

# Image/Mesh Filtering & Its Applications

-- non-local means filtering

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# New Idea: NL-Means Filter (Buades 2005)

- Same goals: ‘Smooth within Similar Regions’
- **KEY INSIGHT:** Generalize, extend ‘Similarity’
  - **Bilateral:**
    - Averages local neighbors with **similar intensities**;
  - **NL-Means:**
    - Averages nonlocal neighbors with **similar neighborhoods!**

## NL-Means Method: Buades (2005)

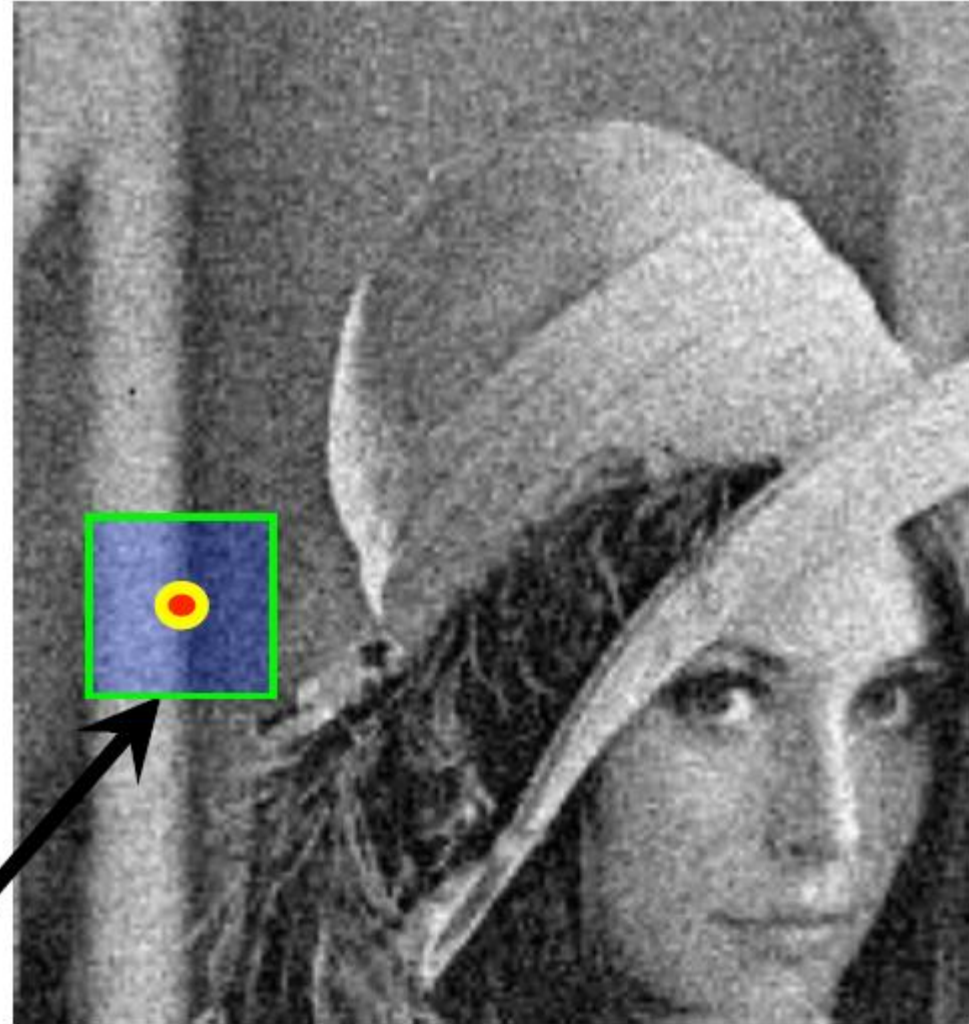
- For each and every pixel **p**:



