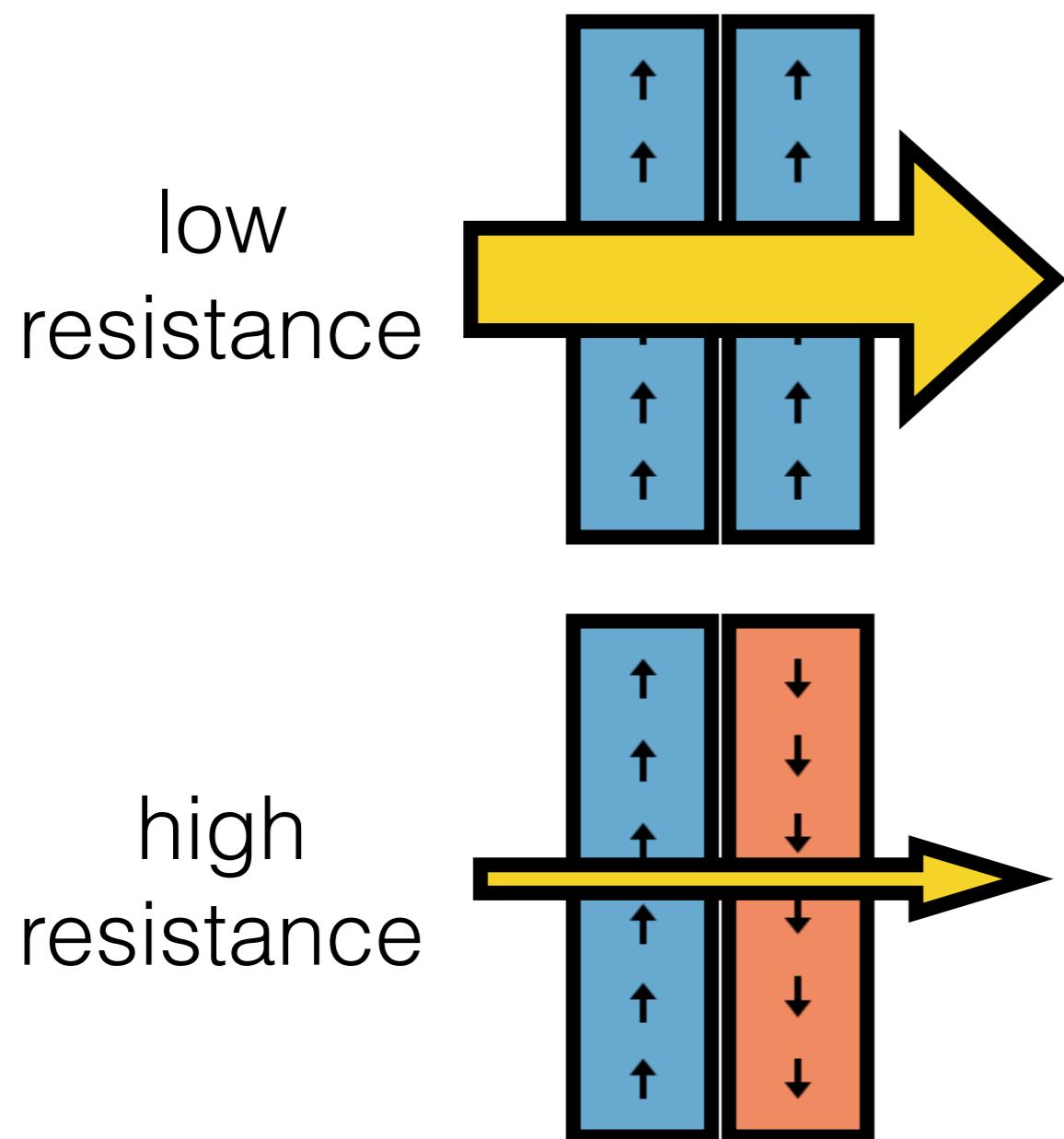


# **Theoretical investigation of magnetic exchange interactions in dilute magnetic semiconductor quantum dots induced by defects**

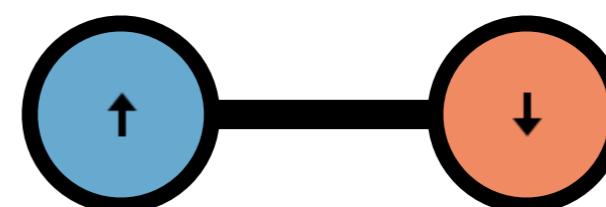
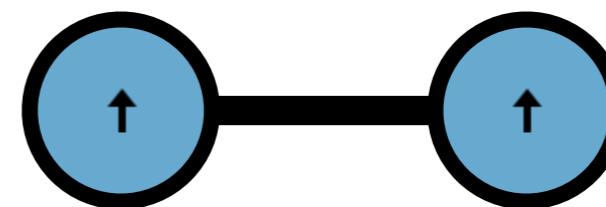
Joshua Goings and Xiaosong Li  
Tuesday, December 15, 11:20am



Controlling magnetism at the nanoscale is important.



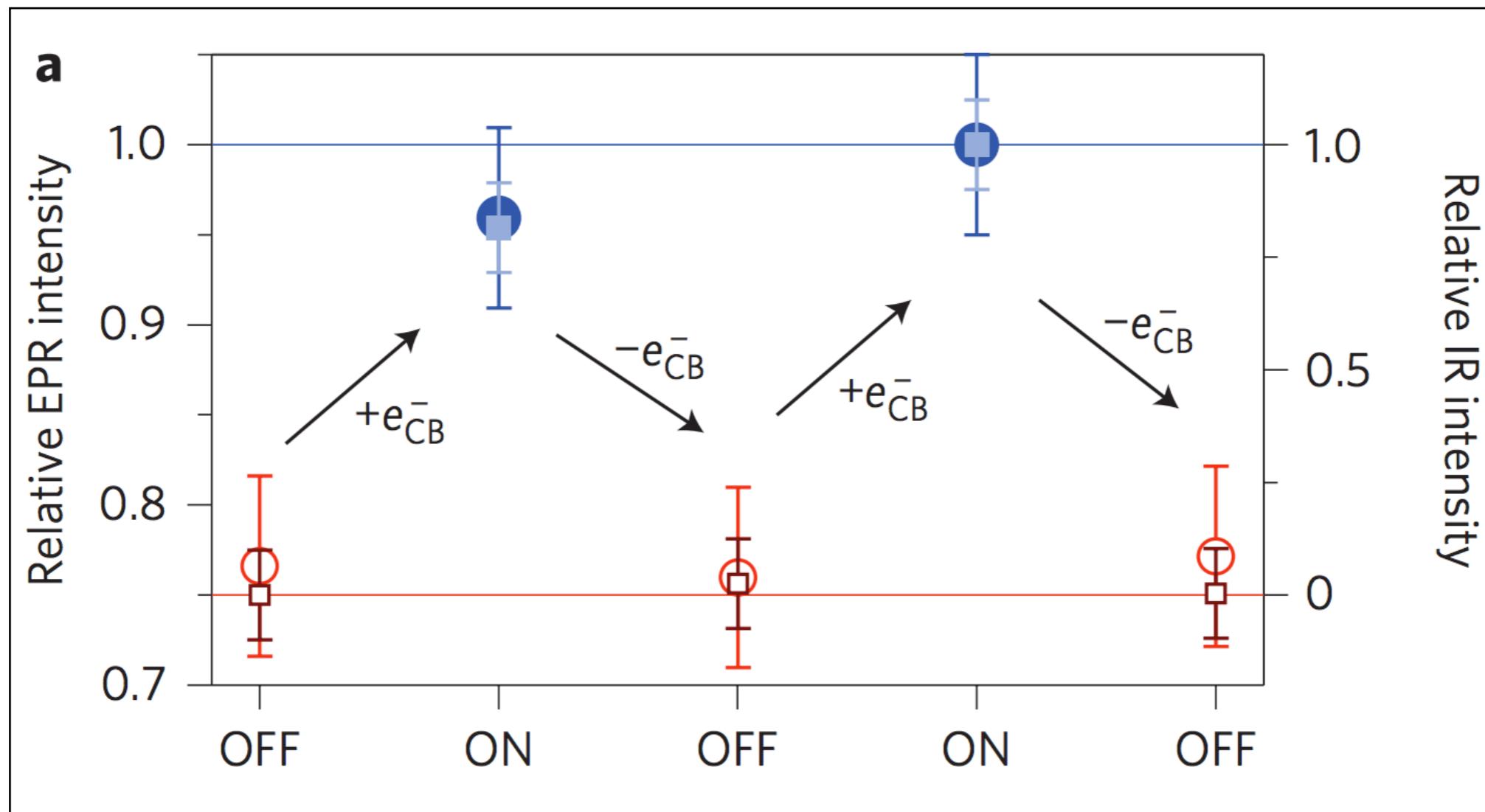
ultimate miniaturization:  
ferromagnetic quantum dots linked  
by semiconducting polymer



