Embedded Vision Design

EVD1 - Week 3

Image Fundamentals Nonlinear Filters Spatial Filters

By Hugo Arends

Image Fundamentals

- Functions for creating and deleting images
- Functions for converting images
- Functions for reading and writing pixels
- Basic image processing operators
- Discrete convolution
- Discrete correlation

- Results in a filtering operation
- Applies a filter mask to an image by convolving the filter mask with the original image
- Two-dimensional discrete convolution is defined as

$$p_{dst}(x,y) = \sum_{i=-n/2}^{i=n/2} \sum_{j=-m/2}^{j=m/2} p_{src}(x-i,y-j) \cdot p_{mask}(i+n/2,j+m/2)$$

where

 $m \times n$: mask size

 $p_{dst}(x,y)$: the calculated result pixel in the destination image at (x,y) $p_{src}(x-i,y-j)$: a pixel value in the src image within the mask $p_{mask}\left(i+\frac{n}{2},j+\frac{m}{2}\right)$: a pixel value in the mask image

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 All pixels in the
$$m \times n$$
 neighbourhood of the src pixel at
$$(x,y)$$

- Results in a filtering operation
- Applies a filter mask to an image by convolving the filter mask with the original image
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All pixels in the $m \times n$ mask

The corresponding pixels in the src image and mask are flipped in both horizontal and vertical direction.

Mask					lippe mask	
а	b	С		i	h	Į
d	e	f		f	e	C
g	h	i		С	b	(

IIIask				
i	h	g		
f	e	d		
С	b	a		

If the mask is not symmetrical in both horizontal and vertical direction, the mask should be flipped before performing a convolution.

