LSTM_Captioning

March 31, 2020

1 Image Captioning with LSTMs

In the previous exercise you implemented a vanilla RNN and applied it to image captioning. In this notebook you will implement the LSTM update rule and use it for image captioning.

```
[1]: # As usual, a bit of setup
   from __future__ import print_function
   import time, os, json
   import numpy as np
   import matplotlib.pyplot as plt
   import nltk
   from cs231n.gradient_check import eval_numerical_gradient,_
    ⇔eval_numerical_gradient_array
   from cs231n.rnn_layers import *
   from cs231n.captioning_solver import CaptioningSolver
   from cs231n.classifiers.rnn import CaptioningRNN
   from cs231n.coco_utils import load_coco_data, sample_coco_minibatch, u
     →decode_captions
   from cs231n.image_utils import image_from_url
   %matplotlib inline
   plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
   plt.rcParams['image.interpolation'] = 'nearest'
   plt.rcParams['image.cmap'] = 'gray'
    # for auto-reloading external modules
   # see http://stackoverflow.com/questions/1907993/
    \rightarrow autoreload-of-modules-in-ipython
   %load ext autoreload
   %autoreload 2
   def rel_error(x, y):
        """ returns relative error """
       return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

2 Load MS-COCO data

As in the previous notebook, we will use the Microsoft COCO dataset for captioning.

```
[2]: # Load COCO data from disk; this returns a dictionary
    # We'll work with dimensionality-reduced features for this notebook, but feel
    # free to experiment with the original features by changing the flag below.
    data = load_coco_data(pca_features=True)

# Print out all the keys and values from the data dictionary
for k, v in data.items():
    if type(v) == np.ndarray:
        print(k, type(v), v.shape, v.dtype)
    else:
        print(k, type(v), len(v))
```

```
train_captions <class 'numpy.ndarray'> (400135, 17) int32
train_image_idxs <class 'numpy.ndarray'> (400135,) int32
val_captions <class 'numpy.ndarray'> (195954, 17) int32
val_image_idxs <class 'numpy.ndarray'> (195954,) int32
train_features <class 'numpy.ndarray'> (82783, 512) float32
val_features <class 'numpy.ndarray'> (40504, 512) float32
idx_to_word <class 'list'> 1004
word_to_idx <class 'dict'> 1004
train_urls <class 'numpy.ndarray'> (82783,) <U63
val_urls <class 'numpy.ndarray'> (40504,) <U63
```

3 LSTM

If you read recent papers, you'll see that many people use a variant on the vanialla RNN called Long-Short Term Memory (LSTM) RNNs. Vanilla RNNs can be tough to train on long sequences due to vanishing and exploding gradiants caused by repeated matrix multiplication. LSTMs solve this problem by replacing the simple update rule of the vanilla RNN with a gating mechanism as follows.

4 LSTM: step forward

Implement the forward pass for a single timestep of an LSTM in the <code>lstm_step_forward</code> function in the file <code>cs231n/rnn_layers.py</code>. This should be similar to the <code>rnn_step_forward</code> function that you implemented above, but using the LSTM update rule instead.

Once you are done, run the following to perform a simple test of your implementation. You should see errors around 1e-8 or less.

```
[3]: N, D, H = 3, 4, 5
x = np.linspace(-0.4, 1.2, num=N*D).reshape(N, D)
prev_h = np.linspace(-0.3, 0.7, num=N*H).reshape(N, H)
prev_c = np.linspace(-0.4, 0.9, num=N*H).reshape(N, H)
Wx = np.linspace(-2.1, 1.3, num=4*D*H).reshape(D, 4 * H)
```

```
Wh = np.linspace(-0.7, 2.2, num=4*H*H).reshape(H, 4 * H)
b = np.linspace(0.3, 0.7, num=4*H)

next_h, next_c, cache = lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)

expected_next_h = np.asarray([
        [ 0.24635157,  0.28610883,  0.32240467,  0.35525807,  0.38474904],
        [ 0.49223563,  0.55611431,  0.61507696,  0.66844003,  0.7159181 ],
        [ 0.56735664,  0.66310127,  0.74419266,  0.80889665,  0.858299 ]])

expected_next_c = np.asarray([
        [ 0.32986176,  0.39145139,  0.451556,   0.51014116,  0.56717407],
        [ 0.66382255,  0.76674007,  0.87195994,  0.97902709,  1.08751345],
        [ 0.74192008,  0.90592151,  1.07717006,  1.25120233,  1.42395676]])

