

ENME 314-21S1 Homework 1

- This is worth 2.5% of the course marks.
 - Attempt all the questions.
 - Marks may be lost for illegible script, incorrect number of significant figures and failure to state assumptions.
 - You may discuss general concepts and methods with others, but you should not discuss or share your solutions to these specific questions. Submitting solutions based on such a discussion will be treated as plagiarism.
 - Hand in a hardcopy version of your answers.
 - Your submission should be clearly marked with your name, 8 digit student ID, date and “ENME 314 Homework 1” on all pages. Keep a copy of your solution (a photo is adequate if the writing can be read).
 - Place your submission into the dropbox on level 2 of the Mechanical Engineering Lab Wing, on the balcony overlooking the RJ Scott Atrium.
 - The deadline is 5pm Fri 12th March.
 - You may assume the acceleration due to gravity $g = 9.81 \text{ ms}^{-2}$
- 1) A pressure field is described by the equation $p = 1,000x + 500y + 10,000$ where p is the absolute static pressure in Pascals and x, y are Cartesian coordinates in metres. Determine the static pressure at $x = 0.10 \text{ m}, y = 2.0 \text{ m}$ (2 marks)
 - 2) Calculate the static pressure 2500 m above sea level in a stationary atmosphere. Assume the atmosphere has a constant density of 1.2 kgm^{-3} (note, this is not very realistic). Also assume the absolute static pressure at sea level is 101,325 Pa. (1 mark)
 - 3) Calculate the absolute stagnation pressure in a flow of water (density $1,000 \text{ kg m}^{-3}$ to 2 s.f.) moving at $10. \text{ ms}^{-1}$ in at a depth of 15 m with atmospheric pressure equal to 101,325 Pa at the free surface. (3 marks)
 - 4) If atmospheric pressure is 101,000 Pa, what is an absolute pressure of 401,000 Pa, expressed as a gauge pressure?
 - 5) Water at $15.0 \text{ }^{\circ}\text{C}$, flows at 1.5 m/s in a pipe of 0.050 m diameter.
 - a. Calculate the Reynolds number. (1 mark)
 - b. Is the flow laminar or turbulent? (1 mark)
 - 6) An aircraft is climbing (gaining altitude) at constant speed, through air which has constant properties. Is the flow steady or unsteady, and what is its dimensionality (0, 1, 2 or 3 D)? (2 marks)

- 7) A hydraulic jack has one cylinder of 100. mm diameter, and another of 200. mm diameter. If a force of 2,500 N is used to push down the piston in the smaller cylinder, what is the force developed on the piston the larger cylinder? (1 mark)
- 8) Calculate the absolute static pressure in Pipe B in the system shown in Figure 1 (2 marks).

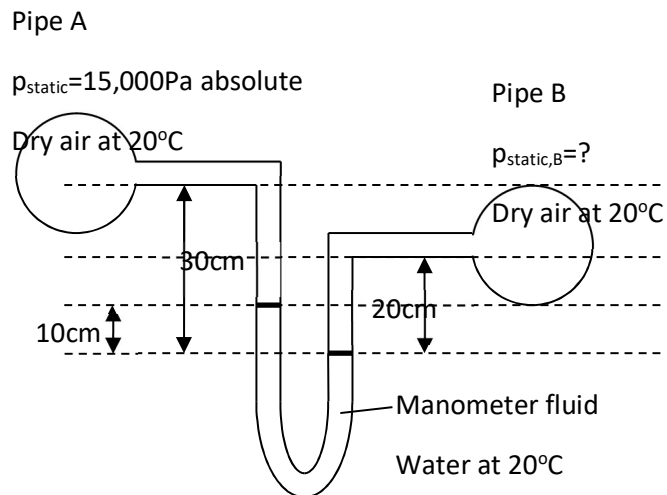


Figure 1: pipe and manometer system for question 8. All values are to 2 s.f.