flip -15 0 -10

No need to

IIIppca				
0	0	1		
0	1	0		
0	1	0		

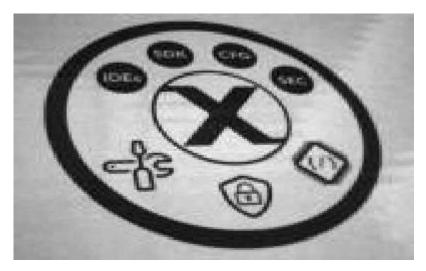
Must be

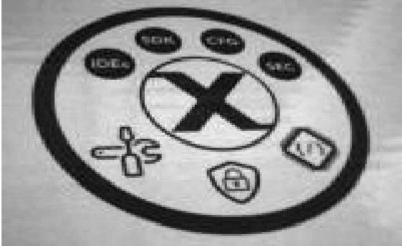
flinned

Discrete convolution - example

Identity

0	0	0
0	1	0
0	0	0

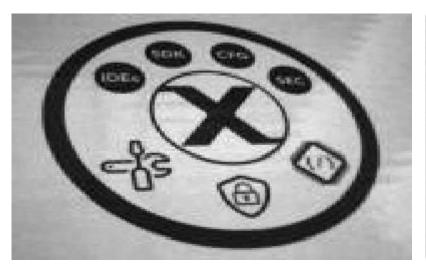


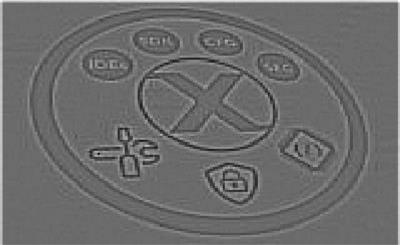


Discrete convolution - example

Edge

-1	-1	-1
-1	8	-1
-1	-1	-1

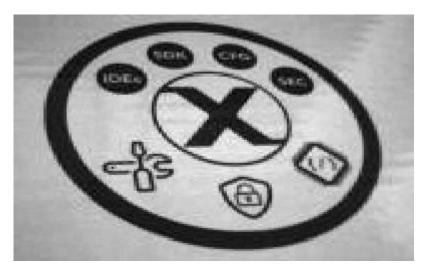




Discrete convolution - example

Sharpen

0	-1	0
-1	5	-1
0	-1	0





See file EVDK_Operators\image_fundamentals.c

```
int32_t val = 0;
int32_t dr = (msk->rows/2);
int32_t dc = (msk->cols/2);
// Apply the kernel only for pixels within the image
for(int32_t j=-dr; j<=dr; j++)</pre>
    for(int32 t i=-dc; i<=dc; i++)</pre>
        if((x-i) >= 0 &&
           (y-j) >= 0 &&
           (x-i) < src->cols &&
           (y-j) < src->rows)
            val += getInt16Pixel(src,x-i,y-j) * getInt16Pixel(msk,i+dc,j+dr);
```

```
// Clip the result
if(val>INT16_PIXEL_MAX)
    val=INT16_PIXEL_MAX;

if(val<INT16_PIXEL_MIN)
    val=INT16_PIXEL_MIN;

// Store the result
    setInt16Pixel(dst, x, y, val);
}
}</pre>
```

```
// Clip the result
if(val>INT16_PIXEL_MAX)
     val=INT16_PIXEL_MAX;

if(val<INT16_PIXEL_MIN)
     val=INT16_PIXEL_MIN;

// Store the result
    setInt16Pixel(dst, x, y, val);
}
}</pre>
```

Optimize most (-O3)
UVC connected
~35 ms

Discrete convolution – improve performance

Assume a 3x3 mask and ignore border pixels

Discrete convolution – improve performance

Assume a 3x3 mask and ignore border pixels

Discrete convolution – improve performance

- Assume a 3x3 mask and ignore border pixels
- Avoid using getters and setters

EVD1 – Assignment



Study guide

Week 3

2 Image fundamentals - convolveFast()

Discrete correlation

- Compares two images mathematically
- The result is a two-dimensional expression of equivalence
- The mask image is often referred to as the template
- The correlation is then called template matching
- Two-dimensional discrete correlation is defined as

$$p_{dst}(x,y) = \sum_{i=-n/2}^{i=n/2} \sum_{j=-m/2}^{j=m/2} p_{src}(x+i,y+j) \cdot p_{mask}(i+n/2,j+m/2)$$

where

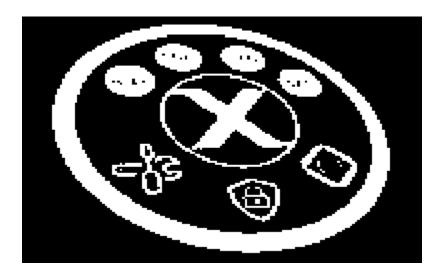
 $m \times n$: mask size

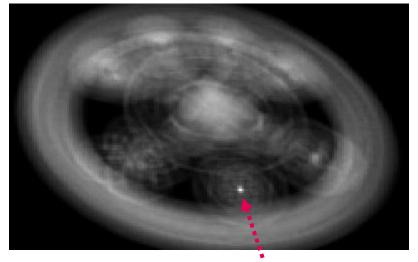
 $p_{dst}(x,y)$: the calculated result pixel in the destination image at (x,y) $p_{src}(x+i,y+j)$: a pixel value in the src image within the mask $p_{mask}\left(i+\frac{n}{2},j+\frac{m}{2}\right)$: a pixel value in the mask image

Discrete correlation – example

Binary template matching



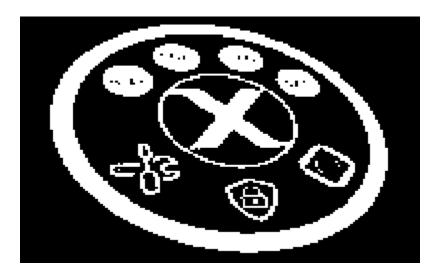


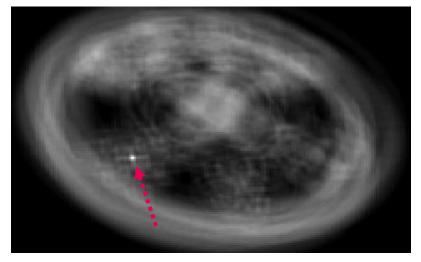


Discrete correlation – example

Binary template matching







Discrete correlation – implementation

See file EVDK_Operators\image_fundamentals.c

Discrete correlation – implementation

```
val += getInt16Pixel(src,<mark>x+i,y+j</mark>) * getInt16Pixel(msk,i+dc,j+dr);
```