## NL-Means Method: Buades (2005)

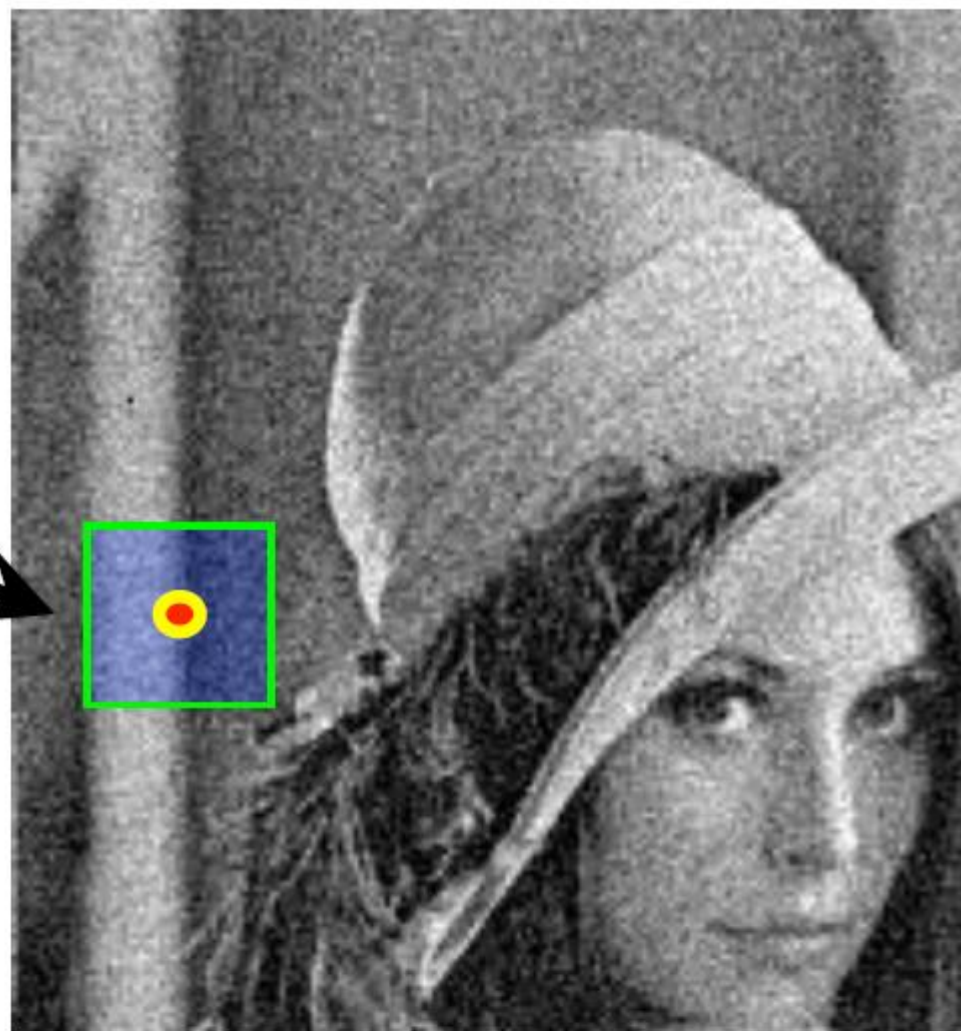
- For each and every pixel **p**:

- Define a small, simple fixed size neighborhood;



## NL-Means Method: Buades (2005)

$$\mathbf{V}_p = \begin{bmatrix} 0.74 \\ 0.32 \\ 0.41 \\ 0.55 \\ \dots \\ \dots \\ \dots \end{bmatrix}$$



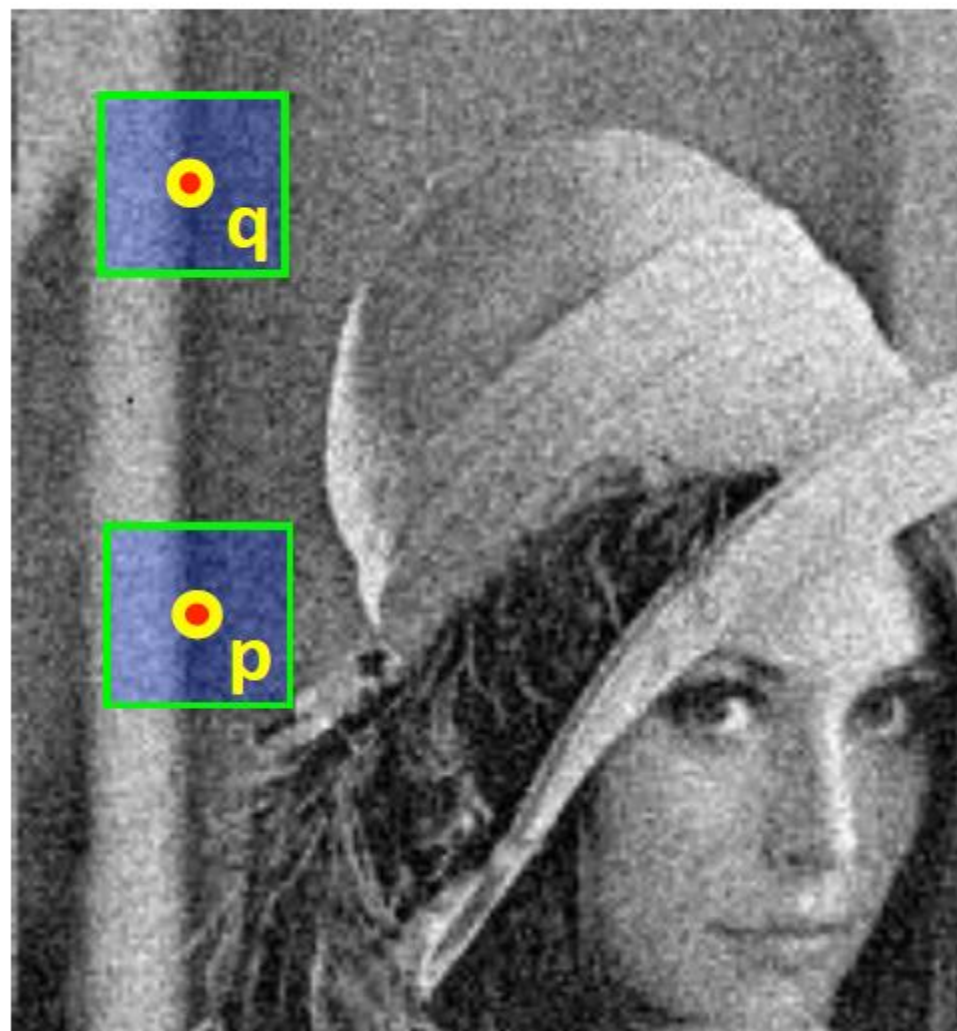
- For each and every pixel  $\mathbf{p}$ :
  - Define a small, simple fixed size neighborhood;
  - Define vector  $\mathbf{V}_p$ : a list of neighboring pixel values.



