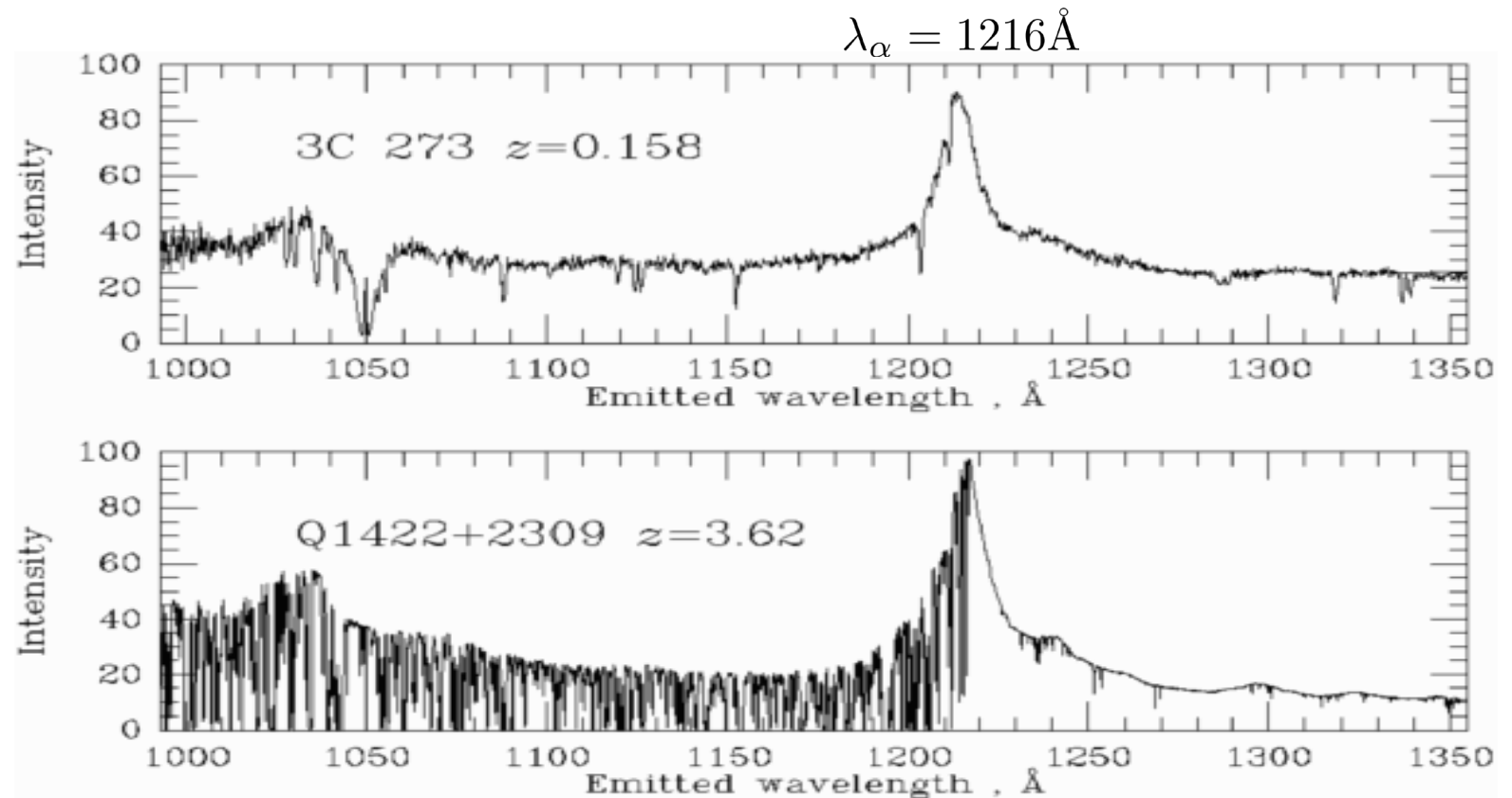
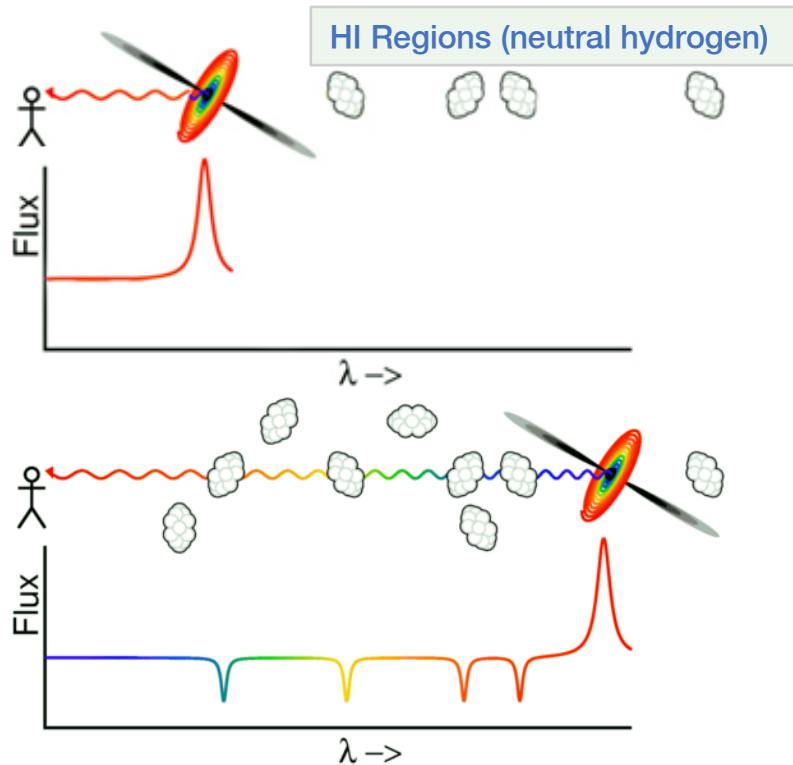