- 9) Water flows into a pond with a flow rate of $0.015 \text{ m}^3/\text{hour}$ and out of the same pond with a flow rate of $0.010 \text{ m}^3/\text{hour}$. If the pond is empty at the start, and has a maximum capacity of 2.0 m^3 , how long does it take to fill? You may assume that evaporation is negligible. (2 marks)

- 1) A pressure field is described by the equation $p = 1,000x + 500y + 10,000$ where p is the absolute static pressure in Pascals and x, y are Cartesian coordinates in metres. Determine the static pressure at $x = 0.10 \text{ m}$, $y = 2.0 \text{ m}$ (2 marks)

$$p = 1000x + 500y + 10000$$

$$x = 0.1 \text{ m}$$

$$y = 2.0 \text{ m}$$

$$p = 1000(0.1) + 500(2) + 10000$$

$$= 100 + 1000 + 10000$$

$$= 11.1 \text{ kPa}$$

$$= 11 \text{ kPa abs (2 s.f.)}$$

- 2) Calculate the static pressure 2500 m above sea level in a stationary atmosphere. Assume the atmosphere has a constant density of 1.2 kg m^{-3} (note, this is not very realistic). Also assume the absolute static pressure at sea level is 101,325 Pa. (1 mark)

Using piezometric pressure $p_* = p(z) + \rho g z$

@ sea level ($z = 0$) $p_* = 101325 + 0 = 101325 \text{ Pa}$

rearrange for $p(z) \rightarrow p(z) = p_* - \rho g z$

@ $z = 2500$ with $\rho_{\text{air}} = 1.2 \text{ kg m}^{-3}$, $g = 9.81 \text{ ms}^{-2}$

$$p(2500) = 101325 - 1.2 \times 9.81 \times 2500$$

$$= 71895 \text{ Pa}$$

$$= 72 \text{ kPa abs. (2 s.f.)}$$

- 3) Calculate the absolute stagnation pressure in a flow of water (density $1,000 \text{ kg m}^{-3}$ to 2 s.f.) moving at $10. \text{ ms}^{-1}$ in at a depth of 15 m with atmospheric pressure equal to 101,325 Pa at the free surface. (3 marks)

$$p_{\text{stagnation}} = p_{\text{static}} + \frac{1}{2} \rho U^2$$

$$p_{\text{static}} = p_{\text{atm}} + \rho g h$$

$$\rho = 1000 \text{ kg m}^{-3}$$

$$U = 10 \text{ ms}^{-1}$$

$$h = 15 \text{ m}$$

$$p_{\text{atm.}} = 101325 \text{ Pa}$$

$$p_{\text{stagnation}} = p_{\text{atm}} + \rho g h + \frac{1}{2} \rho U^2$$

$$= 101325 + (1000 \times 9.81 \times 15) + \frac{1}{2} (1000 \times 10^2)$$

$$= 298475 \text{ Pa}$$

$$= 300 \text{ kPa abs (2 s.f.)}$$

- 4) If atmospheric pressure is 101,000 Pa, what is an absolute pressure of 401,000 Pa, expressed as a gauge pressure?

$$p_{\text{abs}} - p_{\text{atm}} = p_{\text{gauge}}$$

$$401000 - 101000 = 300000$$

$$= 300 \text{ kPa gauge (2 s.f.)}$$

- 5) Water at 15.0°C , flows at 1.5 m/s in a pipe of 0.050 m diameter.

a. Calculate the Reynolds number. (1 mark)

b. Is the flow laminar or turbulent? (1 mark)

a) $U = 1.5 \text{ ms}^{-1}$ μ for water at 15.0°C

$$d = 0.050 \text{ m} \quad \mu = 1.41 \times 10^{-6}$$

$$Re = \frac{UL}{\mu}$$

$$= \frac{1.5 \times 0.05}{1.41 \times 10^{-6}}$$

$$= 65789 \text{ (5 s.f.)}$$

$$= 66000 \text{ (5 s.f.)}$$

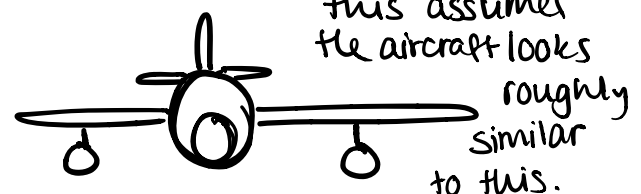
- b) flow is almost certainly turbulent as Reynolds number is $\gg 4000$

- 6) An aircraft is climbing (gaining altitude) at constant speed, through air which has constant properties. Is the flow steady or unsteady, and what is its dimensionality (0, 1, 2 or 3 D)? (2 marks)

Depends on what is meant by the air's 'properties'.

→ Assuming that 'constant properties' means that the pressure, temperature, density, kinematic viscosity, etc. do not change in any way, particularly time or altitude, then the flow will be steady.

