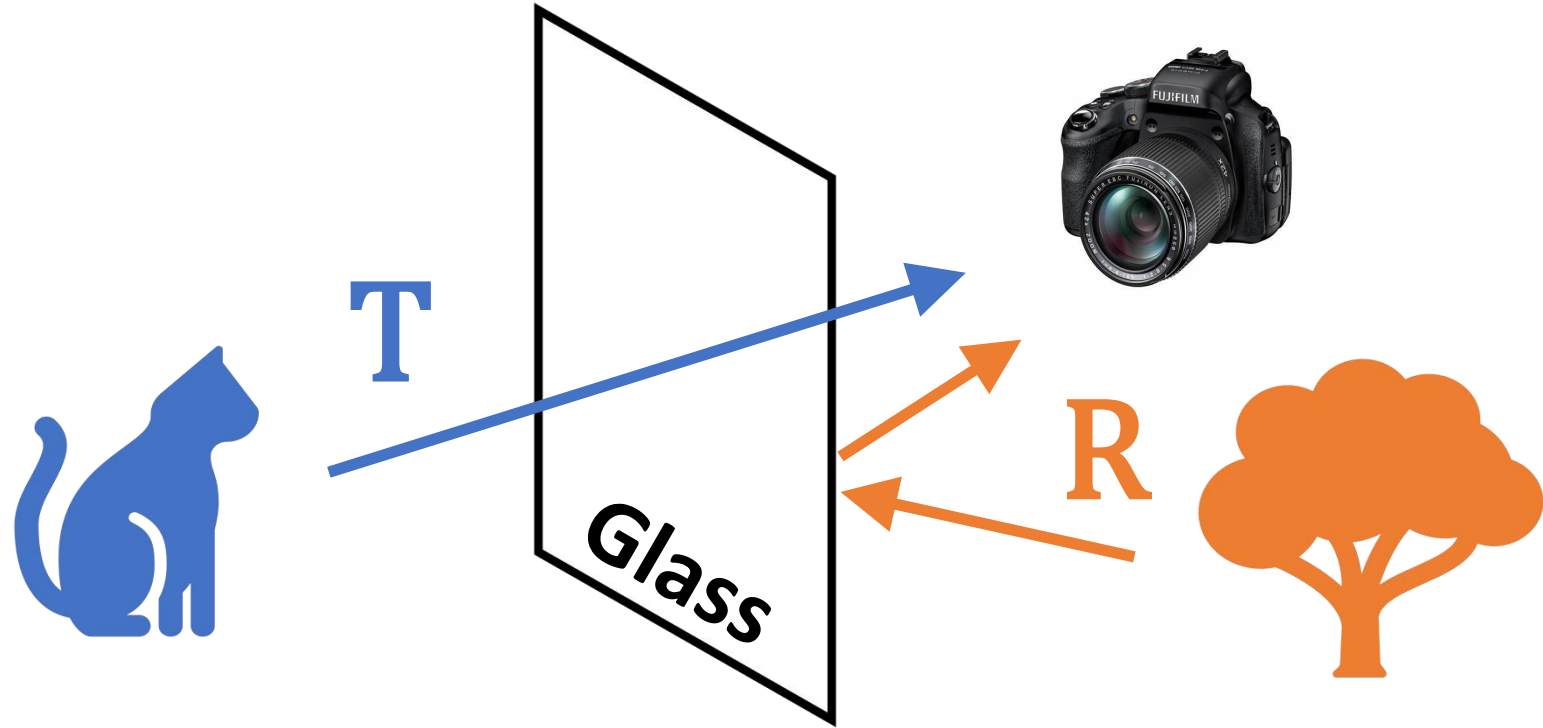


## Introduction

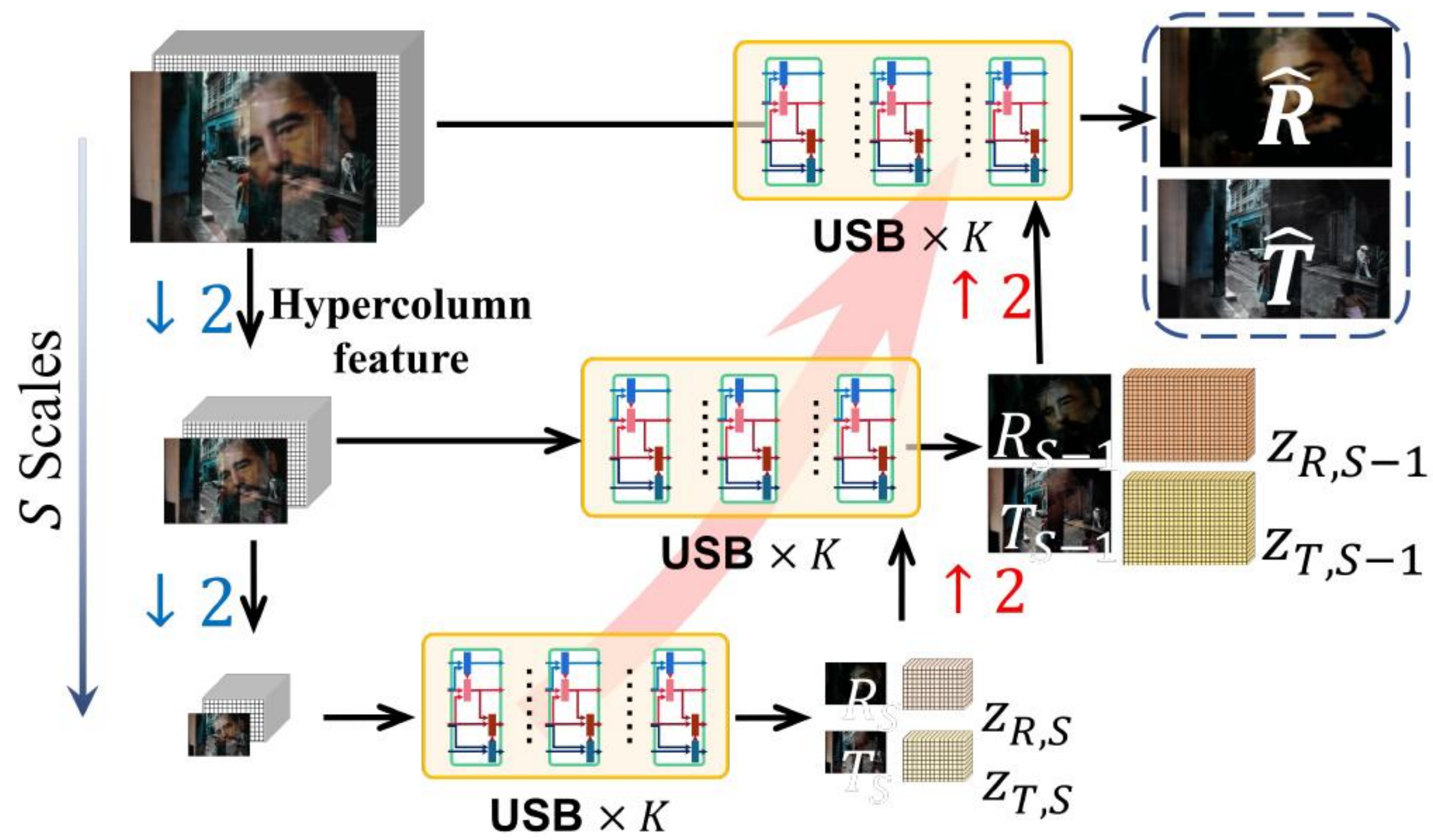
**Single Image Reflection Removal** is a typical Blind Source Separation problem. It aims to decompose a reflection-contaminated image **I** captured through a glass into a transmission image **T** and a reflection image **R**.



- Highly ill-posed problem
- Minimize shared image contents

In this paper, we propose a **principle approach** to design a novel **Deep Unfolded Reflection Removal Network**