print('next_h error: ', rel_error(expected_next_h, next_h))
print('next_c error: ', rel_error(expected_next_c, next_c))
```

next_h error: 5.7054131967097955e-09
next_c error: 5.8143123088804145e-09

5 LSTM: step backward

Implement the backward pass for a single LSTM timestep in the function <code>lstm_step_backward</code> in the file <code>cs231n/rnn_layers.py</code>. Once you are done, run the following to perform numeric gradient checking on your implementation. You should see errors around <code>1e-6</code> or less.

```
[4]: np.random.seed(231)
   N, D, H = 4, 5, 6
   x = np.random.randn(N, D)
   prev_h = np.random.randn(N, H)
   prev_c = np.random.randn(N, H)
   Wx = np.random.randn(D, 4 * H)
   Wh = np.random.randn(H, 4 * H)
   b = np.random.randn(4 * H)
   next_h, next_c, cache = lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)
   dnext_h = np.random.randn(*next_h.shape)
   dnext_c = np.random.randn(*next_c.shape)
   fx_h = lambda x: lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)[0]
   fh_h = lambda h: lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)[0]
   fc_h = lambda c: lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)[0]
   fWx_h = lambda Wx: lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)[0]
   fWh_h = lambda Wh: lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)[0]
   fb h = lambda b: lstm step_forward(x, prev h, prev_c, Wx, Wh, b)[0]
```

```
fx c = lambda x: lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)[1]
fh_c = lambda h: lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)[1]
fc_c = lambda c: lstm step_forward(x, prev h, prev_c, Wx, Wh, b)[1]
fWx_c = lambda Wx: lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)[1]
fWh_c = lambda Wh: lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)[1]
fb_c = lambda b: lstm_step_forward(x, prev_h, prev_c, Wx, Wh, b)[1]
num grad = eval numerical gradient array
dx_num = num_grad(fx_h, x, dnext_h) + num_grad(fx_c, x, dnext_c)
dh_num = num_grad(fh_h, prev_h, dnext_h) + num_grad(fh_c, prev_h, dnext_c)
dc_num = num_grad(fc_h, prev_c, dnext_h) + num_grad(fc_c, prev_c, dnext_c)
dWx_num = num_grad(fWx_h, Wx, dnext_h) + num_grad(fWx_c, Wx, dnext_c)
dWh num = num grad(fWh h, Wh, dnext h) + num grad(fWh c, Wh, dnext c)
db_num = num_grad(fb_h, b, dnext_h) + num_grad(fb_c, b, dnext_c)
dx, dh, dc, dWx, dWh, db = lstm_step_backward(dnext_h, dnext_c, cache)
print('dx error: ', rel_error(dx_num, dx))
print('dh error: ', rel_error(dh_num, dh))
print('dc error: ', rel_error(dc_num, dc))
print('dWx error: ', rel_error(dWx_num, dWx))
print('dWh error: ', rel error(dWh num, dWh))
print('db error: ', rel_error(db_num, db))
```

dx error: 6.335228376583295e-10 dh error: 3.3963774090592634e-10 dc error: 1.5221795880129153e-10 dWx error: 2.1010957817542796e-09 dWh error: 9.712296109943072e-08 db error: 2.4915214652298706e-10

6 LSTM: forward

In the function lstm_forward in the file cs231n/rnn_layers.py, implement the lstm_forward function to run an LSTM forward on an entire timeseries of data.

When you are done, run the following to check your implementation. You should see an error around 1e-7.

```
[5]: N, D, H, T = 2, 5, 4, 3
x = np.linspace(-0.4, 0.6, num=N*T*D).reshape(N, T, D)
h0 = np.linspace(-0.4, 0.8, num=N*H).reshape(N, H)
Wx = np.linspace(-0.2, 0.9, num=4*D*H).reshape(D, 4 * H)
Wh = np.linspace(-0.3, 0.6, num=4*H*H).reshape(H, 4 * H)
b = np.linspace(0.2, 0.7, num=4*H)
```