Tunnel Magnetoresistance  
(TMR)

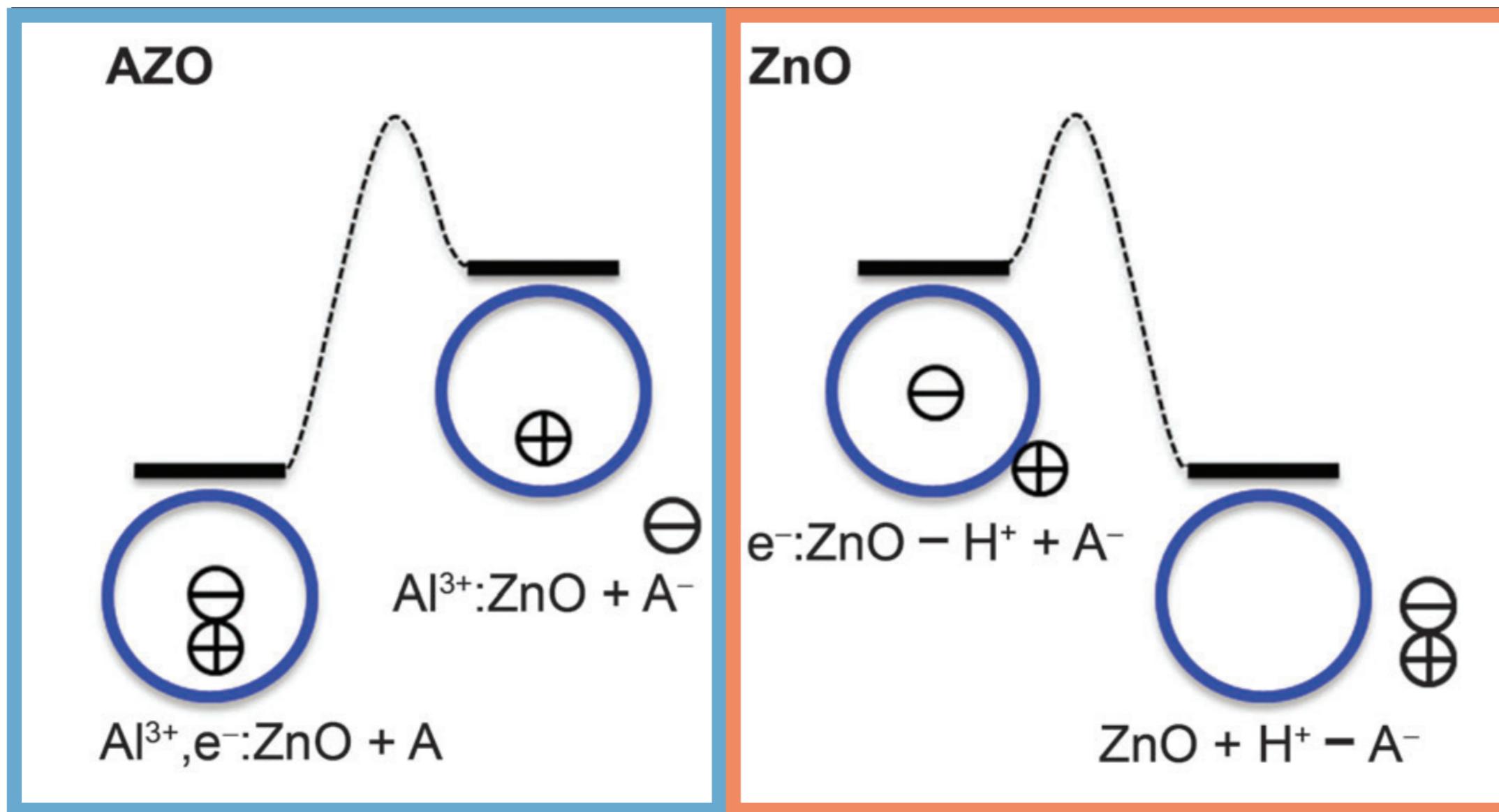
# **Mn<sup>2+</sup>:ZnO** Nanocrystals (NC)