Optimize most (-O3)
UVC connected
25x25 mask
> 1000 ms



Discrete correlation – improve performance

- For template matching it does not make sense to assume a 3x3 mask, because the size of a mask is at least tens by tens pixels
- Although the border pixels can be skipped, if the mask size increases, so are the number of skipped pixels
- In other words, a template matcher with a reasonable sized mask takes too long to execute on the microcontroller

- Operate on an image by computing a given nonlinear function over a local window
- The local window can vary in size, is often a square
- Replace one specified pixel within the local window with the computed value, often the centre pixel (hence window size is an odd value)
- Are not solely used for filtering, e.g. binary erosion, binary dilation, and edge detection

Image

m_1	m_2	m_3		
m_4	m_5	m_6		
m_7	m_8	m_9		

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Image

m_1	m_2	m_3	
m_4	m_5	m_6	
m_7	m_8	m_9	

Nonlinear filters – implementation

Implementation is very similar to convolution

Handles border pixels by just taking the valid pixels into account in
the filter specific operation

Nonlinear filters - implementation

Nonlinear filters - implementation

```
// Initialize filter specific variables
int32 t cnt = 0;
int32 t sum = 0;
// Apply the kernel only for pixels within the image
for(int32_t j=-n/2; j<=n/2; j++)</pre>
    for(int32 t i=-n/2; i<=n/2; i++)
        if((x+i) >= 0 &&
           (y+j) >= 0 &&
           (x+i) < src->cols &&
           (y+j) < src->rows)
            // Count the number of pixels in the calculation
            cnt++;
            // Get pixel and perform filter specific calculation
            sum += getUint8Pixel(src,x+i,y+j);
```

Nonlinear filters - implementation

```
// Calculate and store the result
    setUint8Pixel(dst,x,y,(uint8_pixel_t)((float)sum/(float)cnt + 0.5f));
}
}
```

Nonlinear filters - arithmetic mean

- Calculates the arithmetic mean of the pixels within the window
- The arithmetic mean is defined as

$$p_{dst}(x,y) = \frac{1}{n^2} \sum_{i=-n/2}^{i=n/2} \sum_{j=-n/2}^{j=n/2} p_{src}(x+i,y+j)$$

where

 $p_{dst}(x,y)$: the calculated result pixel in the destination image at (x,y) $p_{src}(x+i,y+j)$: a pixel value in the src image within the window n: the window size

Nonlinear filters - arithmetic mean

```
void mean( const image_t *src, image_t *dst, const uint8_t n);
```

See file EVDK_Operators\nonlinear_filters.c

Nonlinear filters - arithmetic mean

```
void mean( const image_t *src, image_t *dst, const uint8_t n);
```

See file EVDK_Operators\nonlinear_filters.c

```
// -----
// Image processing pipeline
// -----
convertBgr888ToUint8(img, src);
mean(src, dst, 3);
```

Nonlinear filters - arithmetic mean

```
void mean( const image_t *src, image_t *dst, const uint8_t n);
```

See file EVDK_Operators\nonlinear_filters.c

Optimize most (-O3)

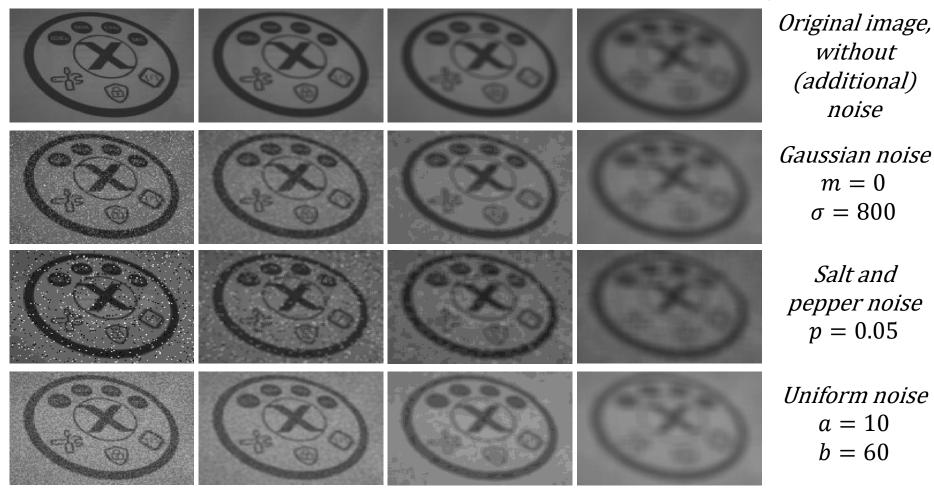
UVC connected

3x3 mask: **56 ms**

5x5 mask: **136 ms**

11x11 mask: **594 ms**

Nonlinear filters - arithmetic mean examples



Nonlinear filters

An overview of all nonlinear filters

Nonlinear filters – harmonic mean

- Is better at removing Gaussian type noise and preserves edges
- Removes positive outliers
- Harmonic mean filter is defined as

$$p_{dst}(x,y) = \begin{cases} 0 & \text{If any } p_{src}(x+i,y+j) = 0\\ \frac{m}{\sum_{i=-n/2}^{i=n/2} \sum_{j=-n/2}^{j=n/2} \frac{1}{p_{src}(x+i,y+j)}} & \text{otherwise} \end{cases}$$

where

 $p_{dst}(x,y)$: the calculated result pixel in the destination image at (x,y) $p_{src}(x+i,y+j)$: a pixel value in the src image within the window m: the number of pixels included in the summation calculation

Nonlinear filters – median

- Removes long tailed noise and salt and pepper type noise
- Has minimum bluring effect and preserves spatial details
- Can remove outlier noise from images that contain less than 50% of its pixels as outliers
- The median is defined as

$$p_{dst}(x,y) = \begin{cases} X[\frac{n}{2}] & \text{if } n \text{ is odd} \\ X[\frac{n-1}{2}] + X[\frac{n}{2}] & \text{if } n \text{ is even} \end{cases}$$

where

 $p_{dst}(x,y)$: the calculated result pixel in the destination image at (x,y)n: the window size

X: sorted list of values from the source image in the window $\left[window(x+i,y+j)\right]_{i=-n/2}^{i=n/2}{}_{j=-n/2}^{j=n/2}$

$$[window(x+i,y+j)]_{i=-n/2}^{i=-n/2}$$

Nonlinear filters – minimum

- Outputs the local minimum
- Is used to remove positive outlier noise
- Minimum filter is defined as

$$p_{dst}(x,y) = min[window(x+i,y+j)]_{i=-n/2}^{i=n/2} j^{i=n/2}$$

where

Nonlinear filters – maximum

- Outputs the local maximum
- Is used to remove negative outlier noise
- Maximum filter is defined as

$$p_{dst}(x,y) = max[window(x+i,y+j)]_{i=-n/2}^{i=n/2} {}_{j=-n/2}^{j=n/2}$$

where

Nonlinear filters – midpoint

- Outputs the average of the local minimum and maximum
- Used to remove short tailed noise, such as Gaussian and uniform type noise
- Midpoint filter is defined as

$$p_{dst}(x,y) = \frac{min[window(x+i,y+j)]_{i=-n/2}^{i=n/2} j=n/2}{2} + max[window(x+i,y+j)]_{i=-n/2}^{i=n/2} j=n/2}{2}$$

where

Nonlinear filters – range

- Outputs the difference between the local maximum and minimum
- Range filter is defined as

$$p_{dst}(x,y) = \max[window(x+i,y+j)]_{i=-n/2}^{i=n/2} - \min[window(x+i,y+j)]_{i=-n/2}^{i=n/2} - \min[window(x+i,y+j)]_{i=-n/2}^{i=-n/2} - \min[window(x+i,y+j)]_$$

where

EVD1 – Assignment



Study guide

Week 3

3 Nonlinear filters – meanFast()

4 Nonlinear filters – EXTRA

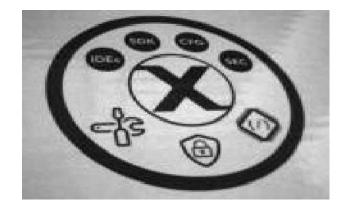
Spatial Filters

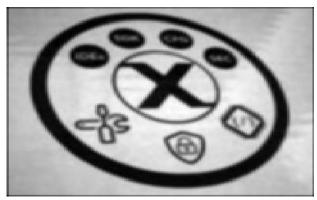
- Are basically discrete convolution filters
- The filter is known as a spatial mask
- Copy an image pixel-by-pixel while allowing for the effects of the pixel values in the local area (mask)
- Filter operations include multiplication, addition, and shifting
- Convolution is a time-consuming operation, so a 3x3 mask is typically used
- Typically uses odd masks and the centre of the mask for the pixel that is to be replaced, but this is by no means a requirement
- It can be implemented in parallel hardware for extremely fast execution
- Gaussian filters
- Laplacian filters
- Sobel filter

Gaussian

- Gaussian filters are masks formed from a two-dimensional Gaussian distribution
- Removes high frequency noise, but causes blurring

Gaussian - example









3x3

1	2	1
2	4	2
1	2	1

5x5

1	4	7	4	1
4	16	26	16	4
7	26	41	26	7
4	16	26	16	4
1	4	7	4	1

Gaussian - algorithm

```
void gaussianFilter_3x3( const image_t *src, image_t *dst);
void gaussianFilter_5x5( const image_t *src, image_t *dst);
```

Gaussian - algorithm

```
void gaussianFilter_3x3( const image_t *src, image_t *dst);
void gaussianFilter_5x5( const image_t *src, image_t *dst);
```

```
// Qt example

// Create additional int16_pixel_t images, because calculations with such
// masks will not be in the uint8_pixel_t range
image_t *src_int16 = newInt16Image(IMG_WIDTH, IMG_HEIGHT);
image_t *dst_int16 = newInt16Image(IMG_WIDTH, IMG_HEIGHT);

cv::Mat cv_src_int16(IMG_HEIGHT, IMG_WIDTH, CV_16UC1, src_int16->data);
cv::Mat cv_dst_int16(IMG_HEIGHT, IMG_WIDTH, CV_16UC1, dst_int16->data);
```

Gaussian - algorithm

```
void gaussianFilter_3x3( const image_t *src, image_t *dst);
void gaussianFilter_5x5( const image_t *src, image_t *dst);
```

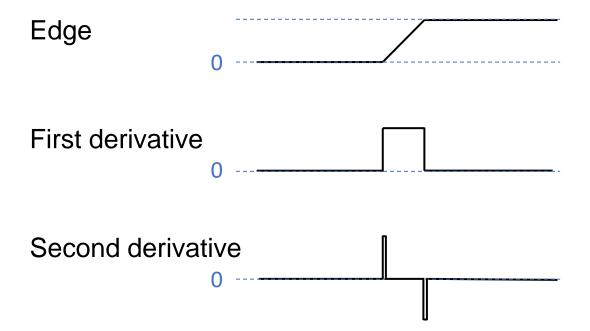
```
// -----
// Image processing pipeline
// -----
// Convert input image
convertBgr888ToUint8(img, src);
convertBgr888ToInt16(img, src_int16);

// Filter
gaussianFilter_3x3(src_int16, dst_int16);

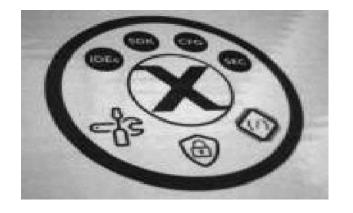
// Scale both images to uint8_pixel_t for convenient visualisation
scale(src, src);
scaleInt16ToUint8(dst_int16, dst);
```

Laplacian

- Gives the second derivative in two directions
- Enhances changes and only changes



Laplacian - example









3x3

0	-1	0
-1	4	-1
0	-1	0

5x5

-1	-1	-1	-1	-1
-1	-1	-1	-1	-1
-1	-1	24	-1	-1
-1	-1	-1	-1	-1
-1	-1	-1	-1	-1

Laplacian - algorithm

```
void laplacian_3x3( const image_t *src, image_t *dst);
void laplacian_5x5( const image_t *src, image_t *dst);
```

Sobel

- Edge detection algorithm with two results:
 - 1. Edge magnitude
 - 2. Edge direction
- Sobel magnitude and direction are defined as

$$M_{sobel}(x,y) = |G_H(x,y)| + |G_V(x,y)|$$
 $\varphi_{sobel}(x,y) = tan^{-1}(\frac{G_V(x,y)}{G_H(x,y)})$

where

 $M_{sobel}(x,y)$: the calculated magnitude in the destination image at (x,y) $\varphi_{sobel}(x,y)$: the calculated direction in the destination image at (x,y) $G_H(x,y)$: the pixel at (x,y) in the horizontal enhanced image $G_V(x,y)$: the pixel at (x,y) in the vertical enhanced image

Sobel

• The horizontal enhanced image G_H is obtained by a convolution with mask

ЭХЭ			
-1	-2	-1	
0	0	0	
1	2	1	

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• The vertical enhanced image G_V is obtained by a convolution with mask

-1	0	1
-2	0	2
-1	0	1

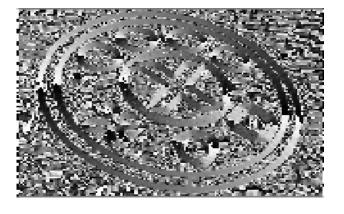
3x3

Sobel - example





Magnitude



Direction between $-\frac{\pi}{2}$ and $\frac{\pi}{2}$

void sobel(const image_t *src, image_t *mag, image_t *dir);

See file EVDK_Operators\spatial_filters.c

void sobel(const image_t *src, image_t *mag, image_t *dir);

See file EVDK_Operators\spatial_filters.c

```
// EVDK example

// Create additional int16_pixel_t images, because calculations with such
// masks will not be in the uint8_pixel_t range
image_t *src_int16 = newInt16Image(IMG_WIDTH, IMG_HEIGHT);
image_t *dst_int16 = newInt16Image(IMG_WIDTH, IMG_HEIGHT);
```

void sobel(const image_t *src, image_t *mag, image_t *dir);

See file EVDK_Operators\spatial_filters.c

```
// -----
// Image processing pipeline
// -----
// Convert uyvy_pixel_t camera image to int16_pixel_t image
convertUyvyToInt16(cam, src_int16);
```

void sobel(const image_t *src, image_t *mag, image_t *dir);

See file EVDK_Operators\spatial_filters.c

```
// Copy timestamp
ms1 = ms;

// Detect edges using Sobel edge detect
sobel(src_int16, dst_int16, NULL);

// Copy timestamp
ms2 = ms;
```

void sobel(const image_t *src, image_t *mag, image_t *dir);

See file EVDK_Operators\spatial_filters.c

```
// Scale uint8_pixel_t for convenient visualisation
scaleInt16ToUint8(dst_int16, dst);

// Convert uint8_pixel_t image to bgr888_pixel_t image for USB
convertToBgr888(dst, usb);
```

void sobel(const image_t *src, image_t *mag, image_t *dir);

See file EVDK_Operators\spatial_filters.c

The dir image can be omitted (NULL). If not omitted, it must be of image type IMGTYPE_FLOAT.

Optimize most (-O3)
UVC connected

72 ms



EVD1 – Assignment



Study guide
Week 3
5 Spatial filters – sobelFast()

References

• Myler, H. R., & Weeks, A. R. (2009). *The pocket handbook of image processing algorithms in C.* Prentice Hall Press.