

## ENME 314 Fluids Tutorial problems 2 Concepts

In these solutions, a full stop between numbers indicates multiplication i.e. 10.2=20

1. A mass
2.  $20\text{kg} \cdot 9.81\text{N/kg} = 200\text{N}$  (2s.f.)
3.  $20\text{ Kg} / 0.4536 = 44\text{ lbs}$

4.  $\lambda = \frac{kT}{\sqrt{2\pi} d^2 p} = 2.3 \times 10^{-8}\text{ m}$

5. a.  $\underline{v} = 3 \times 1\underline{\hat{i}} + 5 \times 2\underline{\hat{j}} + z \times 0\underline{\hat{k}} = 3\underline{\hat{i}} + 10\underline{\hat{j}}\text{m/s}$   
b. 10 m/s

6.  $B \approx -V \frac{\Delta p}{\Delta V}$  or  $\Delta p \approx -B \frac{\Delta V}{V}$  i.e. pressure must decrease for volume to increase.

$$\Delta p \approx -B \frac{\Delta V}{V}$$
$$= -513000\text{ Pa} [(5.8\text{ ml})/(10^6\text{ ml/m}^3)]/1.15\text{ m}^3 = \underline{-2.5873\text{ Pa}}$$

or -2.6 Pa to the correct number of significant figures (SF)

7.  $1\text{m}^3 \cdot 1000\text{kg/m}^3 \cdot 9.81\text{N/kg} = 9800\text{N}$  (2s.f.)
8. Mass is  $4896.2\text{N}/9.81\text{N/kg} = 499.\text{kg}$ , density is  $499\text{kg}/0.5\text{m}^3 = 998\text{kg/m}^3$  (2s.f.) so temperature is  $20^\circ\text{C}$  (closest match on the supplied table)
9.  $1.164\text{kg/m}^3$
10.  $965.3\text{ kg/m}^3$
11.  $p = \rho R' T$   $P = 202,650\text{Pa}$ ,  $T = 373\text{K}$  (must convert to Kelvin!),  $R'$ =specific gas constant  $287\text{J K}^{-1}\text{kg}^{-1}$  for dry air, so  $\rho = 1.89\text{kgm}^{-3}$  (3 s.f.)
12. Must be drilled at right angles to the pipe wall, free of burrs with nothing protruding into the pipe, and closed at one end by the pressure gauge.
13.  $P = -\rho g z = -1000\text{kg/m}^3 \cdot 9.81\text{N/kg} \cdot (-1\text{m}) = 10,000\text{Pa}$  (1s.f.)
14. Piezometric pressure =  $p(z) + \rho g z = p_o = \text{atmospheric pressure} = 101,325\text{Pa}$ . The piezometric pressure is the same at both heights: it does not vary with height.

15.  $5.0\text{ kph} = 1.4\text{ms}^{-1}$   $p = \rho R' T$   $p = 101,325\text{Pa}$ .  $T = 293\text{K}$  must convert to Kelvin.  $R'$ =specific gas constant  $287\text{J K}^{-1}\text{kg}^{-1}$  for dry air. So  $\rho = 1.20\text{kgm}^{-3}$ . Dynamic pressure =  $\frac{1}{2} \rho u^2 = 1.2\text{Pa}$  to 2.s.f.

16.  $\Delta p = \rho V^2/2$  or  $V = [2(\Delta p)/\rho]^{0.5} = [2(20. \text{ kPa})/998.2 \text{ kg/m}^3] = 6.3303 \text{ m/s}$

$= \underline{6.3 \text{ m/s (2 SF)}}$

17.  $P_{\text{static}}=101,325\text{Pa}$ .  $\frac{1}{2}\rho V^2=0.5 \times 1.2 \times 100^2=6,000\text{Pa}$ .  $P_{\text{stagnation}}=101,325\text{Pa}+6,000\text{Pa}=107,000 \text{ Pa (2s.f.)}$

18.  $P_{\text{static}}=1\text{m} \times 1000 \times 9.81=9810\text{Pa}$ .  $\frac{1}{2}\rho V^2=0.5 \times 1000 \times 10^2=50,000\text{Pa}$ .  $P_{\text{stagnation}}=9,810\text{Pa}+50,000\text{Pa}=60,000\text{Pa}$   
(2s.f.)

19.  $101325+120=101,445\text{Pa abs}$

20.  $200,000-101325=98,675\text{Pa g}$

21.  $90,000-101325=-11,325\text{Pa g}$  (negative: vacuum): answer should be written  $-11,300\text{Pa g}$  (3 s.f.)

22.  $100,000 \text{ Pa}/9810 \text{ N/m}^3=10.2 \text{ m}$  or  $10 \text{ m}$  to 1 s.f.

23. Spanwise

24. Streamwise

25. If you've found the data, you will know the answer now!

26. Water- yes. Ketchup- no: it's thixotropic.

27. It depends on how fast the milk moves. If you pour it in quickly, you see eddies of milk growing and splitting into smaller eddies, and it mixes quickly. This indicates a turbulent flow. If you pour it very slowly, you don't see these eddies and it takes a long time for the milk to mix into the tea, as the mixing is occurring mostly by diffusion.

28.  $Re=1.2\text{kg/m}^3 \cdot 2.0\text{m} \cdot 3.0\text{m/s}/1.8 \times 10^{-5} \text{ Pa.s}=400,000$

29.  $Re=1.2\text{kg/m}^3 \cdot 0.15\text{m} \cdot 3.0\text{m/s}/1.8 \times 10^{-5} \text{ Pa.s}=30,000$ .  $Re>4,000$  so this is turbulent.

30. Unsteady.

31. Unsteady (as the speed is changing) and 2D.

32. It can't be a free vortex, as the spoon is forcing the rotation; if stirred at constant speed there will be a forced vortex with solid body rotation. At the wall of the cup the no-slip condition will hold, so it will be like a Rankine vortex, or more realistically a Lamb-Oseen vortex, as tea has viscosity.

33.  $A=3.141 \cdot (0.080\text{m})^2/4=5.0 \times 10^{-3} \text{ m}^2$ . Drag force  $=0.45 \cdot 5.0 \times 10^{-3} \text{ m}^2 \cdot 0.5 \cdot 1.2\text{kgm}^{-3} \cdot (10\text{m/s})^2=0.14 \text{ N}$