

# **Xorshift\* and Erlang/OTP: Searching for Better PRNGs**

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2010-2015 speaker (for *six*  
consecutive years!)



**Executive  
summary: do not  
try inventing  
your own  
random number  
generators!**

# PRNGs matter

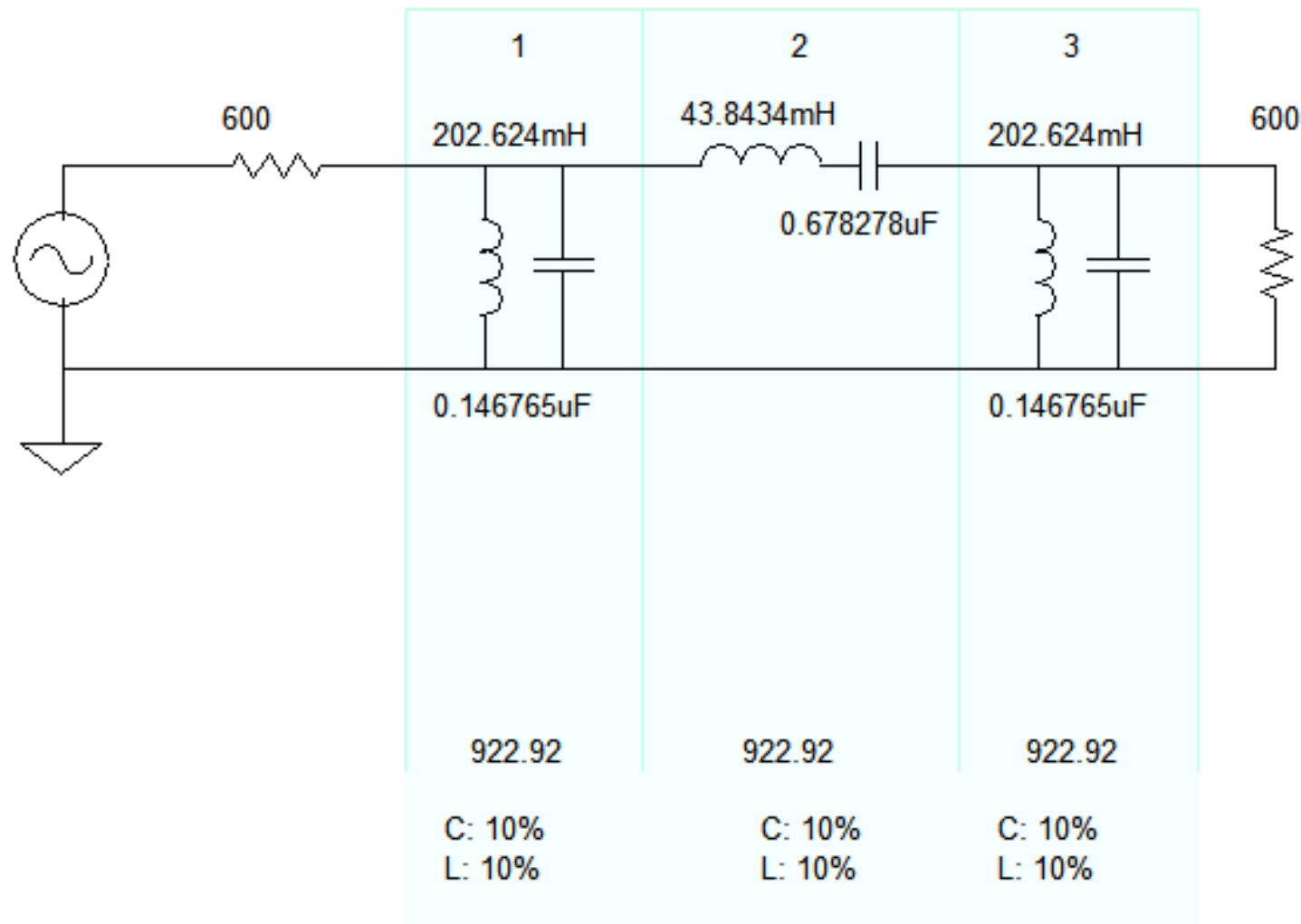
- The first talk of pseudo random number generators in Erlang Factory events was on 2011
- Now four years later, people are *still using* the good-old random module, already *fully exploited*. **We should stop using it!**
- So I decided to do the talk again with new algorithms, and the talk is accepted