→ The flow will be 3-dimensional as the plane has only mirror symmetry



'Aircraft' could mean anything. A flying sphere would only have 2D flow

- 7) A hydraulic jack has one cylinder of 100. mm diameter, and another of 200. mm diameter. If a force of 2,500 N is used to push down the piston in the smaller cylinder, what is the force developed on the piston the larger cylinder? (1 mark)

$$p_1 = p_2 \quad F_1 = p_1 A_1, F_2 = p_2 A_2$$

$$F_1 d_1 = F_2 d_2 \text{ e.g. } W_1 = W_2$$

$$p_1 A_1 d_1 = p_2 A_2 d_2 \quad \text{let } D = \text{diameter}$$

$$p_1 \frac{\pi D_1^2}{4} d_1 = p_2 \frac{\pi D_2^2}{4} d_2 \rightarrow \text{canceling } p_1 = p_2, \frac{\pi}{4}$$

$$D_1^2 d_1 = D_2^2 d_2$$

MUCH
FASTER
WAY

$$0.1^2 d_1 = 0.2^2 d_2$$

$$d_1 = \frac{0.2^2}{0.1^2} d_2$$

$$d_1 = 4 d_2$$

$$F_1 d_1 = F_2 d_2 \text{ subs}$$

$$4 F_1 d_2 = F_2 d_2 \text{ cancel}$$

$$4 F_1 = F_2$$

$$F_2 = 10 \text{ kN (2 s.f.)}$$

let smaller piston = 1, larger = 2

$$p_1 = p_2 \rightarrow F_1 = p_1 A_1, F_2 = p_2 A_2$$

$$p_1 = \frac{F_1}{A_1} \quad p_2 = \frac{F_2}{A_2}$$

$$\frac{F_1}{A_1} = \frac{F_2}{A_2}$$

$$F_2 = \frac{A_2}{A_1} F_1 \leftarrow F_1 = 2500 \text{ N}$$

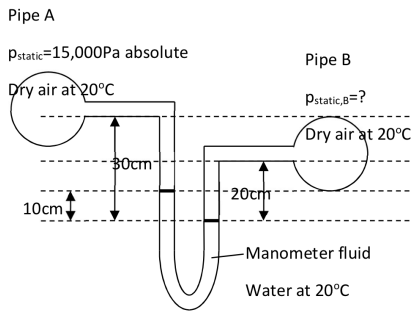
$$A_2 = \frac{\pi \times 0.2^2}{4} \Rightarrow \frac{A_2}{A_1} = \frac{0.2^2}{0.1^2} = 4$$

$$A_1 = \frac{\pi \times 0.1^2}{4}$$

$$F_2 = 4 F_1 = 4(2500) = 10,000 \text{ N}$$

$$= 10 \text{ kN (2 s.f.)}$$

- 8) Calculate the absolute static pressure in Pipe B in the system shown in Figure 1 (2 marks).



$$P_A + \rho_{\text{air}} \times 0.2 \text{ m} \times 9.81 + \rho_{\text{water}} \times 0.1 \times 9.81 = P_B + \rho_{\text{air}} \times 0.2 \text{ m}$$

$$15000 + 1.204 \times 0.2 \times 9.81 + 998.2 \times 0.1 \times 9.81 = P_B + 1.204 \times 0.2 \times 9.81$$

$$15000 + 979.23 = P_B$$

$$= 15979.23 \text{ Pa}$$

$$= 16 \text{ kPa abs (2 s.f.)}$$

- 9) Water flows into a pond with a flow rate of 0.015 m³/hour and out of the same pond with a flow rate of 0.010 m³/hour. If the pond is empty at the start, and has a maximum capacity of 2.0 m³, how long does it take to fill? You may assume that evaporation is negligible. (2 marks)

and no other losses
↓

Taking the pond as control volume * Assume evaporation is negligible and volume is conserved throughout system, no changes in pressure, density, etc.

$$\sum \dot{V} = \frac{dV}{dt} \Rightarrow \text{let flow into control volume be +ve, flow out be -ve}$$

$$\text{flow in} = 0.015 \text{ m}^3/\text{hour}$$

$$\text{flow out} = -0.010 \text{ m}^3/\text{hour}$$

$$\sum \dot{V} = 0.015 - 0.010$$

$$\therefore \frac{dV}{dt} = 0.005 \text{ m}^3/\text{hour}$$

$$\text{maximum capacity} = 2.0 \text{ m}^3$$

$$\frac{2.0 \text{ m}^3}{0.005 \text{ m}^3/\text{hour}} = 400 \text{ hours (2 s.f.)}$$

$$\approx 17 \text{ days (2 s.f.)}$$