# Identifying Galaxy Blends with Gaussian Processes

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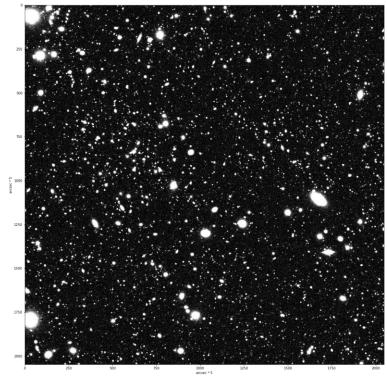


# **Galaxy scene simulation**

#### Sersic model bulge and disk for each galaxy

 Sersic parameters, ellipticity components, relative component fluxes from cosmoDC2 catalog; overall flux in each band and lensed RA,Dec from DESC DC2 truth catalog

- Weak lensing shear and magnification
  - Gamma components and convergence from cosmoDC2 catalog
- Kolmogorov PSF
  - FWHM = 0.7 (+- 10% per exposure)
- Random sub-pixel-scale scene offset ('dither')
- Photon shooting
- Silicon sensor
  - 'lsst\_itl\_32' in galsim
- Sky background
  - Dark sky magnitudes from smtn-002.lsst.io
  - +- 5% mean flux per exposure
  - Poisson noise in each pixel
- 100 separate exposures simulated, then added together



i-band, 2048^2 pixels (409.6^2 arcsec)

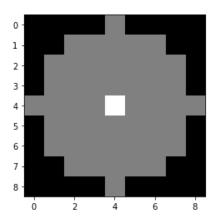
## **Footprint Construction**

- Subtract estimated sky background
- Convolve with Gaussian approximation of PSF
- Threshold each pixel at S/N >~ 5 to get initial footprints
  - In the background-subtracted, PSF-convolved image, single-pixel S/N = pixel intensity / sqrt(sky)\*sqrt(A)

where A = sum over pixels of (integrated, normalized PSF)^2

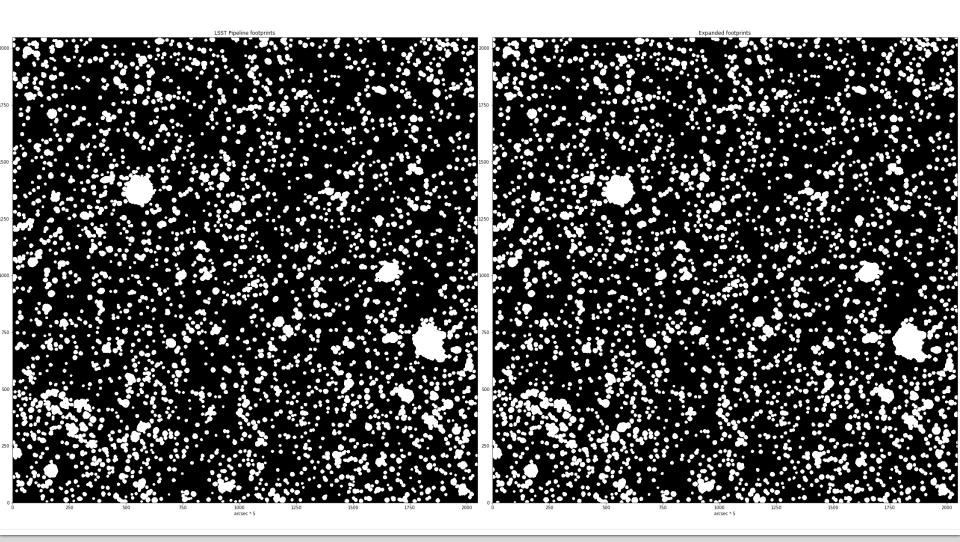
[doi:10.1093/pasj/psx080]

- Expand these initial footprints by ~2.4\*PSF width
- Merge the expanded footprints



# **LSST Pipeline footprints**

# My replication



### **Dataset**

- Define an i-band footprint as blended if it contains the center of > 1 galaxy with 5-sigma i-band flux
- Across 10 total scenes:
  - 65299 total galaxies with i-band flux >= 5 sigma
  - 64.3% of these galaxies are contained in i-band footprints
  - 8107 blended footprints
  - 15137 unblended footprints
    - For model training/evaluation: Choose a random subset of unblended footprints so that datasets are balanced
  - 0.4% of footprints contain no galaxies
    - These are on the scene boundaries, cut off at the edges
    - Ignoring these here



# **Preprocessing**

### For each footprint:

- Make a cutout of a fixed size, centered on that footprint
  - >= 23 pixels to a side
  - Specific centering strategy doesn't matter much
- Zero out any pixels that aren't part of the footprint
- Flatten the pixel array and normalize
  - Specific normalization doesn't matter much as long as values are constrained to lie between 0 and 1
- PCA embedding to reduce dimensionality
  - PCA dimension between 7 and 10