Adding charge carriers can induce magnetic response



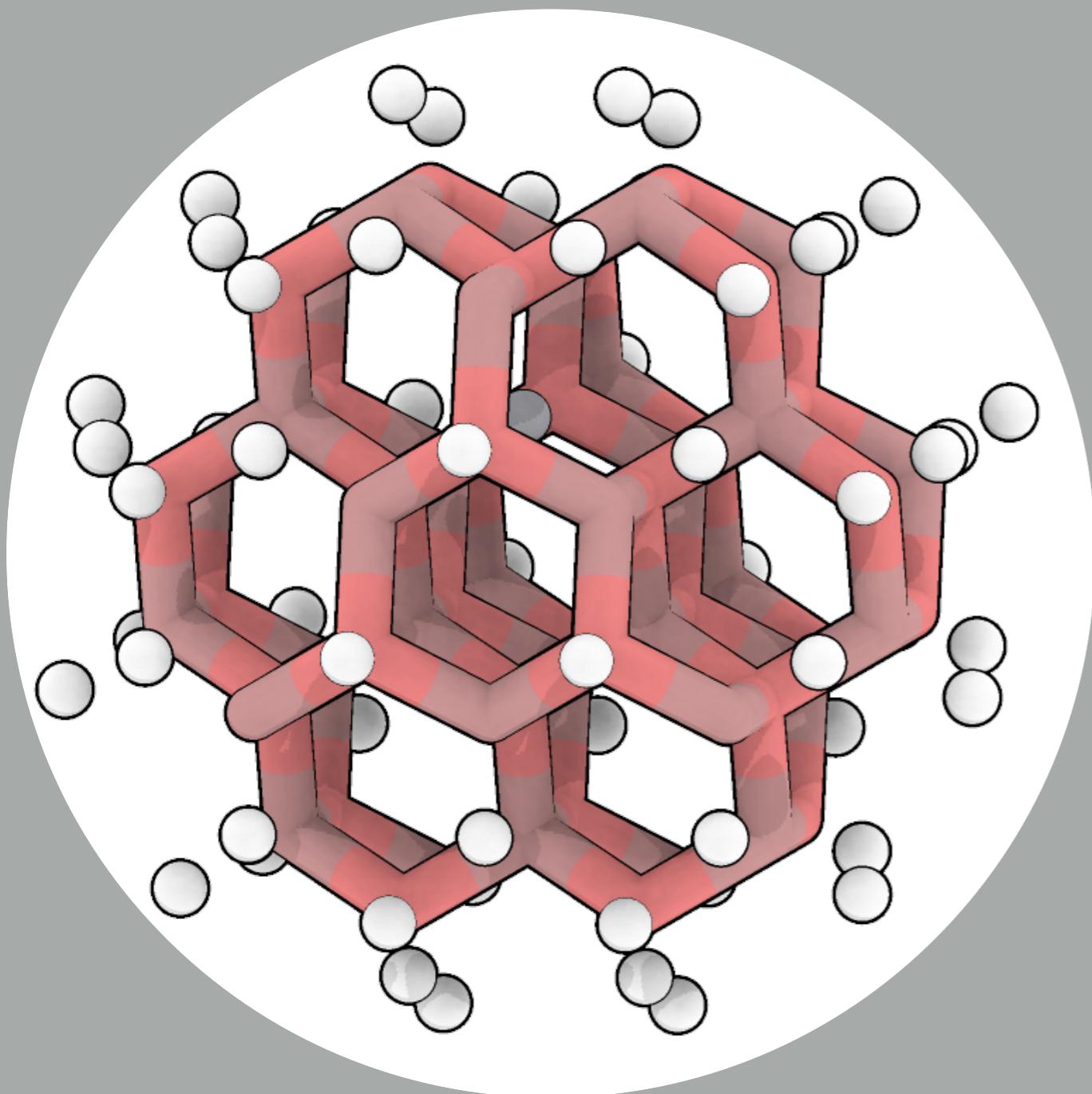
# **Al<sup>3+</sup>-doping ZnO:**

a stable way to add electrons to a ZnO nanocrystal.



Can we create permanent ferromagnetic QDs by co-doping (Al,Mn)-ZnO?

**Is Al-doped MnZnO fundamentally any different than electronically doped MnZnO?**

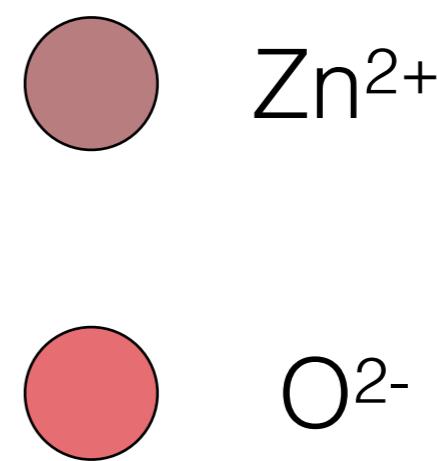
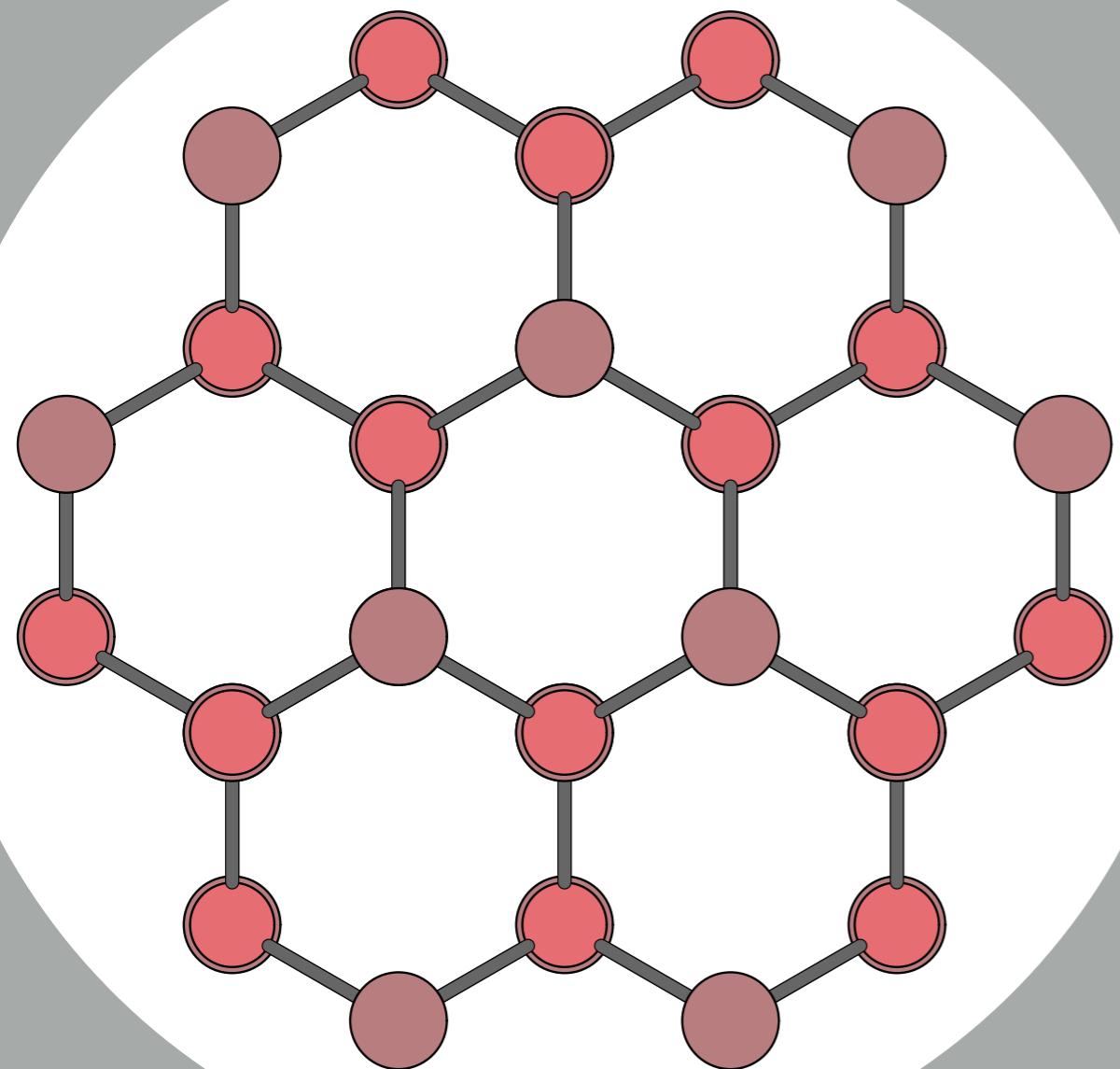