# PRNGs are everywhere

- Rolling dice (for games)
- (Property) testing (QuickCheck, ProPer, Triq)
- Variation analysis of electronic circuits
- Network congestion and delay analysis
- Risk analysis of project schedules
- Passwords (*Secure PRNGs* only!)
- Generating noise

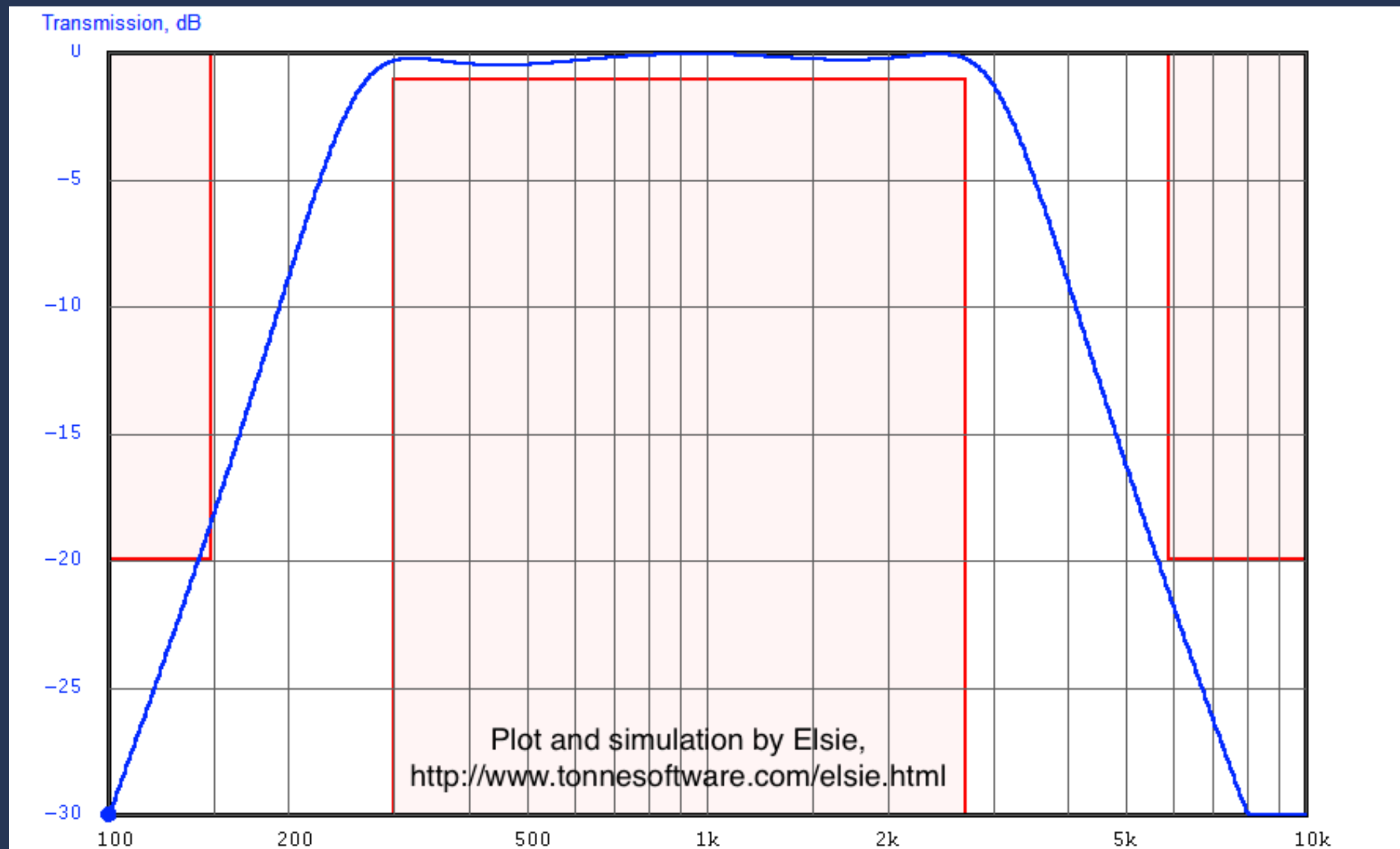


# Variation analysis of a band pass filter

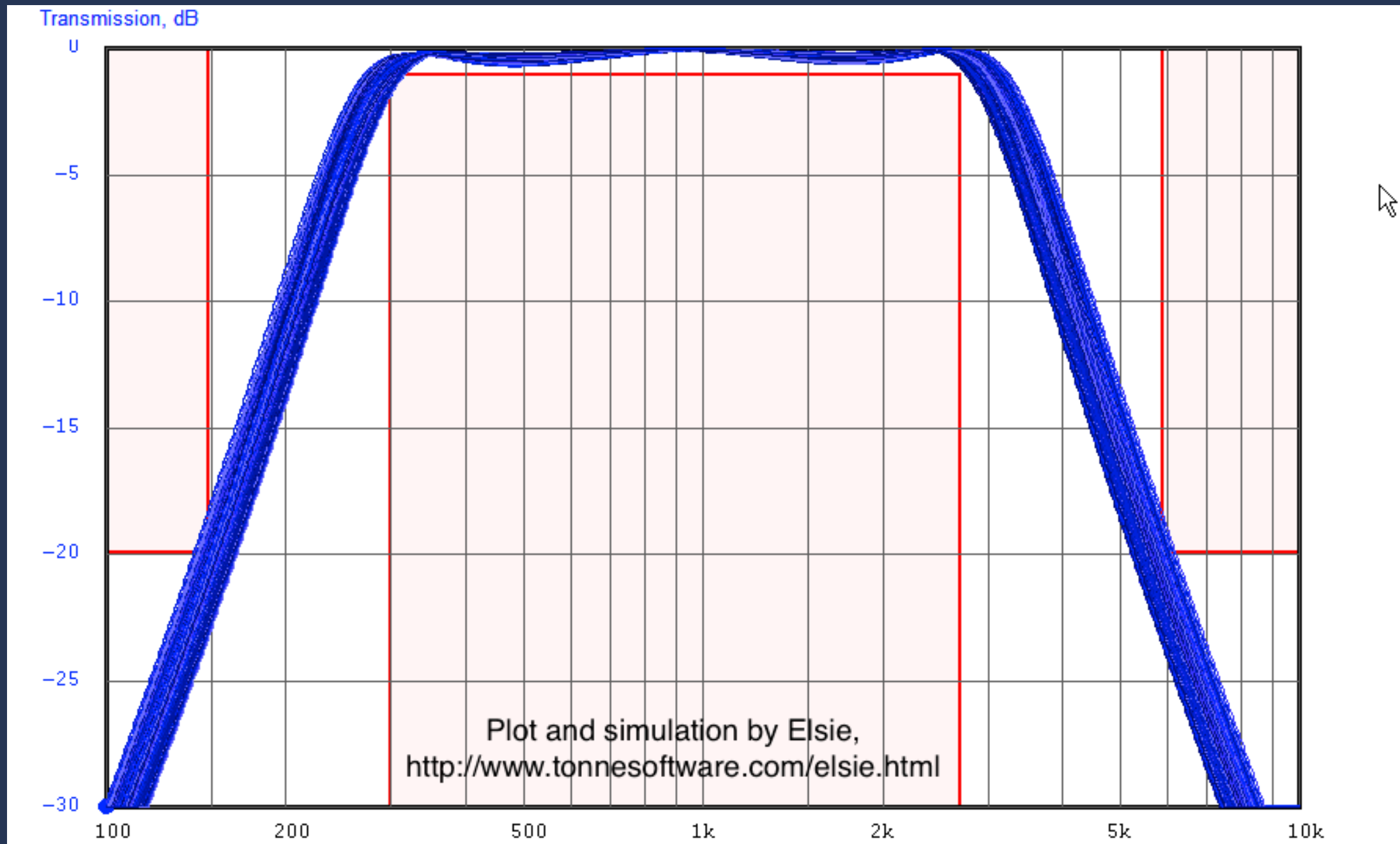


A circuit example of Elsie, <http://www.tonnesoftware.com/elsie.html>

# Without variance



# With 10% variance





# How PRNG works

- Sequential iterative process
- For multiple processes, seeds and other parameters should be chosen carefully to prevent sequence overlapping

```
% Give a seed S1  
{Result1, S2} = prng(S1),  
{Result2, S3} = prng(S2),  
% ... and on and on
```

# NOT in this talk: Secure PRNGs

- For password and cryptographic key generation with strong security
- Use `crypto:strong_rand_bytes/1`
- Remember entropy gathering takes time
- This is *cryptography* - use and *only* use proven algorithms! *Do not invent yours!*