## NL-Means Method: Buades (2005)

'Similar' pixels **p**, **q**  
→ **SMALL**  
vector distance;

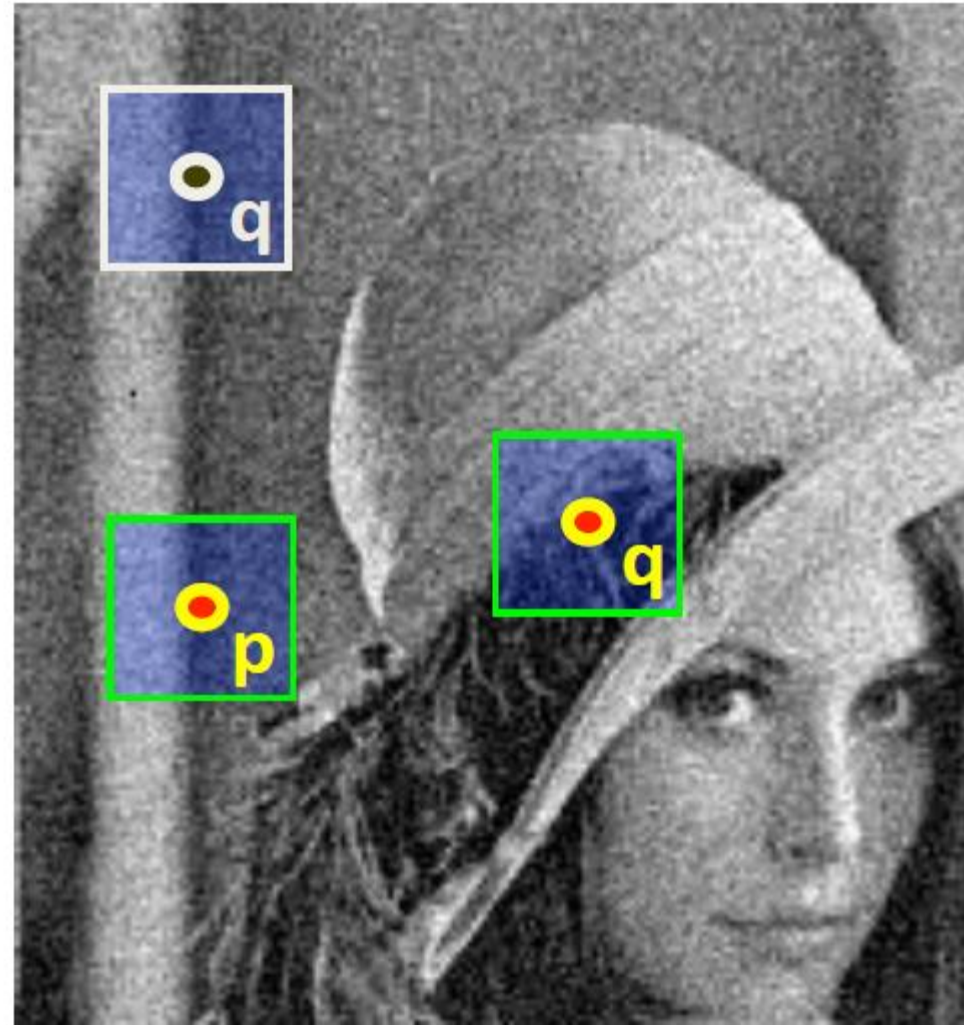
$$|| \mathbf{v}_p - \mathbf{v}_q ||^2$$



## NL-Means Method: Buades (2005)

'Dissimilar' pixels **p, q**  
→ **LARGE**  
vector distance;