FIG. 9.— Comparison of the evolution of observed GP optical depth with simulations. Data points are the same as in Fig. 5. The dotted line is the power-law fit to the optical depth evolution at  $z < 5.5$ :  $\tau_{GP} \propto (1+z)^{4.3}$ . The solid line with error bars is the result from simulations of Paschos & Norman (2005), which have  $z_{reion} \sim 7$ . The dashed and dot-dashed lines are the 4 and 8 Mpc simulations of Gnedin (2004), respectively, which have  $z_{reion} \sim 6.5$ . The data points fall between the two simulations but are somewhat closer to those of Gnedin.



# A Sidenote - Ly $\alpha$ Forest

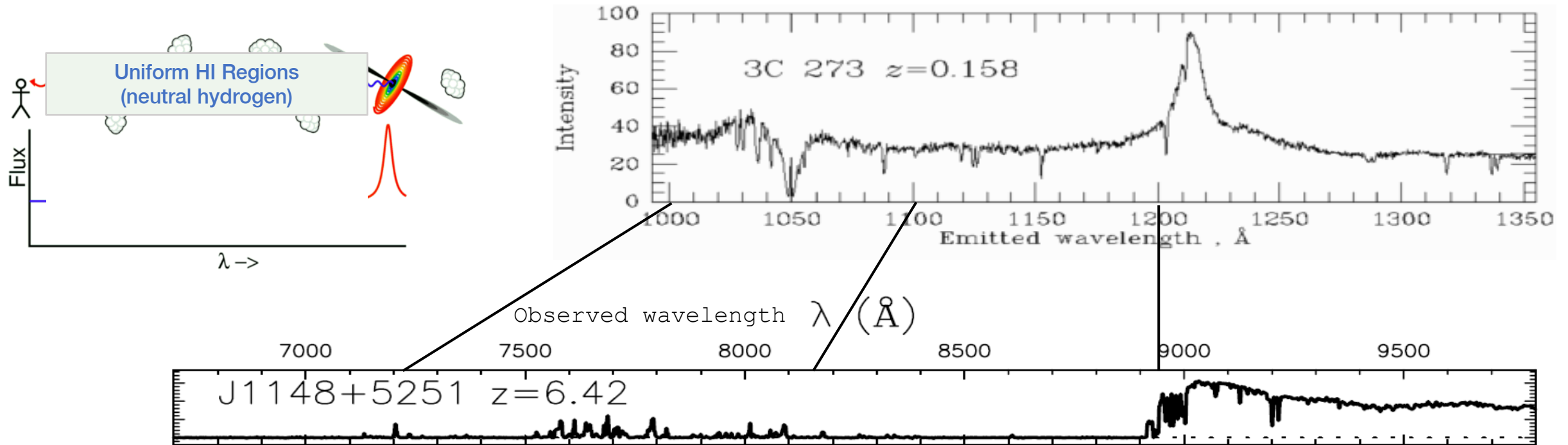
- At low  $z$ , **HI (neutral hydrogen)** is ionized into **HII (ionized hydrogen)**.
- At low  $z$ , only small portion of spectrum is absorbed by light-of-sight scattered **HI regions**.
- As more **HI regions** appear along line-of-sight, or redshift increases, the radiation from quasars can be scattered: “Ly $\alpha$  Forest”.





# A Sidenote - Gunn-Peterson Trough

- Notice: “ $\text{Ly}\alpha$  Forest” has discrete absorptions since it is not uniform along line-of-sight.
  - Assume we have a uniform and optically-thick HI gas in IGM.
- Just on the left of  $\lambda_\alpha = 1216\text{\AA}$ , the forest should turn into a continued absorption (close to zero) dip.