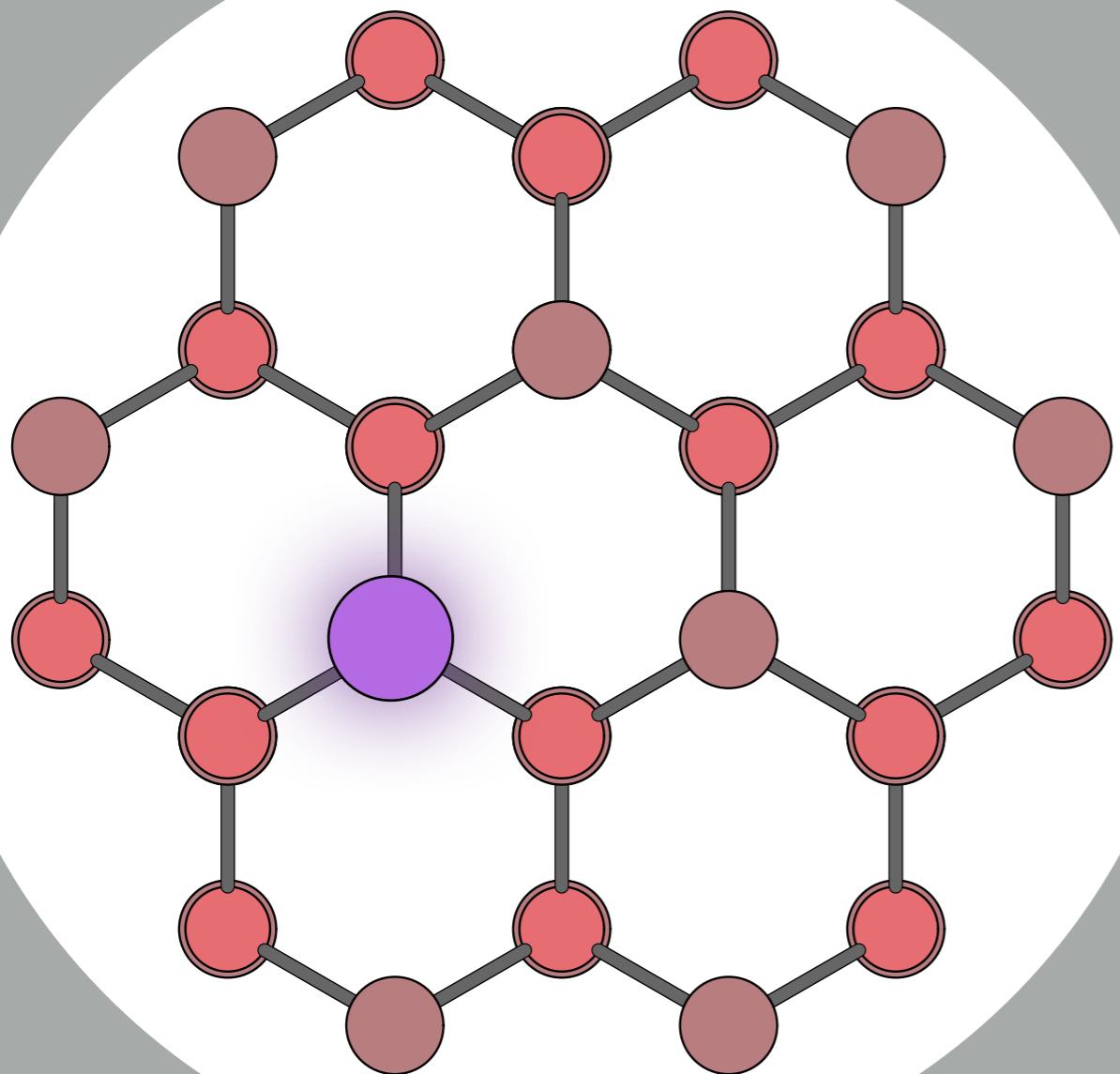
model ZnO

1.3 nm diameter

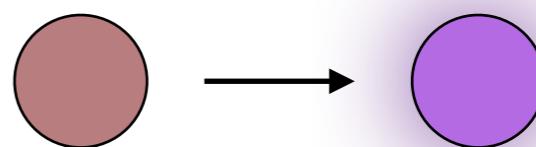
PBE1PBE/LANL2DZ

pseudohydrogen  
capping

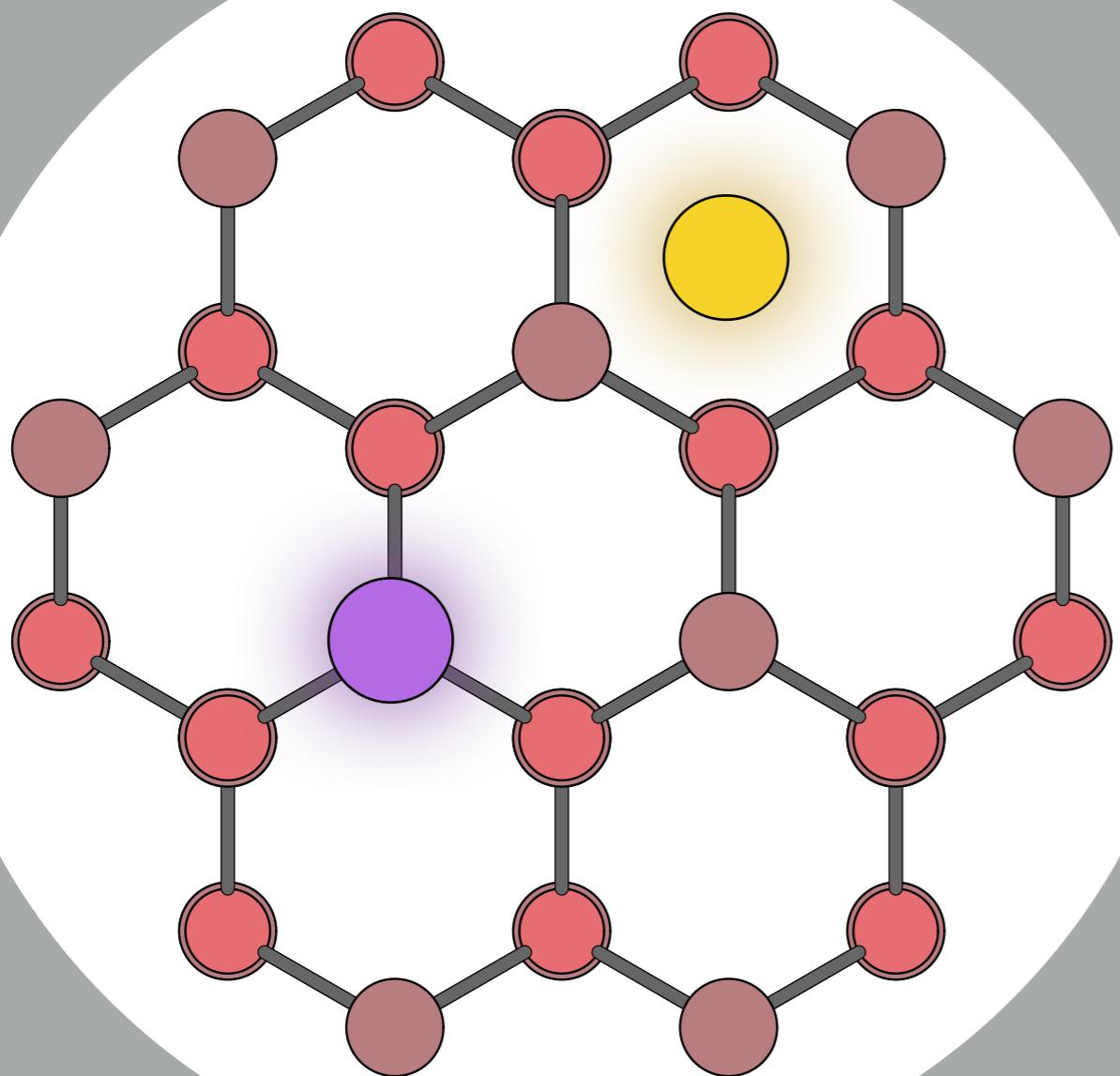




Replace  $\text{Zn}^{2+}$  with  $\text{Mn}^{2+}$



$$S = 5/2$$



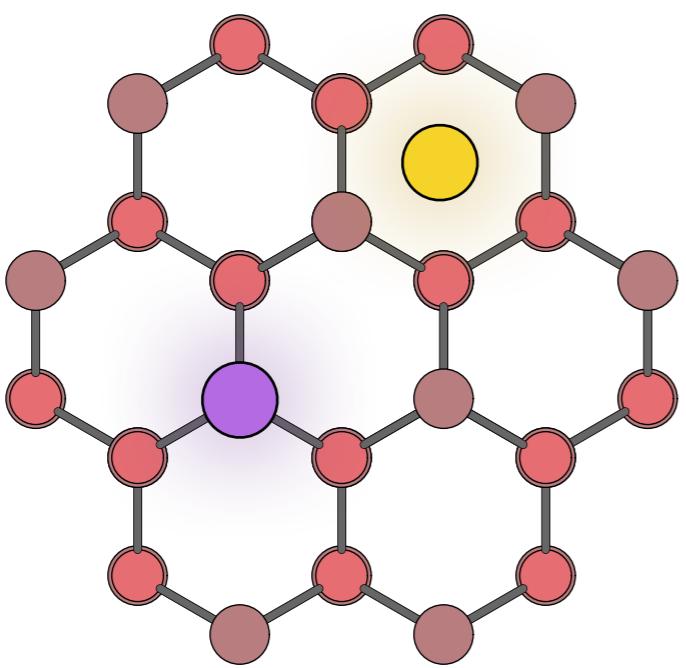
Add charge carrier

electron

hole

$$S = 1/2$$

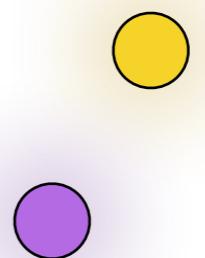
$\hat{H}_{exact}$



unparameterized;  
all interactions

Map DFT to  
spin Hamiltonian

$\hat{H}_{HDVV}$



$$-2J\hat{S}_i\hat{S}_j$$

only spin  
interactions



# Map DFT to spin Hamiltonian

$H_{\text{eff}} =$  Energy difference of DFT spin configurations