```
h, cache = lstm_forward(x, h0, Wx, Wh, b)

expected_h = np.asarray([
    [[ 0.01764008,  0.01823233,  0.01882671,  0.0194232 ],
    [ 0.11287491,  0.12146228,  0.13018446,  0.13902939],
    [ 0.31358768,  0.33338627,  0.35304453,  0.37250975]],
    [[ 0.45767879,  0.4761092,  0.4936887,  0.51041945],
    [ 0.6704845,  0.69350089,  0.71486014,  0.7346449 ],
    [ 0.81733511,  0.83677871,  0.85403753,  0.86935314]]])

print('h error: ', rel_error(expected_h, h))
```

h error: 8.610537452106624e-08

7 LSTM: backward

Implement the backward pass for an LSTM over an entire timeseries of data in the function <code>lstm_backward</code> in the file <code>cs231n/rnn_layers.py</code>. When you are done, run the following to perform numeric gradient checking on your implementation. You should see errors around <code>1e-7</code> or less.

```
[6]: from cs231n.rnn_layers import lstm_forward, lstm_backward
   np.random.seed(231)
   N, D, T, H = 2, 3, 10, 6
   x = np.random.randn(N, T, D)
   h0 = np.random.randn(N, H)
   Wx = np.random.randn(D, 4 * H)
   Wh = np.random.randn(H, 4 * H)
   b = np.random.randn(4 * H)
   out, cache = lstm_forward(x, h0, Wx, Wh, b)
   dout = np.random.randn(*out.shape)
   dx, dh0, dWx, dWh, db = lstm_backward(dout, cache)
   fx = lambda x: lstm forward(x, h0, Wx, Wh, b)[0]
   fh0 = lambda h0: lstm_forward(x, h0, Wx, Wh, b)[0]
   fWx = lambda Wx: lstm_forward(x, h0, Wx, Wh, b)[0]
   fWh = lambda Wh: lstm_forward(x, h0, Wx, Wh, b)[0]
   fb = lambda b: lstm_forward(x, h0, Wx, Wh, b)[0]
   dx_num = eval_numerical_gradient_array(fx, x, dout)
   dh0_num = eval_numerical_gradient_array(fh0, h0, dout)
   dWx_num = eval_numerical_gradient_array(fWx, Wx, dout)
```

```
dWh_num = eval_numerical_gradient_array(fWh, Wh, dout)
db_num = eval_numerical_gradient_array(fb, b, dout)

print('dx error: ', rel_error(dx_num, dx))
print('dh0 error: ', rel_error(dh0_num, dh0))
print('dWx error: ', rel_error(dWx_num, dWx))
print('dWh error: ', rel_error(dWh_num, dWh))
print('db error: ', rel_error(db_num, db))
```

dx error: 6.993886058711491e-09 dh0 error: 1.5042771782195826e-09 dWx error: 3.226295800444722e-09 dWh error: 2.6984653332291804e-06 db error: 8.236643805250263e-10

8 LSTM captioning model

Now that you have implemented an LSTM, update the implementation of the loss method of the CaptioningRNN class in the file cs231n/classifiers/rnn.py to handle the case where self.cell_type is lstm. This should require adding less than 10 lines of code.

Once you have done so, run the following to check your implementation. You should see a difference of less than 1e-10.

```
[7]: N, D, W, H = 10, 20, 30, 40
   word_to_idx = {'<NULL>': 0, 'cat': 2, 'dog': 3}
   V = len(word to idx)
   T = 13
   model = CaptioningRNN(word_to_idx,
              input_dim=D,
              wordvec_dim=W,
              hidden_dim=H,
              cell_type='lstm',
              dtype=np.float64)
   # Set all model parameters to fixed values
   for k, v in model.params.items():
       model.params[k] = np.linspace(-1.4, 1.3, num=v.size).reshape(*v.shape)
   features = np.linspace(-0.5, 1.7, num=N*D).reshape(N, D)
   captions = (np.arange(N * T) % V).reshape(N, T)
   loss, grads = model.loss(features, captions)
   expected_loss = 9.82445935443
   print('loss: ', loss)
   print('expected loss: ', expected_loss)
```