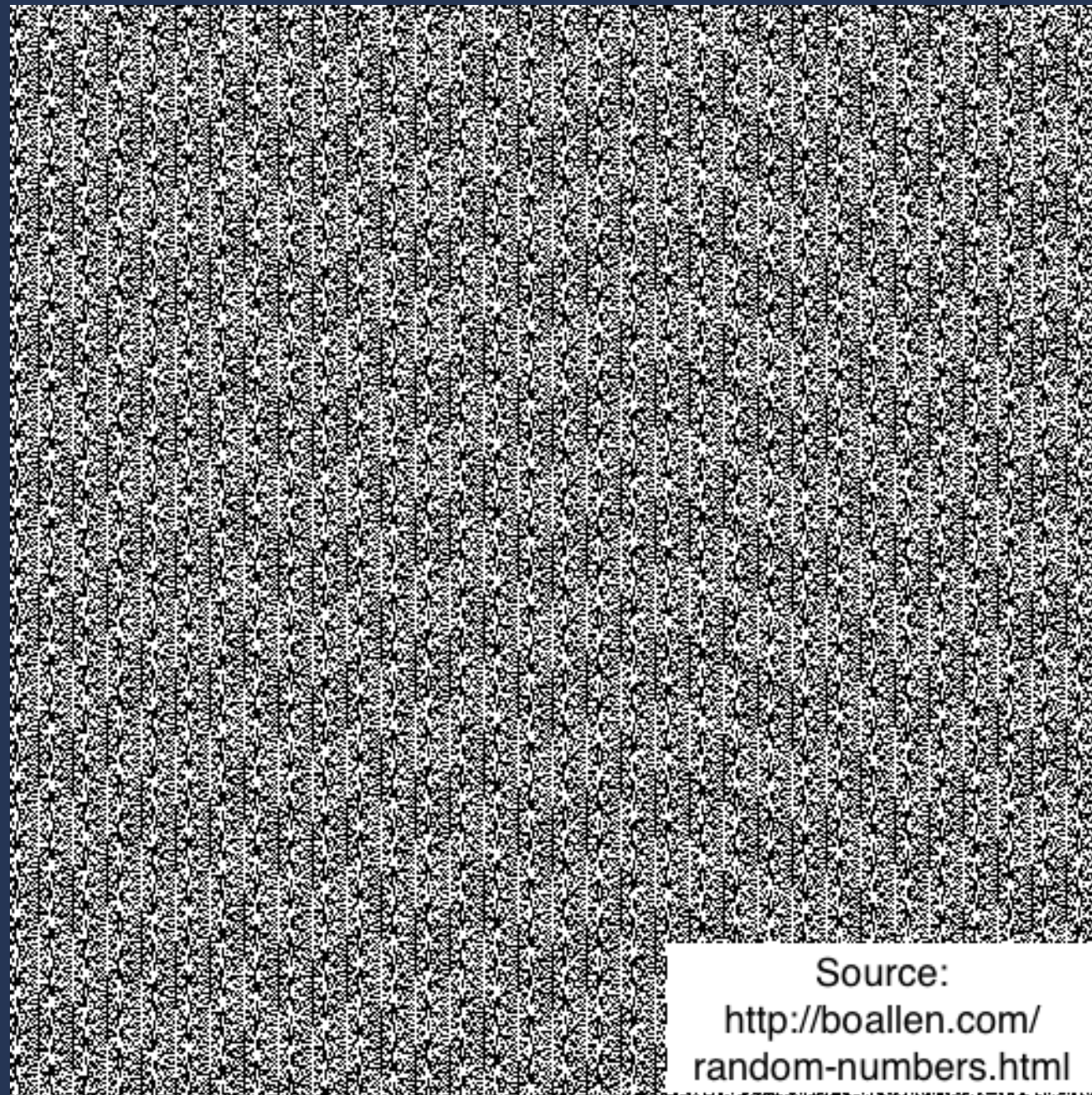
# In this talk: non-secure PRNGs

- May be *vulnerable to cryptographic attacks*
- (Uniform) distribution guaranteed
- *Predictive*: same seed = same result
- Lots of seed (internal state) choices
- Long period: no intelligible patterns

# Even non-secure PRNGs fail

- Found from the observable patterns by making a graphical representation