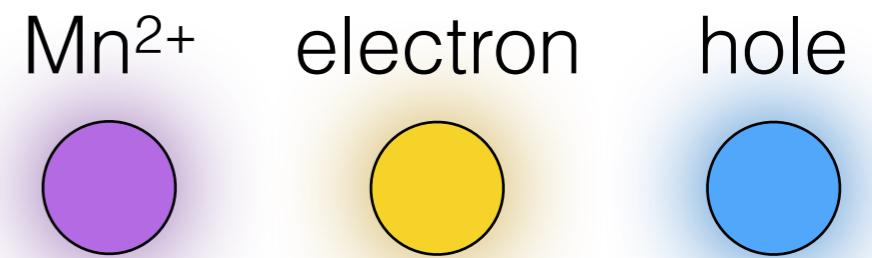
Plug in spin of  
local spin subsystem

$$H_{\text{eff}} = J[S_i(S_i + 1) + S_j(S_j + 1) - S_{i+j}(S_{i+j} + 1)]$$

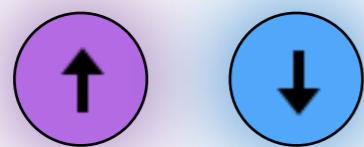
Solve for  $J$

\*more details at end

# Two-center spin interactions: charge-doped MnZnO quantum dots

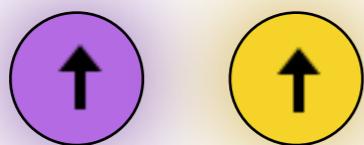


h<sup>+</sup>



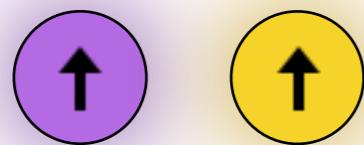
$$J_{\text{p-d}} = -152 \text{ meV}$$

e<sup>-</sup>



$$J_{\text{s-sd}} = +11 \text{ meV}$$

Al<sup>3+</sup>



$$J_{\text{s-sd}} = +9 \text{ meV}$$

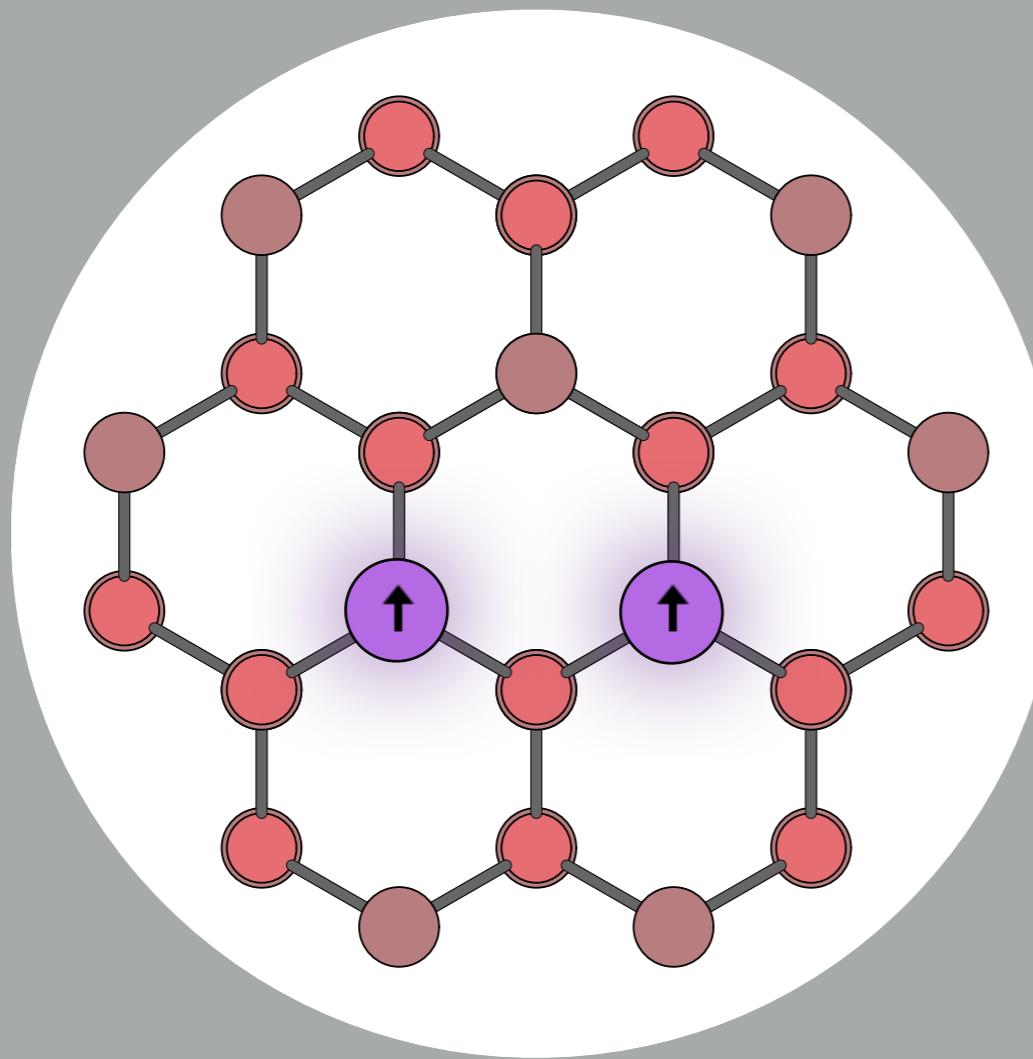
anti-ferromagnetic (AFM)

ferromagnetic (FM)

ferromagnetic (FM)

