

# Lab 5 Momentum and impulse

TA: Chen-Hsuan Hsu

## Theory

- Newton's second law tells us  $F_{net} = ma$ , where  $F_{net}$  is the net force,  $m$  is the mass of an object, and  $a$  is acceleration. Using  $a = dv/dt$  with the velocity  $v$ , we can rewrite the law as  $F_{net} = mdv/dt$ . If we generalize this law to the varying mass case, then we have  $F_{net} = d(mv)/dt = dP/dt$ , where  $p = mv$  is the momentum of the object. Therefore,  $\Delta P = \int F_{net} dt$ , or

$$m(v_2 - v_1) = \int F_{net} dt. \quad (1)$$

## Experimental Process

### Initial Setup: Calibrate the Force Sensor

1. Link the force sensor to "Ch A." Double click on the force sensor icon, click "Measurement" tab, and check the box for "Voltage." The sensor will produce force readings, but we are going to ignore these and do our own calibration of the sensor, so we can convert the voltage readings to forces. When calibrating the force sensor, use the screw hook, and mount the sensor vertically downward on the horizontal bar of the ring stand.
2. Click Sampling Options tab on the setup window, check the box "Keep data values only when commanded," and type in "mass" for name and "g" for units. Drag a table over to the force sensor, and drag the voltage data and mass values over to the table, so that you have two columns showing these data. We will convert the masses to forces later in Excel.
3. Click Start. The "Start" button changes to Keep and Stop button as shown on page 43. Also, you will see the running voltage reading in your table. With no mass hanging on the force sensor, push the "Tare" button on the sensor to zero the reading, and click Keep. You will be prompted to enter the mass value (zero in this case).
4. Now add the 50-gram mass holder. Click Keep and enter a mass of -50 g. (The minus sign is because of the opposite direction.) Perform another 50-gram step, and then 100-gram steps up to a total of 500-grams. Remember to type in MINUS signs for the mass values. Click the red Stop button when you are finished.
5. Your table now contains a column of the voltage readings for corresponding masses. Call up an Excel worksheet, copy the voltage column of this table into column A of Excel. In column B, copy your mass values from Data Studio. In column C, convert the mass values to force in Newtons; for example, you may type in "=(B2/1000\*9.8)".
6. Select data in column A and C to plot the Force-versus-Voltage graph. Fit the data to obtain the equation for the trend line, write down the equation here: \_\_\_\_\_

## Procedure

1. Level the air track carefully. Mount the force sensor horizontally on the vertical rod of the ring stand at the end of the track so glider bumper will strike the sensor as the glider moves down the track. Replace the screw hook of the force sensor with the rubber bumper. Set up the photogate so the glider flag passes through the gate before the bumper strikes the sensor. (Please see the figures on page 44.)

2. Weigh the glider, and record its mass in kg:  $M = \text{_____} kg$
3. Measure the length of the glider flag, and record its length in m:  $d = \text{_____} m$
4. We want to set up the photogate to measure the velocity of the glider. In Sampling Options, disengage "Keep data values only when commanded." Link the photogate to "Ch 1." Click "Setup Timers" tab. Under "Timing Consequence choices," choose "Blocked," and then "Unblocked." Pictures of a blocked and an unblocked gate should appear in the window. Click Done to close the timer window. Click Calculate, and type in " $v=d/t$ ". Click Accept, and define d as the length of the glider flag and t as a data measurement (timer 1). Click Accept again.
5. Click the photogate icon, and in "Measurements" tab, check "State." Click Sampling Options and "Delayed Start" tab, check "Data Measurement." Set the first box to "State, Ch 1(V)." Set the next box to "Is Below." In the voltage text box, type in "4.9". Click OK.
6. Double click the force sensor icon. Set the sampling rate to 2000 Hz. Drag a table over to the force sensor, and set it to read a column of voltages and a column of velocities. Get rid of the time measurement column by clicking the "Show time" button.
7. Turn on the air track, and click Start. Push "Tare" button on the sensor. Send the glider down the track so it passes through the photogate, strikes and bounces off the sensor, and crosses the gate again. Click Stop. Your table should show a long list of force and voltage readings and two velocity readings at the top.
8. Drag a graph over the force sensor to plot Voltage-versus-time graph. You should see the impulse as page 46. To calculate the impulse, copy the voltage readings in the impulse area by pressing Ctrl+C and paste into a new Excel sheet. (See page 47.) In the next Excel column, use the calibration equation you obtained to convert the voltage to forces.
9. Since  $\int F_{net} dt = \Delta t \Sigma F_i$ , we can find impulse by summing over all forces and multiply it by  $\Delta t = 0.0005(\text{sec})$ . In other words, you can type in something like " $=0.0005*\text{SUM}(\text{B2:B147})$ ". The result will be the impulse for the first trial.
10. To find the change in momentum, calculate  $\Delta P = Mv_1 - Mv_2 = M(|v_1| + |v_2|)$ .
11. Repeat (7)-(10) and make totally three measurements with different glider speeds to check eq. (1). Record the three values of change in momentum and impulse in the following chart, as well as the percentage difference.

#	$\Delta P$ (N/s)	Impulse (N/s)	% difference
1			
2			
3			

## Additional Part

Skip this part.