```
print('difference: ', abs(loss - expected_loss))
```

loss: 9.824459354432264 expected loss: 9.82445935443 difference: 2.2648549702353193e-12

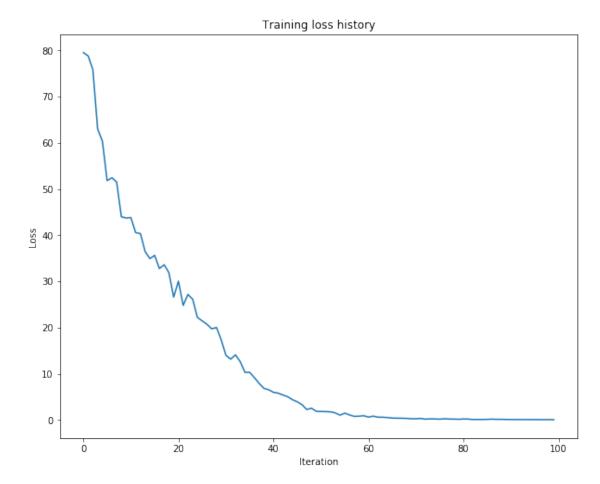
9 Overfit LSTM captioning model

Run the following to overfit an LSTM captioning model on the same small dataset as we used for the RNN previously. You should see losses less than 0.5.

```
[8]: np.random.seed(231)
   small_data = load_coco_data(max_train=50)
   small_lstm_model = CaptioningRNN(
              cell_type='lstm',
              word_to_idx=data['word_to_idx'],
              input_dim=data['train_features'].shape[1],
              hidden_dim=512,
              wordvec_dim=256,
              dtype=np.float32,
            )
   small_lstm_solver = CaptioningSolver(small_lstm_model, small_data,
               update_rule='adam',
               num epochs=50,
               batch_size=25,
               optim_config={
                 'learning_rate': 5e-3,
               },
               lr_decay=0.995,
               verbose=True, print_every=10,
             )
   small_lstm_solver.train()
   # Plot the training losses
   plt.plot(small_lstm_solver.loss_history)
   plt.xlabel('Iteration')
   plt.ylabel('Loss')
   plt.title('Training loss history')
   plt.show()
```

(Iteration 1 / 100) loss: 79.551150 (Iteration 11 / 100) loss: 43.829101 (Iteration 21 / 100) loss: 30.062624

```
(Iteration 31 / 100) loss: 14.020127
(Iteration 41 / 100) loss: 6.004181
(Iteration 51 / 100) loss: 1.849470
(Iteration 61 / 100) loss: 0.640726
(Iteration 71 / 100) loss: 0.280547
(Iteration 81 / 100) loss: 0.232692
(Iteration 91 / 100) loss: 0.121932
```



10 LSTM test-time sampling

Modify the sample method of the CaptioningRNN class to handle the case where self.cell_type is lstm. This should take fewer than 10 lines of code.

When you are done run the following to sample from your overfit LSTM model on some training and validation set samples.

```
[9]: for split in ['train', 'val']:
    minibatch = sample_coco_minibatch(small_data, split=split, batch_size=2)
    gt_captions, features, urls = minibatch
    gt_captions = decode_captions(gt_captions, data['idx_to_word'])
```

```
sample_captions = small_lstm_model.sample(features)
sample_captions = decode_captions(sample_captions, data['idx_to_word'])

for gt_caption, sample_caption, url in zip(gt_captions, sample_captions,usurls):
    plt.imshow(image_from_url(url))
    plt.title('%s\n%s\nGT:%s' % (split, sample_caption, gt_caption))
    plt.axis('off')
    plt.show()
```

train
a man standing on the side of a road with bags of luggage <END>
GT:<START> a man standing on the side of a road with bags of luggage <END>



train
a man <UNK> with a bright colorful kite <END>
GT:<START> a man <UNK> with a bright colorful kite <END>



val
a person that is <UNK> of a <UNK> <END>
GT:<START> a sign that is on the front of a train station <END>



val
a cat sitting with a <UNK> <END>
GT:<START> a car is parked on a street at night <END>



11 Train a good captioning model (extra credit for 4803)

Using the pieces you have implemented in this and the previous notebook, train a captioning model that gives decent qualitative results (better than the random garbage you saw with the overfit models) when sampling on the validation set. You can subsample the training set if you want; we just want to see samples on the validation set that are better than random.

In addition to qualitatively evaluating your model by inspecting its results, you can also quantitatively evaluate your model using the BLEU unigram precision metric. In order to achieve full credit you should train a model that achieves a BLEU unigram score of >0.3. BLEU scores range from 0 to 1; the closer to 1, the better. Here's a reference to the paper that introduces BLEU if you're interested in learning more about how it works.

Feel free to use PyTorch for this section if you'd like to train faster on a GPU... though you can definitely get above 0.3 using your Numpy code. We're providing you the evaluation code that is compatible with the Numpy model as defined above... you should be able to adapt it for PyTorch if you go that route.

Create the model in the file cs231n/classifiers/mymodel.py. You can base it after the CaptioningRNN class. Write a text comment in the delineated cell below explaining what you

tried in your model.

Also add a cell below that trains and tests your model. Make sure to include the call to evaluate_model which prints out your highest validation BLEU score for full credit.

