

$$\text{L'01. } w(x, t) = \sin(x + ct)$$

$$\frac{\partial w}{\partial t}(x, t) = \cos(x + ct) \cdot (0 + c \cdot 1) = \cos(x + ct) \cdot c$$

$$\frac{\partial^2 w}{\partial t^2} = \frac{\partial}{\partial t} \cdot (\cos(x + ct) \cdot c) = -\sin(x + ct) \cdot (0 + c \cdot 1) \cdot c = -\sin(x + ct) \cdot c^2$$

$$\frac{\partial w}{\partial x}(x, t) = \cos(x + ct) \cdot (1 + c \cdot 0) = \cos(x + ct) \cdot 1 = \cos(x + ct)$$

$$\frac{\partial^2 w}{\partial x^2} = \frac{\partial}{\partial x} \cdot (\cos(x + ct)) = -\sin(x + ct) \cdot (1 + c \cdot 0) = -\sin(x + ct) \cdot 1 = -\sin(x + ct)$$

$$\frac{\partial^2 w}{\partial t^2} = c^2 \cdot \frac{\partial^2 w}{\partial x^2} \Leftrightarrow \underline{\underline{c^2 \cdot -\sin(x + ct) = c^2 \cdot -\sin(x + ct)}}$$

$$2a_2) v(x, t) = \sin(x+ct) + \cos(2x+2ct)$$

$$\begin{aligned} \frac{\partial v}{\partial t} &= v'(x, t) = \cos(x+ct) \cdot (0+c \cdot 1) + -\sin(2x+2ct) \cdot (0+2 \cdot c \cdot 1) \\ &= c \cdot \cos(x+ct) + 2c \cdot -\sin(2x+2ct) \end{aligned}$$

$$\begin{aligned} \frac{\partial^2 v}{\partial t^2} &= \frac{\partial}{\partial t} \cdot (c \cdot \cos(x+ct) + 2c \cdot -\sin(2x+2ct)) = c \cdot -\sin(x+ct) \cdot (0+c \cdot 1) + 2c \cdot -\cos(2x+2ct) \cdot (0+2 \cdot c \cdot 1) \\ &= c \cdot c \cdot -\sin(x+ct) + 2c \cdot 2c \cdot -\cos(2x+2ct) = c^2 \cdot -\sin(x+ct) + 4c^2 \cdot -\cos(2x+2ct) \end{aligned}$$

$$\frac{\partial v}{\partial x} = \cos(x+ct) \cdot (1+c \cdot 0) + -\sin(2x+2ct) \cdot (2+2 \cdot c \cdot 0) = 1 \cdot \cos(x+ct) + 2 \cdot -\sin(2x+2ct)$$

$$\begin{aligned} \frac{\partial^2 v}{\partial x^2} &= \frac{\partial}{\partial x} \cdot (\cos(x+ct) + 2 \cdot -\sin(2x+2ct)) = -\sin(x+ct) \cdot (1+c \cdot 0) + 2 \cdot -\cos(2x+2ct) \cdot (2+2 \cdot c \cdot 0) \\ &= -\sin(x+ct) + 4 \cdot -\cos(2x+2ct) \end{aligned}$$

$$\frac{\partial^2 v}{\partial t^2} = c^2 \frac{\partial^2 v}{\partial x^2} \Rightarrow \underbrace{c^2 \cdot (-\sin(x+ct) + 4 \cdot -\cos(2x+2ct))}_{\frac{\partial^2 v}{\partial t^2}} = c^2 \cdot \underbrace{(-\sin(x+ct) + 4 \cdot -\cos(2x+2ct))}_{\frac{\partial^2 v}{\partial x^2}}$$