$J > 0 \rightarrow \text{FM}, \quad J < 0 \rightarrow \text{AFM}$

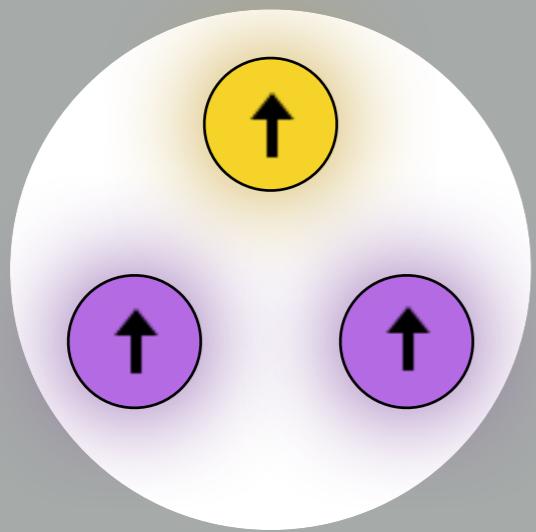
# Nearest neighbor $\text{Mn}^{2+}$ — $\text{Mn}^{2+}$ anti-ferromagnetic (AFM) super exchange (SE) interactions



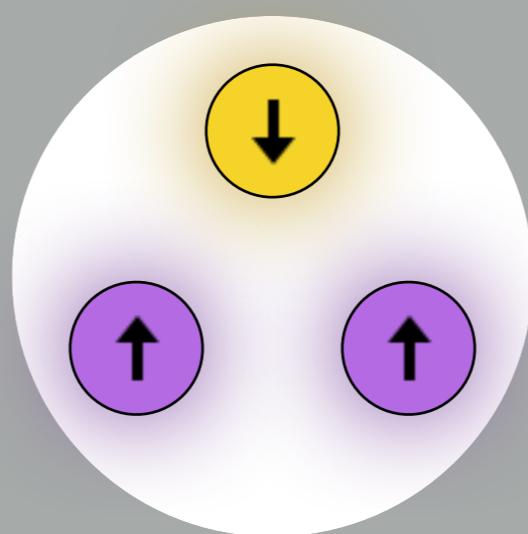
$$J_{\text{SE}} = -2.4 \text{ meV}$$

Subsequent interaction with charge carrier  
leads to spin frustrated interactions

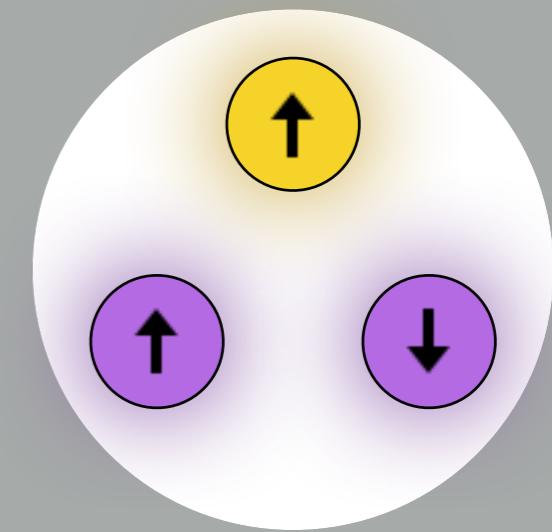
Gives rise to three possible spin configurations



High-spin  
(HS)

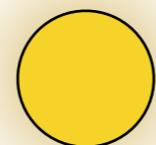
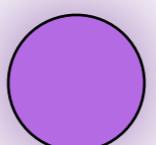


ferromagnetic  
(FM)

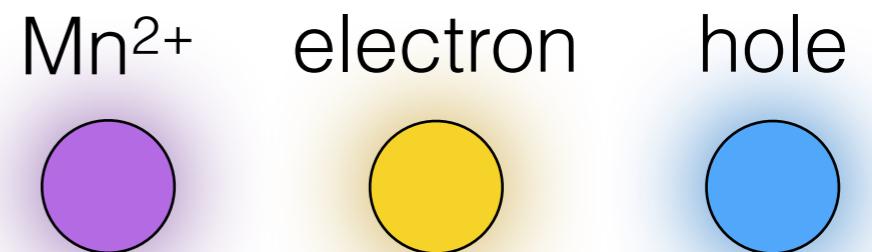


anti-ferromagnetic  
(AFM)