$$|| \mathbf{V}_p - \mathbf{V}_q ||^2$$



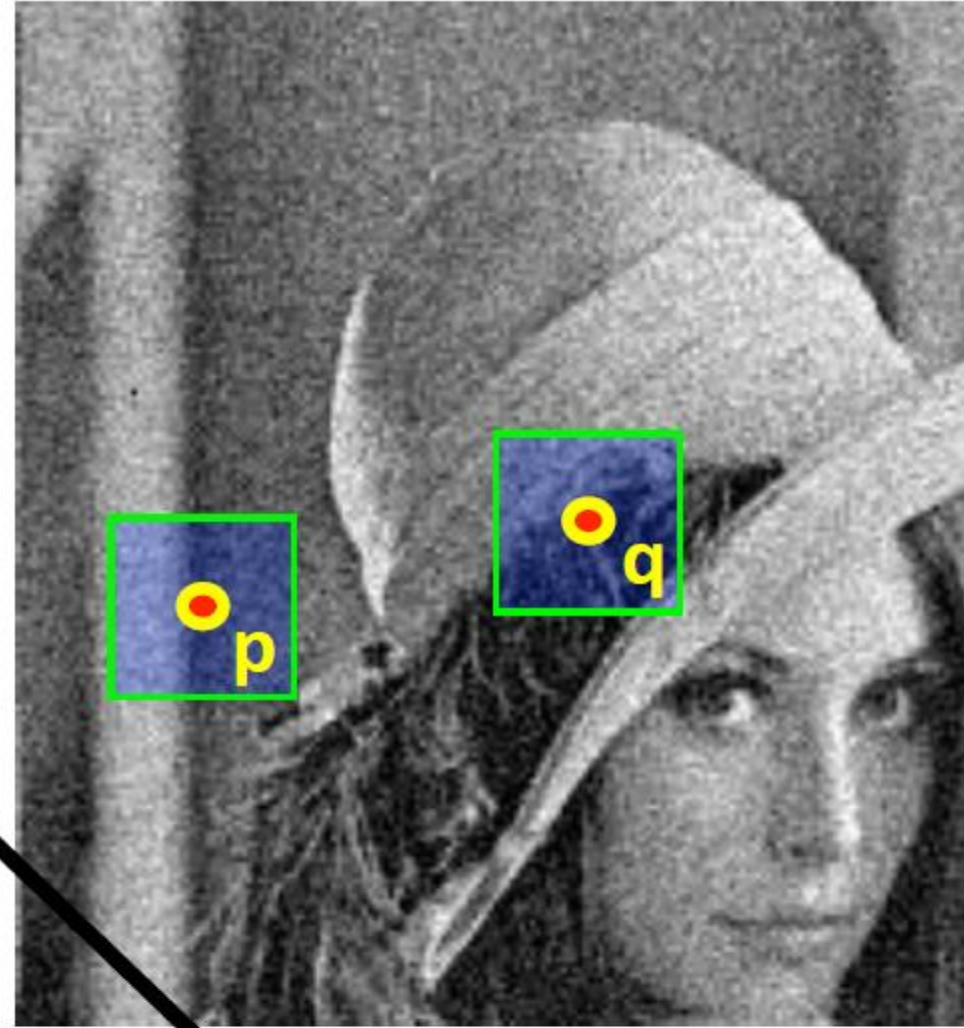
# NL-Means Method: Buades (2005)

**p, q** neighbors define  
a vector distance;

$$|| \vec{V}_p - \vec{V}_q ||^2$$

**Filter with this:**

**No spatial term!**



$$NLMF[I]_p = \frac{1}{W_p} \sum_{q \in S} \cancel{G_{\sigma_s}(\|\mathbf{p} - \mathbf{q}\|)} G_{\sigma_r} \left( || \vec{V}_p - \vec{V}_q ||^2 \right) I_q$$





- Input, Gaussian, Anisotropic Diffusion, Bilateral, NLM

# Advanced introduction