- *Very short period* of showing up the same number sequence again
- Even a fairly long sequence of numbers can be *fully exploited* and made predictable

# PHP5 on Windows (2012)

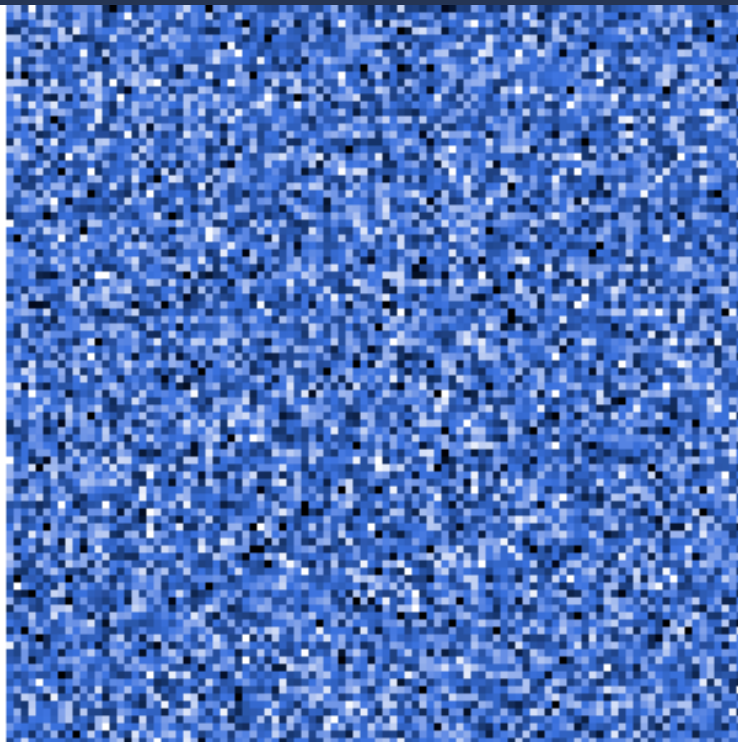


Source:  
[http://boallen.com/  
random-numbers.html](http://boallen.com/random-numbers.html)