## **Gaussian Process Model**

- Gaussian process: An infinite collection of random variables, any finite subset of which is Gaussian-distributed
- The random variables: For each possible value of the PCAembedded data vectors, yield a number specifying the "blendedness"
  - If that number is > 0, classify the footprint as blended
- The Gaussian distribution: Prior mean of 0; covariance matrix is a function of the observed data vectors (kernel)
  - Common kernel choice: RBF
    - One hyperparameter length scale
  - Generalization: Matérn
    - Additional hyperparameter smoothness



## **Gaussian Process Model**

- For each training example i, define y<sub>i</sub> = +1 if blended, -1 if unblended
- Let f denote the model-estimated blendedness of training examples, f\* for test examples
- Matérn kernel:

$$k_{\text{Matérn}}(\vec{x}, \vec{x'}) = \frac{2^{1-\nu}}{\Gamma(\nu)} \left( \sqrt{2\nu} \frac{\|\vec{x} - \vec{x'}\|_{2}^{2}}{\ell} \right)^{\nu} K_{\nu} \left( \sqrt{2\nu} \frac{\|\vec{x} - \vec{x'}\|_{2}^{2}}{\ell} \right)$$

Kernel matrices:

$$(K_{\mathbf{ff}})_{i,j} \equiv k(x_i^{\text{train}}, x_j^{\text{train}})$$

$$(K_{\mathbf{f*}})_{i,j} \equiv k(x_i^{\text{train}}, x_j^{\text{test}}) = (K_{\mathbf{*f}})_{j,i}$$

$$(K_{\mathbf{**}})_{i,j} \equiv k(x_i^{\text{test}}, x_j^{\text{test}})$$

## **Gaussian Process Hyperparameters**

- Kernel length scale (ℓ)
  - Between 1e1 and 1e2
- Kernel smoothness (v)
  - At least 1(Note: As v -> inf, Matérn -> RBF)
- Assume that  $y_i \sim N(f_i, \sigma^2)$ 
  - $-\sigma$  between 1e-6 and 1e-4

### More math

• Given the PCA encodings of train and test examples, assert Bayesian prior on the joint distribution of blendedness of training and test sets:

$$\begin{bmatrix} \mathbf{y} \\ \mathbf{f}_* \end{bmatrix} = \mathcal{N} \left( 0, \begin{bmatrix} K_{\mathbf{ff}} + \sigma^2 I_n & K_{\mathbf{f}*} \\ K_{*\mathbf{f}} & K_{**} \end{bmatrix} \right).$$

 Additionally given the actual blendedness of the training examples, we can analytically compute the posterior joint distribution of blendedness of test set:

$$\mathbf{f}^* \mid X_{\text{train}}, X_{\text{test}}^*, \mathbf{y} \sim \mathcal{N}(\overline{\mathbf{f}}^*, C),$$

$$\bar{\mathbf{f}}^* \equiv K_{*\mathbf{f}}(K_{\mathbf{f}\mathbf{f}} + \sigma^2 I_n)^{-1} \mathbf{y}$$

$$C \equiv K_{**} - K_{*\mathbf{f}}(K_{\mathbf{f}\mathbf{f}} + \sigma^2 I_n)^{-1} K_{\mathbf{f}*}$$

• Classify test example as blended if  $\bar{\mathbf{f}}^* > 0$ 

# Model Comparison: Replication of LSST Pipeline Footprints

#### GP classifier

- Balanced accuracy = 0.884
- Unblended acc: 0.827, Blended acc: 0.940

- Logistic regression with 12 regularization
  - Balanced accuracy = 0.827
  - Unblended acc: 0.786, Blended acc: 0.868
- Peak counting
  - Balanced accuracy = 0.888
  - Unblended acc: 0.982, Blended acc: 0.713

- Binomial uncertainty: 0.001-4
- Variability due to random training data selection ~ Bin. unc.





# Model Comparison: Fainter+smaller footprints

#### GP classifier

- Balanced accuracy = 0.863
- Unblended acc: 0.810, Blended acc: 0.915

- Logistic regression with 12 regularization
  - Balanced accuracy = 0.786
  - Unblended acc: 0.723, Blended acc: 0.850
- Peak counting
  - Balanced accuracy = 0.759
  - Unblended acc: 0.997, Blended acc: 0.522

- Binomial uncertainty: 0.003-4
- Variability due to random training data selection ~ Bin. unc.



# **Topics for further study**

- Multi-class classification (e.g. 1 vs. 2 vs. >=3)
- Maybe combine GP and peak counting into one better classifier
- Galaxy localization
- Incorporate multiple bands



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