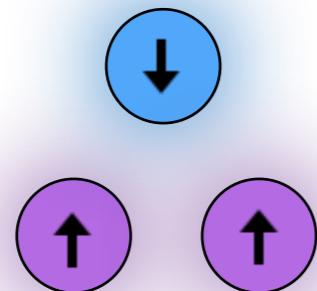
Mn<sup>2+</sup>      charge-carrier



# Three-center spin interactions: charge-doped MnZnO quantum dots

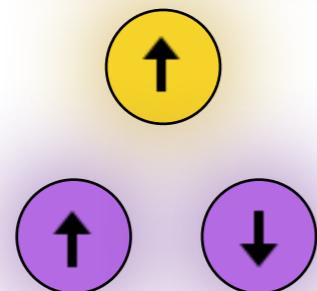


h<sup>+</sup>



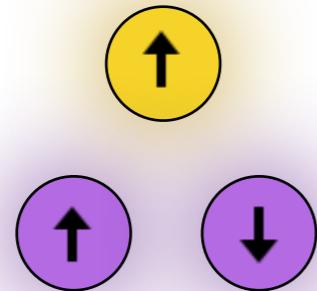
$$J_{\text{SE}} = -13 \text{ meV}$$
$$J_{\text{p-d}} = -127 \text{ meV}$$

e<sup>-</sup>



$$J_{\text{SE}} = -2 \text{ meV}$$
$$J_{\text{s-sd}} = +11 \text{ meV}$$

Al<sup>3+</sup>



$$J_{\text{SE}} = -2 \text{ meV}$$
$$J_{\text{s-sd}} = +9 \text{ meV}$$

ferromagnetic  
(FM)

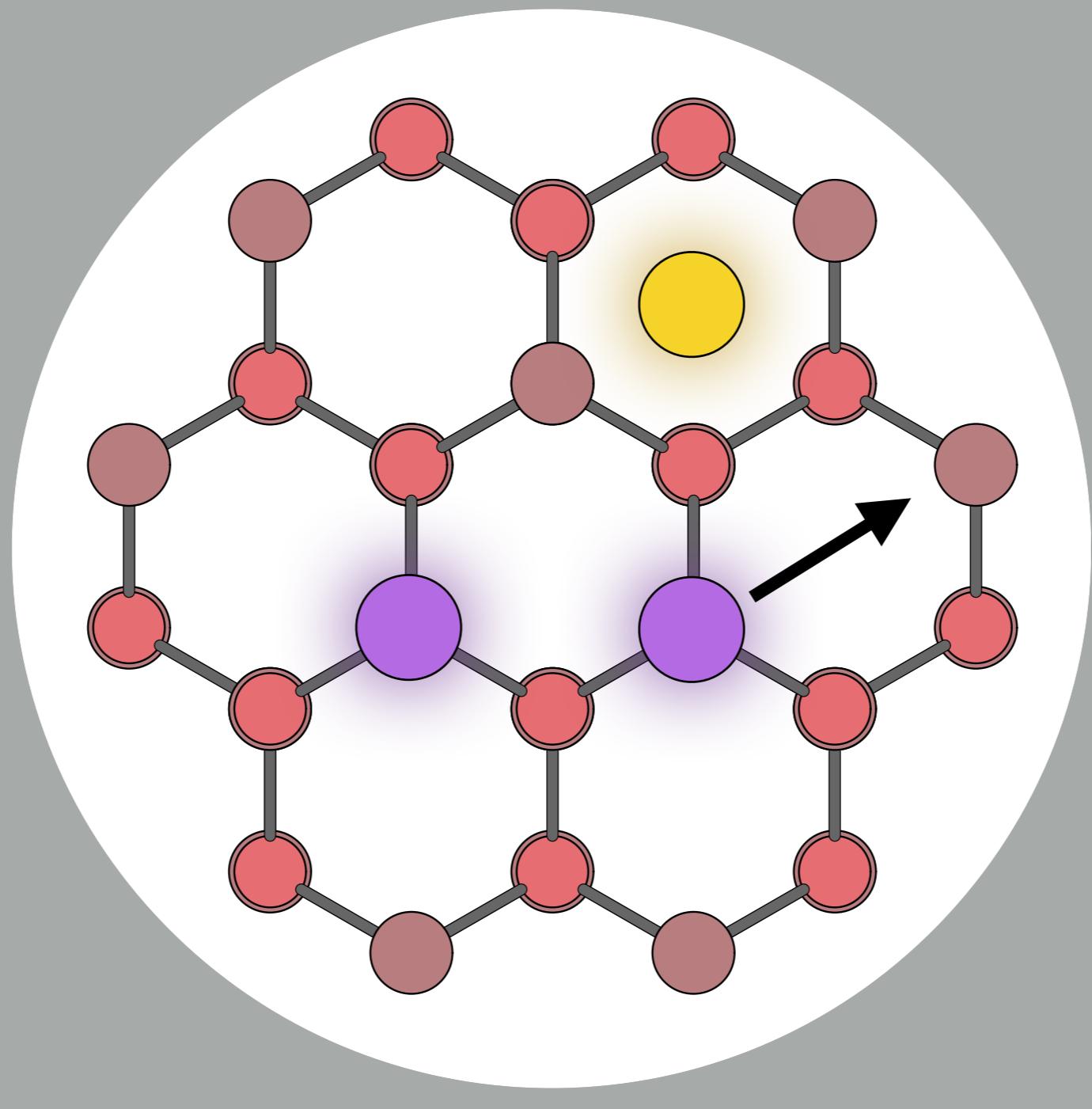
anti-ferromagnetic  
(AFM)

anti-ferromagnetic  
(AFM)