- ✓ good interpretability
- ✓ good trade-off between performance and complexity

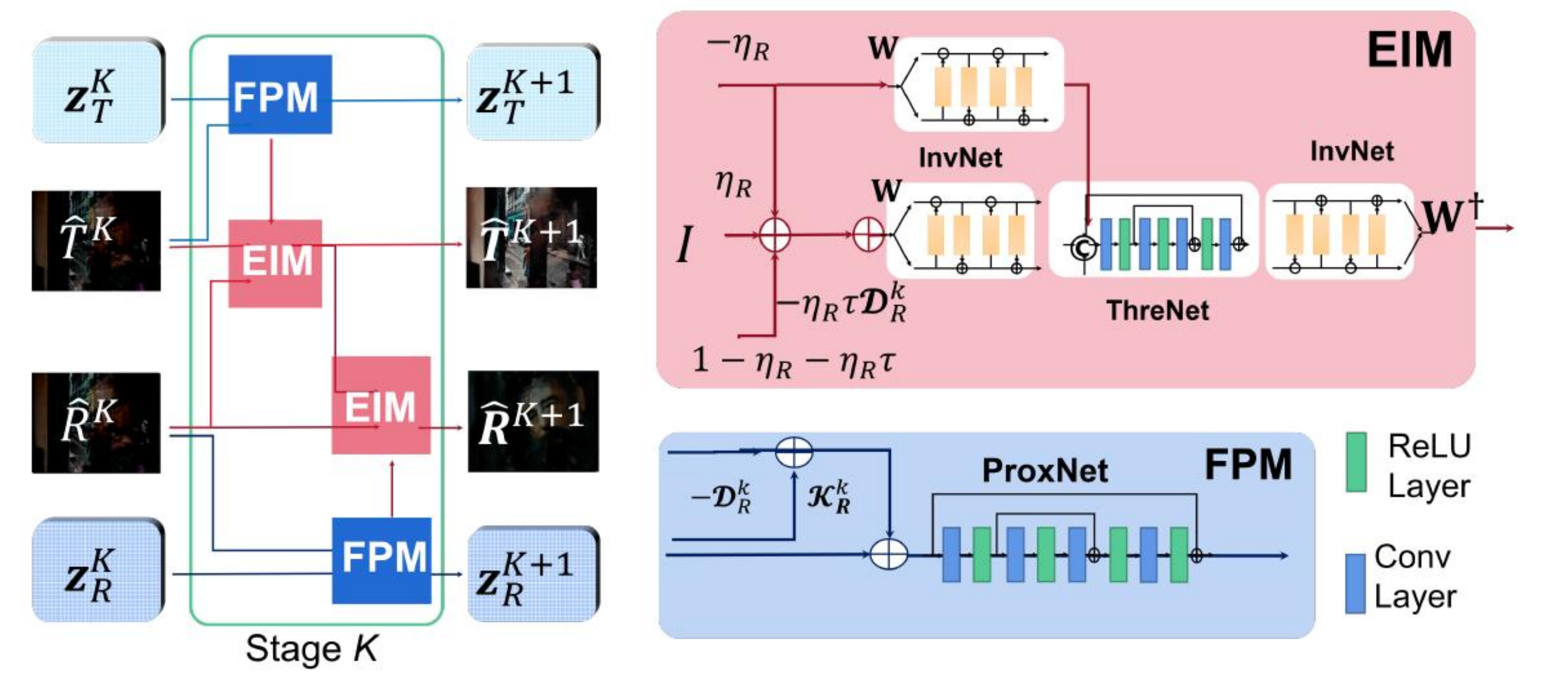


## Proposed Deep Unfolded Network

We unfold and parameterize each iteration of i-FAST algorithm into a **Unfolded Separation Block (USB)**:

■ **Feature Prediction Module (FPM)**: the proximal operators  $\text{prox}_{\eta\lambda/\tau}(\cdot)$  are parameterized by a learnable ProxNet which is a deep residual network with a global skip connection to learning from training dataset to capture the prior information

■ **Exclusion Interaction Module (EIM)**: we propose to overparameterize the fixed **wavelet transform** as a learnable **Invertible Neural Network (InvNet)** and to use a Thresholding Network (ThreNet) to replace the soft-thresholding operator.