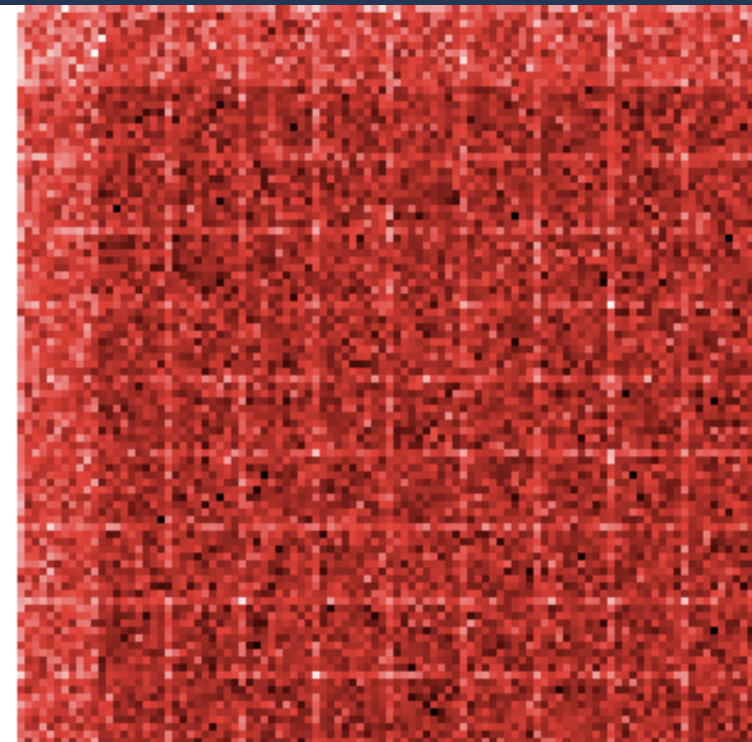


# Other PRNG failures

- Cryptocat 2013 (blue: OK, red: bad)



Colourmap of 20,000,000 Cryptocat floats (derived from /dev/urandom values 0..249)



Colourmap of 20,000,000 old-school Cryptocat floats (derived from PRNG values 0..250)



# Erlang/OTP's first ever security advisory

- ... was about PRNG! (R14B02, 2011)
- US CERT VU#178990: Erlang/OTP SSH library uses a weak random number generator (CVE-2011-0766)
- Used random non-secure PRNG for the SSH session RNG seed, easily exploitable

# Erlang random's problem

- The algorithm AS183 is too old (designed in 1980s for 16-bit computers)
- Period: 6953607871644  $\approx 2^{(42.661)}$ , too short for modern computer exploits
- Fully exploited in < 9 hours on Core i5 (single core) ([my C source](#)) - Richard O'Keefe told me this was *nothing new in either academic and engineering perspectives* (he is right!)

# Alternative Erlang PRNGs

- sfmt-erlang (SFMT,  $2^{19937}-1$ , 32-bit)
- tinymt-erlang (TinyMT,  $2^{127}-1$ ,  $\sim 2^{56}$  orthogonal sequences, 32-bit)
- exs64 (XorShift\*64,  $2^{64}-1$ , 64-bit)
- exsplus (Xorshift+128,  $2^{128}-1$ , 64-bit)
- exs1024 (Xorshift\*1024,  $2^{1024}-1$ , 64-bit)

# SFMT

- Mersenne Twister: default PRNG on Python, MATLAB, C++11, R, etc.
- Internal state: 624 32-bit integers (2496 bytes)
- SIMD-oriented Fast Mersenne Twister (SFMT)  
= MT improved
- Extremely long period ( $2^{19937}-1$ , longer variants available)
- On Erlang: NIF and non-NIF versions available

# sfmt-erlang: on NIFs

sfmt-erlang gains a lot by NIFs because:

- It needs bulk state initialization (624 x 32-bit)
- NIFnizing it makes ~16 times faster on FreeBSD 10.1-STABLE, Core i5-3427U (2.3GHz, 8 HTs), Erlang/OTP 17.4.1, clang
- Execution time: ~1600 -> ~15 microseconds
- Reductions: 1569 -> 4 (process\_info/2)

# TinyMT

- Tiny Mersenne Twister for restricted resources
- Shorter but sufficient period ( $2^{127}-1$ )
- 127-bit state + three 32-bit words for the polynomial parameters
- $\sim 2^{56}$  choice of orthogonal polynomials, suitable for parallelism
- On Erlang: non-NIF implementation (NIF tested but abandoned)



# tinymt-erlang: on NIFs

tinymt-erlang did not gain much from NIFs presumably because:

