

A Theorem Proving Assistant

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- What is Theorem Proving
- What I Built
- How does it work

What is a Theorem?

A Theorem is a proposition which is not necessarily self-evident but can be proved with a chain of reasoning.

Theorem (\vee zero)

$$P \vee \text{true} \equiv \text{true}$$

What is Theorem Proving?

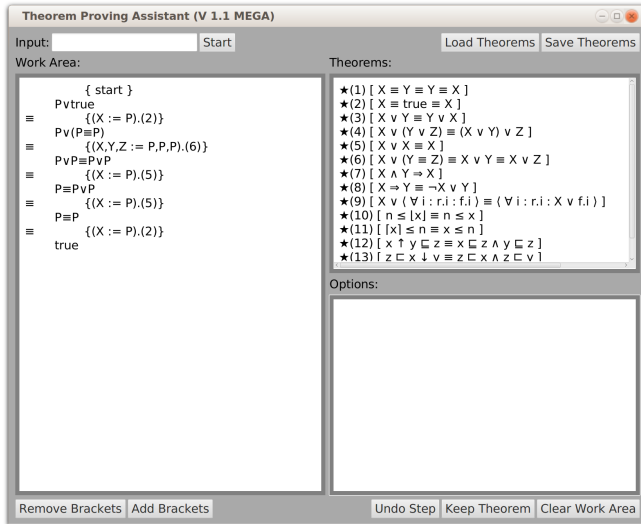
Proof of \vee zero

$$\begin{aligned} & P \vee \text{true} \\ \equiv & \{(X := P).(0)\} \\ & P \vee (P \equiv P) \\ \equiv & \{(X, Y, Z := P, P, P).(1)\} \\ & P \vee P \equiv P \vee P \\ \equiv & \{(X := P).(2)\} \\ & P \equiv P \\ \equiv & \{(X := P).(0)\} \\ & \text{true} \end{aligned}$$

Theorems

$$\begin{aligned} (0) & [X \equiv X \equiv \text{true}] \\ (1) & [X \vee (Y \vee Z) \equiv (X \vee Y) \vee Z] \\ (2) & [X \vee X \equiv X] \end{aligned}$$

What I Built

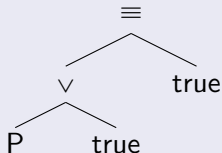


How it Works - Expression Representation

String Representation (\vee zero)

$P \vee \text{true} \equiv \text{true}$

Tree Representation (\vee zero)



- Syntax trees are used to represent expressions.

How it Works - Pattern Matching

Questions...