# A Sidenote - Quasars' Spectra Around $z \sim 6$

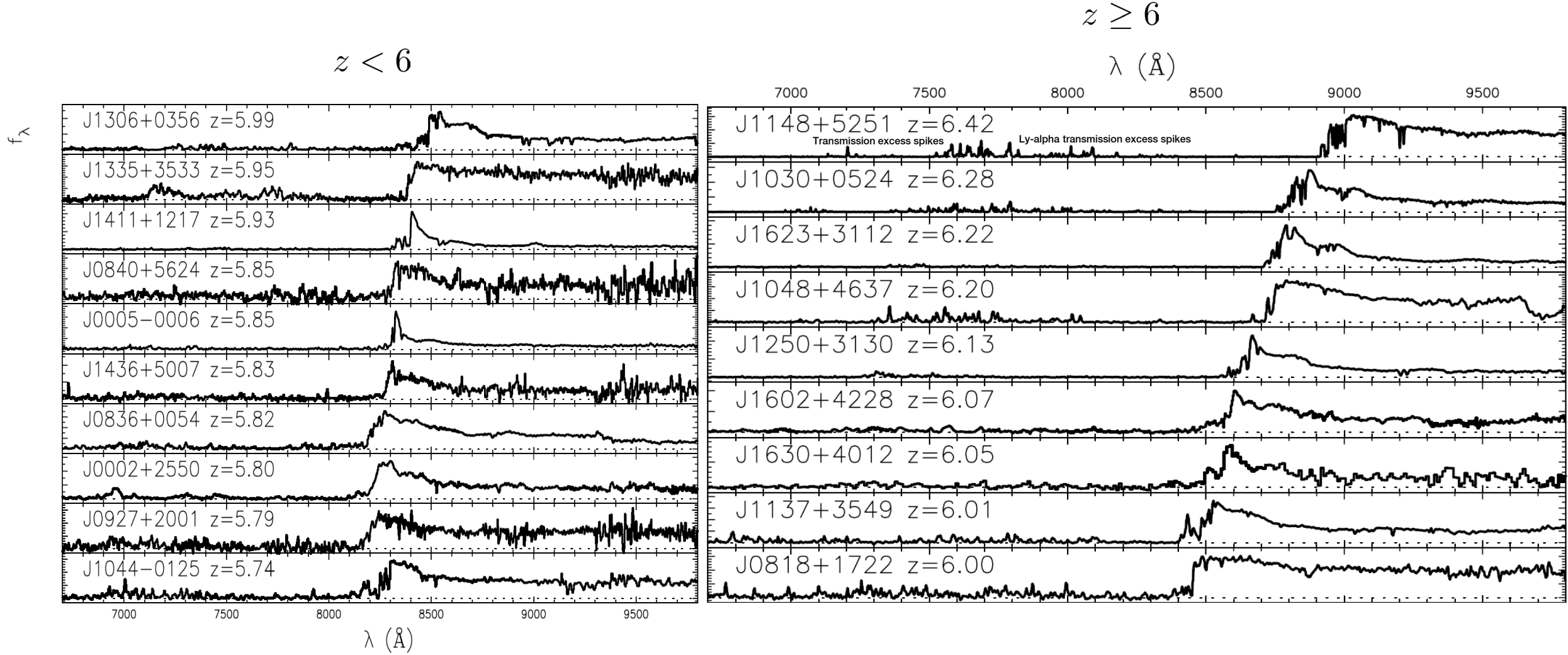


Fig. 1. — Spectra of our sample of 19 SDSS quasars at  $5.74 < z < 6.42$ . Twelve of the spectra were taken with Keck ESI, while the others were observed with the MMT Red Channel and Kitt Peak 4 m MARS spectrographs. See Table 1 for detailed information. (Fan et al., 2006, AJ, 132, 117)

## Takeaway

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Gunn-Peterson limit provided the first evidence that the universe was reionized by the formation of the first stars and quasars.

Most of the 30 most distant quasars are known in 2000s, which have led to the constraints of the epoch of reionization, predicted 60 years ago by Gunn and Peterson.

# References

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## Appendix 1: UV Spectral Slope (Power Law)

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The ultraviolet part of the emitted light contains information on various facets of the state of the galaxy. The UV continuum between roughly 1250 Å and 2600 Å is commonly parametrized as a power law of the

$$F_{\lambda} \sim \lambda^{-\alpha}.$$

This parametrization was first introduced by Calzetti et al. (1994) as a means of studying the effects of dust extinction in galaxies, and has later been shown to trace the dust extinction at higher redshifts, as well as being correlated with far-infrared dust emission (see e.g. Finkelstein et al. 2012, Meurer et al. 1999, Reddy et al. 2012).