- Bulk initialization is not applicable
- State calculation complexity is small
- Calling overhead of Erlang functions takes most of execution time
- sfmt-erlang in NIFs was *faster* for generating a large set of numbers

# So are NIFs effective?

- Not really, unless processing a bulk generation/computation
- Remember NIFs *block* the scheduler
- If NIFs are not needed, don't use them
- If NIFs are really needed, tuning the scheduler is *inevitable* - ask the gurus for the details

# Xorshift\*/+ algorithms

- Marsaglia's Xorshift, output scrambled by the algorithm of Sebastiano Vigna for the best result against TestU01 strength test
- Xorshift64\*, Xorshift128+, Xorshift1024\* are so far the most practical three choices
- C code in public domain
- Deceptively simple

# Xorshift64\*

```
% See https://github.com/jj1bdx/exs64
-type uint64() :: 0..16#ffffffffffffffff.
-opaque state() :: uint64().
-define(UINT64MASK, 16#ffffffffffffffff).
-spec next(state()) -> {uint64(), state()}.
next(R) ->
    R1 = R bxor (R bsr 12),
    R2 = R1 bxor ((R1 bsl 25) band ?UINT64MASK),
    R3 = R2 bxor (R2 bsr 27),
    {(R3 * 2685821657736338717) band ?UINT64MASK, R3}.
```

# Xorshift1024\* (1/2)

```
% See https://github.com/jj1bdx/exs1024
-type uint64() :: 0..16#ffffffffffffffff.
-opaque seedval() :: list(uint64()). % 16 64-bit integers
-opaque state() :: {list(uint64()), list(uint64())}.
-define(UINT64MASK, 16#ffffffffffffffff).
%% calc(S0, S1) -> {X, NS1} / X: random number output
-spec calc(uint64(), uint64()) -> {uint64(), uint64()}.
calc(S0, S1) ->
    S11 = S1 bxor ((S1 bsl 31) band ?UINT64MASK),
    S12 = S11 bxor (S11 bsr 11),
    S01 = S0 bxor (S0 bsr 30),
    NS1 = S01 bxor S12,
    {(NS1 * 1181783497276652981) band ?UINT64MASK, NS1}.
```

# Xorshift1024\* (2/2)

```
-spec next(state()) -> {uint64(), state()}.  
% with a ring buffer using a pair of lists  
next({[H], RL}) ->  
    next({[H|lists:reverse(RL)], []});  
next({L, RL}) ->  
    [S0|L2] = L,  
    [S1|L3] = L2,  
    {X, NS1} = calc(S0, S1),  
    {X, {[NS1|L3], [S0|RL]}}.
```



# Performance implications

- HiPE highly recommended
- Handling full 64-bit numbers means handling BIGNUMs and slow; short integers are up to  $(2^{59})$
- `exs64`: < x2 execution time of random
- `exs1024`: slower, but ~ x2 of random
- Speed penalty: worth being paid for

# Suggested purposes for the alternative PRNGs

- sfmt-erlang: proven, can be chosen in ProPer
- tinymt-erlang: proven, has ~268 million polynomial parameters available at [tinymtdc-longbatch](#)
- exs64: replacement of AS183
- exsplus: an alternative to exs64
- exs1024: good choice for simulation

# Merging to OTP (1/2)

- Dan Gudmundsson (of OTP Team) offered me to help writing a multi-algorithm successor of random module
- `exs64/plus/1024`: MIT licensed (by me)
- `sfmt-erlang/tinymt-erlang`: BSD licensed
- All pieces of code had to be relicensed in *Erlang Public License* to be included in OTP

# Merging to OTP (2/2)

- It was expected to be called as new random, but the OTP team didn't want it (presumably due to backward compatibility issues), so it's called rand
- Project name: emprng
- random-compatible functions currently available for the six algorithms: as183, exs64 (default), exsplus, exs1024, sfmt, tinymt

# Future directions

- Keep promoting banning/deprecating the good-old random module and use *something else that is much better* (try exs64)
- Merge emprng to OTP: more algorithms, user-supplied functions, tests
- Analyze performance implication on large-scale applications

**Thanks**  
**Questions?**