```
[10]: def BLEU score(gt caption, sample caption):
         gt caption: string, ground-truth caption
         sample_caption: string, your model's predicted caption
         Returns unigram BLEU score.
         reference = [x for x in gt_caption.split(' ')
                      if ('<END>' not in x and '<START>' not in x and '<UNK>' not in_{\sqcup}
      →x)]
         hypothesis = [x for x in sample_caption.split(' ')
                       if ('<END>' not in x and '<START>' not in x and '<UNK>' not
         BLEUscore = nltk.translate.bleu_score.sentence_bleu([reference],_
      →hypothesis, weights = [1])
         return BLEUscore
     def evaluate model(model):
         model: CaptioningRNN model
         Prints unigram BLEU score averaged over 1000 training and val examples.
         BLEUscores = {}
         for split in ['train', 'val']:
             minibatch = sample_coco_minibatch(data, split=split, batch_size=1000)
             gt_captions, features, urls = minibatch
             gt_captions = decode_captions(gt_captions, data['idx_to_word'])
             sample_captions = model.sample(features)
             sample_captions = decode_captions(sample_captions, data['idx_to_word'])
             total score = 0.0
             for gt_caption, sample_caption, url in zip(gt_captions,__
      →sample_captions, urls):
                 total_score += BLEU_score(gt_caption, sample_caption)
             BLEUscores[split] = total_score / len(sample_captions)
         for split in BLEUscores:
             print('Average BLEU score for %s: %f' % (split, BLEUscores[split]))
```

12 write a description of your model here:

To generalize the model for the dataset, I choose 25000 samples. Since I observe that the word_dim has more influence so I use 2048 and hidden_dim=1024 to increase the complexity and prevent overfitting. However, if the learning rate is too low, the model could be downfitting. So I choose 5e-4 as learning rate.

```
[23]: # write your code to train your model here.
     # make sure to include the call to evaluate_model which prints out your highest_{\sqcup}
      →validation BLEU score.
     from cs231n.classifiers.mymodel import custom_RNN
     np.random.seed(231)
     small_data = load_coco_data(max_train=25000)
     small_lstm_model = custom_RNN(
               cell_type='lstm',
               word_to_idx=data['word_to_idx'],
               input_dim=data['train_features'].shape[1],
               hidden_dim=1024,
               wordvec_dim=2048,
               dtype=np.float64,
             )
     small_lstm_solver = CaptioningSolver(small_lstm_model, small_data,
                update_rule='adam',
                num_epochs=20,
                batch_size=32,
                optim_config={
                  'learning_rate': 5e-4,
                },
                lr_decay=0.996,
                verbose=True, print_every=1000,
     small_lstm_solver.train()
     evaluate_model(small_lstm_model)
```

```
(Iteration 1 / 15620) loss: 75.182688
(Iteration 1001 / 15620) loss: 25.804503
(Iteration 2001 / 15620) loss: 24.208552
(Iteration 3001 / 15620) loss: 19.496554
(Iteration 4001 / 15620) loss: 15.911798
(Iteration 5001 / 15620) loss: 14.905738
(Iteration 6001 / 15620) loss: 12.409035
(Iteration 7001 / 15620) loss: 10.133162
```

```
(Iteration 8001 / 15620) loss: 10.053890
(Iteration 9001 / 15620) loss: 8.618081
(Iteration 10001 / 15620) loss: 6.064745
(Iteration 11001 / 15620) loss: 5.352113
(Iteration 12001 / 15620) loss: 2.945726
(Iteration 13001 / 15620) loss: 4.682234
(Iteration 14001 / 15620) loss: 3.075816
(Iteration 15001 / 15620) loss: 3.299403
Average BLEU score for train: 0.325480
Average BLEU score for val: 0.303842
```

[]: