

# 1 Logarithmns

Perhaps the numbers most easy to provide irrational are certain logarithmns. Here is a proof by contradiction that  $\log_2 3$  is irrational (  $\log_2 3 \approx 1.58 > 0$  ).

Assume  $\log_2 3$  is rational. For some positive integers  $m$  and  $n$ , we have

$$\log_2 3 = \frac{m}{n}.$$

It follows that

$$\begin{aligned} 2^{m/n} &= 3 \\ (2^{m/n})^n &= 3^n \\ 2^m &= 3^n. \end{aligned}$$