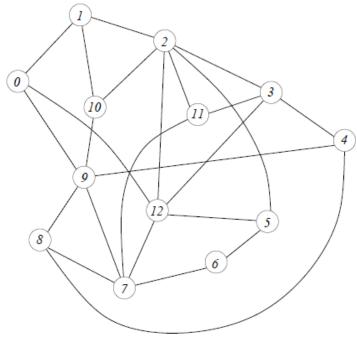
## Data Structures and Algorithms, COSC-2336 Assessment Graphs and Applications

Exercise 1. Let us consider the following graph.



Answer the following questions:

- a) What is the set of vertices and set of edges?
- b) Is the graph directed or undirected?
- c) Which are the vertices adjacent with vertex 12?
- d) Which are the edges adjacent with edge (3, 12)?
- e) What is the degree of vertices 0, 2, 3, and 12?
- f) What node has the maximum degree in the above graph?
- g) Enumerate all cycles which contain the edge (3, 12).
- h) Is the graph connected?
- i) Is the graph complete?

Exercise 2. Let us consider the following graph over the nodes {1, 2, 3, 4, 5, 6}. (**NOT a programming question**)

$$1 \to 2 \to 3 \to 4 \to 6$$

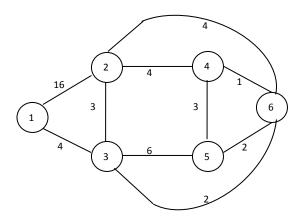
$$\uparrow \qquad \downarrow$$

$$\leftarrow 5$$

$$\begin{array}{ccc}
1 \to 2 \to 3 \to 4 \\
\uparrow & \downarrow \\
6 \leftarrow 5
\end{array}$$

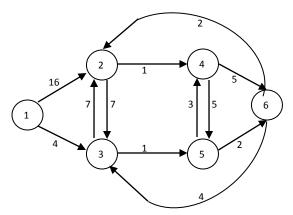
- a) Find the adjacency list of the above graphs;
- b) Display the Depth First Traversal and Breadth First Traversal of the above graphs;

Exercise 3. Let us consider the following graph over the nodes  $\{1, 2, 3, 4, 5, 6\}$ .



Using Prim's Algorithm, find the minimum spanning tree (note that the spanning tree is a tree with the minimum total weight). (**NOT** a programming question. You just need to show the steps to create the minimum spanning tree)

**Exercise 4.** Let us consider the following graph over the nodes {1, 2, 3, 4, 5, 6}.



Using Dijkstra's Algorithm, find a shortest path between vertex 1 and any other vertex in the graph. (NOT a programming question. You just need to show the steps to find the shortest path)