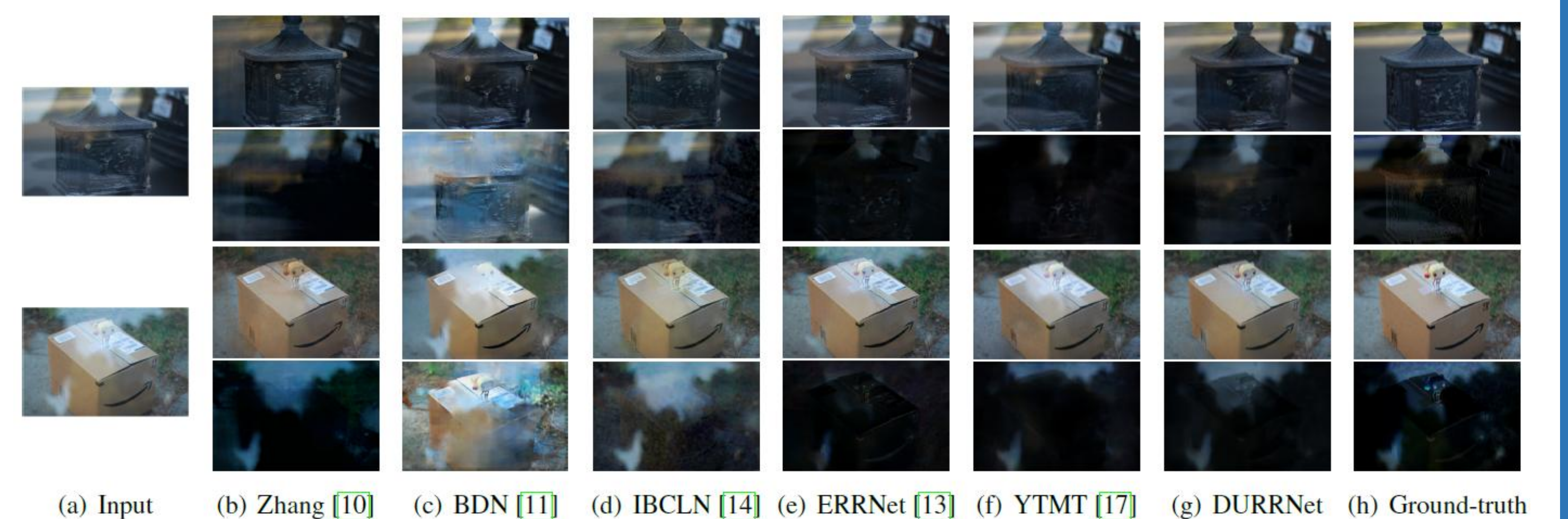


## Experimental Results

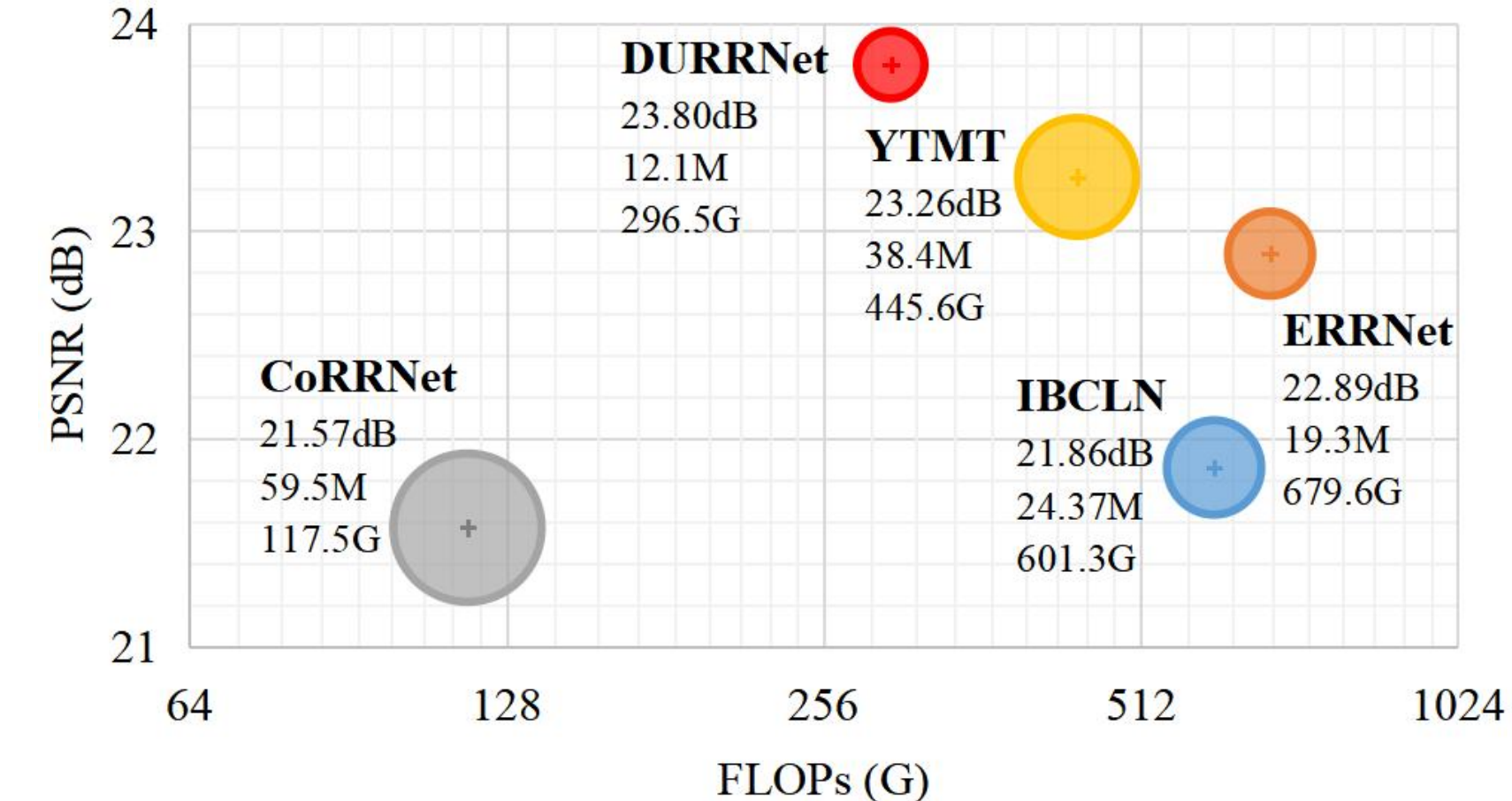
➤ Objective comparisons:

Dataset	Metrics	CEILNet [8]	Zhang <i>et al.</i> [10]	BDN [11]	IBCLN [14]	CoRRN [22]	ERRNet [13]	YTMT [17]	DURRNet (proposed)
Real20 (20)	PSNR (↑)	18.45	22.55	18.41	21.86	21.57	22.89	23.26	<b>23.80</b>
	SSIM (↑)	0.690	0.788	0.726	0.762	0.807	0.803	0.806	<b>0.814</b>
Nature (20)	PSNR (↑)	19.33	19.56	18.92	23.57	21.84	20.60	23.85	<b>24.24</b>
	SSIM (↑)	0.745	0.736	0.737	0.783	0.805	0.755	0.810	<b>0.812</b>

➤ Subjective comparisons



➤ PSNR v.s. FLOPs and #Params



➤ By combining the merits of model-based and learning-based paradigms, DURRNet achieves SOTA performance with fewer parameters and lower complexity.

## Proposed Method

### Model Formulation

The interplay between the shared contents of image layers are essential for effective separation, while is often overlooked by the existing deep architectures.

We propose a Convolutional Sparse Coding (CSC) based optimization formulation with a transform-based exclusion prior:

$$\min_{\mathbf{z}_T, \mathbf{z}_R} \frac{1}{2} \left\| \mathbf{I} - \sum_{i=1}^N \mathbf{D}_T^i \otimes \mathbf{z}_T^i - \sum_{i=1}^N \mathbf{D}_R^i \otimes \mathbf{z}_R^i \right\|_F^2 + \lambda_T p_T(\mathbf{z}_T) + \lambda_R p_R(\mathbf{z}_R) + \kappa \mathcal{E} \left( \sum_{i=1}^N \mathbf{D}_T^i \otimes \mathbf{z}_T^i, \sum_{i=1}^N \mathbf{D}_R^i \otimes \mathbf{z}_R^i \right)$$

**Exclusion Prior:**  $\mathcal{E}(\mathbf{T}, \mathbf{R}) = \sum_{m=1}^M \|(\mathbf{W}_m \otimes \mathbf{T}) \odot (\mathbf{W}_m \otimes \mathbf{R})\|_1$   
where  $\mathbf{W}$  denotes **wavelet transform**.

### Optimization Algorithm

The optimization formulation is reformulated by Half-Quadratic Splitting (HQS) algorithm. Based on Proximal Gradient Descent (PGD), we design an iterative Feature and Auxiliary Separation (i-FAST) algorithm with closed-form solutions for each sub-problem:

$$\begin{cases} \mathbf{z}_T^{k+1} = \text{prox}_{\eta_1 \lambda_T / \tau} (\mathbf{z}_T^k - \eta_1 \nabla f(\mathbf{z}_T^k)), \\ \mathbf{z}_R^{k+1} = \text{prox}_{\eta_2 \lambda_R / \tau} (\mathbf{z}_R^k - \eta_2 \nabla h(\mathbf{z}_R^k)), \\ \hat{\mathbf{T}}^{k+1} = \sum_{m=1}^M \mathbf{W}_m^\dagger \otimes \mathcal{S}_{\kappa|\mathbf{W}_m \otimes \hat{\mathbf{R}}^k|} (\mathbf{W}_m \otimes \phi(\hat{\mathbf{T}}^k)), \\ \hat{\mathbf{R}}^{k+1} = \sum_{m=1}^M \mathbf{W}_m^\dagger \otimes \mathcal{S}_{\kappa|\mathbf{W}_m \otimes \hat{\mathbf{T}}^{k+1}|} (\mathbf{W}_m \otimes \psi(\hat{\mathbf{R}}^k)), \end{cases}$$

## Conclusions

- ✓ A novel model-inspired single image reflection removal network.
- ✓ Model-based optimization formulation which exploits the sparsity based image model with joint priors.
- ✓ By unfolding i-FAST, the proposed DURRNet is constructed using multiple scales of Unfolded Separation Blocks (USB).