Spins compete, and FM favored when

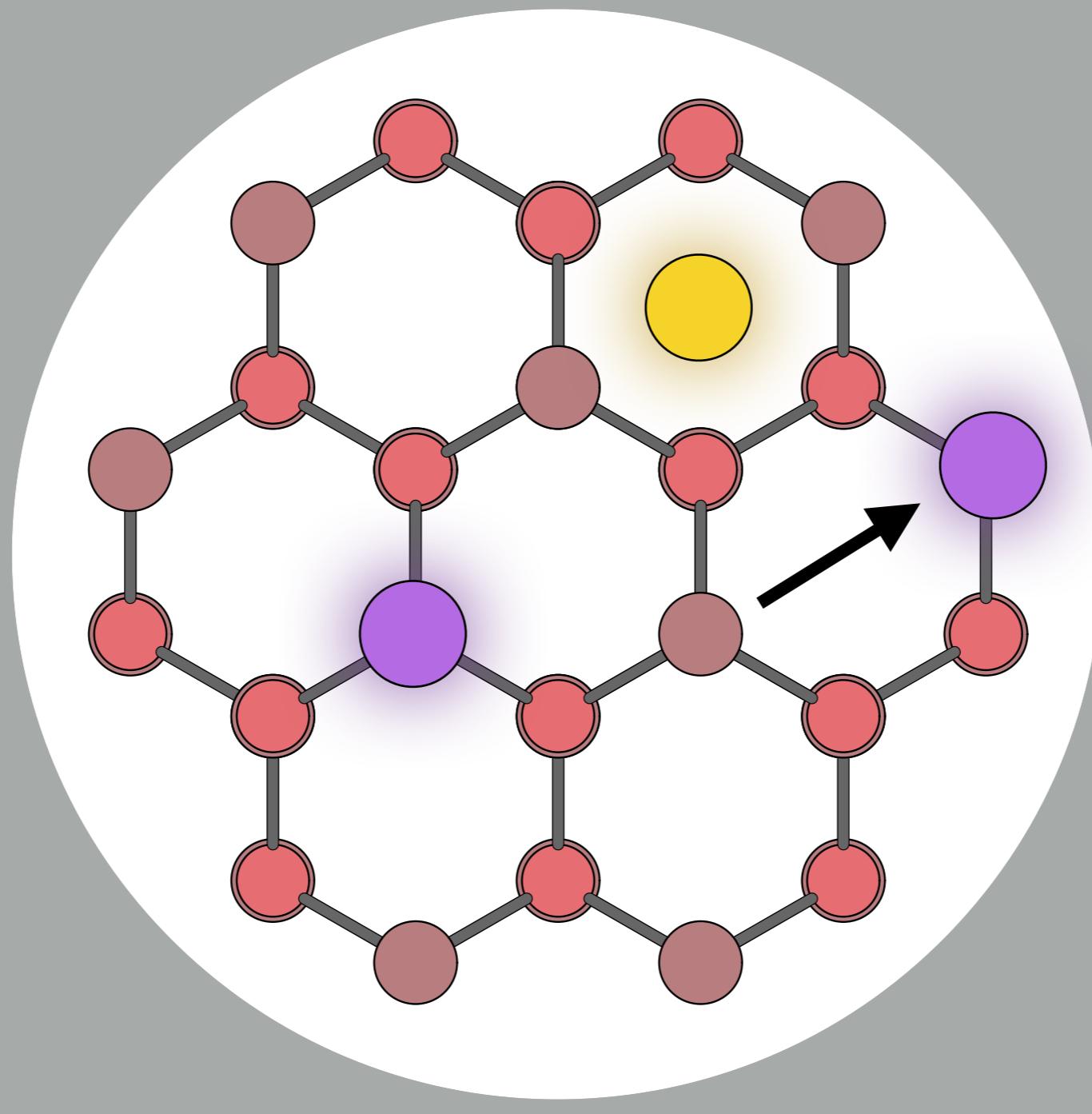
$$5J_{\text{SE}} > J_{\text{carrier-Mn}}$$

Of course, the interaction is highly position dependent.



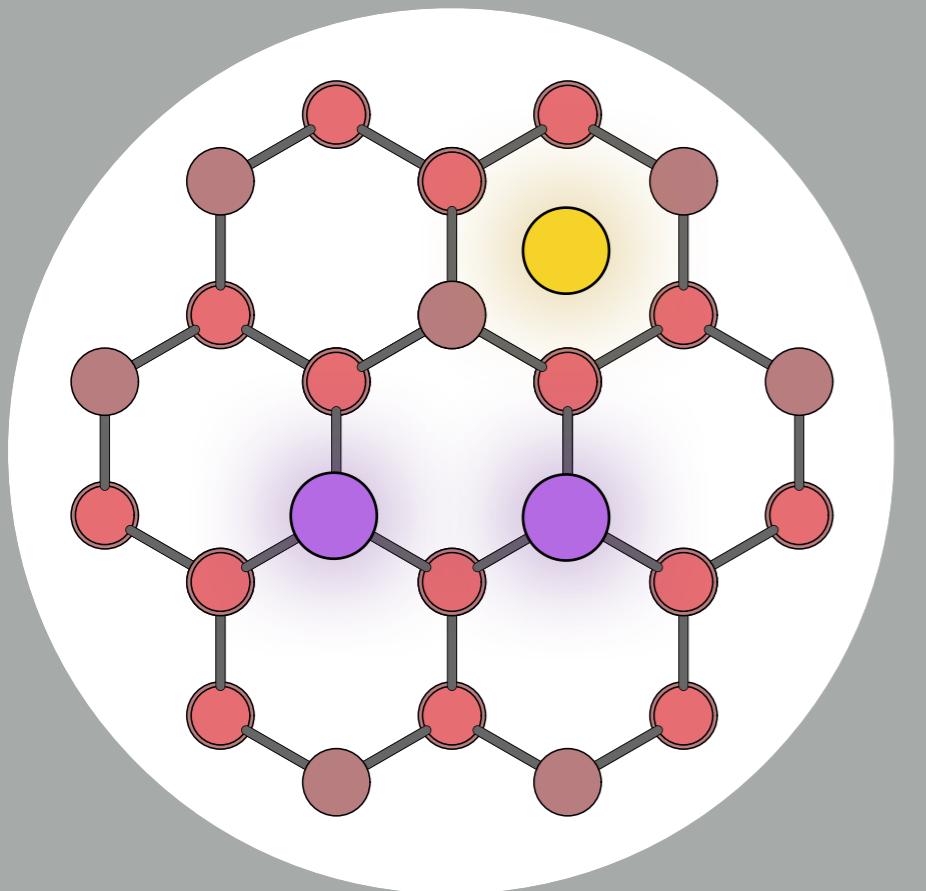
Split up Mn dimer, lose SE interactions, FM favored again.

Of course, the interaction is highly position dependent.



Split up Mn dimer, lose SE interactions, FM favored again.

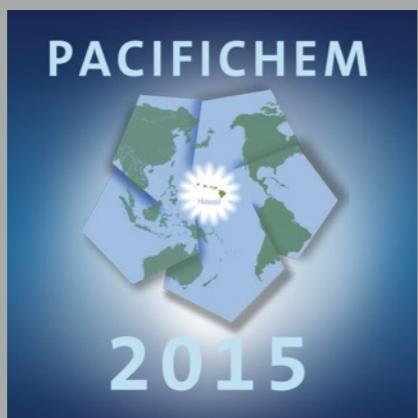
# (Mn,Al) co-doped ZnO quantum dots



Aluminum-doping leads  
to stable charge carrier

Charge can mediate ferromagnetic  
spin coupling between distant Mn  
centers

Thank you!







## Map DFT to spin Hamiltonian

$$H_{\text{eff}} = \Delta E = E(\text{DFT spin config 1}) - E(\text{DFT spin config 2})$$

$$H_{\text{eff}} = -2J\hat{S}_i \cdot \hat{S}_j$$

$$-2\hat{S}_i \cdot \hat{S}_j = \hat{S}_i^2 + \hat{S}_j^2 - (\hat{S}_i + \hat{S}_j)^2 \quad \text{complete the square}$$

$$\hat{S}_i^2 |\psi\rangle = S_i(S_i + 1) |\psi\rangle \quad \text{act on spin eigenfunction}$$

This gives for spin subsystems ( $i$ ) and ( $j$ ):

$$H_{\text{eff}} = J[S_i(S_i + 1) + S_j(S_j + 1) - S_{i+j}(S_{i+j} + 1)]$$